

1 Growth and adaptation mechanisms of tumour spheroids with 2 time-dependent oxygen availability

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7 **Abstract**

8 Tumours are subject to external environmental variability. However, *in vitro* tumour spheroid
9 experiments, used to understand cancer progression and develop cancer therapies, have been
10 routinely performed for the past fifty years in constant external environments. Furthermore,
11 spheroids are typically grown in ambient atmospheric oxygen (normoxia), whereas most *in vivo*
12 tumours exist in hypoxic environments. Therefore, there are clear discrepancies between *in*
13 *vitro* and *in vivo* conditions. We explore these discrepancies by combining tools from exper-
14 imental biology, mathematical modelling, and statistical uncertainty quantification. Focusing
15 on oxygen variability to develop our framework, we reveal key biological mechanisms govern-
16 ing tumour spheroid growth. Growing spheroids in time-dependent conditions, we identify and
17 quantify novel biological adaptation mechanisms, including unexpected necrotic core removal,
18 and transient reversal of the tumour spheroid growth phases.

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19 **1 Introduction**

20 *In vivo* tumours are subject to various types of environmental variability, for example due to fluctuating oxygen and nutrient availability [1–4]. To study cancer progression and develop cancer therapies, tumour spheroid experiments have been successfully and routinely performed for the past 22 fifty years [2, 5–12]. However, tumour spheroid experiments are typically performed in constant 24 environments and focus on the overall size of spheroids [2, 13–18]. By experimentally controlling 25 oxygen availability and using mathematical modelling and statistical uncertainty quantification, we 26 develop a new framework to study the impact of external environmental variability on the growth of 27 tumour spheroids and their internal structure. Using our framework we identify and quantify novel 28 biological adaptation mechanisms driven by environmental variability. This work begins to bridge 29 the gap between *in vitro* and *in vivo* conditions, and lays the foundation for future experimental, 30 mathematical, and statistical spheroid studies.

31 Oxygen availability is of particular importance since it is vital to the effectiveness of cancer 32 therapies, such as chemotherapy and radiotherapy [1, 19, 20], and can be controlled in spheroid 33 experiments. However, spheroid experiments are typically performed in ambient atmospheric conditions 34 (21% oxygen), sometimes referred to as normoxia [13, 16]. In contrast, untreated tumours 35 typically grow in variable hypoxic conditions (0.3–4.2% oxygen) [1, 20–22]. While many single-cell 36 studies, and some spheroid studies, explore the role of environmental variability [2, 22–27], oxygen 37 parameters critical to reproduce results are commonly not reported [28].

38 To visualise spheroid growth in normoxia, hypoxia, and time-dependent oxygen conditions we 39 use fluorescent ubiquitination cell cycle indicator (FUCCI) transduced cell lines and hypoxia markers 40 (Figure 1a–e) [13, 14, 29, 30]: nuclei of cells in gap 1 (G1) phase fluoresce red, shown in magenta 41 for clarity (Figure 1d); nuclei of cells in synthesis, gap 2, and mitotic (S/G2/M) phases fluoresce 42 green (Figure 1d); and, regions of hypoxia are indicated by cyan (Figure 1b,c,e). Spheroids grown 43 in constant normoxia experience three phases of growth (Figure 1a–c,f). In phase (i) spheroids grow 44 exponentially as all cells are able to proliferate, indicated by the presence of cells in the S/G2/M 45 phases throughout the tumour spheroid shown by green (Figure 1a). In phase (ii) cells in the central 46 region of the spheroid arrest in G1 phase while cells at the periphery continue to proliferate resulting 47 in inhibited growth (Figure 1b). This arrested region is thought to arise due spatial differences in 48 nutrient availability, possibly oxygen, and/or a build up of metabolic waste from cells. In phase 49 (iii) the spheroid is characterised by three regions: a central region composed of a necrotic core, 50 $0 < r < R_n(t)$; an intermediate region of living but proliferation-inhibited cells, $R_n(t) < r < R_i(t)$; 51 and, a region at the periphery composed of living and proliferating cells, $R_i(t) < r < R_o(t)$ (Figure 52 1c). In comparison to spheroids grown in normoxia, spheroids grown in hypoxia form their necrotic 53 core earlier, the distance from the edge of the spheroid to the hypoxic region and overall size are 54 smaller (Figure 2).

55 To investigate environmental variability we perform additional experiments in time-dependent

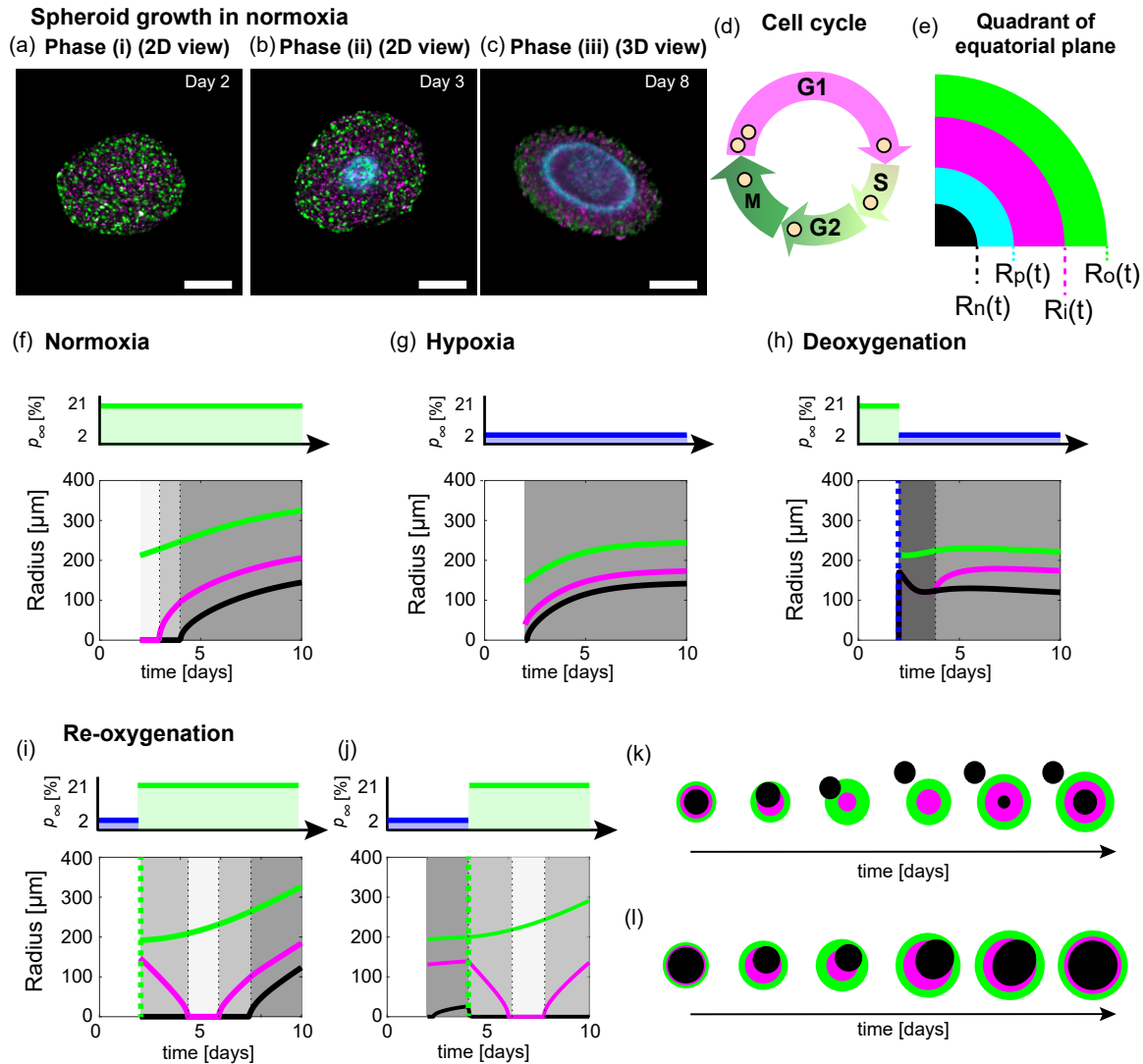


Figure 1: Impact of external environment on the structure of growing tumour spheroids: a focus on oxygen availability. (a-c) Tumour spheroid growth in standard experimental protocols occurs in three phases. Experimental images shown for Fucci-transduced human melanoma WM983b spheroids grown in normoxia. (a-b) Experimental images of the equatorial plane of spheroids on Day 2 and 3 after seeding. (c) 3D z-stack representation of half of a spheroid on Day 8 after seeding. Scale bars are 200 μ m. Colours in (a-c) correspond to cell cycle schematic shown in (d): cells in G1 phase (magenta) and cells in S/G2/M phase (green). Pimonidazole staining reveals the hypoxic regions of spheroid (cyan). (e) Schematic for spherically symmetric spheroid structure representing a quadrant of the equatorial plane of a spheroid. Spheroids in normoxia experience three phases of growth, resulting in a spheroid with three regions at later times: a central region composed of a necrotic core, $0 < r < R_n(t)$ (black); an intermediate region of living but proliferation-inhibited cells, $R_n(t) < r < R_i(t)$ (magenta); and, a region at the periphery composed of living and proliferating cells, $R_i(t) < r < R_o(t)$ (green). The hypoxic radius, $R_p(t)$ (cyan) satisfies $R_n(t) \leq R_p(t) \leq R_o(t)$. (f-j) Schematics for oxygen conditions and time evolution of spheroid structure and overall size in (f) normoxia, (g) hypoxia, (h) deoxygenation experiments, and (i-j) re-oxygenation experiments. Note in (i-j) spheroids transiently undergo the growth phases in reverse. Greyscale shading in (f-j) represent growth phases. (k-l) Spheroid schematics showing (k) necrotic core removal and (l) movement of necrotic core without removal.

