| 1 | The effect of diffusion on asymmetric spin echo based quantitative BOLD: |
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| 2 | An investigation of the origin of deoxygenated blood volume overestimation |
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1 Abstract

| 2 | Quantitative BOLD (qBOLD) is a technique for mapping oxygen extraction fraction (OEF) |
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| 3 | and deoxygenated blood volume (DBV) in the human brain. Recent measurements using an |
| 4 | asymmetric spin echo (ASE) based qBOLD approach produced estimates of DBV which |
| 5 | were systematically higher than measurements from other techniques. In this study, we |
| 6 | investigate two hypotheses for the origin of this DBV overestimation and consider the |
| 7 | implications for in vivo measurements. Investigations were performed by combining Monte |
| 8 | Carlo simulations of extravascular signal with an analytical model of the intravascular signal. |
| 9 | Hypothesis 1: DBV overestimation is due to the presence of intravascular signal |
| 10 | which is not accounted for in the analysis model. Intravascular signal was found to have a |
| 11 | weak effect on qBOLD parameter estimates. |
| 12 | Hypothesis 2: DBV overestimation is due to the effects of diffusion which aren't |
| 13 | accounted for in the analysis model. The effect of diffusion on the extravascular signal was |
| 14 | found to result in a vessel radius dependent variation in qBOLD parameter estimates. In |
| 15 | particular, DBV overestimation peaks for vessels with radii from 20 to 30 μ m and is OEF |
| 16 | dependent. This results in the systematic underestimation of OEF. |
| 17 | In vivo implications: The impact on in vivo qBOLD measurements was investigated |
| 18 | by simulating a distribution of vessel sizes with a small number of discrete radii. |
| 19 | Overestimation of DBV consistent with previous experiments was observed, which was also |
| 20 | found to be OEF dependent. This results in the progressive underestimation of the measured |
| 21 | OEF. Furthermore, the relationship between the measured OEF and the true OEF was found |
| 22 | to be dependent on echo time and spin echo displacement time. |
| 23 | The results of this study demonstrate the limitations of current ASE based qBOLD |
| 24 | measurements and provides a foundation for the optimisation of future acquisition |
| 25 | approaches. |
| | |

1 Introduction

| 2 | The quantitative BOLD (qBOLD) technique is a relaxometry based approach for mapping |
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| 3 | oxygen extraction fraction (OEF) and deoxygenated blood volume (DBV) in the human brain |
| 4 | (He and Yablonskiy, 2007). An elevated OEF is indicative of tissue at risk of infarction, such |
| 5 | as the penumbral tissue surrounding the core infarct of an ischaemic stroke (Astrup et al., |
| 6 | 1981). When combined with a measurement of cerebral blood flow (CBF), the cerebral |
| 7 | metabolic rate of oxygen consumption (CMRO ₂) can also be estimated (Kety and Schmidt, |
| 8 | 1948). Since qBOLD can provide this valuable information in a non-invasive and rapidly |
| 9 | acquired manner, it has a great deal of potential for providing these quantitative physiological |
| 10 | measurements in clinical research applications. |
| 11 | The analytical model used to analyse qBOLD data assumes that the signal decay |
| 12 | behaves as though it were in the static dephasing regime (SDR) i.e. the diffusion of water in |
| 13 | tissue does not influence the signal decay due to magnetic field inhomogeneity (Yablonskiy |
| 14 | and Haacke, 1994). However, simulations of the Gradient Echo Sampling of Spin Echo |
| 15 | (GESSE) pulse sequence, which is often used to acquire qBOLD data, have shown that this is |
| 16 | not the case and that diffusion introduces a vessel size dependent effect on the signal decay |
| 17 | (Dickson et al., 2010; Pannetier et al., 2014). However, qBOLD data can also be acquired |
| 18 | using the Asymmetric Spin Echo (ASE) pulse sequence, and it is unclear whether a similar |
| 19 | effect is observed in these experiments (An and Lin, 2003; Stone and Blockley, 2017). |
| 20 | Interestingly estimates of DBV made using this ASE based acquisition are systematically |
| 21 | higher than those reported for GESSE based measurements (He and Yablonskiy, 2007), |
| 22 | suggesting that different effects may be at play. |
| 23 | The overestimation of DBV by ASE based qBOLD is at least partially responsible for |
| 24 | the underestimation of the OEF (Stone and Blockley, 2017). This overestimation has |
| 25 | previously been suggested to be due to the presence of intravascular blood signal, which is |
| | |

| 1 | not accounted for in the analytical qBOLD model, with flow crushing gradients proposed as a |
|----------------------------------|---|
| 2 | solution (An and Lin, 2003). However, since it has been shown that diffusion results in |
| 3 | additional signal attenuation (Dickson et al., 2010), which is similarly unaccounted for in the |
| 4 | analytical qBOLD model, this may also provide a mechanism for DBV overestimation. |
| 5 | In this study, we investigate both mechanisms to discover whether either can account |
| 6 | for the overestimation of DBV in ASE based qBOLD. The effect of diffusion on the |
| 7 | extravascular tissue signal was examined using Monte Carlo simulations (Boxerman et al., |
| 8 | 1995a) and the intravascular blood signal was simulated using a recently published analytical |
| 9 | model (Berman and Pike, 2018). Whilst these effects are initially considered using |
| 10 | simulations with vessels of a single radius, these results are also integrated using an in vivo |
| 11 | vessel size distribution to investigate sources of systematic error in real world measurements. |
| 12 | |
| 13 | Theory |
| 14 | Transverse signal decay results from dephasing of the net magnetisation due to the presence |
| 15 | |
| | of magnetic field inhomogeneity at multiple scales. The effect of these scales on the qBOLD |
| 16 | of magnetic field inhomogeneity at multiple scales. The effect of these scales on the qBOLD signal can be considered with reference to a spin echo pulse sequence. At the microscopic |
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| | signal can be considered with reference to a spin echo pulse sequence. At the microscopic |
| 17 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins |
| 17 18 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins that are rapidly varying. Due to this rapid magnetic field variation, the phase evolution cannot |
| 17 18 19 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins that are rapidly varying. Due to this rapid magnetic field variation, the phase evolution cannot be rewound by the application of a refocussing pulse. The resulting signal decay is described |
| 17 18 19 20 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins that are rapidly varying. Due to this rapid magnetic field variation, the phase evolution cannot be rewound by the application of a refocussing pulse. The resulting signal decay is described by the irreversible transverse relaxation rate R_2 . The macroscopic scale describes magnetic |
| 17 18 19 20 21 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins that are rapidly varying. Due to this rapid magnetic field variation, the phase evolution cannot be rewound by the application of a refocussing pulse. The resulting signal decay is described by the irreversible transverse relaxation rate R_2 . The macroscopic scale describes magnetic field inhomogeneity on the scale of the head i.e. due to the nasal sinuses or ear canals. This |
| 17 18 19 20 21 22 | signal can be considered with reference to a spin echo pulse sequence. At the microscopic scale spins experience local magnetic field inhomogeneities caused by neighbouring spins that are rapidly varying. Due to this rapid magnetic field variation, the phase evolution cannot be rewound by the application of a refocussing pulse. The resulting signal decay is described by the irreversible transverse relaxation rate R_2 . The macroscopic scale describes magnetic field inhomogeneity on the scale of the head i.e. due to the nasal sinuses or ear canals. This effect can be reversed by a refocussing pulse due to its static nature, enabling the phase |

