

1 **RUNNING TITLE:** Scaling photosynthesis from gene to leaf

2

3 **TITLE:** Combining gene network, metabolic, and leaf-level models show means to future-
4 proof soybean photosynthesis under rising CO₂.

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21

22 **ABSTRACT**

23 Global population increase coupled with rising urbanization underlies the predicted need for
24 60% more food by 2050, but produced on the same amount of land as today. Improving
25 photosynthetic efficiency is a largely untapped approach to addressing this problem. Here, we
26 scale modeling processes from gene expression through photosynthetic metabolism to predict
27 leaf physiology in evaluating acclimation of photosynthesis to rising [CO₂]. Model integration
28 with the yggdrasil interface enabled asynchronous message passing between models. The
29 multiscale model of soybean photosynthesis calibrated to physiological measures at ambient
30 [CO₂] successfully predicted the acclimatory changes in the photosynthetic apparatus that
31 were observed at 550 ppm [CO₂] in the field. We hypothesized that genetic alteration is

32 necessary to achieve optimal photosynthetic efficiency under global change. Flux control
33 analysis in the metabolic system under elevated $[\text{CO}_2]$ identified enzymes requiring the
34 greatest change to adapt optimally to the new conditions. This predicted that Rubisco was less
35 limiting under elevated $[\text{CO}_2]$ and should be down-regulated allowing re-allocation of
36 resource to enzymes controlling the rate of regeneration of ribulose-1:5 bisphosphate (RubP).
37 By linking the GRN through protein concentration to the metabolic model it was possible to
38 identify transcription factors (TF) that matched the up- and down-regulation of genes needed
39 to improve photosynthesis. Most striking was TF GmGATA2, which down-regulated genes
40 for Rubisco synthesis while up-regulating key genes controlling RubP regeneration and starch
41 synthesis. The changes predicted for this TF most closely matched the physiological ideotype
42 that the modeling predicted as optimal for the future elevated $[\text{CO}_2]$ world.

43

44 **KEYWORDS:** Gene network model, metabolic model, photosynthesis, global change, Soybean,
45 transcription factors, multiscale modeling, model integration

46 INTRODUCTION

47 As the world's most important seed legume and most widely grown dicotyledonous crop,
48 the future-proofing of photosynthesis in soybean (*Glycine max* (L.) Merr.) under rising
49 atmospheric concentrations of CO₂ ([CO₂]) is of importance. Down-regulation of light-saturated
50 net leaf CO₂ uptake (A_{sat}) at elevated [CO₂] has been reported for many C₃ crops, yet the
51 mechanism underlying this response is poorly understood. Under current [CO₂], A_{sat} in C₃ crops
52 is most commonly limited by the *in vivo* Rubisco activity ($V_{c,max}$) (Long et al., 2004). However,
53 as [CO₂] continues to rise, it follows from the steady-state biochemical model of photosynthesis
54 of (Farquhar et al., 1980) and its subsequent modifications (Von Caemmerer, 2000) that control
55 will shift from Rubisco to RubP regeneration (Long et al., 2004), which is represented by the
56 maximum *in vivo* rate of whole chain electron transport (J_{max}). While described by electron
57 transport, most evidence now points to this being limited by the metabolic steps of carbon
58 metabolism leading to RubP regeneration (Raines, 2003, Stitt and Sonnewald, 1995). This shift
59 from Rubisco- to RubP- limited photosynthesis permits a reduction in leaf Rubisco content
60 without a loss in A_{sat} (Woodrow, 1994, Long et al., 2004, Ainsworth and Long, 2005). Because
61 Rubisco accounts for the largest single share of leaf N, optimization of Rubisco content would
62 maximize the efficiency of use of this commonly limiting resource (Drake et al., 1997, Long et
63 al., 2004).

64 When [CO₂] is increased around a photosynthesizing leaf, A_{sat} can increase for two
65 reasons, first the K_M of Rubisco for CO₂ is close to the current atmospheric concentration, so
66 elevated [CO₂] increases the velocity of carboxylation, and secondly, CO₂ competitively inhibits
67 the oxygenation reaction that produces phospho-glycolate and in turn photorespiration. This
68 latter effect is particularly important because it increases the efficiency of net CO₂ uptake by
69 diverting ATP and NADPH (generated by the light reactions) away from photorespiratory
70 metabolism to photosynthetic assimilation, and so will increase A_{sat} regardless of other limiting
71 factors. Under rising [CO₂] both factors will increase A_{sat} when $V_{c,max}$ is limiting, but only the
72 second factor when J_{max} is limiting. Assuming the average specificity and K_M for CO₂ and O₂
73 for Rubisco from terrestrial plants, and a constant intercellular versus external [CO₂], one can
74 calculate the increase in A_{sat} that would result from an increase in atmospheric [CO₂]. Following
75 the procedure of (Long et al., 2004) for a leaf temperature of 25 °C, the increase in atmospheric
76 [CO₂] from today's 400 $\mu\text{mol mol}^{-1}$ to 550 $\mu\text{mol mol}^{-1}$ would increase Rubisco-limited and

77 RubP-limited photosynthesis by 31% and 9%, respectively. $550 \mu\text{mol mol}^{-1}$ is the concentration
78 forecast for 2050 assuming current emissions trends continue (RCP8.5, (Pachauri et al., 2014)).
79 At current atmospheric $[\text{CO}_2]$ soybean leaf photosynthesis is at the transition point between
80 $V_{c,\text{max}}$ - and J_{max} -limitation (Bernacchi et al., 2005). Therefore, as $[\text{CO}_2]$ rises soybean
81 photosynthesis would become RubP-limited. If however, resource currently invested in Rubisco
82 was re-allocated to increased J_{max} then this transition point would move to a higher $[\text{CO}_2]$ and a
83 31% rather than 9% increase in A_{sat} could be obtained, without any increased total investment of
84 protein in the photosynthetic apparatus. When grown under elevated $[\text{CO}_2]$ in open-air field
85 conditions, is an increase in J_{max} observed at the expense of $V_{c,\text{max}}$?

86 In two consecutive years, (Bernacchi et al., 2005) analyzed photosynthesis in a modern
87 highly productive soybean cultivar under open-air $[\text{CO}_2]$ elevation using Free-Air Concentration
88 Enrichment (FACE) (Long et al., 2006). Compared to control plants those grown in $[\text{CO}_2]$
89 elevated to $550 \mu\text{mol mol}^{-1}$ showed a shift in control of A_{sat} from co-limitation of $V_{c,\text{max}}$ and J_{max}
90 to limitation solely by RubP-limitation. There was a significant 5% decrease in the ratio of
91 $V_{c,\text{max}}:J_{\text{max}}$, showing a decline in Rubisco activity relative to the capacity for RubP regeneration
92 (Bernacchi et al., 2005). However, while acclimation had occurred it was insufficient to
93 maximize the potential increase in A_{sat} , had the system responded to fully re-optimize investment
94 of resources. At 25°C , re-optimizing the system to 550 ppm was calculated to require a 35%
95 reduction of investment in Rubisco and re-allocation of that protein to the apparatus for
96 regeneration of RubP (Drake et al., 1997, Long et al., 2004), while only a 5% change was
97 observed. The plant was apparently over-investing in Rubisco and under-investing in the
98 apparatus determining regeneration of RubP. How might genetic manipulation be used to
99 achieve re-optimization and prepare soybean and other crops to sustainably maximize
100 photosynthetic efficiency and in turn crop productivity under future conditions?

101 Here we combine a metabolic model of C_3 photosynthetic metabolism, including the C_2
102 photorespiratory pathway, mathematically representing all discrete steps of photosynthesis from
103 light and CO_2 absorption to starch and sucrose synthesis (Zhu et al., 2007, Zhu et al., 2013) with
104 a gene network model to predict observed acclimatory changes. This is successfully tested
105 against observed acclimatory changes of photosynthesis in soybean grown at elevated $[\text{CO}_2]$.
106 Finally, via sensitivity analysis and dynamic gene regulatory network analysis, the combined

107 model is used to predict genetic changes, including expression levels of transcription factors, that
108 could fully optimize leaf photosynthetic efficiency to future elevated [CO₂] conditions.