56 oxygen conditions. In these experiments we observe various tumour spheroid adaptation mechanisms
57 (Figure 1h-l). For instance, in re-oxygenation experiments we discover a novel adaptation process
58 where the necrotic core of the spheroid that has formed prior to re-oxygenation moves within the
59 spheroid and in certain situations exits the spheroid as a single object (Figure 1k). Further, for
60 fifty years tumour spheroid growth has been described by three sequential growth phases but re-
61 oxygenation experiments show that spheroids can transiently experience these phases in the reverse
62 order (Figure 1i,j). Other observations from these experiments agree with intuitive expectations,
63 but have not previously been explored nor quantified.

64 Throughout this study we quantitatively analyse experimental data using mathematical modelling
65 and statistical uncertainty quantification. We start with the seminal Greenspan mathematical model
66 [10, 15, 16, 31]. Greenspan's model describes the three phases of growth and is relatively simple in
67 comparison to other models [31–34]. This simplicity is a great advantage. We are able to extend
68 the model to analyse environmental variability while retaining physical and biologically insightful
69 interpretations of results. Further, by using parameter identifiability analysis, with both profile
70 likelihood and Bayesian inference approaches, we estimate key biological parameters and reveal
71 biological adaptation mechanisms.

72 In the following we first analyse spheroid experiments in normoxia and hypoxia. Such experiments
73 demonstrate that Greenspan's model describes the experimental data remarkably well. Further, that
74 oxygen mechanisms accurately describe the growth and formation of the necrotic core, whereas other
75 mechanisms, possibly waste mechanisms, likely result in the growth and formation of the inhibited
76 region. We then extend the mathematical model to interpret deoxygenation and re-oxygenation
77 experiments, providing quantitative insights to biological adaptation mechanisms throughout. We
78 conclude by describing the unexpected behaviours observed in re-oxygenation experiments.

2 Results

Here we focus on WM983b spheroids in normoxia, hypoxia and deoxygenation experiments. Similar results for WM793b and WM164 spheroids are discussed in Supplementary Discussion E - F. For re-oxygenation experiments, we compare results from WM983b and WM793b spheroids as we observe a range of behaviours. In Supplementary Discussion F we discuss additional WM164 re-oxygenation experiments.

2.1 Oxygen diffusion alone is insufficient to describe spheroid growth

We capture end-point equatorial plane images for spheroids grown in normoxia and hypoxia measuring $R_o(t)$, $R_i(t)$, $R_n(t)$, and $R_p(t)$ (Figure 2a,c,d,f) (Methods: Image processing). These measurements are remarkably consistent within each condition and time point (Figures 2c,f). Comparing spheroids grown in normoxia and hypoxia, we observe vastly different tumour growth dynamics and internal structure ($\xi_n(t) = R_n(t)/R_o(t)$, $\xi_i(t) = R_i(t)/R_o(t)$, $\xi_p(t) = R_p(t)/R_o(t)$), even when comparing spheroids of similar size (Figures 2c,f, S21).

For deeper mechanistic insight we use mathematical modelling and statistical uncertainty quantification to interpret our observations. Specifically, we show that Greenspan's mathematical model [10] accurately describes spheroid growth in both normoxia and hypoxia. Then using parameter estimation we identify biological mechanisms that differ between normoxia and hypoxia. Key model details are now discussed, for further details see Methods 4.1.1 and Supplementary Discussion C.1. The model assumes each spheroid is spherically symmetric and maintained by cell-cell adhesion or surface tension. The independent variables are time t [days], and radial position, r [μm]. Conservation of volume gives an equation describing the time evolution of the outer radius, $R_o(t)$ [μm],

$$R_o^2(t) \frac{dR_o(t)}{dt} = \frac{s}{3} [R_o^3(t) - \max(R_i^3(t), R_n^3(t))] - \lambda R_n^3(t), \quad (1)$$

where s [day^{-1}] is the rate at which cell volume is produced by mitosis per unit volume of living cells, and λ [day^{-1}] is the proportionality constant describing the rate at which cell volume is lost from the necrotic core. In these experiments, Equation (1) simplifies as $R_i(t) \geq R_n(t)$. This restricts our attention to two interpretations of the model that differ with respect to how $R_i(t)$ is defined. In the following discussion, we refer to these interpretations as *hypotheses* and show that hypothesis 2, where oxygen mechanisms drive $R_n(t)$ and waste mechanisms drive $R_i(t)$, is more consistent with the spheroids considered in this study.

In hypothesis 1 (Figure 3a), oxygen diffuses with diffusivity, k [$\text{m}^2 \text{s}^{-1}$], and is consumed by living cells at a constant rate, α [$\text{m}^3 \text{kg}^{-1} \text{s}^{-1}$]. The external oxygen partial pressure is p_∞ [%]. Oxygen diffusion is fast relative to the growth of the spheroid, so that the oxygen partial pressure within the

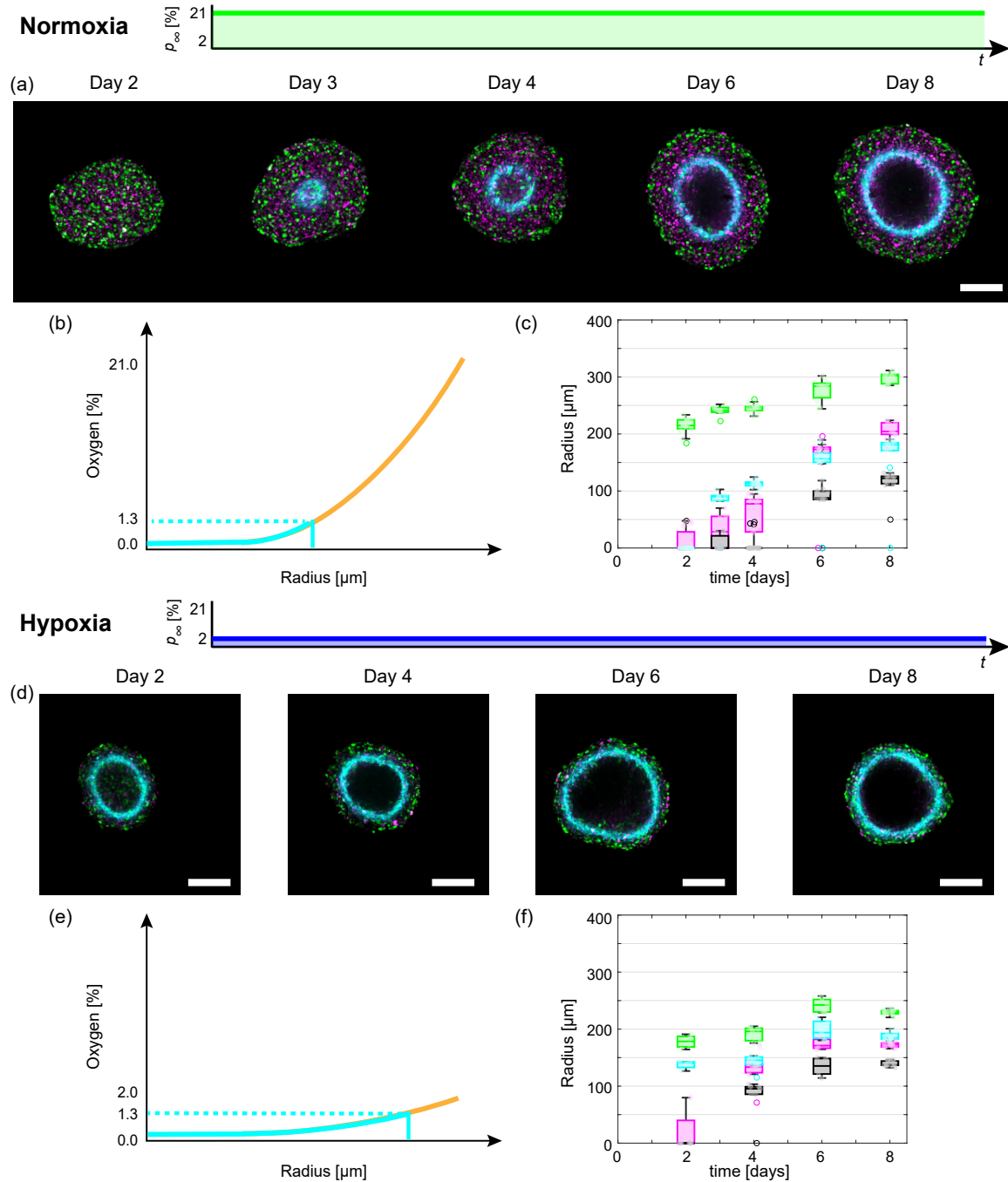


Figure 2: Tumour spheroid growth in normoxia and hypoxia. (a,d) Experimental images of the equatorial plane of Fucci-transduced WM983b spheroids grown in (a) normoxia (21% oxygen) and (b) hypoxia (2% oxygen). (a) Images shown on Day 2, 3, 4, 6, and 8 after seeding. (d) Images shown in Day 2, 4, 6, and 8 after seeding. Scale bars are 200 μm . (b,e) Schematics for oxygen partial pressure within spheroids for (b) normoxia and (e) hypoxia. (c,f) Time-evolution of $R_o(t)$ (green), $R_i(t)$ (magenta), $R_n(t)$ (black), and $R_p(t)$ (cyan) for spheroids grown in (c) normoxia, and (f) hypoxia. Note that each spheroid measurement is an end-point measurement.