| 1 | diffusion becomes increasingly important as the so called Diffusion Narrowing Regime is |
|----|---|
| 2 | approached. The transition between these regimes is dependent on the scale of the magnetic |
| 3 | field inhomogeneity and the distance the spin travels due to diffusion. More precisely, the |
| 4 | characteristic diffusion time ($\tau_d \propto r^2/D$), which is dependent on the radius (r) of the |
| 5 | deoxygenated blood vessel and the diffusion coefficient (D), is on the order of the time taken |
| 6 | by a water molecule to diffuse a distance equivalent to the radius of the vessel (Yablonskiy |
| 7 | and Haacke, 1994). This results in an averaging of the magnetic field distribution surrounding |
| 8 | the vessels and a loss of phase history, meaning that signal cannot be efficiently recovered by |
| 9 | a refocussing pulse. |
| 10 | |
| 11 | Modelling the qBOLD signal |
| 12 | The qBOLD model relies on the known relationship between R_2 and the baseline OEF, E_0 , |
| 13 | and deoxygenated blood volume, V_0 , for a network of randomly oriented blood vessels |

14 approximated as infinite cylinders (Yablonskiy and Haacke, 1994),

$$R_2' = \frac{4}{3}\pi \gamma B_0 \Delta \chi V_0 Hct E_0$$
⁽¹⁾

15 where γ is the proton gyromagnetic ratio, B_0 is the main magnetic field, $\Delta \chi$ is the difference 16 in volume magnetic susceptibility between fully oxygenated and fully deoxygenated blood 17 and *Hct* is the haematocrit. However, further modelling has shown that the R₂'-weighted 18 signal is not purely monoexponential, displaying a quadratic exponential behaviour around 19 the spin echo. Under the assumption that the signal decays in the SDR, the following solution 20 has been found,

$$S(\tau) = S_0 \, e^{-t_E \, R_2} e^{-V f_c(\tau \, R_2'/V)} \tag{2}$$

$$f_c(\tau R'_2/V) = \frac{1}{3} \int_0^1 du \ (2+u) \ \sqrt{1-u} \frac{1-J_0 \ (1.5 \ \tau \ (R'_2/V) \ u)}{u^2}$$
(3)

- 1 where t_E is the echo time, τ is the spin echo displacement time and J_0 is the zeroth-order
- 2 Bessel function (He and Yablonskiy, 2007). For simplicity this continuous function can be
- 3 broken down into two asymptotic solutions and applied piece wise (An and Lin, 2000).

$$S^{S}(\tau) = S_{0}e^{-t_{E}R_{2}}e^{-0.3(\tau R_{2}')^{2}/V}, \qquad \tau < \frac{1.5V}{R_{2}'}$$
(4)

$$S^{L}(\tau) = S_{0}e^{-t_{E}R_{2}}e^{-\tau R_{2}'}e^{V}, \qquad \tau > \frac{1.5 V}{R_{2}'}$$
(5)

In the long τ regime (Eq. (5)) the signal decay takes a monoexponential form, whilst in the short τ regime (Eq. (2)) the signal follows a quadratic exponential form. A log-linear fit to long τ data enables R_2 to be estimated. Furthermore, comparison of the measured signal at $\tau=0$ ($S_{meas}^{S}(0)$) with the intercept extrapolated from long τ data ($S_{extrap}^{L}(0)$) enables V_0 to be calculated.

$$V_0 = \ln S_{extrap}^L(0) - \ln S_{meas}^S(0)$$
(6)

9 Henceforth we will refer to this as the SDR qBOLD model.

10

11 <u>Simulating the effect of diffusion</u>

12 Monte Carlo simulations of the qBOLD signal were performed by repeating the following

13 three steps for each simulated proton.

14 Step 1: Generate a system of vessels. The vessel system was defined as a sphere with 15 radius R_s . Vessel origin points (O) were randomly selected, with half placed on the surface of 16 the sphere and half within the sphere (Dickson et al., 2010). A uniform distribution of points 17 over the surface of the sphere was ensured by generating a unit vector (X_i) from a normally 18 distributed random number generator (mean 0, standard deviation 1) and scaling by R_s 19 (Muller, 1959). Within the sphere, uniform density was maintained by taking account of the 20 increased volume occupied by points far from the centre of the system. This scaling factor, U, 21 is selected from a uniform distribution of random numbers (range 0 to 1).

$$(O_1, O_2, O_3) = \begin{cases} R_s \frac{(X_1, X_2, X_3)}{\sqrt{X_1^2 + X_2^2 + X_3^2}}, & \text{on sphere surface} \\ R_s U \frac{(X_1, X_2, X_3)}{\sqrt{X_1^2 + X_2^2 + X_3^2}}, & \text{within sphere} \end{cases}$$
(7)

1 Vessels are modelled as randomly oriented infinitely long cylinders with a single radius, R_c, 2 placed at the vessel origin points described by Eq. (7) and added until the target volume 3 fraction (V_f) is reached. Random orientation was ensured by generating a unit vector from a 4 normally distributed random number generator (mean 0, standard deviation 1).

5 Step 2: Proton random walk. Protons are initially placed at the centre of the vessel 6 system. Each step taken by the proton is independently selected along each dimension from a 7 normal distribution of random numbers with mean 0 and standard deviation σ with diffusion 8 coefficient, D, and time interval between steps, Δt .

$$\sigma = \sqrt{2 D \Delta t} \tag{8}$$

9 Step 3: Estimate the phase accrued at each step. The phase, $\Delta \phi$, accumulated by the 10 proton during each time interval is calculated by summing over the field contributions from 11 all N vessels (Boxerman et al., 1995a),

$$\Delta \phi = 2\pi \gamma B_0 \Delta t (1 - Y) Hct \Delta \chi \sum_{i=1}^N \left(\frac{R_c}{r_i}\right)^2 \cos 2\varphi_i \sin^2 \theta_i , \qquad r \ge R$$
(9)

12 where θ is the angle of the vessel with respect to B_0 , φ is the angle with respect to the 13 projection of B_0 onto a plane orthogonal to the vessel, r_i is the perpendicular distance to the 14 vessel and Y is the blood oxygen saturation. Only the equation for the magnetic field outside 15 of the vessel is presented, since only extravascular signal was simulated.