109

110 **MULTISCALE MODEL DEVELOPMENT**

111 To predict what genes may transcriptionally regulate the soybean response to elevated
112 [CO₂], it was necessary to develop a mechanistically informed model in which the multi-scale
113 response could be explored. We have previously developed complete mechanistic metabolic
114 models of photosynthetic carbon metabolism that successfully predict dynamic responses of leaf
115 chlorophyll fluorescence and fluxes of CO₂ and O₂ to changes in light, [CO₂] and [O₂] (Zhu et
116 al., 2007, Zhu et al., 2013). While each of these models provided new insights about
117 photosynthesis, when combined with optimization routines to predict optimal investments for
118 different environments, they are not equipped to predict transcriptomic and genetic changes that
119 could achieve those optimal patterns of investment. The generalization of whole plant
120 metabolism and signaling pathways often results in simulations with low prediction accuracy
121 upon model perturbation. Multiscale models that mimic the biological flow of information across
122 scales have been shown to have higher prediction accuracy than models at individual scales,
123 especially when simulating conditions different from the original training data (Chew et al.,
124 2014). To our knowledge, no current model of photosynthesis in soybean scales from genes to
125 organs. Such a model could potentially simulate system-wide changes in photosynthesis in
126 response to targeted genetic perturbations.

127 To predict leaf-level responses of net CO₂ uptake, a metabolic model (e-Photosynthesis)
128 was combined with a leaf micrometeorological model that integrated boundary layer
129 conductance, stomatal conductance, and leaf energy balance (Drewry et al., 2010, Nikolov et al.,
130 1995). Our prior e-Photosynthesis model (Zhu et al., 2013) simulates fluxes through some 70
131 reactions involved in the light and dark reactions of C₃ photosynthesis. The steady-state
132 photosynthesis rate predicted by the e-Photosynthesis model replaced the leaf model prediction
133 that was based on the Farquhar model of photosynthesis (Nikolov et al., 1995). Leaf temperature,
134 light intensity and intercellular CO₂ concentration predicted by the leaf model were used as
135 inputs for the e-Photosynthesis model. The integrated leaf metabolic and micrometeorological
136 model effectively simulates the observed response to net leaf CO₂ uptake to [CO₂] observed for
137 soybean in the field (Bernacchi et al., 2005) (Figure 1, Supplemental figure 1). However, it lacks

138 any capacity to predict the observed decrease in $V_{c,max}$ and increase in J_{max} that resulted from
139 growth in elevated $[CO_2]$. This is because the model lacks any connection to the underlying
140 changes in gene expression that may cause this altered photosynthetic phenotype.

141 The altered photosynthetic phenotype likely resulted from adjusted enzyme
142 concentrations in soybean leaves grown under ambient and elevated CO_2 concentrations. Such
143 CO_2 -induced changes in protein concentrations was shown for total protein concentration in
144 barley, rice, wheat, soybean, and potato (Taub et al., 2007) and for specific proteins via
145 proteomic analysis in rice (Bokhari et al., 2007), wheat (Yousuf et al., 2017), and grape (Zhao et
146 al., 2019). A decrease in the quantity of Rubisco is a pervading feature of plants grown in the
147 field under elevated $[CO_2]$ (Ainsworth and Long, 2005). However, the e-Photosynthesis model
148 only allows substrate (CO_2) concentration to change, which results in altered reaction rates, but
149 lacks capacity to predict acclimatory changes in enzyme concentrations. By including gene
150 expression data from soybean plants grown under ambient and elevated $[CO_2]$ (Leakey et al.,
151 2009), it is possible to make predictions about changes in enzyme concentrations.

152 Gene expression data cannot be used as direct input for the e-Photosynthesis model,
153 which can only accept enzyme concentrations. Also, transcriptome data from microarray or
154 RNA-sequencing technologies provide relative and not absolute quantification of mRNA
155 transcripts. To overcome these challenges and inform the e-Photosynthesis model with gene
156 expression data, a model was needed to computationally translate mRNA to protein
157 concentration. An ordinary differential equation (ODE) was adapted from (Becskei and Serrano,
158 2000), and given as: $(\Delta p = \left(\frac{1}{1 + \frac{p}{d}} \times L \times r \right) - (U \times p))$,

159 Eq. 1

160 where, L and U are the estimated gene family-specific protein synthesis and degradation rates (Li
161 et al., 2017), respectively, r is the mRNA level, p is the initial protein concentration, and d is the
162 upper limit of protein translation. It is assumed that r and p are equal (Edfors et al., 2016), and p
163 is based on starting protein concentration estimates from the e-Photosynthesis model. To
164 simulate steady-state protein concentrations in elevated CO_2 , p was adjusted based on the
165 proportion of change in mRNA level between ambient and elevated $[CO_2]$ for a given gene.

166 The change in predicted, relative protein concentrations between ambient and elevated
167 CO_2 conditions (ProteinRatio) was used to adjust the enzyme concentration and activity of each

168 gene involved in the light and dark reactions of photosynthesis represented in the e-
169 Photosynthesis model, as follows:

$$V_{\max_ele} = V_{\max_0} \cdot [E.ProteinRatio] \quad \text{Eq 2}$$

170
171 where, V_{\max_ele} is the maximum activity of each enzyme in elevated CO₂, V_{\max_0} is the original
172 maximum activity of each enzyme in ambient CO₂, and E is the estimated enzyme
173 concentration.

174 Because the protein translation model and metabolic/leaf level models are implemented
175 in different programming languages (Python and MATLAB) respectively, they cannot
176 communicate with each other directly without significant alteration of the model code or through
177 manual integration by running the model programs independently and using files to pass
178 information between them. In order to integrate the models programmatically (Figure 2), we
179 used the yggdrasil framework. yggdrasil is an open-source Python package developed by the
180 Crops *in silico* research group for connecting models written in different programming languages
181 through simple interfaces in the model's language of implementation. Based on information on
182 the target models and connections between the models provided in human-readable specification
183 files, yggdrasil runs the designated models in parallel and coordinates asynchronous
184 communication between the models as they run. Asynchronous message passing allows models
185 to continue working after sending output to the next model in the network without waiting for
186 the output to be received, thereby improving the performance of the overall model integration as
187 models can complete calculations simultaneously in separate processes. yggdrasil currently
188 supports connecting models written in Python, Matlab, C and C++ on Linux, Mac OS, and
189 Windows operating systems. Additional information on the yggdrasil package can be found in
190 (Lang, 2019) or in the documentation (<https://cropsinsilico.github.io/yggdrasil/>).

191

192 **METHODS**

193 **Differential Expression Analysis of Genes Responding to CO₂**

194 The soybean transcriptome differential responses to growth in ambient and elevated [CO₂] was
195 obtained previously using the Affymetrix *Glycine max* genechip (Leakey et al., 2009). These
196 data were re-analyzed here to identify differentially expressed (DE) genes corresponding to leaf

197 tissue collected at the beginning of seed set when the canopy has attained full maturity. Probe
198 sets were normalized using the GC Robust Multi-array Average (GCRMA) method. A one-way
199 ANOVA was done in the R statistical software environment using the aov function of the stats
200 package. The reanalysis identified 5005 DEGs on a statistical cutoff of P value ≤ 0.05 and
201 Benjamini-Hochberg False Discover Rate (FDR) ≤ 0.3 .

202 **Construction of CO₂ responsive Gene Regulatory Network**

203 *Co-expression using mutual rank*

204 Mutual rank analysis (Obayashi and Kinoshita, 2009) was used to obtain highly significant co-
205 expression relationships among differentially expressed genes (DEGs). In mutual rank analysis,
206 the Pearson Correlation Coefficient (PCC) is calculated between the gene of interest and all other
207 DEGs, then sorted based on their PCC ranks, in which the gene pair having the highest
208 correlation value is given rank 1 (Obayashi and Kinoshita, 2009). Mutual Rank is calculated
209 from PCC rank by taking the geometric mean between PCC ranks from gene A to gene B and
210 from gene B to gene A, as these can be different. The ranks are scaled between 0 to 1, where MR
211 of 1 indicates the most significant coexpression interaction. All interactions having an MR \geq
212 $|0.8|$ and a PCC $\geq |0.6|$ were selected for the coexpression network. Interactions having a
213 significant correlation were further filtered to retain only those that had predicted binding
214 interactions between the TF and target gene as described below.