110 spheroid, $p(r(t))$ for $0 \leq r \leq R_o(t)$, is governed by

$$\frac{k}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial}{\partial r} p(r(t)) \right) = \Omega \alpha \text{H}(r - R_n(t)) \text{H}(R_o(t) - r), \quad 0 \leq r \leq R_o(t), \quad (2)$$

111 where $\text{H}(\cdot)$ is the heaviside function and Ω [mmHg kg m⁻³] is a conversion constant from volume of
112 oxygen per unit tumour mass to oxygen partial pressure [35]. The inhibited radius, $R_i(t)$, is implicitly
113 defined by $p(r(t)) = p_i$ [%] provided the oxygen partial pressure is sufficiently large (Figure 3a), and
114 $R_i(t) = 0$ otherwise.

115 In hypothesis 2 (Figure 3b), diffusible metabolic waste is produced by living cells at a constant rate
116 per unit volume, P [mol μm^{-3} day⁻¹], and diffuses with diffusivity κ [μm^2 day⁻¹]. Waste diffusion
117 is fast relative to the growth of the spheroid, so the waste concentration within the spheroid, $\beta(r(t))$
118 [mol μm^{-3}], is governed by

$$\frac{\kappa}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial}{\partial r} \beta(r(t)) \right) = -PH(r - R_n(t)) \text{H}(R_o(t) - r), \quad 0 \leq r \leq R_o(t). \quad (3)$$

119 The inhibited radius, $R_i(t)$, is implicitly defined through $\beta(r(t)) = \beta_i$ [mol μm^{-3}] provided the waste
120 concentration is sufficiently large (Figure 3b), and $R_i(t) = 0$ otherwise.

121 Both hypothesis 1 and 2 assume that $R_n(t)$ is implicitly defined by $p(R_n(t)) = p_n$ provided the
122 oxygen partial pressure is sufficiently small, and $R_n(t) = 0$ otherwise. Informed by experimental
123 results [35], we set $p_n = 0$ [%].

124 Analysis of the model provides an analytical expression for the time when the inhibited region
125 forms (Equation 7.1). For hypothesis 2, the inhibited region is predicted to form at the same time
126 independent of oxygen dynamics, provided the spheroids grown in normoxia and hypoxia are initially
127 the same size. This appears consistent with results in Figure 2a-d where the inhibited region has
128 formed on day 2 for both conditions. In contrast, with hypothesis 1 the time to form the inhibited
129 region depends on oxygen mechanisms and specifically p_∞ , but without knowledge of additional
130 parameters further insights are unclear.

131 By incorporating statistical uncertainty quantification to estimate parameters of the model we
132 gain further mechanistic insights. A key assumption common to hypothesis 1 and 2 is that oxygen
133 diffusion and consumption drives the time evolution of $R_n(t)$. We test this assumption directly by
134 analysing radius measurements of each spheroid at each time point independently [35]. Using mea-
135 surements of $R_o(t)$ and $R_n(t)$ we estimate: the outer radius when the necrotic region first forms, R_c ;
136 α ; and $R_p(t)$ (Figure 3c-d, Supplementary Discussion D.1.1). Image processing to measure $R_p(t)$ is
137 more challenging than for $R_o(t)$ due to gradients in the pimonidazole signal (Supplementary Discus-
138 sion B). However, after careful image processing we find good agreement between experimentally
139 measured and predicted values of $R_p(t)$ ($R^2 = 0.749$, Figure 3e). This approach allows us to esti-
140 mate the oxygen partial pressure within each spheroid at each time point (Figure 3g-h). From the
141 results in Figures 3e,g,h, S22 we conclude that oxygen of diffusion alone is a reasonable and sufficient
142 mechanism to describe the formation of the necrotic core in WM983b spheroids [35]. Furthermore,

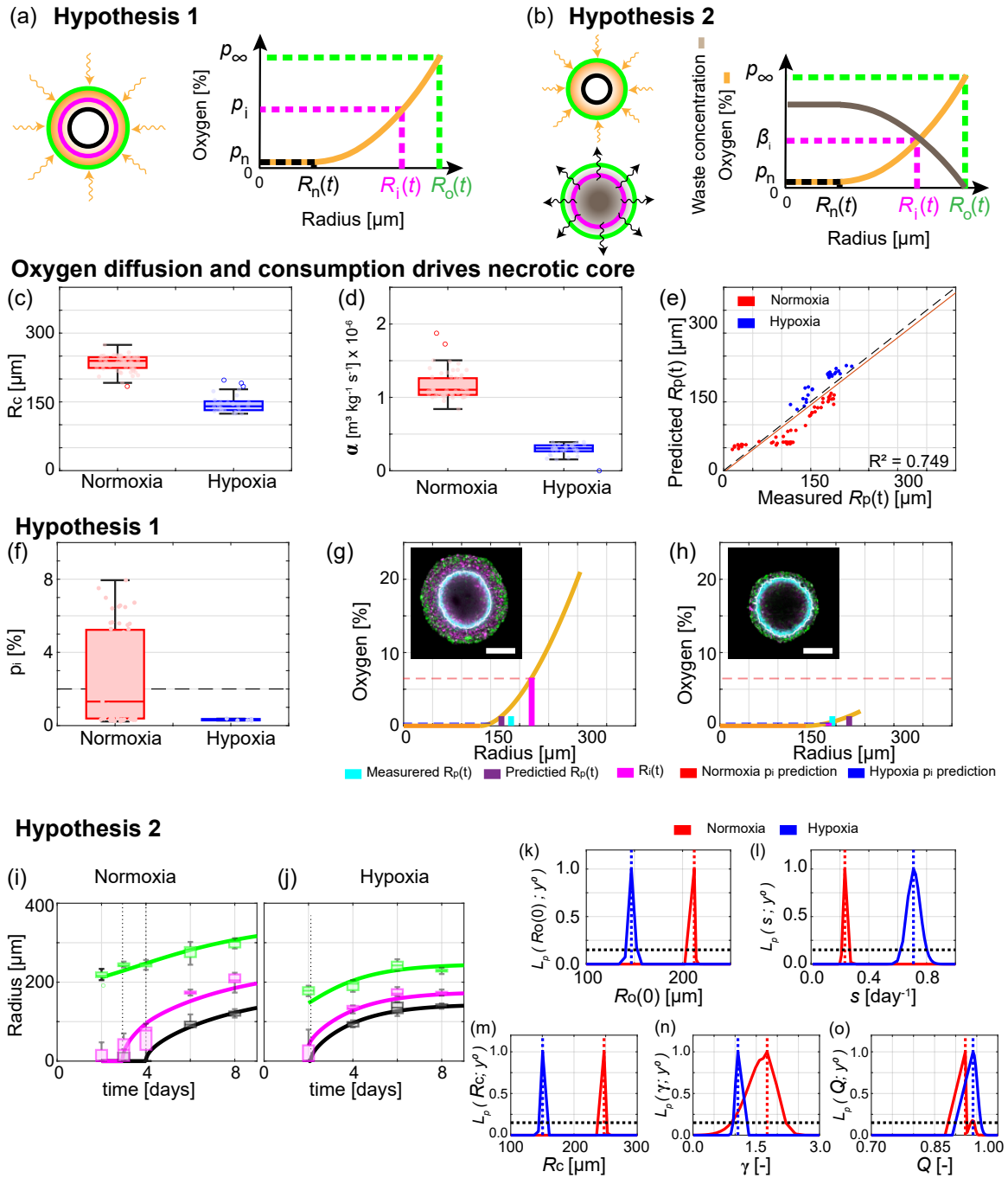


Figure 3: (Caption next page).