16 By appropriate combination of the phase accrued in each interval it is possible to 17 simulate the phase evolution of the ASE and GESSE pulse sequences as a function of τ , 18 φ(τ).

$$\phi(\tau) = \sum_{j=1}^{m} \Delta \phi_j - \sum_{j=m+1}^{n} \Delta \phi_j$$
(10)

where *m* defines the transition from signal decay to signal recovery due to the refocussing pulse, *n* is the point at which the signal is acquired and where $0 \le m \le n$. For ASE m = $(t_E - \tau) / 2 \Delta t$ and $n = t_E / \Delta t$, whilst for GESSE $m = t_{SE} / 2 \Delta t$ and $n = (t_{SE} + \tau) / \Delta t$. Here, t_E is defined as the timing of the centre of the readout and t_{SE} is the time at which the spin echo forms (see Fig. 1). These definitions reflect an important distinction between the ASE and GESSE pulse sequences, whereby t_E is fixed for ASE and variable for GESSE whilst t_{SE} is variable for ASE and fixed for GESSE.

8 The phase evolution of *P* protons is then summed to simulate the decay of the
9 extravascular ASE or GESSE signal (Boxerman et al., 1995a),

$$S_{EV}(t_E, \tau) = \left| \frac{1}{P} \sum_{k=1}^{P} e^{i \phi(\tau)} \right| e^{-\frac{t_E}{T_{2,t}}}$$
(11)

10

11 where $T_{2,t}$ is the underlying tissue T_2 .

12 Intravascular signal has traditionally been difficult to simulate, with empirical measurements of blood R_2 and R_2^* commonly used (Griffeth and Buxton, 2011). However, 13 simulating the R_2' -weighted signal using the difference between R_2 and R_2^* is likely to be 14 15 inaccurate in the short τ regime. Recently an analytical model of the blood signal during a 16 Carr-Purcell Meiboom-Gill (CPMG) pulse sequence was extended to capture the signal 17 evolution between an arbitrary number of spin echoes (Berman and Pike, 2018), i.e. the 18 conditions that exist for ASE and GESSE pulse sequences. Using this model, the 19 intravascular signal, S_{IV} , is described by,

$$S_{IV}(t_E,\tau) = \exp\left\{-\frac{\gamma^2}{2}G_0\tau_D^2\left[\frac{t_E}{\tau_D} + \left(\frac{1}{4} + \frac{t_E}{\tau_D}\right)^{\frac{1}{2}} + \frac{3}{2} - 2\left(\frac{1}{4} + \frac{t_E - t_{SE}/2}{\tau_D}\right)^{\frac{1}{2}} - (12)\right\}\right\}$$

$$2\left(\frac{1}{4}+\frac{t_{SE}/2}{\tau_D}\right)^{\frac{1}{2}}\right] \exp\left(-\frac{t_E}{T_{2,b|0}}\right).$$

1 Here $\tau_D = R_{rbc}^2/D_b$, where R_{rbc} is the characteristic size of red blood cells and D_b is the

2 diffusion coefficient of blood, $T_{2,b|0}$ is the intrinsic T₂ of blood and G₀ is the mean square field

3 inhomogeneity in blood,

$$G_0 = \frac{4}{45} Hct (1 - Hct) (4 \pi \Delta \chi (0.95 - Y) B_0)^2.$$
(13)

4 The value of t_{SE} is fixed for GESSE but is variable for ASE with $t_{SE} = t_E - \tau$. By definition

5 t_E is fixed for ASE and varying for GESSE.

Finally, the total signal, *S_{TOT}*, is calculated by taking a volume weighted sum of the
intra- and extravascular signals.

$$S_{TOT} = (1 - V_f) S_{EV} + V_f S_{IV}$$
(14)

8

9 Methods

10

11 <u>Simulations</u>

12 Simulations of the tissue signal were performed following the theory outlined above. Firstly, 13 extravascular signal decay was simulated using Monte Carlo simulations (B₀=3 T, $\gamma = 267.5 \times 10^6$ rad s⁻¹ T⁻¹). The radius of the spherical system of vessels, U, was chosen to 14 15 maintain a similar number of vessels, N, regardless of the vessel radius ($N \sim 1,300$). For each 16 proton, a complete random walk was generated with a step size, Δt , of 20 µs, which was downsampled to 200 µs, and $D=1 \text{ µm}^2 \text{ms}^{\mathbb{Z}^1}$. The perpendicular distance, r_i , to each vessel in 17 the system was then calculated. For protons that passed close to vessels, defined as $R_c^2/r_i^2 >$ 18 19 0.04, the perpendicular distance was recalculated using the original 20 µs time step to better 20 sample the rapid magnetic field variation expected close to vessels (Dickson et al., 2010). 21 Walks that moved the proton inside a vessel were flagged to be discarded in order to simulate

| 1 | non-permeable blood vessels. The phase of each proton was allowed to evolve for 120 ms |
|----|---|
| 2 | after the excitation with $\Delta \chi$ =0.27 ppm (Spees et al., 2001). Phase accrual was stored for each |
| 3 | proton in 2 ms intervals, Δt . A new system of vessels was generated for each proton and a |
| 4 | total of 10,000 protons were simulated for each vessel radius investigated. However, the |
| 5 | number of protons that passed within a vessel increased rapidly for smaller vessel radii. |
| 6 | Therefore, only the first P=5,000 protons that did not pass within a vessel were used to |
| 7 | calculate S_{EV} using Eq. (11) with $T_{2,t}=80$ ms. Secondly, intravascular signal decay was |
| 8 | simulated using Eqs. (12) and (13), which are independent of vessel radius. Based on |
| 9 | previous work the following parameters were used (Berman et al., 2017): $T_{2,b 0}=189$ ms, |
| 10 | $R_{rbc}=2.6 \ \mu m$ and $D_b=2 \ \mu m^2 m s^{-1}$. The total signal was then calculated using Eq. (14). |
| 11 | Whilst the intravascular simulations are rapid to perform, Monte Carlo simulations of |
| 12 | the extravascular signal are time consuming. Therefore, the following approaches were taken |
| 13 | to accelerate these simulations, with examples presented as supplementary figures. We have |
| 14 | previously shown that different oxygenation levels can be simulated by scaling the accrued |
| 15 | phase of a nominal oxygenation value by the target value (Blockley et al., 2008). This is |
| 16 | made possible by saving the phase of each proton and the fact that phase is a linear function |
| 17 | of blood oxygenation for a network of vessels with the same oxygenation (Fig. S1). Different |
| 18 | volume fractions can be simulated from the signal magnitude generated by Eq. (11). It has |
| 19 | been shown that the extravascular signal, S_{EV} , can be described as a radius dependent shape |
| 20 | function, $f(R_c, \tau)$, scaled by the volume fraction (Dickson et al., 2011; Kiselev and Posse, |
| 21 | 1999) (Fig. S2). |

$$S_{EV}(R_c,\tau) = \exp\left[-V_f(R_c)f(R_c,\tau)\right]$$
(15)

Finally, it is possible to simulate the effect of a system with multiple vessel radii by
combining multiple single vessel radius simulations of the extravascular signal (Dickson et
al., 2011; Kiselev and Posse, 1999). The resulting combined signal, *S_{EV}^{MULTI}*, can be calculated

- 1 as the product of the signals of M single vessel simulations which have already been scaled
- 2 for blood oxygenation and volume fraction as described above (Fig. S3).