215 *Static Gene Regulatory Network construction and analysis*

216 To analyze gene regulatory networks, a DNA pattern search algorithm was performed
217 (PlantPAN, <http://plantpan2.itps.ncku.edu.tw/>) (Medina-Rivera et al., 2015) to identify the
218 presence of known *Cis*-regulatory elements (CREs) in the promoter region of genes of interest.
219 Known CREs were obtained from the transcription factor databases Transfac (Matys et al.,
220 2006), JASPAR (Sandelin et al., 2004), CISBP (Weirauch et al., 2014), and PlantTFDB (Jin et
221 al., 2013), and NewPLACE (Higo et al., 1999). The promoter region considered in this study
222 was the sequence 1 Kb upstream of the predicted or experimentally verified Transcription Start
223 Site (TSS) for every gene obtained from PlantProm (Shahmuradov et al., 2003). Promoter
224 regions of target genes were analyzed for an enrichment of CREs for a particular TF family. For
225 this analysis, the average number of binding sites for a CRE in the putative 1 Kb up-stream
226 promoter region of all the genes present in Soybean Wm82.a1.v1 was calculated. If a target gene

227 promoter has a greater than average number of TF family-specific binding sites present in its
228 promoter, then the CRE of interest is considered over-represented.

229

230 **Dynamic Gene Regulatory Network Model Construction**

231 A dynamic Gene Regulatory Network (GRN) model was built using a linear regression
232 algorithm to infer relationships between a dependent variable (in this case the expression of the
233 putative target gene) and one or more independent variables (or predictors; in this case TFs). The
234 resulting linear model was used to predict the response variable based on the states of the
235 dependent variables. The regression algorithm was run in R using the LM function (Team,
236 2013), which optimizes variables of the linear model using a least squares fit between the
237 response and dependent variables on training data (Eq 1) (Bjorck, 1996).

238 For example:

$$mRNA_{Target} = g_0 + (W_1 * mRNA_{TF1}) + (W_2 * mRNA_{TF2}) + \dots \quad \text{Eq 3}$$

239 where, g_0 , W_1 , W_2 are least squares optimized parameters for the linear model. $mRNA_{TF1}$,
240 $mRNA_{TF2}$, etc. are expression values of TFs predicted to regulated target genes of interest in
241 the static GRN. Parameters were optimized using training data, which ultimately resulted in a
242 weight (W_x) that corresponds to the level of influence that a TF exerts on a predicted target
243 gene's expression. A linear model was generated for every gene in the static CO₂-responsive
244 GRN, and used to simulate the expression of genes of interest in both ambient and elevated CO₂
245 environments. All linear model equations are listed in Supplemental Table 1.

246 The training data was obtained from seven soybean Affymetrix microarray transcriptome
247 datasets (GSE8432, GSE23129, GSE26198, GSE29740, GSE29741, GSE35427, GSE44685).
248 While these datasets were derived from a variety of experimental conditions, they were chosen
249 because samples were taken from similar tissue and developmental stage as those in the CO₂-
250 responsive dataset used to build the static GRN (Leakey et al., 2009). Expression data from all
251 training sets were commonly normalized by GCRMA and quality control analysis was
252 performed; samples with a high variation in their median expression level within replicates were
253 removed from the analysis. A total of 213 samples were used to train the linear regression model.
254 The CO₂-responsive dataset that is used to build the static GRN was used as a test dataset for the
255 linear model, to predict expression of the target gene using the optimized weight associated with
256 every TF.

257

258 **Protein translation model**

259 A protein translation model (PTM) adapted from (Becskei and Serrano, 2000) was used to
260 predict steady-state protein concentrations based on relative mRNA transcript levels (See Eq. 1)
261 The model parameter p (and thus r) is obtained from the initial protein concentration used in the
262 e-Photosynthesis metabolic model under the control (ambient $\text{CO}_2 = 380$ ppm) condition. To
263 predict initial protein concentration in elevated CO_2 conditions (550 ppm), p was adjusted using
264 the relative fold change in mRNA transcript levels measured between ambient and elevated CO_2
265 conditions. As stated earlier, L and U are protein synthesis and degradation rates, respectively,
266 and denotes the increase or decrease in protein abundance per hour (denoted as g/L/hour).
267 Soybean gene-specific L and U rates were estimated based on the rates of their Arabidopsis
268 orthologs taken from (Li et al., 2017). If ortholog information for a gene was not available, L and
269 U were estimated by taking an average of L and U rates for all Arabidopsis genes involved in
270 photosynthesis.

271 The PTM model simulations resulted in steady-state protein concentration ratios between
272 ambient and elevated $[\text{CO}_2]$ conditions for every gene. Optimized parameter ' d ' was obtained in
273 a gene specific manner such that, the steady-state protein concentration ratio between the two
274 conditions (elevated/ambient) remains constant for that gene after a particular threshold ' d ' (see
275 Supplemental Table 2). This protein concentration ratio was then used as one of the inputs for the
276 e-Photosynthesis model (described below) in order to account for changes in gene expression as
277 a factor influencing the enzyme kinetics of proteins in the primary C metabolism machinery. The
278 model assumes constant temperature and constant concentration of RNA polymerase (El Samad
279 et al., 2005).

280 **Metabolic photosynthesis model**

281 The soybean photosynthesis metabolic flux (MF) model is based on the e-Photosynthesis model
282 (Zhu et al., 2013) and implemented in MATLAB. The e-Photosynthesis model is a general C_3
283 photosynthesis model that includes each discrete process from light capture to carbohydrate
284 synthesis, including photorespiratory C_2 metabolism. In the model, the rate of change of the
285 concentration of each metabolite is represented by an ordinary differential equation (ODE):

$$\frac{dC}{dt} = V_p - V_u \quad \text{Eq 4}$$

286 Where, [C] represents metabolite concentration; V_p is the total rate of reaction(s) that produces C,
287 and V_u is the rate of consumption. Rate equations for each enzyme catalyzed reaction were
288 developed based on standard Michaelis-Menten equations for enzyme kinetics, with kinetic
289 parameters corresponding to a temperature of 25°C. Four enzymes, including Rubisco, did not
290 satisfy the conditions needed to apply Michaelis-Menten kinetics, and equations for their
291 catalysis were as in (Zhu et al., 2007). Initial protein concentration of enzymes in the MM
292 kinetics equation were obtained from (Zhu et al., 2013) (Supplemental Table 3). $V_{c,max}$ and J_{max}
293 of soybean grown under ambient and elevated [CO₂] in the field had been determined previously
294 (Bernacchi et al., 2005). This was the same germplasm, site and treatments from which the
295 transcriptional data, used in developing the GRN, was obtained. Here the $V_{c,max}$ and J_{max}
296 obtained in ambient [CO₂] was used to calibrated the metabolic model, which on integration with
297 the other models was then used to attempt to predict the observed changes in the $V_{c,max}$ and J_{max}
298 observed with growth at elevated [CO₂]. Calibration was achieved by adjusting amounts of
299 Rubisco to match the $V_{c,max}$ described for soybean grown in ambient [CO₂]. All other protein
300 amounts in the metabolic model, were elevated maintaining the proportion used in (Zhu et al.,
301 2013), until a J_{max} was achieved that matched that observed by (Bernacchi et al., 2005). This
302 required multiplying each by 1.2 over those used in (Zhu et al., 2013) (Supplemental table 3).
303 The enzyme kinetic parameters of e-Photosynthesis are for 25°C. Leaf temperatures in the
304 simulations used here slightly exceeded this. To deal with these slight, but variable, increases in
305 temperature parameters were adjusted to the actual leaf temperature (T_i) using a Q_{10} function, as
306 described previously (Woodrow and Berry, 1988).

$$k_i = k_{25} \cdot Q_{10}^{\frac{T_i - 25}{10}} \quad \text{Eq 5}$$

307 The predicted enzyme protein concentration changes as a percentage of that in ambient [CO₂]
308 were assumed in direct proportion to the changes of enzyme activities (V_{max}) in the metabolic
309 model. For example, if the predicted sedoheptulose-1:5 bisphosphatase (SBPase) protein
310 concentration was predicted to increase by 3% under elevated [CO₂], then SBPase activity
311 ($V_{max_Rubisco}$) was also increased by 3% in metabolic model.

312

313 *Sensitivity analysis of each step in the metabolic model*

314 Metabolic control analysis defines the quantitative link between the flux through a pathway and
315 the activity of an enzyme in terms of the flux control coefficient (Fell, 1998). The maximum
316 activity of each enzyme ($V_{max i}$) was both increased and decreased by 1% individually in the
317 model to calculate the new photosynthesis rate (A^+ and A^-) for the two CO_2 concentrations (350
318 ppm vs 550 ppm) to identify the enzymes that most influence the net photosynthetic rate. The
319 flux control coefficient (CC) of each enzyme was calculated as:

$$CC = \frac{\partial A}{\partial V_{max i}} \frac{V_{max i}}{A} \approx \frac{A^+ - A^-}{0.02 \cdot A} \quad \text{Eq 6}$$

320 Where A is the original net leaf CO_2 uptake rate, before the simulated change in activity of
321 enzyme i ($\partial V_{max i}$).