Figure 3: Mechanisms governing tumour spheroid growth in normoxia and hypoxia. (a,b) Schematics for two hypotheses. (a) Oxygen mechanisms describe $R_i(t)$ and $R_n(t)$. (b) Oxygen mechanisms describe $R_n(t)$ and waste mechanisms describe $R_i(t)$. (c-e) Oxygen diffusion and consumption describes $R_n(t)$. (c) Box chart for estimated outer radius when necrotic region forms, R_c [μm]. (d) Box chart for estimated oxygen consumption rate, α [$\text{m}^3 \text{kg}^{-1} \text{s}^{-1}$]. (e) Comparison of measured and predicted $R_p(t)$. (f) Box chart for estimated oxygen partial pressure defining inhibited region from hypothesis 1, p_i [%]. (g-h) Estimated oxygen partial pressure within (g) a spheroid grown in normoxia and (h) a spheroid grown in hypoxia. Insets in (f,g) show Fucci signal and pimonidazole staining from Day 8 and 6, respectively, with scale bar is $200 \mu\text{m}$. In (c-f) data points for normoxia and hypoxia shown in red and blue, respectively. (i,j) Comparison of experimental data with Greenspan's mathematical model simulated with the maximum likelihood estimates of parameters for (i) normoxia and (j) hypoxia. Time-evolution of outer radius, $R_o(t)$ (green), inhibited radius, $R_i(t)$ (magenta), and necrotic radius, $R_n(t)$ (black). Data represent an average of twelve spheroids on days 2, 3, 4, 6, and 8 for spheroids grown in normoxia and an average of seven spheroids on days 2, 4, 6, and 8 for spheroids grown in hypoxia (Methods: Experimental methods 4.3). (k-o) Profile likelihoods for (k) initial outer radius, R_o [μm], (l) proliferation rate, s [day^{-1}], (m) outer radius when necrotic region first forms, R_c [μm], (n) dimensionless parameter relating proliferation rate and mass loss from necrotic core, γ [-], and (o) dimensionless parameter relating oxygen and waste mechanisms, Q [-] (Methods 4.1.1).

143 these results suggest that the following assumptions are reasonable: $p_n = 0$; a constant oxygen con-
144 sumption rate within the spheroid; spherical symmetry; oxygen at the edge of the spheroid can be
145 approximated with the oxygen settings on the incubator.

146 Given that $R_n(t)$ is reasonably described by oxygen mechanisms we now examine hypothesis 1.
147 Hypothesis 1 assumes that oxygen mechanisms alone drive the time evolution of $R_i(t)$. We then
148 estimate p_i using the estimated oxygen partial pressure within each spheroid, $p(r(t))$ for $0 < r <$
149 $R_o(t)$, measurements of $R_i(t)$ and the definition $p(R_i(t)) = p_i$ (Figure 3a,g,h). Estimates of p_i are
150 consistently larger for spheroids grown in normoxia compared to spheroids grown in hypoxia (Figure
151 3f). This is inconsistent with hypothesis 1. Specifically, results from normoxia suggest that spheroids
152 grown in hypoxia should have larger inhibited regions than experimentally measured (Figure 3g,h).
153 Similarly, results from spheroids grown in hypoxia suggest that spheroids grown in normoxia should
154 have smaller inhibited regions than experimentally measured. These results provide strong evidence
155 to suggest that oxygen alone is insufficient to describe the formation of the inhibited region across
156 multiple oxygen conditions for this cell line, consistent with results for other cell lines [17].

157 To test hypothesis 2, which assumes that waste mechanisms drive the time evolution of $R_i(t)$,
158 we first analyse measurements of each spheroid at each time point independently. Experimentally
159 measuring waste within spheroids is challenging, so we estimate the waste concentration within each
160 spheroid and use measurements of $R_i(t)$ to estimate the outer radius when the inhibited region first
161 forms, $\mathcal{R} = \beta_i \kappa / P$ (Figure S23). We observe that \mathcal{R} is larger for spheroids grown in normoxia than
162 hypoxia, which may be due to changes in β_i or P or κ (Figure S23). These results do not provide
163 sufficient evidence to reject hypothesis 2.

164 To test whether hypothesis 2 is reasonable we estimate model parameters for spheroids grown in
165 normoxia and hypoxia. Specifically, we estimate the five key parameters: $\Theta_g = (R_o(0), s, R_c, \gamma, Q)$,
166 where $\gamma = \lambda/s$ [-] and Q [-] are dimensionless quantities (Methods 4.2). Simulating the model

167 with the maximum likelihood estimate (MLE), $\hat{\Theta}_n$, for normoxia shows good agreement with the
168 experimental data from spheroids grown in normoxia (Figure 3i). Similarly, simulating the model at
169 $\hat{\Theta}_h$ for hypoxia shows good agreement with the experimental data from spheroids grown in hypoxia
170 (Figure 3j). These results suggest the model accurately captures the dynamics of tumour spheroid
171 growth.

172 Alongside the point estimates $\hat{\Theta}_n$ and $\hat{\Theta}_h$, we are interested in forming approximate 95% con-
173 fidence intervals for each of the parameters. To perform this analysis we employ profile likelihood
174 analysis (Methods 4.2). All profile likelihoods computed here are narrow and well-formed around a
175 single central peak, the MLE, indicating that parameters are identifiable and that a relatively narrow
176 range of parameters give a similar match to the data as the MLE (Figure 3k-o) [16]. Approximate
177 95% confidence intervals are obtained from these profile likelihoods for each parameter. The profile
178 likelihoods for the initial outer radius, $R_o(0)$, do not overlap and agree with observations that $R_o(0)$
179 is smaller for spheroids grown in hypoxia than normoxia (Figure 3k). The profile likelihood for s
180 interestingly estimates that the rate of cell proliferation per unit volume is faster in hypoxia than
181 normoxia (Figure 3l). This result may seem surprising as a simplistic assumption would be that less
182 oxygen results in less proliferation. However, our result is consistent with observations from other cell
183 lines where an intermediate level of hypoxia encourages more proliferation than normoxia [36–38].
184 Profile likelihoods for R_c are consistent with estimates of R_c obtained by analysing spheroid mea-
185 surements independently, a good consistency check for the two methods (Figure 3c,m). The other
186 profile likelihoods for γ and Q overlap suggesting that these parameters are consistent across nor-
187 moxic and hypoxic conditions (Figure 3n,o). Posterior densities and prediction intervals, estimated
188 using Bayesian inference, also show good agreement with results here and the experimental data
189 (Figure S24). Similar results hold for the other two cell lines (Supplementary Discussion E-F).

190 In the remainder of this study, we take the most fundamental approach and proceed with
191 Greenspan’s mathematical model and interpret the governing mechanisms with hypothesis 2. We
192 note that other biological mechanisms may also be relevant. However, as the model already appears
193 to capture the key dynamics (Figure 3i,j) we will avoid overcomplicating the model. Furthermore, in
194 the following analysis of deoxygenation and re-oxygenation experiments we necessarily extend the
195 model.

196 2.2 Adaptation to deoxygenation

197 The mechanisms underlying how tumour spheroids adapt to time-dependent external environments
198 is unclear. Here, we perform a series of deoxygenation experiments, where spheroids grown in nor-
199 moxia are transferred to hypoxic conditions at $t = t_s$ [days]. Analysing spheroid snapshots reveals
200 how spheroids, and in particular their internal structure, adapt. Extending Greenspan's mathe-
201 matical model and using parameter estimation, we identify and quantify key biological adaptation
202 mechanisms.

203 In the deoxygenation experiments we set $p_\infty = 21$ [%] for $0 < t \leq t_s$ [days], $p_\infty = 2$ [%] for
204 $t_s < t < 8$ [days], and $t_s = 2$ [days] (Figure 4a). At $t_s = 2$ [days] all spheroids are in phase (i) of
205 growth with proliferating cells throughout and no inhibited or necrotic region (Day 2 of Figure 4b).
206 At $t_s + 1$ [days] the FUCCI signal in the central region of the spheroid is blurred, relative to the
207 signal at the periphery, indicating dying and dead cells (Day 3 of Figure 4b, Figure S20). Therefore,
208 we identify this central region as the necrotic core (Supplementary Discussion B). Experimental
209 images at later times show that $R_n(t)$, $R_i(t)$ and $R_p(t)$ continue to increase but at a much slower
210 rate (Days 4-8 of Figure 4b,c). Throughout the experiment $R_o(t)$ remains approximately constant
211 (Days 2-8 of Figure 4b,c) confirming that the most important changes involve the internal structure
212 and not the overall spheroid size. Further, $\xi_n(t)$, $\xi_i(t)$, and $\xi_p(t)$ approach values observed at late
213 times for spheroids grown in hypoxia (Figure 4c, S25).

214 To interpret these deoxygenation experiments we extend Greenspan's mathematical model [10].
215 We assume that the change in p_∞ at t_s is instantaneous, which is reasonable since the switch from
216 normoxia to hypoxia requires only 1-2 minutes when the spheroids are transferred between incu-
217 bators. This time is very short in comparison to the duration of the experiment and time interval
218 between data points. Similarly, we assume that the oxygen partial pressure within the spheroid
219 adapts to the change in p_∞ instantaneously, which is reasonable since oxygen takes approximately
220 10 seconds to diffuse across a distance of 100 μm [10]. Then we estimate the oxygen partial pressure
221 within the spheroid at t_s under normoxic and hypoxic conditions (Methods 4.1.2, Figure 4d). Imme-
222 diately after t_s the predicted necrotic radius, denoted $R_n^+(t)$ and implicitly defined by $p(R_n^+(t)) = 0$,
223 is greater than the actual necrotic radius, $R_n(t)$, specifically $R_n^+(t) > R_n(t)$ (Figure 4d-f).