$$S_{EV}^{MULTI} = \prod_{k=1}^{M} S_{EV}(k)$$
(16)

3

4 Parameter quantification

- 5 The following framework was used to quantify the parameters of the qBOLD model from the
- 6 simulated decay curves. The parameters of the SDR qBOLD model (R_2 and DBV) were
- 7 organised as a vector of unknowns (x) in a linear system (A·x=B) (Stone et al., 2019). The
- 8 first row of the matrix A represents Eq. (4) when $\tau=0$ with subsequent rows representing Eq.
- 9 (5) with values of τ beyond the transition between the quadratic and linear exponential
- 10 regime. In this case only values of τ greater than 15 ms were used. Vector B contains the
- 11 ASE signals, $S(\tau)$.

$$\begin{bmatrix} 0 & 0 & 1 \\ 1 & -\tau_1 & 1 \\ 1 & -\tau_2 & 1 \\ \vdots & \vdots & \vdots \\ 1 & -\tau_n & 1 \end{bmatrix} \begin{bmatrix} V_0 \\ R_2' \\ \log(S_0) - t_E \cdot R_2 \end{bmatrix} = \begin{bmatrix} \log(S(0)) \\ \log(S(\tau_1)) \\ \log(S(\tau_2)) \\ \vdots \\ \log(S(\tau_n)) \end{bmatrix}$$
(17)

Parameters were estimated via Eq. (17) using the least square solution, with the error in each
parameter determined from the covariance matrix. Finally, OEF can be estimated by
rearranging Eq. (1).

$$E_0 = \frac{3 \cdot R'_2}{4\pi \cdot \gamma B_0 \cdot \Delta \chi_0 \cdot Hct \cdot V_0}$$
(18)

15

16 Effect of diffusion on ASE measurements

17 Initial simulations were performed for a selection of vessel radii ($R_c=5$, 10, 50, 1000 μ m), a

- venous Y of 60%, a Hct of 40% and a DBV of 3%. Simulations of the ASE pulse sequence
- 19 were performed with t_E=60 ms and -60 ms $\leq \tau \leq 60$ ms for both extra- and intravascular

signal, where τ=60 ms corresponds to pure gradient echo decay. For validation purposes,
 similar simulations were performed for the GESSE pulse sequence using t_{SE}=60 ms and -30
 ms ≤ τ ≤ 60 ms.

4

5 Effect of diffusion on qBOLD parameters

6 A further set of synthetic ASE signal decay curves were generated for vessel radii 7 logarithmically spaced between 1 and $1,000 \,\mu\text{m}$. All other parameters were set consistent 8 with previous qBOLD measurements (Stone and Blockley, 2017). In the context of these 9 simulations this required $t_E=80$ ms with $\tau=0$ and $\tau=16$ to 64 ms in 4 ms steps. The apparent 10 value of $R \Box'$, DBV and OEF were then estimated using Eq. (17) and (18). The effect of 11 diffusion on the estimation of qBOLD parameters was investigated by first fixing OEF and 12 varying DBV and then by fixing DBV and varying OEF. In the former case a fixed OEF of 13 40% was coupled with DBV values of 1, 3 and 5%, whilst in the latter case DBV was fixed at 14 3% and OEF took values of 20, 40 and 60%. These values are considered to be the true 15 parameters in both cases. The results of varying DBV were also used to consider the 16 percentage error in DBV as a function of vessel radius. In these single vessel simulations 17 arterial blood is assumed to have an oxygen saturation, Y, of 100% hence the venous 18 saturation, $Y_{\nu} = 1 - E_0$.

The effect of intravascular signal on qBOLD parameter estimates was investigated by repeating these simulations, but excluding the intravascular compartment. In this way it was possible to quantify the percentage of the parameter estimate (PE) which results from the presence of intravascular signal i.e. $(PE_{EV} - PE_{EV+IV})/PE_{EV+IV}$.

Further investigation of the effect of diffusion on DBV estimates was pursued based on a consideration of Eq. (6), which suggests that errors must be due to either the signal measured at $\tau=0$ ($S_{meas}^{s}(0)$) or the extrapolated estimate of the signal at $\tau=0$ from the R₂' fit 1 $(S_{extrap}^{L}(0))$, or both. However, given the analysis approached represented by Eq. (17) 2 $S_{extrap}^{L}(0)$ is not estimated and $S_{meas}^{S}(0)$ is confounded by T₂ decay. The latter was corrected 3 by calculating the signal decay relative to the value at R=1,000 µm, where previous 4 simulations would suggest the SDR applies and hence signal attenuation should be zero. The 5 former was estimated by subtracting this relative measure of $S_{meas}^{S}(0)$ from the estimated 6 value of apparent DBV.

7

8 Effect of an *in vivo* vessel radius distribution

9 The *in vivo* effect of a distribution of vessel radii was investigated by integrating the results 10 from single radius simulations. A compartmental model of the vasculature derived from the 11 morphology of the sheep brain was selected (Sharan et al., 1989). This model has five orders 12 of arterial and venous vessels, with a range of radii, and a capillary compartment with a 13 single vessel radius (Table 1). Additional Monte Carlo simulations for this range of vessel 14 radii were performed and combined using the acceleration techniques described above. 15 Arterial vessels were assigned an arterial oxygen saturation, Y_a , of 98%, which was used to 16 calculate the venous saturation, Y_v , for a given OEF.

$$Y_{\nu} = Y_a (1 - E_0) \tag{19}$$

The capillary compartment was an intermediate oxygen saturation, Y_c, calculated as an
average of the arterial and venous saturations weighted by a factor, κ, equal to 0.4
representing a weighting towards the venous saturation (Griffeth and Buxton, 2011; Tsai et
al., 2003).

$$Y_c = \kappa Y_a + (1 - \kappa) Y_v \tag{20}$$

Relative blood volume fractions for each vessel type were calculated by estimating the
volume of each vessel radius population as cylinders with the properties described in Table 1.
These relative blood volume fractions were then scaled by the total cerebral blood volume

1 (CBV). Pairs of OEF and CBV values were drawn from a uniform random number generator 2 within the following ranges: OEF 0-100%, CBV 0-10%. The qBOLD parameters were 3 quantified for 1,000 random OEF-CBV pairs to examine the effect of diffusion across the 4 physiological range. In the absence of a strict definition of DBV, the ground truth was 5 assumed to be equal to the combined blood volume occupied by capillary and venous vessels. 6 This is therefore only a working assumption, since it is likely the *true* DBV is weighted by 7 blood oxygenation and vessel radius. Deoxyhaemoglobin content, dHb, was calculated based 8 on the same assumption for DBV and a value for the density of brain tissue ρ =1.04 g/ml 9 (Rempp et al., 1994) using the following equation.

$$dHb = 100 \frac{V_0}{\rho} \frac{Hct}{0.03} E_0$$
(21)

10 For comparison these simulations were also repeated for the original ASE based qBOLD

11 implementation with $t_E=64$ ms with $\tau=0$ and $\tau=10$ to 18 ms in 4 ms steps (An and Lin, 2003).