322

323 **Leaf level photosynthesis model**

324 At the leaf level, the metabolic model was integrated with leaf level models of stomatal
325 physiology, and energy balance based on the method of (Nikolov et al., 1995). Here, stomatal
326 conductance is a function of predicted net leaf CO_2 uptake rate, humidity, and $[CO_2]$ after
327 (Collatz et al., 1991). Leaf energy balance takes account of intercepted short and long wave
328 radiation, radiative energy loss from the leaf, convection and latent heat loss in transpiration.
329 However, these models are inter-dependent. For example, CO_2 uptake rate affects stomatal
330 conductance, stomatal conductance affects leaf temperature and leaf temperature affects CO_2
331 uptake rate. Solving these circular connections is achieved iteratively. Iteration continues until
332 change to obtain a numerical solution of stomata conductance, leaf temperature, boundary-layer
333 conductance and photosynthesis rate until changes in all four are $<0.1\%$ between iterations. This
334 model is also implemented in MATLAB. Equations and parameters are listed in supplemental
335 information (Supplemental table 4).

336

337 **RESULTS**

338 **A multiscale model of soybean can mimic photosynthetic acclimation observed in FACE**
339 **experiments**

340 The integrated model predicted new steady-state enzyme concentrations for selected
341 reactions belonging to the dark reactions and starch synthesis in the e-Photosynthesis model in
342 response to growth of soybean leaves under elevated [CO₂]. The ratio of predicted steady-state
343 enzyme concentrations in elevated to ambient CO₂ is used as one of the inputs in the e-
344 Photosynthesis model (Supplemental Table 5). Though the magnitude of the change is small, the
345 predicted CO₂ response is consistent with the altered photosynthetic phenotype, as shown by the
346 improved fit to the measured response of A_{sat} to leaf intercellular [CO₂] and the values of $V_{c,max}$
347 and J_{max} calculated from this response (Bernacchi et al., 2005) (Figure 1). Including the gene
348 expression data, the $V_{c,max}$ of the predicted CO₂ response curve decreases from 115 to 109 μmol
349 $\text{m}^{-2} \text{s}^{-1}$, and J_{max} of the predicted curve increase from 149 to 153 $\mu\text{mol} \text{m}^{-2} \text{s}^{-1}$. Simulations reveal
350 no significant change in leaf temperature, transpiration and stomatal conductance
351 (Supplementary Figure 1). Importantly, the fully integrated model was able to simulate the
352 change in photosynthetic rate due to the acclimation response observed in soybean plants grown
353 under elevated [CO₂] (Figure 1). The predicted A_{sat} in 550 ppm [CO₂] increased by 17.7%
354 compared to ambient. Predicted metabolite concentrations also changed dynamically with
355 elevation of [CO₂], for example RubP decreased, PGA, T3P and SBP increased, as would be
356 expected from an increased flux into these pools with accelerated carboxylation and decreased
357 oxygenation at Rubisco (Figure 3).

358
359 ***in silico* perturbations reveal potential mechanisms for the transcriptional regulation of**
360 **photosynthetic acclimation**

361 Genes with a functional role in the same biological pathway are often co-expressed and
362 sometimes co-regulated. The identification of common cis-regulatory elements in the promoters
363 of tightly co-expressed genes is a good proxy for co-regulation (Allocco et al., 2004). The
364 corresponding transcription factors that bind to these CREs are promising targets for the
365 manipulation of whole pathway expression. The re-engineering of photosynthesis is needed to
366 increase crop productivity in response to climate change (Zhu et al., 2010), such as overcoming
367 the limitations caused by photosynthetic acclimation at elevated atmospheric [CO₂]. With a fully
368 integrated model of photosynthesis it was then possible to simulate the field-level photosynthetic

369 response to genetic perturbations under both ambient (380 ppm) and elevated (550 ppm) [CO₂].
370 The ideotype for elevated [CO₂] is one in which Rubisco content is substantially decreased and
371 controlling components of the apparatus for RubP regeneration substantially increased. This
372 problem was approached by revisiting the individual models to identify gene targets that
373 significantly contribute to deliver this metabolic ideotype.

374

375 *Sensitivity of the system to individual steps within photosynthetic carbon metabolism*

376 To determine which steps in the system exert the strongest control on A_{sat} in both ambient and
377 elevated [CO₂], a sensitivity analysis was performed by varying each parameter +/- 1% (Table
378 1). Control coefficients (CCs) are calculated as the ratio of change in the amount of one enzyme
379 divided by change in A_{sat} . If a 1% change in enzyme x results in a 1% change in A_{sat} CC = 1, the
380 maximum possible, while if the change in A_{sat} is zero, then CC = 0, meaning that no control is
381 exerted by that enzyme. The sum of all control coefficients should approximate to 1. Rubisco
382 has the highest CC of all enzymes in ambient [CO₂], while SBPase has the highest control
383 coefficient in elevated CO₂ (Table 1). Nine enzymes with the highest CCs overall (>0.01) were
384 further evaluated for transcriptional regulation.

385 *A CO₂-responsive gene regulatory network reveals co-regulated genes*

386 A static gene regulatory network (GRN) of the nine enzymes with the highest CCs from
387 the e-Photosynthesis model was constructed using transcriptome data from soybean grown under
388 ambient and elevated [CO₂] (Leakey et al., 2009). Network nodes represent the genes that
389 encode the nine enzymes involved in photosynthesis with the highest CC. Network edges
390 represent regulatory interactions between TFs and putative, co-expressed target genes as
391 determined by rank correlation of expression (MR \geq 0.8 and PCC \geq |0.6|) and the significant
392 presence of CREs in the promoter of target genes for a corresponding TF gene. The static GRN
393 was used to define the regulatory interactions that contribute to the expression of each target
394 gene, in which each gene of interest (GOI) may have more than one TF protein regulating its
395 expression. A linear regression modeling approach (Karlebach and Shamir, 2008) was used to
396 determine the strength of influence, or weight (w), of each TF predicted to regulate a GOI. The
397 resulting equations containing weighted TF-target interactions that enabled dynamic simulations
398 with the GRN, where the expression of any TF in the network could be modified (up- or down-
399 regulated) and result in a predicted change in expression of the target GOI (Figure 4).

400 The dynamic GRN (Figure 5) was explored to identify TFs that would simultaneously
401 down-regulate carboxylation of Rubisco and up-regulate RubP regeneration and starch synthesis.
402 Based on network topology, the top three candidate TFs are GmWRKY71 (Glyma.07G023300),
403 a bHLH transcription factor (Glyma.18G115700), and GmGATA2 (Glyma.01G169400)
404 (Supplemental Figure 2). *in silico* perturbations were performed for each candidate TF in which
405 the TF expression was eliminated (knock-out) or overexpressed. Simulations within the dynamic
406 GRN resulted in newly predicted expression levels of all genes targeted by the TF of interest
407 (Figure 4).

408 The predicted change in mRNA expression provided input for the protein translation
409 model that in turn predicted steady-state enzyme concentrations under elevated and ambient
410 [CO₂] as described in the Model Development section. The ratio of steady-state protein levels
411 were then fed into the fully integrated photosynthesis model to obtain predicted changes in
412 photosynthesis rate. The *in silico* over-expression of GmWRKY71 and GmGATA2, and the
413 knockout of the bHLH TF resulted in a predicted increase in photosynthetic rate under both
414 ambient and elevated [CO₂]. A simultaneous *in silico* over-expression of GmWRKY71 and
415 knock-out of bHLH TF increased the overall photosynthesis rate compared to wild type, but
416 these failed to significantly lower Rubisco and release the resource that would be needed to
417 elevate capacity for RubP regeneration without more resource investment (Figure 6A-C). The
418 most promising TF candidate according to model simulations is the overexpression of
419 GmGATA2, which results in the most dramatic change to both the down-regulation of
420 carboxylation and up-regulation of RubP regeneration based on the simulated A/Ci curve (Figure
421 6D).