224 Before considering the region $R_n(t) < r < R_n^+(t)$, recall that parameter estimates from spheroids
225 grown in normoxia and hypoxia differ. Specifically, α (Figure 3d), $\lambda = \gamma s$ (Figure 3l,n), s (Figure 3l),
226 and \mathcal{R} (Figure S23) are all different. Therefore, we expect that these parameter values will evolve

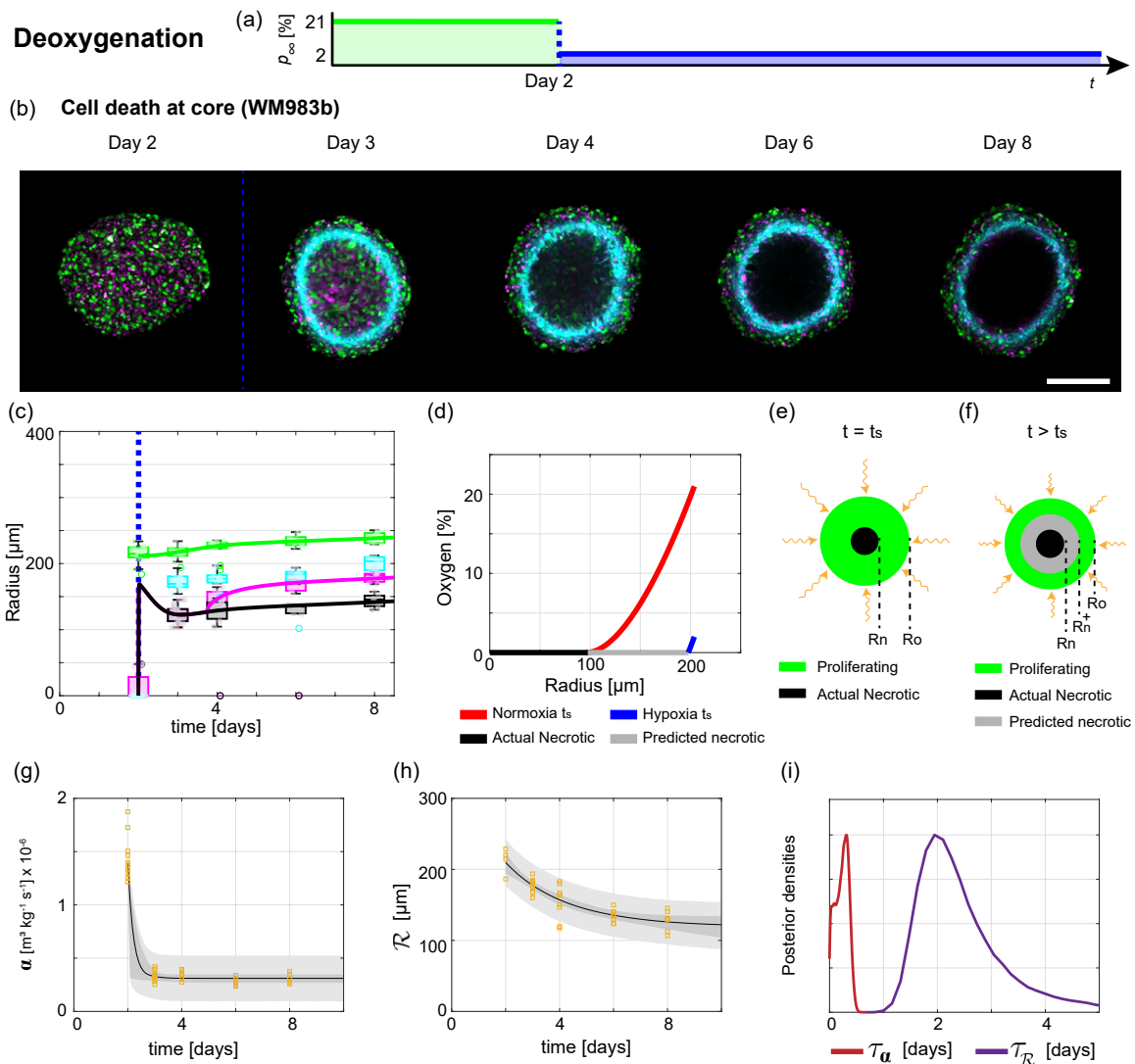


Figure 4: Analysis of deoxygenation experiments reveals tumour spheroid adaptation mechanisms. (a) Schematic for deoxygenation experiment, where the external oxygen environment switches from normoxia to hypoxia at $t_s = 2$ [days]. (b) Experimental images of the equatorial plane of WM983b spheroids on Days 2, 3, 4, 6, and 8 after seeding. Scale bar is 200 μm . Colours in (b) correspond to cell cycle schematic shown in Figure 2(c) and hypoxic regions are shown by pimonidazole staining (cyan). (c) Time evolution of outer radius $R_o(t)$ (green), inhibited radius $R_i(t)$ (magenta), hypoxic radius $R_p(t)$ (cyan), and necrotic radius $R_n(t)$ (black). Blue dashed lines in (b-c) indicate t_s . (d) Oxygen partial pressure within a spheroid estimated at t_s under normoxia (red) and hypoxia (blue). (e-f) Immediately after t_s the predicted necrotic radius, $R_n^+(t_s)$, is greater than the actual necrotic radius, $R_n(t_s)$. Cells in region $R_n^+(t) < r < R_n(t)$ die and increase the volume of the necrotic core. (g) Estimates of $\alpha(t)$ from experimental data compared to prediction intervals generated from the mathematical model. (h) Estimates of the outer radius when the inhibited region forms, \mathcal{R} , from experimental data compared to prediction intervals generated from the mathematical model. In (g-h) experimental data shown as orange squares, mathematical model simulated with the posterior means of the parameters (black), 50% posterior region of prediction interval (dark grey), and 97.5% posterior region of prediction interval (light grey). (i) Posterior density estimates for adaptation timescales τ_α (dashed) and $\tau_{\mathcal{R}}$ (solid).

227 in time after t_s . To account for such changes we define the following, for $t \geq t_s$,

$$\alpha(t) = \alpha_h + (\alpha_n - \alpha_h) \exp\left(-\frac{1}{\tau_\alpha}(t - t_s)\right), \quad (4.1)$$

$$\lambda(t) = \lambda_h + (\lambda_n - \lambda_h) \exp\left(-\frac{1}{\tau_\lambda}(t - t_s)\right), \quad (4.2)$$

$$s(t) = s_h + (s_n - s_h) \exp\left(-\frac{1}{\tau_s}(t - t_s)\right), \quad (4.3)$$

$$\mathcal{R}(t) = \mathcal{R}_h + (\mathcal{R}_n - \mathcal{R}_h) \exp\left(-\frac{1}{\tau_{\mathcal{R}}}(t - t_s)\right), \quad (4.4)$$

228 where τ_α [days], τ_λ [days], τ_s [days], and $\tau_{\mathcal{R}}$ [days] denote timescales of adaptation for α , λ , s , and
 229 \mathcal{R} , respectively. Further, the new constants in Equation (4) with subscripts n and h , for example α_n
 230 and α_h , represent parameter estimates from spheroids grown in normoxia and hypoxia, respectively.
 231 The other parameters (k, Ω, κ), are assumed to be constants. Hence, $R_c^2(t) = 6kp_\infty/(\alpha(t)\Omega)$ [μm^2],
 232 $Q^2(t) = \mathcal{R}^2(t)R_c^2(t)$ [-], and $\gamma(t) = \lambda(t)/s(t)$ [-] are functions of time.

233 In the region $R_n(t) < r < R_n^+(t)$ we assume cells die and increase the size of the necrotic core at
 234 a rate $\hat{\lambda}(t) = \hat{\lambda} \exp((t - t_s)/\tau_{\hat{\lambda}}) > 0$ [day^{-1}] per unit volume (Figure 4f). Conservation of volume for
 235 the necrotic core at time t , $V_n(t)$, gives (Supplementary Discussion C.2.1)

$$\frac{dV_n(t)}{dt} = 3\hat{\lambda}(t) \left[\frac{4\pi}{3} R_n^+(t)^3 - V_n(t) \right] - 3\lambda(t)V_n(t). \quad (5)$$

236 Volume is converted to radius for comparison with experimental data using $R_n^3(t) = 3V_n(t)/4\pi$. At
 237 later times the term involving $\hat{\lambda}(t)$ dominates the right hand side of Equation (5) and $R_n(t)$ tends
 238 to $R_n^+(t)$. Equation (1), obtained by conservation of volume arguments, remains valid by including
 239 the time dependence in $s(t)$ and $\lambda(t)$. At t_s there is no immediate change in the waste concentration
 240 within the spheroid and so no immediate change to $R_i(t)$. However, as $\mathcal{R}(t)$ changes with time
 241 (Equation (4.4)) the waste concentration within the spheroid and $R_i(t)$ evolve over time in part
 242 directly due to deoxygenation.