Details on how to access the simulation code, simulation results and analysis codethat underlie this study can be found in Appendix A.

14

15 Results

Figure 2 presents simulations of the signal generated by the ASE pulse sequence in the absence of T_2 decay. The extravascular signal (Fig. 2a) was found to be symmetric with respect to the spin echo (τ =0) regardless of vessel radius. Similarly, the intravascular signal (Fig. 2b) was symmetric, but displayed a relatively weak signal decay as a function of τ . In contrast, simulations of the GESSE pulse sequence demonstrated increasing asymmetry with reducing vessel radius for the extravascular signal and strong asymmetry for the intravascular signal (Fig. S4).

Figure 3 displays the effect of vessel size on the parameter estimates from the SDR
qBOLD model. The apparent values of R₂' plateau above a critical vessel radius of

| 1 | approximately 40 μ m (Fig. 3a,d) and are then consistent with predictions from the SDR |
|----------|---|
| 2 | qBOLD model (dashed lines calculated using Eq. (1)). The apparent DBV is found to be |
| 3 | strongly dependent on vessel radius, peaking between 20 and 30 μ m (Fig. 3b,e). Estimates of |
| 4 | the apparent OEF increase monotonically with vessel radius reaching the value predicted by |
| 5 | the SDR qBOLD model as the vessel radius approaches 1,000 μ m (Fig. 3c,f). When the true |
| 6 | OEF was fixed whilst DBV was varied (Fig. 3c) estimates of apparent OEF were consistent |
| 7 | across DBV levels, suggesting that the error in DBV is a linear scale factor. Likewise, it can |
| 8 | be seen that the profile of apparent DBV when the true DBV was fixed and OEF was varied |
| 9 | (Fig. 3e) peak at different vessel radius values, suggesting that the error in DBV is OEF |
| 10 | dependent. Furthermore, this effect can be seen to result in a reduced dynamic range for the |
| 11 | estimates of apparent OEF as vessel size is reduced (Fig. 3f). Figure 4 confirms that the |
| 12 | percentage error in DBV is constant for a given combination of OEF and vessel radius (Fig. |
| 13 | 4a), but differs for different OEF values (Fig. 4b). |
| 14 | Figure 5 considers the contribution of intravascular signal to the parameter estimates |
| 15 | in Fig. 3 as a function of vessel radius. This contribution is generally small for R_2^{\prime} and DBV |
| 16 | at around $\pm 1\%$ for vessel radii greater than 10 μ m. However, the intravascular signal appears |
| 17 | to reflect a larger contribution when OEF is low, conditions where qBOLD contrast is low. |
| 18 | Despite this the effect of the intravascular signal appears to be largely cancelled in the |
| 19 | estimation of OEF (Fig. 5c,f). A reproduction of Fig. 3 without intravascular signal is |
| 20 | included in the supplementary material for comparison and shows little discernible difference |
| 21 | by eye (Fig. S5). |
| 22 | Figure 6 investigates the origin of the DBV estimation error attributed either to an |
| 23 | error in the measured signal at $\tau=0$ (orange markers) or an error in the intercept extrapolated |
| 24 | from long τ data (green markers). In the case of the former, $-\ln S_{meas}^{S}(0)$ is plotted such that |
| <u>-</u> | |

25 the sum of the two curves representing the apparent DBV (represented by grey shading).

When interpreting these curves, it is useful to consider the orange markers as a reflection of
the deviation of the spin echo from perfect refocusing (with positive values representing
increased signal attenuation) and the green markers as a reflection of the deviation of the
measured R₂' from the SDR qBOLD estimate of R₂'. The former is found to be subject to
increasing signal attenuation as vessel size is reduced, which is strongly affected by blood
oxygenation via OEF. The latter is found to plateau and is relatively consistent with the SDR
qBOLD model for vessel radii greater than approximately 20 μm.

8 Figure 7 explores the combined effect of a distribution of vessel radii on parameter 9 estimates from the SDR qBOLD model. The apparent R_2 is plotted against values of R_2 10 predicted by the SDR model via Eq. (1), with DBV estimated according to the working 11 assumption described above (Fig. 7a). Data points are colour coded to reflect the true voxel deoxyhaemoglobin content in ml^{dHb}/100 g^{tissue}. A linear dependence is maintained, albeit with 12 13 a shallower gradient than predicted by the SDR qBOLD model. A large amount of 14 uncertainty is observed in estimates of apparent DBV over the large physiological range 15 tested (Fig. 7b), with data points colour coded by true OEF value. However, this level of 16 uncertainty does not propagate into estimates of apparent OEF (Fig 7c) where data points are 17 colour coded by true DBV. Apparent OEF increases monotonically between 0 and 50%, but 18 reaches a plateau for higher values, and is inappropriately scaled compared with the true 19 OEF. In a similar manner to Fig. 4, the percentage error in the apparent DBV can be plotted 20 as a function of true OEF (Fig. 8). As noted for the single vessel radius simulations, this error 21 is strongly OEF dependent.

These simulations were repeated for different ASE pulse sequence parameters,
namely variations in t_E and τ, and included in supplemental material. The results in Fig. S6
largely mirror those in Fig. 7 with the following variations. The slope of the relationship
between apparent R₂' and SDR qBOLD predicted R₂' is slightly reduced for the alternative

parameters (Fig. S6a). More noticeable is the reduction in the range of apparent DBV values
 (Fig. S6b), with the error in the apparent DBV reduced by more than a half (Fig. S7). Whilst
 the apparent OEF is also inappropriately scaled, the relationship with true OEF is more
 monotonic in nature.

5

6 **Discussion**

7 In this study numerical simulations were used to investigate the effect of diffusion on ASE 8 based qBOLD measurements and the origin of DBV overestimation in such measurements. In 9 contrast to the previously observed shift of the GESSE signal maximum due to the effect of 10 diffusion, the ASE signal was observed to maintain its symmetry as vessel radius is reduced 11 and the effect of diffusion is increased. Two hypotheses for the origin of the observed DBV 12 overestimation were tested: (i) the effect of intravascular blood signal and (ii) the effect of 13 diffusion on the extravascular tissue signal. The presence of intravascular blood signal was 14 found to have a minor effect on qBOLD parameter estimates. It is therefore unlikely to be 15 responsible for the majority of the overestimation observed in DBV measurements. In 16 contrast, the extravascular signal was shown to have a very strong dependence on vessel 17 radius providing the potential for a large error in DBV and is considered to be the dominant 18 cause of DBV overestimation. Furthermore, the error in DBV is predicted to be blood oxygen 19 saturation level dependent. Integration of these single vessel radius simulations via an in vivo 20 vessel distribution revealed three main findings. Firstly, that the relationship between the 21 apparent R_2' and deoxyhaemoglobin content is retained. Secondly, there is an inherent 22 uncertainty in estimates of DBV. Finally, this uncertainty is not propagated to apparent OEF 23 estimates, but results in inappropriate scaling of these estimates. Furthermore, the monotonic 24 behaviour of the relationship between apparent and true OEF was found to be dependent on 25 the pulse sequence parameters t_E and τ . These results provide new directions for improving

| 1 | the modelling of ASE qBOLD signal and the reduction of systematic error in parameter |
|---|--|
| | |