422

423 **DISCUSSION**

424 Multi-scale models have the potential to identify and add missing mechanistic details
425 about system function and generate new hypotheses to prioritize targeted engineering efforts in
426 plant science (Marshall-Colon et al., 2017, Millar et al., 2019). More than 4,000 mathematical
427 plant models were published over the last decade. The majority of these models describe one
428 biological scale or process and generalize the un-modeled spatio-temporal processes as a single
429 output from a black box. Linking single-scale models will improve the comprehensive
430 investigation of biological systems, resulting in explanatory models with higher prediction

431 accuracy than models limited to one biological scale. The ability to interrogate biology at many
432 resolutions can reveal emergent system behaviors that cannot easily be measured (Walpole et al.,
433 2013). Multiscale models that link genes to phenotypes can accelerate the directed development
434 of crop ideotypes. Until now metabolic modeling has predicted ideotypes with maximal
435 photosynthetic efficiency for given environmental conditions with respect to distribution of
436 resources between photosynthetic proteins. Achieving the ideotype then depends on identifying
437 individual genes that might be up- or down- regulated. The multi-scale model may now be used
438 not only to predict the metabolic ideotype, but the gene expression changes at the network level
439 needed to achieve this. In turn, this has led, as demonstrated here, to the identification of
440 transcription factors that can achieve the multiple gene expression changes needed by alteration
441 of the expression of just one or two transcription factors.

442 In this study, we constructed a multiscale model of soybean leaf photosynthesis by
443 integrating three models across molecular and organ-level scales using asynchronous message
444 passing. By informing the leaf micrometeorological model with gene-level data, we were able to
445 simulate the field-observed phenomena of photosynthetic acclimation in soybean plants grown
446 under two different atmospheric CO₂ concentrations. Acclimation was previously suggested to
447 be a transcriptionally driven process that increases the capacity of respiration (Leakey et al.,
448 2009). This though does not explain the observed decrease in in vivo Rubisco activity ($V_{c,max}$)
449 and increase in capacity for RuBP regeneration (J_{max}) by (Bernacchi et al., 2005). Existing
450 models of photosynthesis do not provide a means to link observed transcriptional changes with
451 metabolism and photosynthetic capacity at the leaf level. Our integrated model overcomes this
452 and not only suggests the changes in mRNA levels and how these affect photosynthetic
453 metabolism, but was able to predict the acclimation of photosynthetic CO₂ assimilation that had
454 been observed (Figure 1). Previous studies have reported proteome-level changes in response to
455 elevated CO₂ in soybean and other crop species (Ainsworth and Long, 2005, Bokhari et al.,
456 2007, Taub et al., 2007, Yousuf et al., 2017, Zhao et al., 2019).

457 Interestingly, only 48 out of the 81 genes that encode enzymes in the e-Photosynthesis
458 model had a statistically significant change in expression in elevated [CO₂], and only 17 had a
459 fold change >1.5. Since the ratio of change in enzyme concentration was proportional to the
460 change in transcript concentration, it reveals that even a slight modification to the e-
461 Photosynthesis model resulted in better prediction accuracy of field observations. This result

462 represents the double-edged sword of multiscale modeling, in which fine-tuning at the molecular
463 level can have drastic consequences at higher scales. Errors can propagate in multiscale models
464 as information is exchanged across spatial and temporal scales. However, empirical validation of
465 the model outputs at any scale can minimize error propagation. In our study, field data
466 corroborated model simulations, providing confidence in the success of the modeling approach
467 and the biologically relevant flow of information from genes to organs.

468

469 *in silico perturbations identified transcriptional regulators of photosynthesis*

470 The successful manipulation of photosynthetic efficiency has been achieved through
471 targeted engineering of individual enzymes (Köhler et al., 2017, Driever et al., 2017), but an
472 alternative strategy is to simultaneously alter the expression of suites of enzymes involved in
473 different parts of the photosynthesis pathway (Simkin et al., 2017). Understanding the
474 transcriptional regulation of photosynthesis genes may help to fine-tune pathway expression
475 under different environmental conditions, so avoiding the need to directly engineer change in
476 expression of genes for each enzyme. This study uncovered three TFs, GmWRKY71,
477 GmGATA2, and a bHLH TF, which potentially regulate the expression of genes encoding key
478 enzymes involved in photosynthesis. While the transcriptional and post-transcriptional regulation
479 of genes involved in photosynthesis have previously been explored (Isono et al., 1997,
480 Fankhauser and Aubry, 2016, Saibo et al., 2008, Wang et al., 2017a, Zhang et al., 2016), this is
481 the first report of targeted GRN analysis to identify TFs that specifically co-regulate the
482 carboxylation of Rubisco and RubP regeneration.

483 Our hypothesis driven approach sought to explore how decreasing Rubisco and
484 reallocating resources to RubP regeneration might increase A_{sat} . The dynamic GRN identified
485 high-confidence TF-target gene relationships between photosynthesis genes that have a high
486 control coefficient and TFs tightly co-expressed with those genes. Using diverse training data,
487 we were able to derive weights associated with each TF-target interaction, indicating which TFs
488 exerted the greatest transcriptional control. Several TFs were found to co-regulate genes
489 affecting Rubisco and RubP regeneration (Figure 5). However, only GmGATA2 was predicted
490 to significantly down-regulate genes affecting Rubisco synthesis and up-regulating genes that
491 would increase RubP regeneration and starch synthesis. The multiscale model simulations for the
492 knockout and overexpression of GmGATA2 suggest a mechanism by which the transcriptional

493 regulation of key photosynthetic genes can alter flux through the pathway. For example, the
494 overexpression of GmGATA2 resulted in decreased V_{c_max} and increased J_{max} , as would be
495 required to maximize efficiency in an elevated $[CO_2]$ environment (Table 2; (Drake et al., 1997,
496 Long et al., 2004)). The rewiring of metabolism, under both ambient and elevated CO_2 , produces
497 a change in photosynthetic efficiency, which is a leaf-level phenotype. Specifically, the KO of
498 GmGATA2 decreases overall photosynthetic capacity only in ambient $[CO_2]$, while
499 overexpression results in a large decrease in carboxylation and increase in RubP regeneration
500 according to the A/Ci curve (Figure 6D).

501 All of the top candidate TFs from our model simulations belong to TF families that have
502 previously been implicated in the transcriptional regulation of photosynthesis (Saibo et al.,
503 2008). For example, bHLH TFs (Myc Family of TFs) were found to regulate aspects of C_4
504 photosynthesis that are also related to genes in the ancestral C_3 state (Borba et al., 2018).
505 Interestingly, a number of other studies identified the GATA family of transcription factors as
506 important regulators of photosynthesis and of carbon and nitrogen balance. The overexpression
507 of Class B GATAs and GLKs in Arabidopsis roots improved photosynthesis by increasing root
508 chlorophyll content (Ohnishi et al., 2018). GmGATA2 is annotated as NITRATE-INDUCIBLE,
509 CARBON METABOLISM-INVOLVED (GNC) and is homologous to AtGATA5, and both are
510 Class A GATAs that are associated with the light regulation of gene expression and
511 photomorphogenesis (Zhang et al., 2015). The overexpression of the poplar PdGNC gene in
512 Arabidopsis improved photosynthesis under low N levels by increasing the size and number of
513 chloroplasts per cell. The photosynthetic rate in transgenics increased by 42% compared to WT
514 lines (An et al., 2014). These studies with structurally or functionally similar GATA TFs provide
515 support for the role of GmGATA2 in the regulation of photosynthesis. Our GRN analysis
516 uncovered a strong positive correlation (co-expression) between GmGATA2 and FBP-aldolase
517 and starch synthase and a strong negative correlation (anti-correlation) between GmGATA2 and
518 the gene Rbcs that encodes the RuBisCO small sub-unit. Metabolic modeling and direct up-
519 regulation have suggested that both FBP-aldolase and starch synthase exert strong control on
520 RubP-regeneration (Zhu et al., 2007, Uematsu et al., 2012, Tian et al., 2018). These network
521 predictions provide testable hypotheses for the next round of experimentation and modeling.

522 The multiscale modeling strategy described here represents a uni-directional flow of
523 information from genes to physiological phenotype. However, bi-directional inputs and outputs

524 exist between the e-Photosynthesis model and the leaf micrometeorological model, in which the
525 metabolic model can accept environmental parameters from the organ-level model. Ideally, a
526 truly dynamic and biologically accurate model would have a bi- or multi-directional flow of
527 information across scales. A limitation of this model is a lack of feedback from the metabolic
528 model to gene expression. This limitation stems from an inadequate amount of species- and
529 condition-specific transcriptional studies. Given the availability of more expression data, it
530 would be possible to include a model component with switch-like behavior that pulls in
531 appropriate expression data based on environment-level inputs. Alternatively, given protein
532 expression data it may be possible to leverage the proportional relationship between change in
533 protein concentration and change in transcript levels to predict gene expression based on protein
534 levels. Regardless of the method, this gap in information flow is an area of focus to improve the
535 current model. Moreover, this multiscale model is focused on one biological process,
536 photosynthesis. The proof-of-concept modeling approach outlined in our study provides a
537 feasible workflow, and a base model that can be expanded on to include related pathways and
538 processes that are still black boxes and beyond the scope of in our current model.