243 In this new mathematical model (Equations (8.1)-(8.11)) there are fifteen parameters $\Theta_d =$
 244 $(R_o(0), \alpha_n, \alpha_h, \tau_\alpha, \mathcal{R}_n, \mathcal{R}_h, \tau_{\mathcal{R}}, s_n, s_h, \tau_s, \lambda_n, \lambda_h, \tau_\lambda, \hat{\lambda}, \tau_{\hat{\lambda}})$. However, using Bayesian inference for
 245 parameter estimation the biological adaptation mechanisms become clearer (Methods 4.2). First,
 246 we identify fast adaptation to deoxygenation in $\alpha(t)$ with $\tau_\alpha = 0.26$ [days] (Figures 4g,h). Second,
 247 we capture slower adaptation to deoxygenation for $\mathcal{R}(t)$ with $\tau_{\mathcal{R}} = 2$ [days] (Figures 4i,j). Third,
 248 simulating the new deoxygenation mathematical model we find good agreement with the experimen-
 249 tal measurements of $R_o(t)$, $R_n(t)$, and $R_i(t)$ (Figure 4c, S27). Therefore, our new mathematical
 250 model provides a mechanistic description to the observed growth dynamics in the variable external
 251 environment and appears to capture key adaptation mechanisms.

2.3 Adaptation to re-oxygenation

We also perform re-oxygenation experiments, where spheroids grown in normoxia are transferred to hypoxic conditions at time t_s . These re-oxygenation experiments exhibit a range of unexpected biological adaptation mechanisms for each cell line that appear to depend on: t_s ; spheroid size at re-oxygenation, $R_o(t_s)$; and necrotic core fraction at re-oxygenation, $\xi_n(t_s) = R_n(t_s)/R_o(t_s)$.

First we focus on slower growing WM793b spheroids and $t_s = 2$ [days] (Figure 5a,c). In hypoxic conditions prior to re-oxygenation, experimental images show a large hypoxic region (Day 2 of Figure 5a,c,g). However, after re-oxygenation at $t_s + 1$ [days] there is no hypoxic region (Day 3 of Figure 5c,g). Spheroid growth after deoxygenation appears to progress similar to spheroids that are grown in normoxia throughout (Days 3-8 in Figure 5c,g).

For WM793b spheroids and $t_s = 4$ [days], a necrotic core forms before t_s (Day 4 in Figure 5d,h). However, after deoxygenation, at $t_s + 2$ [days] there is no necrotic core (Day 6 of Figure 5d,h). At $t_s + 4$ [days] spheroids are either in phase (i) or phase (ii) (Day 8 of Figure 5d,h). While traditional tumour spheroid experiments progress through phase (i), (ii), and (iii) sequentially, these experiments show that spheroids can transition transiently through the growth phases in reverse order before subsequently growing in the usual order. Similar results are observed for WM164 spheroids. However, WM164 spheroids can also resume growth without losing their necrotic core (Figure S30). These different behaviours appear to be dependent on t_s , $R_o(t_s)$ and $\xi_n(t_s)$.

To interpret the WM793b and WM164 re-oxygenation experiments we proceed analogously to the deoxygenation experiments. We extend Greenspan's mathematical model to account for differences in parameter estimates between normoxia and hypoxia. Estimating the oxygen partial pressure within the spheroid at t_s , the predicted necrotic core, denoted $R_n^+(t_s)$, is smaller than the actual necrotic core, $R_n(t_s)$, provided $R_n(t_s) > 0$. In the region $R_n^+(t) < r < R_n(t)$ where the necrotic core is now supplied with oxygen, we assume that size of the necrotic core decreases at a rate $\tilde{\lambda}(t) = \tilde{\lambda} \exp((t - t_s)/\tau_{\tilde{\lambda}}) > 0$ [day⁻¹] per unit volume. We assume that a fraction, $0 \leq \nu \leq 1$, of the volume lost from the necrotic core recovers from the harsh oxygen conditions and increases the population of living cells, and the remaining volume lost from the necrotic core diffuses out of the spheroid and does not influence $R_i(t)$. Using Bayesian inference we estimate the model parameters, $\Theta_r = (R_o(0), \alpha_n, \alpha_h, \tau_\alpha, \mathcal{R}_n, \mathcal{R}_h, \tau_{\mathcal{R}}, s_n, s_h, \tau_s, \lambda_n, \lambda_h, \tau_\lambda, \tilde{\lambda}, \tau_{\tilde{\lambda}}, \nu)$ and simulate the mathematical model. We observe good agreement with the experimental data suggesting our new re-oxygenation mathematical model captures key mechanisms underlying adaptation and growth (Figures 5g,h, S29, S30).

Results for WM983b spheroids are unexpected. We hypothesised, based on the exploration of the mathematical model, that spheroid growth dynamics may occur in reverse as observed for WM793b and WM164 spheroids. However, we did not anticipate that WM983b spheroids would lose their symmetrical internal structure and necrotic core due to re-oxygenation (Figures 5i-n). The WM983b experiments are performed at four different re-oxygenation times $t_s = 2, 2.5, 4$, and 5.5 [days] (Figures

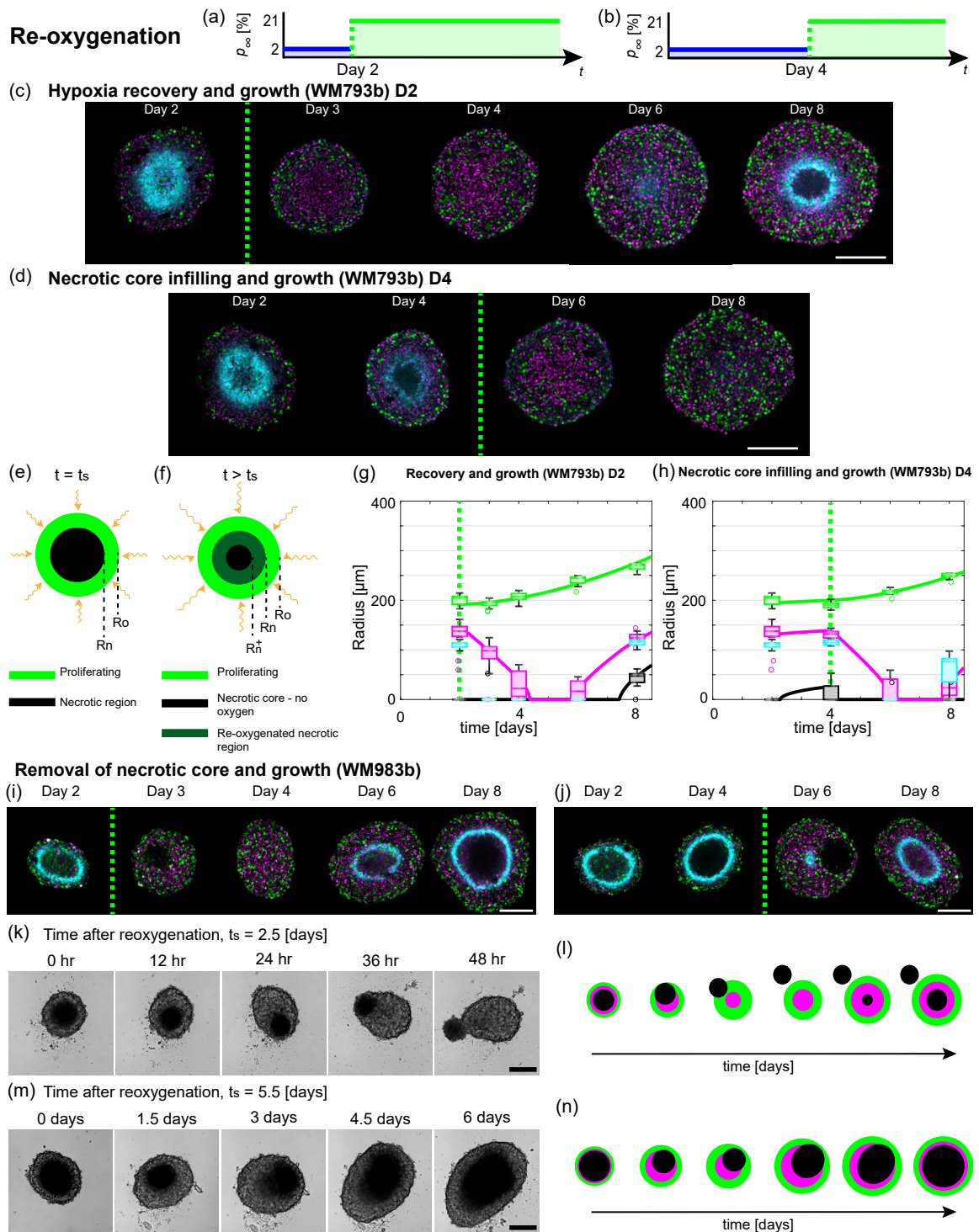


Figure 5: (Caption next page).