- 2 estimates of OEF and DBV.
- 3

4 Effect of diffusion on ASE measurements

5 Whilst several studies have investigated the qBOLD signal as acquired by the GESSE pulse 6 sequence (Christen et al., 2014; Dickson et al., 2011, 2010; Pannetier et al., 2014), this study 7 considered whether the signal decay under an ASE acquisition behaves in the same way. One 8 particular characteristic of the GESSE pulse sequence concerns the maximum of the qBOLD 9 signal decay curve. This would ordinarily be expected to coincide with the spin echo (τ = 0), 10 but has been shown to be shifted towards negative τ values (Fig. S4a) for the GESSE 11 sequence in the presence of diffusion (Dickson et al., 2010; Pannetier et al., 2014). However, 12 this effect is not observed in simulations of the extravascular signal acquired using an ASE 13 pulse sequence (Fig. 2a), where the signal maximum was found to be close to the spin echo 14 (τ =0). However, the GESSE and ASE sequences differ in an important way. The t_E of each 15 successive τ value increases in the GESSE experiment and hence the time for protons to 16 diffuse around blood vessels increases. Whilst the t_E is constant for all τ values in the ASE 17 method and hence the time for diffusion is also constant. This would suggest that there is a t_E 18 dependent component of the R_2 '-weighted signal decay. Such a component has previously 19 been included as a correction to estimates of R_2' (Berman et al., 2017). 20 This study also considered the R_2 '-weighted contribution of the blood to the qBOLD 21 signal using a recently proposed model (Berman and Pike, 2018). In common with the 22 extravascular results, the ASE blood signal is symmetric with respect to the spin echo, but 23 decays far less as a function of τ (Fig. 2b). However, the signal is heavily attenuated at all τ 24 values compared with the extravascular simulations. This is in contrast to simulations of the

GESSE blood signal, which are highly shifted to negative τ values and present largely as an
 exponential decay (Fig. S4b).

3

4 Origin of DBV overestimation

5 Simulations of the combined intravascular and extravascular signal revealed a vessel radius 6 dependent overestimation of DBV (Fig. 3b,e). The error in the apparent DBV was found to 7 be OEF dependent (Fig. 4). However, at larger radii (approaching 1 mm) estimates of DBV 8 were consistent with ground truth values. The contribution of intravascular signal to these 9 parameter estimates was performed by comparing simulations with (Fig. 3) and without (Fig. 10 S5) an intravascular compartment. A small and largely vessel radius independent effect (for 11 $R_c>10 \ \mu$ m) was observed (Fig. 5b,e). The effect of intravascular signal was more pronounced 12 for smaller vessel radii and low OEF, where the relative contribution of intravascular signal is 13 increased by weak extravascular contrast. Despite this, the overestimation of DBV is 14 dominated by the effect of diffusion on the extravascular signal. 15 Finally, Eq. (6) provides the opportunity to consider whether the systematic error in DBV originates in the measurement of the spin echo $(S_{meas}^{s}(0))$, the intercept extrapolated 16 from the long τ regime $(S_{extrap}^{L}(0))$ or a combination of both, as explored in Fig. 6. For 17 vessel radii greater than 20 μ m additional signal attenuation of $S_{meas}^{S}(0)$ is the main driver of 18 overestimation of DBV. However, for vessels with radii below 20 μ m, errors in $S_{extrap}^{L}(0)$ 19 20 provide an additional confound to DBV estimation. These results are consistent with the 21 characteristics of gradient echo versus spin echo BOLD vessel size sensitivity, which correspond to $\ln S_{extrap}^{L}(0)$ and $\ln S_{meas}^{S}(0)$, respectively (Boxerman et al., 1995b). For the 22 23 smallest vessel radii the apparent R_2' is reduced relative to the value expected by the SDR qBOLD model (Fig. 3a,d) due to diffusional narrowing, such that $\ln S_{extrap}^{L}$ (0) is also 24 25 reduced (Fig. 6). Similarly, additional unrecoverable signal decay due to diffusion narrowing

| 1 | results in a decrease in the value of $\ln S_{meas}^{s}(0)$, which is analogous to an increase in |
|---|--|
| 2 | apparent $R\square$ and is strongest for capillary sized vessels (Note that Fig. 6 plots |
| 3 | $-\ln S_{meas}^{s}(0)$). With increasing vessel radius, R \Box ' approaches the SDR qBOLD model |
| 4 | prediction and the value of $\ln S_{extrap}^{L}(0)$ approaches a constant value. Similarly the |
| 5 | attenuation of the spin echo is reduced as the SDR is approached and $\ln S_{meas}^{s}(0)$ reaches its |
| 6 | minimum. Therefore, when the differing profiles of these phenomena are combined the form |
| 7 | of the apparent DBV as a function of vessel radius can be described. |
| 8 | |
| 9 | Effect of an in vivo vessel radius distribution |

Having established the vessel radius dependence of the qBOLD signal, the implications for 10 11 the *in vivo* condition were considered. In order to integrate the single vessel radius results, a 12 vessel distribution with a small number of discrete vessel radii was selected. This enabled 13 different oxygenation levels to be associated with different vessel types. A wide 14 physiological range was investigated by randomly selecting pairs of OEF and CBV values. 15 The apparent R_2 was found to be tightly correlated with the R_2 predicted by SDR qBOLD 16 model (Fig. 7a). This is important as it demonstrates that the relationship between R_2' and the 17 voxel deoxyhaemoglobin content (proportional to the product of deoxyhaemoglobin 18 concentration and DBV) is maintained despite the effects of diffusion. It should therefore be 19 possible to quantify maps of R₂' in terms of deoxyhaemoglobin content with appropriate 20 scaling. Likewise with improved quantification of DBV, either through improvements to the 21 qBOLD technique or via an additional experimental technique (Blockley et al., 2013; Lee et 22 al., 2018), accurate measurements of OEF are possible. A large amount of uncertainty was 23 observed in the apparent DBV (Fig. 7b). This was demonstrated to be blood oxygenation 24 dependent i.e. a function of OEF (Fig. 8). This is consistent with the results of the single 25 vessel simulations (Fig. 4) and demonstrates the important contribution of smaller vessel