539

540 *Future directions.*

541 We are now poised to explore the multiscale model generated hypotheses, including the
542 functional testing of the top TF candidate genes. Ideally, these hypotheses will be tested directly
543 in soybean through the generation of transgenic plants that can be grown in FACE experiments
544 (Ainsworth et al., 2008). Likewise, the model is in place for expansion to include additional
545 metabolic pathways, but also scale to other levels. For example, the leaf micrometeorological
546 model is already a sub-component of a canopy-level model (Drewry et al., 2010, Srinivasan et
547 al., 2017), so an intuitive next step would be link to models that provide 3-D biophysical
548 representations of stands of plants, as for example those developed for sugarcane agronomy
549 (Wang et al., 2017b). This allows simulations with more realistic inputs for light capture and
550 competition between plants. Finally, advanced visualization of multiscale model outputs will be
551 an important next step in the simulation and analysis of *in silico* crops. Combined modeling and
552 visualization approaches will lead to realistic simulations of ideotypes to guide selection of
553 genetic targets for crop improvement (Marshall-Colon et al., 2017).

554

555 *Conclusion*

556 Despite the many assumptions that have had to be made in this first linkage of gene expression
557 networks, through protein concentrations and photosynthetic metabolism to leaf level CO₂
558 exchange, it was successful in accurately predicting the observed acclimation of photosynthetic
559 capacity in soybean when grown under elevated [CO₂]. Most importantly it is shown to provide
560 a numerical means to identify from many hundreds of possible transcription factors, those most
561 likely to adapt photosynthetic efficiency to global atmospheric change. It opens the way to
562 guiding sustainable adaptation of crop photosynthesis to a range of both current and future
563 environments.

564

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574
575 **Author Contributions:** AMC, SPL, YW, and KK designed the study. KK, YW, GSC performed
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577 and MML wrote the paper.

578

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756

757 **TABLES**

758 Table 1. The flux control coefficient of photosynthetic enzymes in ambient and elevated CO₂.

Enzyme	Value ($\mu\text{mol m}^{-2} \text{s}^{-1}$)	Meta (AmbCO₂)	Meta (EleCO₂)	Meta+GE (EleCO₂)	Meta+GE (EleCO₂)*
Rubisco	120	0.443	0.121	0.165	0.108
Sedoheptulose-bisphosphatase	13.35	0.305	0.674	0.605	0.746
Fructose-bisphosphate aldolase	50.2	0.114	0.091	0.077	0.047
Glucose-1-phosphate adenylyltransferase	8.01	0.076	0.058	0.055	0.035
The maximum rate of ATP synthesis	6	0.054	0.047	0.081	0.051
Fructose-bisphosphatases	29.91	0.039	0.031	0.030	0.021
UTP-glucose-1-phosphate uridylyltransferase	3.46	0.021	0.014	0.014	0.009
Fructose-bisphosphatase (C)	1.92	0.014	0.010	0.011	0.007
Fructose-2,6-bisphosphate 2- phosphatase	0.5	0.010	0.007	0.006	0.004
Transketolase	128.57	0.008	0.003	0.003	0.001
Fructose-bisphosphate aldolase (C)	3.22	0.007	0.005	0.005	0.003
Glycine transaminase	82.37	0.007	0.002	0.001	0.001
(S)-2-hydroxy-acid oxidase & Catalase(CAT, EC1.11.1.6)	43.68	0.001	0.000	0.000	0.000
Sucrose-phosphate synthase	1.67	0.001	0.001	0.002	0.002
Phosphoribulokinase	446.19	0.001	-0.001	-0.001	0.000
glycine dehydrogenase (aminomethyl-transferring)	74.84	0.000	0.000	0.000	0.000
Glycerate kinase	171.47	-0.001	0.001	-0.001	0.000
Glyceraldehyde-3-phosphate dehydrogenase (NADP+)	166.35	-0.001	0.001	0.001	0.000
Glycerate dehydrogenase	300.29	-0.001	0.000	0.000	0.000
Phosphoglycolate phosphatase	1572.6	-0.001	0.000	0.000	0.000
Sucrose-phosphate phosphatase	16.65	-0.002	0.000	0.000	0.000
Serine-glyoxylate transaminase	99.19	-0.004	-0.003	-0.002	-0.001
6-phosphofructo-2-kinase	3.03	-0.009	-0.006	-0.006	-0.003
Fructose-bisphosphate aldolase	50.2	-0.015	-0.010	-0.008	-0.004
Phosphoglycerate kinase	1241.24	-0.030	-0.023	-0.023	-0.016
Photosynthesis rate		24.876	29.176	29.047	29.261

759 * Assuming the total nitrogen (protein) resource is a constant

760 Table 2. The V_{cmax} and J_{max} of the predicted ACi curves. The V_{cmax} and J_{max} were predicted using
761 A/Ci curve fitting utility version 2.0 (Sharkey, 2015).

Treatment	$V_{cmax}(25^{\circ}\text{C})$	$J_{max}(25^{\circ}\text{C})$
WT-Amb	115.49	149.22
WT-Ele	109.17	152.57
WT-Ele (ConN)	112.29	153.58

bHLH TFOx-Amb	12.97	33.55
bHLH TFOx-Ele	110.66	90.71
bHLH TFKo-Amb	116.43	153.05
bHLH TFKo-Ele	114.54	154.51
GmWRKY71Ox-Amb	115.12	153.5
GmWRKY71Ox-Ele	112.08	154.97
GmWRKY71Ko-Amb	116.02	142.86
GmWRKY71Ko-Ele	113.37	151.82
bHLH TFKo&GmWRKY71Ox-Amb	118.93	154.76
bHLH TFKo&GmWRKY71Ox-Ele	114.67	155.78
GmGATA2Ox-Amb	91.28	157.58
GmGATA2Ox-Ele	89.67	157.59
GmGATA2Ko-Amb	123.28	135.62
GmGATA2Ko-Ele	119.75	147.49

762 ConN: Assuming the total nitrogen (protein) resource is a constant

763

764 **FIGURE LEGENDS**

765 Figure 1. Simulated and measured (Bernacchi et al., 2005) photosynthetic carbon dioxide
766 response curves of soybean growing in ambient CO₂ (370 μmol mol⁻¹) and elevated CO₂ (550
767 μmol mol⁻¹). PAR is 2000 μmol m⁻² s⁻¹

768

769 Figure 2. Model integration schematic describing the scaling from the gene regulatory network
770 model to the metabolic model to the leaf physiological model. Note that these models interact
771 through state variable indicated in the arrows. Ca is ambient CO₂ concentration, PPFD is the
772 amount of light absorbed by the leaf, T is leaf temperature and A is the net carbon assimilation.

773

774 Figure 3. Metabolic model predicted metabolite concentrations without and with gene expression
775 data (GE). PAR is 1200 μmol m⁻² s⁻¹.

776

777 Figure 4. Gene expression level changes in target genes of interest as a result of *in silico*
778 perturbation of three candidate TFs from the photosynthesis GRN. Figure shows mRNA
779 expression levels in wild type and perturbed TF (bHLH TF knockout in a, GmWRKY71
780 overexpression in b, simultaneous knockout of bHLH TF and GmWRKY71 overexpression in c,
781 GmGATA overexpression in d) conditions under ambient and elevated CO₂.

782

783 Figure 5. Gene regulatory network of metabolic genes having control coefficient > 0.01 based on
784 sensitivity analysis of the metabolic model enzymes after incorporating gene expression data.
785 Figure shows transcription factors as triangles and metabolic genes as squares. The network also
786 shows change in mRNA expression of these genes under elevated CO_2 concentration in leaves
787 with blue nodes indicating downregulation and orange nodes indicating upregulation under
788 elevated CO_2 as compared to ambient CO_2 . Similarly, blue edges indicate predicted repression
789 and orange edges indicate predicted activation of the metabolic gene by the TF. Thickness of the
790 edges are based on linear model weights with more thickness indicating a heavier weight
791 associated with the TF-target interaction.

792 Figure 6. Predicted influence of transcription factor perturbations on photosynthesis rate a)
793 bHLHB TF Knockout; b) GmWRKY71 Overexpression; c) bHLH TF Ko + GmWRKY71 Ox; d)
794 GmGATA2 Overexpression.