Figure 5: Tumour spheroids exhibit a range of adaption mechanisms in response to re-oxygenation. (a,b) Schematics for re-oxygenation experiments, where the external oxygen environment switches from hypoxia to normoxia at (a) $t_s = 2$ [days], and, (b) $t_s = 4$ [days]. (c,g) Hypoxia recovery and growth for WM793b cell line with $t_s = 2$ [days] with (c) experimental images, and (g) radial measurements. (d,h) Necrotic core infilling and growth for WM793b cell line with $t_s = 4$ [days] with (d) experimental images, and (h) radial measurements. Green dashed line in (c,d,g,h,i,j) indicate t_s . Colours in (g,h) $R_o(t)$ (green), $R_i(t)$ (magenta), $R_n(t)$ (black), and $R_p(t)$ (cyan). (e,f) Schematics for tumour spheroid structure due to re-oxygenation at t_s . (i-l) Removal of necrotic core and growth for WM983b cell line. (i) Confocal images for experiment with $t_s = 2$ [days]. (j) Confocal images for experiment with $t_s = 4$ [days]. (k) Bright-field images for experiment with $t_s = 2.5$ [days]. (l) Schematic for removal of necrotic core and growth in WM983b cell line. (m) Bright-field images for experiment with $t_s = 5.5$ [days]. (n) Schematic for movement of necrotic core and growth in WM983b cell line. Colours in (c,d,i,j) correspond to cell cycle schematic shown in Figure 2(c) and hypoxic regions are shown by pimonidazole staining (cyan). Scale bars in (c,d,i,j,k,m) are 200 μm .

289 5i,j,k,m). For all experiments, spheroids at t_s prior to re-oxygenation are in phase (iii). For $t_s = 2$,
290 confocal microscopy reveals that at $t_s + 1$ [days] there is a necrotic region but it is not at the centre
291 of the spheroid (Day 3 of Figure 5i). At later times there is no necrotic region and growth proceeds
292 analogous to spheroids in normoxia. Similarly, for $t_s = 4$ (Figure 5j).

293 To explore this unusual behaviour for $t_s = 2.5$ [days] and $t_s = 5.5$ [days] we perform experiments
294 using the IncuCyte S3 live cell imaging system (Sartorius, Goettingen, Germany) and obtain hourly
295 bright-field images after re-oxygenation. In Figure 5k with $t_s = 2.5$ [days], initially the necrotic core
296 of the spheroid is visible as a dark central region. At later times the necrotic core is located closer
297 to the edge of the spheroid and the radially symmetric internal structure is lost (12, 24 and 36 hours
298 after re-oxygenation in Figure 5k). At $t_s + 2$ [days] the necrotic core appears to have exited the
299 spheroid as a single object (48 hours after re-oxygenation in Figure 5k). Tracking the position of
300 the necrotic core relative to the spheroid suggests the necrotic core moves randomly (Supplementary
301 Discussion D.3.1).

302 We observe similar behaviour for WM983b spheroids with $t_s = 5.5$ [days]. However, likely due to
303 the larger $R_o(t_s)$ and $\xi_n(t_s)$ here, the necrotic core is close to the edge of the spheroid but does not
304 exit as a single object (1.5 and 3 days after t_s in Figure 5). Instead as the spheroid grows necrotic
305 matter forms at the centre of the spheroid and appears to merge with the necrotic matter located
306 closer to the periphery (3, 4.5 and 6 days after t_s in Figure 5). As the WM983b spheroids do not
307 maintain spherical symmetry we do not interpret these experimental data with the re-oxygenation
308 mathematical model. Schematics describing the behaviours are presented in Figure 5l,n.

309 **3 Discussion**

310 Tumours grow in complicated fluctuating external environments. However, spheroid experiments
311 used to study tumours are typically performed in constant external environments and with oxygen
312 partial pressures that are much greater than *in vivo*. To explore this gap between *in vitro* and *in*
313 *vivo* conditions, we analyse a series of tumour spheroid experiments using mathematical modelling
314 and statistical uncertainty quantification. Growing spheroids in time-dependent external oxygen
315 conditions reveals a range of behaviours not observed in standard experimental protocols. For fifty
316 years, tumour spheroid growth has been characterised by three sequential growth phases: phase
317 (i) exponential growth; phase (ii) reduced exponential growth; and phase (iii) saturation. How-
318 ever, here in re-oxygenation experiments, spheroids can transiently undergo these growth phases in
319 reverse. Furthermore, spheroids can lose their spherically symmetric structure and necrotic core.
320 Deoxygenation experiments also show that large changes to the internal structure of spheroids can
321 occur while the overall size remains constant. Overall, our results suggest that oxygen and internal
322 structure play pivotal roles in spheroid growth and should be taken into account when interpreting
323 spheroid experiments. This is important as many studies do not provide sufficient information to
324 replicate oxygen conditions and do not measure spheroid internal structures.

325 Tumour spheroid growth is a complex process involving multiple mechanisms. However, the
326 contribution of each mechanism to growth is unclear using experimentation alone. To quantitatively
327 explore which mechanisms contribute to spheroid growth we use the seminal Greenspan mathematical
328 model [10]. The model describes the growth of spheroids in normoxia and hypoxia remarkably
329 well. Moreover, our analysis suggests that growth and formation of the necrotic core is reasonably
330 described by oxygen diffusion and consumption, whereas the growth and formation of the inhibited
331 region is more accurately described by waste production and diffusion. Using statistical uncertainty
332 quantification we show that the rates at which different biological processes occur differ between
333 normoxia and hypoxia. Therefore, external environmental conditions should be taken into account
334 when interpreting tumour spheroid experiments. Previous studies analysing previously available
335 experimental data with Greenspan's model [15, 16] have not been able to distinguish between the
336 two mechanisms. Further, our results build on studies analysing spheroid snapshots only [17, 35].
337 As the model captures the key dynamics, we do not include other biological mechanisms that may
338 be relevant in future studies, for example glucose [4]. Introducing additional mechanisms prior to
339 developing the deoxygenation and re-oxygenation models would complicate the analysis, and likely
340 result in parameters being non-identifiable and not physically interpretable. Both of which we aim
341 to avoid. Many mathematical models have been developed with additional mechanisms, but they
342 have not been quantitatively tested with experimental data [25, 31–34]. The experimental data and
343 framework that we provide here are suitable to test such models.

344 Deoxygenation and re-oxygenation experiments reveal how spheroid overall size and internal
345 structure adapt to changes in the external environment. However, without a mathematical mod-

346 elling and statistical uncertainty quantification framework like we use here, the mechanisms underlying
347 ing adaptation are challenging to identify and interpret. Extending Greenspan's mathematical model
348 allows us to interpret, analyse, and describe these deoxygenation and re-oxygenation experiments re-
349 markably well. Parameter estimation and identifiability analysis, using profile likelihood analysis and
350 Bayesian inference, allows us to identify and quantify the contributions of key biological mechanisms
351 to adaptation and growth. For both models, the analysis identifies a narrow range of behaviours that
352 differ in terms of the rates of adaptation in $t_s < t < t_s + 1$ [days] and long term dynamics (Supple-
353 mentary Discussion D.2.1). These modelling predictions raise interesting questions (Supplementary
354 Discussion D.2.1). In comparison to standard experimental protocols, we collect more data per time
355 point and over a longer duration. Further, we build on previous studies [13, 15, 16] to improve on
356 standard experimental designs by measuring the internal structure of spheroids and hypoxic regions
357 in addition to the overall size. Even these improvements to standard protocols are insufficient to
358 identify all adaptation processes. As with all studies, additional data would be beneficial. In partic-
359 ular, frequent measurements of oxygen and internal structure at early times would be useful but are
360 challenging to obtain experimentally (Supplementary Discussion D.2).

361 Re-oxygenation experiments reveal unexpected necrotic core removal in WM983b spheroids. To
362 the best of our knowledge this behaviour has not been previously described. The exact mechanisms
363 underlying this behaviour are unclear. We hypothesise that small asymmetry at re-oxygenation,
364 possibly in the distribution of proliferating cells, in combination with changes to cell-cell adhesion
365 and physical interactions contribute. As spheroids formed from other cell lines have more liquid-like
366 necrotic cores than the WM983b spheroids at re-oxygenation, it is unclear whether these observations
367 are relevant to other cell lines. Interesting future work is to explore these unusual behaviours in
368 greater detail. For example, can this phenomenon be induced by other external environmental
369 changes, drug treatments, and *in vivo*.

370 This work lays the foundation for further studies bridging the gap between clinical conditions
371 and standard experimental protocols. Here, we consider normoxia and hypoxia and switches between
372 normoxia and hypoxia. Other oxygen conditions are also worth consideration, for example to mimic
373 *in vivo* oxygen gradients [39], *in vivo* vascularisation, disrupted oxygen supplies, or cyclic hypoxia [1].
374 Microfluidic devices may be one useful approach [25], but challenges visualising the internal structure
375 of spheroids throughout such experiments must be overcome. Intracellular responses to oxygen
376 changes are also of interest [40, 41]. While we focus here on the impact of changing the oxygen
377 conditions, our framework is well suited to explore the role of other changing external conditions on
378 spheroid growth, for example nutrient availability and mechanical confinement [4, 11]. Further, the
379 framework can be extended to explore different treatment strategies, for example radiotherapy and
380 chemotherapy [31, 42].

4 Methods

4.1 Mathematical modelling

4.1.1 Greenspan's mathematical model

Key elements of Greenspan's mathematical model for fixed p_∞ are included in the main text. Further details of the model derivation are included in Supplementary Discussion C.1. Recall that this model has two interpretations, that we refer to as hypotheses 1 and 2.

- Hypothesis 1 assumes that the necrotic and inhibited regions are both driven by oxygen diffusion and consumption.
- Hypothesis 2 assumes that the necrotic region is driven by oxygen diffusion and consumption whereas the inhibited region is driven by waste production and diffusion.