| 1 | radii. This also explains why this uncertainty does not propagate into the apparent OEF, since |
|----|--|
| 2 | the percentage error in apparent DBV is constant at each OEF level (Fig. 7c). However, the |
| 3 | increasing percentage error in apparent DBV with OEF (Fig. 8) results in a progressive |
| 4 | underestimation of apparent OEF. A plateau in the apparent OEF limits the maximum |
| 5 | measured OEF to approximately 50%. Despite this the remaining range covers the majority |
| 6 | of the expected healthy physiological range (Marchal et al., 1992). These simulation were |
| 7 | repeated for an alternative set of ASE pulse sequence parameters, replicating the effects |
| 8 | observed for R_2' and DBV (Fig S6a,b and Fig. S7). However, a monotonic relationship |
| 9 | between apparent and true DBV was revealed suggesting that a shorter t_{E} and/or maximum τ |
| 10 | value could enable the technique to be sensitive to a broader range of OEF values. |
| 11 | Finally, the results of these multi-radius simulations appear to be consistent with |
| 12 | previous measurements of OEF=21±2% and DBV=3.6±0.4% (Stone and Blockley, 2017). |
| 13 | Under the assumption that a true OEF of 40% is healthy, Fig. 7 would predict an apparent |
| 14 | OEF of 23%. Likewise Fig. 8 would predict the percentage error in the apparent DBV is |
| 15 | 100%, which would reduce the measured value above to 1.8%. This would bring these |
| 16 | measurements in line with other MR based measurements of DBV at 1.75% (He and |
| 17 | Yablonskiy, 2007) and venous CBV at 2.2% (Blockley et al., 2013). |
| 18 | |
| 19 | Future work and Limitations |
| 20 | Whilst the simulation methodology used in this study has identified some limitations of the |
| 21 | current implementation of ASE based qBOLD, it also offers an opportunity to optimise future |
| 22 | implementations. Further simulations could be used to identify optimal values of t_{E} and τ |
| 23 | which maximise the linearity of the relationship between apparent OEF and the ground truth. |
| | |

24 They could also be used to estimate a more appropriate scale factor for OEF estimation by

| 1 | treating the $\frac{4}{3}\pi$ geometry factor in Eq. (1) as an arbitrary scale factor. Such an approach has |
|--|--|
| 2 | previously been used in calibrated BOLD to great effect (Griffeth and Buxton, 2011). |
| 3 | The results of this study rely on a detailed model of the qBOLD signal. However, in |
| 4 | this implementation it only accounts for the intra- and extravascular signal contributions of a |
| 5 | single distribution of blood vessels in grey matter. Whilst this two compartment model was |
| 6 | sufficient to investigate the origin of DBV overestimation in ASE based qBOLD, a more |
| 7 | realistic model might include the signal contributions of cerebral spinal fluid (Dickson et al., |
| 8 | 2009), the myelin in white matter (Bouvier et al., 2013), desaturated arterial blood vessels |
| 9 | (Boas et al., 2008), the effect of iron deposition (Wismer et al., 1988) or different vessel |
| 10 | radius distributions (Germuska et al., 2013; Lauwers et al., 2008). As such these |
| 11 | contributions to the qBOLD signal may also provide fertile ground for future exploration. |
| 12 | |
| | |
| 13 | Conclusion |
| 13 14 | Conclusion The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in |
| | |
| 14 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in |
| 14 15 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by |
| 14 15 16 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular |
| 14 15 16 17 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small |
| 14 15 16 17 18 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small contribution. Integrating the results of single vessel simulations using an <i>in vivo</i> distribution |
| 14 15 16 17 18 19 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small contribution. Integrating the results of single vessel simulations using an <i>in vivo</i> distribution of vessel radii revealed several limitations of current measurements and provides a |
| 14 15 16 17 18 19 20 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small contribution. Integrating the results of single vessel simulations using an <i>in vivo</i> distribution of vessel radii revealed several limitations of current measurements and provides a |
| 14 15 16 17 18 19 20 21 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small contribution. Integrating the results of single vessel simulations using an <i>in vivo</i> distribution of vessel radii revealed several limitations of current measurements and provides a foundation for future optimisation of ASE based qBOLD acquisitions. |
| 14 15 16 17 18 19 20 21 21 22 | The ASE qBOLD signal decay was found to be symmetric with respect to the spin echo, in contrast to previous simulation of the GESSE pulse sequence. Overestimation of DBV by ASE based qBOLD was found to be dominated by the effect of diffusion on extravascular signal decay, with the presence of intravascular blood signal having only a small contribution. Integrating the results of single vessel simulations using an <i>in vivo</i> distribution of vessel radii revealed several limitations of current measurements and provides a foundation for future optimisation of ASE based qBOLD acquisitions. |

1 Appendix A

- 2 The results of the simulations performed in this study can be accessed via the Oxford
- 3 University Research Archive, doi: https://doi.org/10.5287/bodleian:mvPY99a9D.
- 4 Furthermore, the code used to generate these simulation results and to analyse experimental
- 5 data can be downloaded from the Zenodo repository, doi:
- 6 https://doi.org/10.5281/zenodo.2586624. Supplementary data related to this article can be
- 7 found at <<u>DOI></u>.
- 8

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Tables

Table 1. Vascular compartment model described by (Sharan et al., 1989). Radius, length and number of vessels were used to calculate the relative volume fractions for each compartment with and without arteriolar vessels.

| | | Arterioles | | | Capillary | | | Venules | | | |
|-------------------------|------|---------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|---------------------|------|
| | al | a2 | a3 | a4 | a5 | с | v5 | v4 | v3 | v2 | v1 |
| Radius (µm) | 60 | 30 | 15 | 10 | 5 | 2.8 | 7.5 | 15 | 22.5 | 45 | 90 |
| Length (µm) | 5390 | 2690 | 1350 | 900 | 450 | 600 | 450 | 900 | 1350 | 2690 | 5390 |
| Number of vessels | 1880 | 1.5×10^{4} | 1.15×10 ⁵ | 3.92×10 ⁵ | 3.01×10 ⁶ | 5.92×10 ⁷ | 3.01×10 ⁶ | 3.92×10 ⁵ | 1.15×10 ⁵ | 1.5×10^{4} | 1880 |
| Relative vol. frac. (%) | 4.3 | 4.3 | 4.1 | 4.1 | 4.0 | 32.6 | 8.9 | 9.3 | 9.2 | 9.6 | 9.6 |
| (all vessel types) | | | | | | | | | | | |
| Relative vol. frac. (%) | | | | | | 41.2 | 11.3 | 11.7 | 11.6 | 12.1 | 12.1 |
| (excluding arterioles) | | | | | | | | | | | |

Figures

Fig. 1. By combining the phases generated by the Monte Carlo simulations different pulse sequences can be simulated. The cumulative sum of the phase accumulated after the 180° refocussing pulse is subtracted from the cumulative sum of the phases accumulated prior to the refocussing pulse. In a standard spin echo pulse sequence (a) the refocussing pulse is placed midway between the 90° excitation pulse and the echo time (t_E), which is equal to the spin echo time (t_{sE}). The GESSE pulse sequence (b) introduces R_2' -weighting through the parameter τ by altering t_E , whilst keeping t_{sE} constant. Note: each value of τ is acquired at a different t_E . The ASE sequence (c) introduces R_2' -weighting the refocussing pulse by a time $\tau/2$ leading to a change in t_{sE} , although t_E is kept constant. By convention positive values of τ occur when the $t_E > t_{sE}$ and negative values occur when $t_E < t_{sE}$.