795

796 **SUPPLEMENTARY TABLES AND FIGURES**

797 Supplemental figure 1. Simulated variation of assimilation (a), transpiration (b), stomatal
798 conductance (c), and leaf temperature (d) as a function of leaf internal CO_2 concentration under
799 ambient CO_2 (black) and elevated CO_2 (red). PPFD is $1200 \mu\text{mol m}^{-2} \text{s}^{-1}$

800 Supplemental figure 2. Sub-networks for three transcription factors from the dynamic
801 photosynthesis GRN chosen for *in silico* perturbation. The figure consists of bHLH TF (a),
802 GmGATA2 (b) and GmWRKY71 (b) along with their predicted direct targets. Network nodes
803 and interactions can be interpreted as in figure 5 of the main text.

804 Supplemental table 1. Least squares optimized weights for transcription factors regulating
805 enzymes with high control coefficient after integration of protein translation model with e-
806 photosynthesis metabolic model in the dynamic photosynthesis GRN. This table is provided
807 separately as an excel workbook.

808 Supplemental table 2. Gene specific 'd' parameter values used in the protein translation model

809 Supplemental table 3. V_{max} , K_{cat} , molecular weight and protein content used in the e-
810 photosynthesis metabolic model

811 Supplemental table 4. Leaf level photosynthesis model parameters

812 Supplemental table 5. Steady state protein concentration ratios predicted by the protein
813 translation model for enzymes that are part of the e-photosynthesis model

814

815 **Appendix 1 Abbreviations and units – Some variables have been added here**

816 *A*: Net carbon assimilation ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

817 *A_{sat}*: Light saturated *A* ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

818 *C_i*: Leaf intercellular CO₂ concentration ($\mu\text{mol mol}^{-1}$)

819 [CO₂]: Atmospheric CO₂ concentration ($\mu\text{mol mol}^{-1}$)

820 FACE: Free Air [CO₂] Enrichment

821 *g_s*: Stomatal conductance ($\text{mmol m}^{-2} \text{s}^{-1}$)

822 *J*: Rate of electron transport ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

823 *J_{max}*: Maximum rate of electron transport ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

824 *R_d*: Mitochondrial respiration ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

825 Rubisco: Ribulose-1,5-bisphosphate carboxylase/oxygenase

826 RubP: Ribulose-1,5-bisphosphate

827 SoyFACE: Soybean Free Air [CO₂] Enrichment

828 *T_{leaf}*: Leaf temperature (°C)

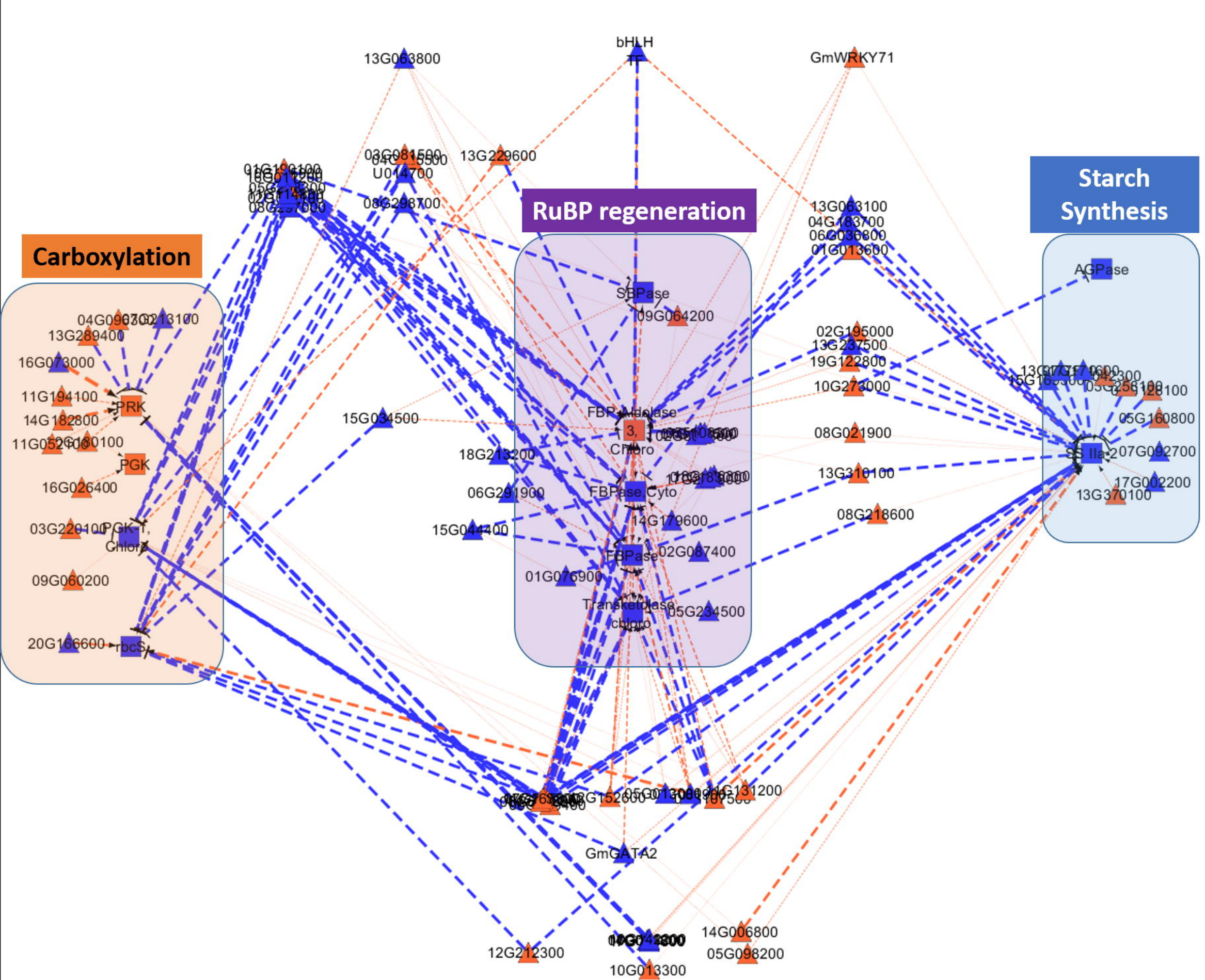
829 *V_{c,max}*: Maximum velocity of carboxylation ($\mu\text{mol m}^{-2} \text{s}^{-1}$)

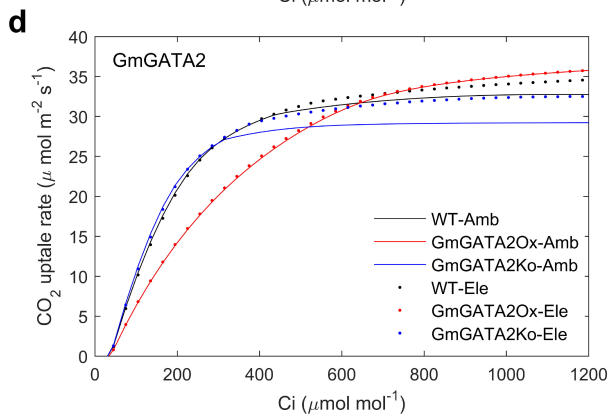
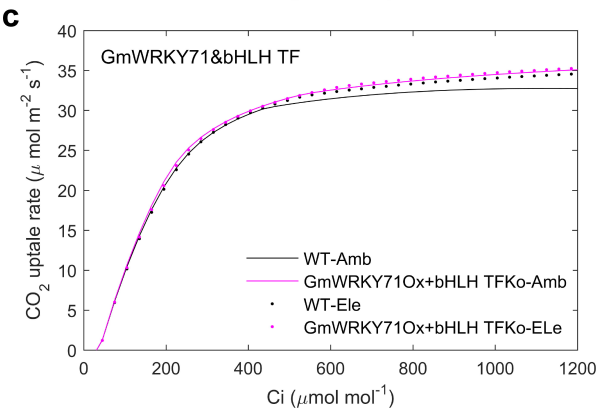
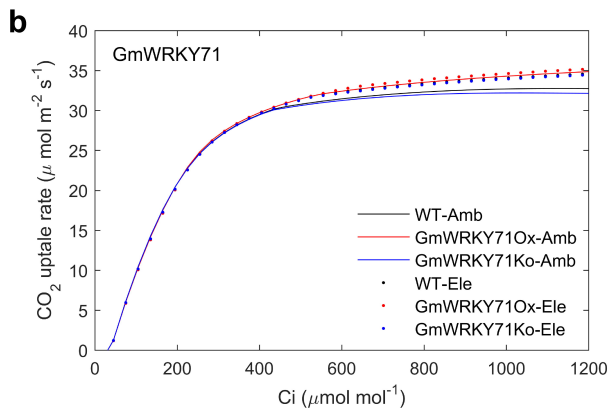
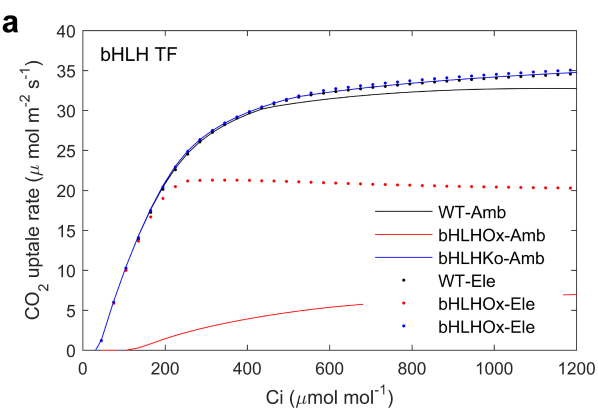
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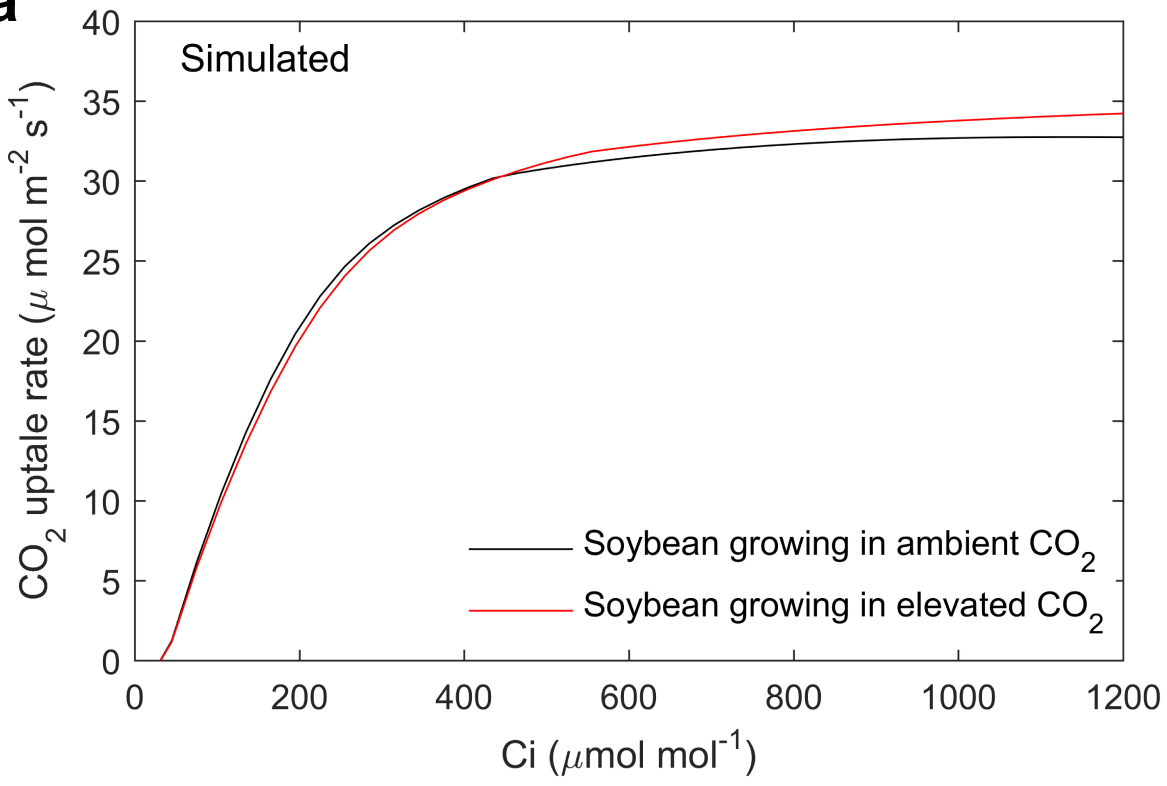
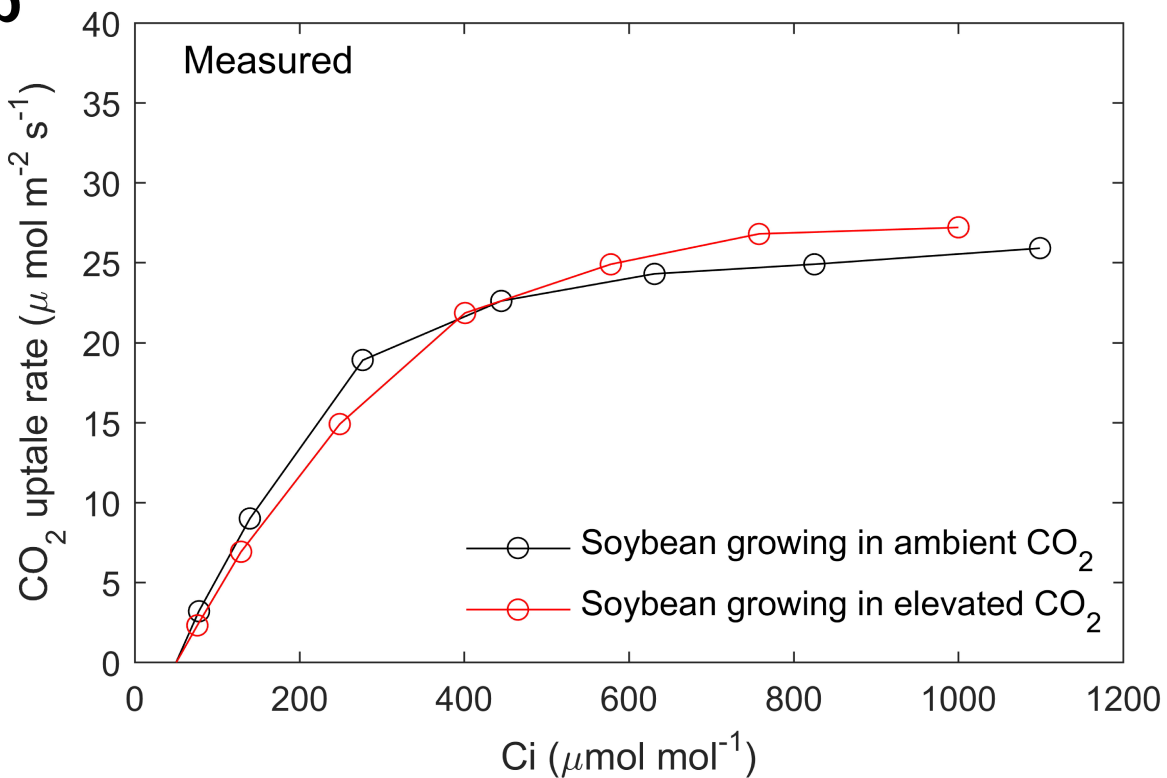
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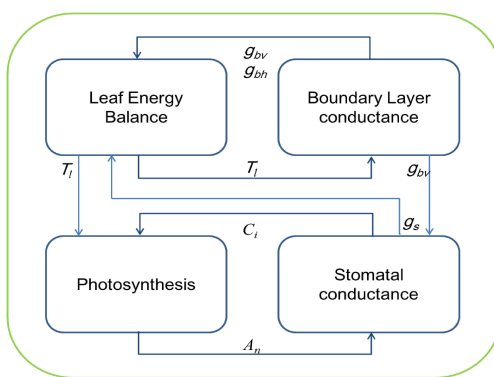
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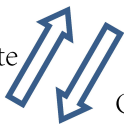
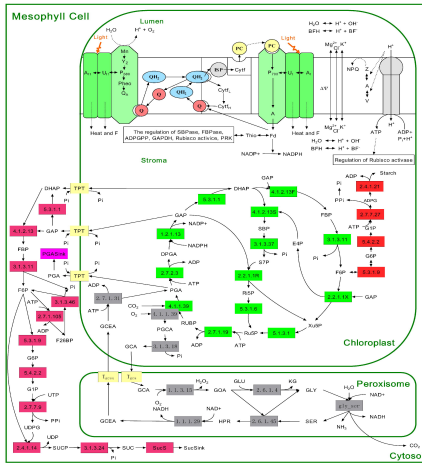




a**b**

a

Photosynthesis rate

CO₂ concentration, light, temperatureCO₂ concentration**c****b**Protein concentration
of enzymes