(a) Spin Echo (SE) ¦90° 180° t_{SE} t_E τ=0 + + + + + (b) GESSE ¦90° 180° $\tau > 0$ + + + + + + ¦90° 180° t_E t_{SE} τ<0 + + + (c) ASE ¦90° 180° tse t_E $\tau > 0$ + + + +90° 180° t_{SF} t_E τ ·<0 + + + + + + +

Combination of accumulated phase

Fig. 2. Examples of the signal decay from the ASE pulse sequence as a function of vessel radius. (a) The extravascular signal (S_{EV}) decay is observed to be symmetric with respect to τ =0 regardless of vessel radius. (b) The intravascular signal (S_{IV}) decay shows considerable signal attenuation which is symmetric and varies weakly with τ .

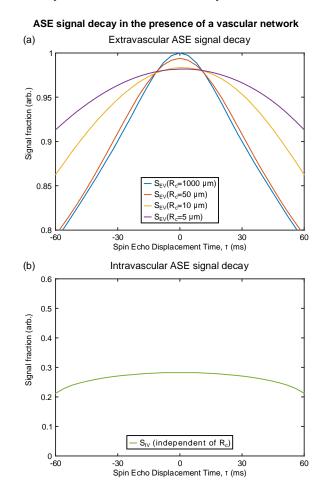


Fig. 3. Investigation of the effect of vessel radius on the parameter estimates derived from ASE based qBOLD. Simulations were first performed with a fixed OEF (E_0 =40%) and three DBV values (top) then with a fixed DBV (V_0 =3%) and three values of OEF (bottom). The apparent R_2' (left) is estimated for each OEF-DBV pair and presented alongside the R_2' values predicted by the SDR qBOLD model (dashed lines). Likewise the apparent DBV (centre) and apparent OEF (right) are presented alongside the true DBV and OEF, respectively, (dashed lines).

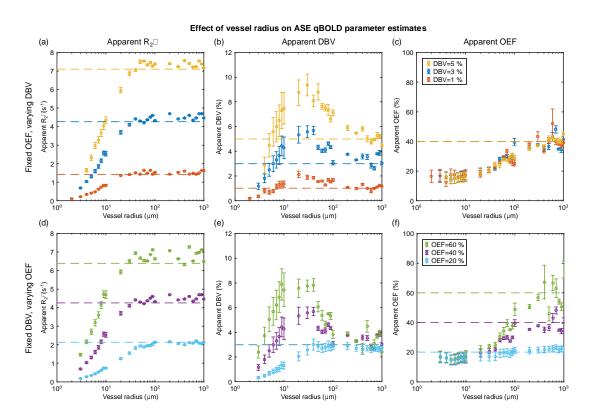


Fig. 4. Estimation of the percentage error in DBV at each of the three simulated values with

(a) fixed $E_0=40\%$, varying DBV and (b) fixed $V_0=3\%$, varying E_0 .

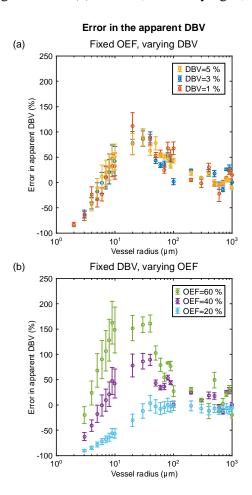


Fig. 5. Investigation of the contribution of intravascular signal to qBOLD parameter estimates (PE) presented in Fig. 3. This contribution was quantified as the percentage difference between PEs simulated with and without intravascular signal i.e. $(PE_{EV} - PE_{EV+IV})/PE_{EV+IV}$. Extravascular only PE results can be found in supplementary materials (Fig. S5).

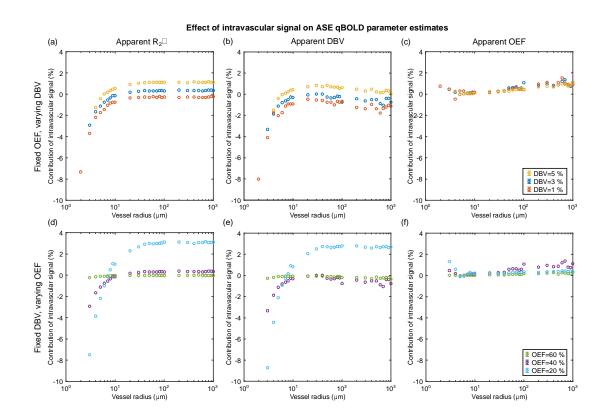


Fig. 6. Investigation of the origin of the overestimation of the measured DBV for three different OEF values; (a) $E_0=60\%$, (b) $E_0=40\%$, (c) $E_0=20\%$ (true $V_0=3\%$). The orange markers represents natural log of the measured signal at $\tau=0$, plotted here as $-\ln S_{meas}^S(0)$, whilst the green markers represent the log of the intercept extrapolated from long τ data points ($\ln S_{extrap}^L(0)$). The sum of these curves is the apparent DBV as in Fig. 3 and represented here by the grey shaded area. Dashed lines display the prediction made by the SDR qBOLD model.

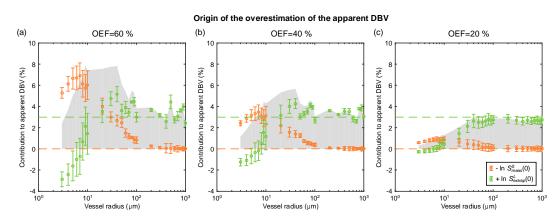


Fig. 7. The effect of multiple vessel radii simulations on the qBOLD parameter estimates was considered by generating many pairs of OEF and CBV values. ASE pulse sequence parameters were t_E =80 ms with τ =0 and τ =16 to 64 ms in 4 ms steps following the work of (Stone and Blockley, 2017). (a) The apparent R₂' is linearly dependent on the R₂' predicted by the SDR model, but with a different gradient. (b) A large amount of uncertainty in the apparent DBV is observed. (c) The apparent OEF appears to plateau beyond 50%, but monotonically increases with true OEF for lower values. Markers are coloured to reflect true dHb content, true OEF and true DBV for parts (a), (b) and (c), respectively.

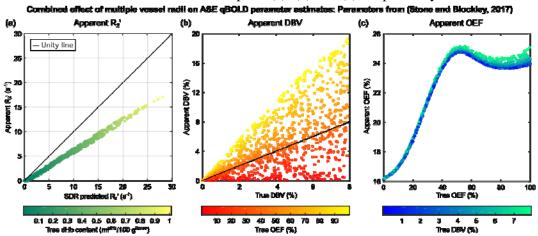
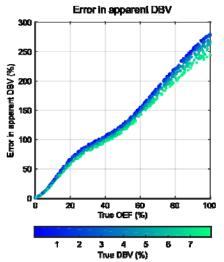


Fig. 8. The uncertainty in DBV in Fig. 7 was investigated by plotting apparent DBV as a function of true OEF. ASE pulse sequence parameters follow the work of (Stone and Blockley, 2017). The results suggest that the error in the apparent DBV is OEF dependent. Markers are coloured to reflect their true DBV.



Multiple vessel radii: Parameters from (Stone and Blockley, 2017)