Here, we present the governing differential-algebraic system of equations for the outer radius, $R_o(t)$, necrotic radius, $R_n(t)$, and inhibited radius, $R_i(t)$, for both hypotheses 1 and 2,

$$R_o^2(t) \frac{dR_o(t)}{dt} = \frac{s}{3} [R_o^3(t) - \max(R_i(t)^3, R_n^3(t))] - \lambda R_n(t)^3, \quad (6.1)$$

$$R_c^2 = R_o^2(t) - R_n^2(t) - \frac{2R_n^2(t)}{R_o(t)} (R_o(t) - R_n(t)), \quad (6.2)$$

$$\mathcal{R}^2 = R_o^2(t) - R_i^2(t) - 2R_n^3(t) \left(\frac{1}{R_i(t)} - \frac{1}{R_o(t)} \right). \quad (6.3)$$

In these experiments, Equation (6.1) simplifies as $R_i(t) \geq R_n(t)$, consistent with our parameter choices (Methods 4.2) [16]. For both hypothesis 1 and 2: the outer radius when the necrotic region forms is $R_c = [6kp_\infty/(\alpha\Omega)]^{1/2}$; Equation (6.1) arises from conservation of volume; and, Equation (6.2) is obtained by evaluating the oxygen partial pressure within the spheroid at the necrotic threshold. For hypothesis 1, Equation (6.3) is obtained by evaluating the oxygen partial pressure within the spheroid at the oxygen inhibited threshold, p_i , and $Q^2 = (p_\infty - p_i)/p_\infty$ so the left hand side of Equation (6.3) is $\mathcal{R}^2 = R_c^2 Q^2 = 6k(p_\infty - p_i)/(\alpha\Omega)$. In contrast, for hypothesis 2, Equation (6.3) arises by evaluating the waste concentration within the spheroid at the waste inhibited threshold, β_i , and $Q^2 = \beta_i \kappa \alpha \Omega / (Pk p_\infty)$ so the left hand side of Equation (6.3) is $\mathcal{R}^2 = R_c^2 Q^2 = 6\beta_i/P$. We solve the system of Equations (6.1)-(6.3) numerically using MATLAB's `ode15s` function.

Analysing the model, the inhibited region forms at [10]

$$t = \frac{3}{s} \log \left(\frac{\mathcal{R}}{R_o(0)} \right). \quad (7.1)$$

For hypothesis 1, Equation (7.1) is $t = (3/s) \log ([6k(p_\infty - p_i)/\alpha]^{1/2}/R_o(0))$. For hypothesis, 2 Equation (7.1) is $t = (3/s) \log ([6\beta_i \kappa/P]^{1/2}/R_o(0))$.

4.1.2 Mathematical model to interpret deoxygenation experiments

Key elements of the mathematical model derived to interpret deoxygenation experiments are included in the main text. Further details of the model derivation are included in Supplementary Discussion C.2. Here, we present the governing equations for $0 < t < t_s$ and $t > t_s$.

For $0 < t < t_s$ we solve Greenspan's mathematical model [10] in normoxia interpreting the governing mechanisms with hypothesis 2. The differential-algebraic system of Equations (6.1)-(6.3) are solved to determine $R_o(t)$, $R_n(t)$, and $R_i(t)$.

After deoxygenation, $t > t_s$, we extend Greenspan's mathematical model to account for adaptation to hypoxia. Rewriting Equations (4), (5), (6.1), and solving Equation (6.2) for $R_n^+(t)$ instead of $R_n(t)$, gives the governing differential-algebraic system of equations

$$R_o^2(t) \frac{dR_o(t)}{dt} = \frac{s(t)}{3} [R_o^3(t) - \max(R_i^3(t), R_n^3(t))] - \lambda(t) R_n^3(t), \quad (8.1)$$

$$\frac{dV_n(t)}{dt} = 3\hat{\lambda}(t) \left[\frac{4\pi}{3} R_n^+(t)^3 - V_n(t) \right] - 3\lambda(t) V_n(t), \quad (8.2)$$

$$R_c^2(t) = R_o^2(t) - R_n^+(t)^2 - \frac{2R_n^+(t)^2}{R_o(t)} (R_o(t) - R_n^+(t)), \quad (8.3)$$

$$\mathcal{R}^2(t) = R_o^2(t) - R_i^2(t) - 2R_n^3(t) \left(\frac{1}{R_i(t)} - \frac{1}{R_o(t)} \right), \quad (8.4)$$

$$\alpha(t) = \alpha_h + (\alpha_n - \alpha_h) \exp\left(-\frac{1}{\tau_\alpha} (t - t_s)\right), \quad (8.5)$$

$$\lambda(t) = \lambda_h + (\lambda_n - \lambda_h) \exp\left(-\frac{1}{\tau_\lambda} (t - t_s)\right), \quad (8.6)$$

$$s(t) = s_h + (s_n - s_h) \exp\left(-\frac{1}{\tau_s} (t - t_s)\right), \quad (8.7)$$

$$\mathcal{R}(t) = \mathcal{R}_h + (\mathcal{R}_n - \mathcal{R}_h) \exp\left(-\frac{1}{\tau_{\mathcal{R}}} (t - t_s)\right), \quad (8.8)$$

$$\hat{\lambda}(t) = \hat{\lambda} \exp\left(\frac{1}{\tau_{\hat{\lambda}}} (t - t_s)\right), \quad (8.9)$$

$$R_n(t) = \left[\frac{3}{4\pi} V_n(t) \right]^{\frac{1}{3}}, \quad (8.10)$$

$$R_c^2(t) = \frac{6kp_\infty}{\alpha(t)\Omega}. \quad (8.11)$$

Note that in the long time limit $t \rightarrow \infty$, we recover Greenspan's mathematical model for normoxia (Equations (6.1)-(6.3)). Specifically, $\alpha(t) \rightarrow \alpha_h$, $\lambda(t) \rightarrow \lambda_h$, $s(t) \rightarrow s_h$ and $\mathcal{R}(t) \rightarrow \mathcal{R}_h$ as $t \rightarrow \infty$. Further, the term involving $\hat{\lambda}(t)$ dominates the right hand side of Equation (8.2) as $t \rightarrow \infty$, so $R_n(t) \rightarrow R_n^+(t)$ as $t \rightarrow \infty$. We solve the system of equations (8.1)-(8.11) numerically using MATLAB's `ode15s` function.

4.1.3 Mathematical model to interpret re-oxygenation experiments

Key details of the mathematical model to interpret re-oxygenation experiments are included in Supplementary Discussion C.3.

424 4.2 Parameter estimation and identifiability analysis

425 Parameter estimation and identifiability analysis is performed using profile likelihood analysis [15,16,
426 43,44], Bayesian inference [45–47], and global optimisation techniques, as now detailed. Throughout
427 we exclude outliers in the experimental data. To detect outliers for each experiment we analyse
428 each measurement type, $R_o(t)$, $R_n(t)$, and $R_i(t)$ at each time point independently using MATLABs
429 `isoutlier` function with method `quartiles`.

430 4.2.1 Greenspan’s model

431 Parameter estimation and identifiability analysis for Greenspan’s model is first performed using pro-
432 file likelihood analysis (Figure 3), see [16]. The Bayesian inference approach to estimate parameters
433 of Greenspan’s model is discussed in the following.

434 4.2.2 Deoxygenation experiments

435 Parameter estimation for the deoxygenation model (Equations (8.1)-(8.11)) is performed using global
436 optimisation and Bayesian inference techniques. We now explain how we estimate the fifteen model
437 parameters, $\Theta_d = (R_o(0), \alpha_n, \alpha_h, \tau_\alpha, \mathcal{R}_n, \mathcal{R}_h, \tau_{\mathcal{R}}, s_n, s_h, \tau_s, \lambda_n, \lambda_h, \tau_\lambda, \hat{\lambda}, \tau_{\hat{\lambda}})$. Informed
438 by experimental measurements we set $R_n(t_s) = 0$ and $R_i(t_s) = 0$, but they could be included as
439 additional parameters in future work.

440 We revisit Greenspan’s mathematical model for spheroids grown in normoxia and hypoxia for
441 first estimates of s_n , s_h , λ_n and λ_h . Starting with data from spheroids grown in normoxia, we fit a
442 normal distribution to the initial outer radius measurements using the MATLAB `fitdist` function.
443 Then for each spheroid we estimate R_c using Equation (6.2) given measurements of $R_o(t)$ and $R_n(t)$
444 and fit a normal distribution using the MATLAB `fitdist` function. Similarly, we estimate \mathcal{R} using
445 Equation (6.3) and measurements of $R_o(t)$, $R_n(t)$ and $R_i(t)$ and fit a normal distribution using
446 the MATLAB `fitdist` function. Next, we seek to estimate the five parameters of Greenspan’s
447 model, $\Theta_n = (R_o(0), R_c, s, \lambda, \mathcal{R})$, using the MATLAB package `MCMCstat` developed by Marko
448 Laine [48,49]. Detailed information on the `MCMCstat` package is available on the GitHub repository
449 (<https://mjlane.github.io/mcmcstat/>).

450 Before we can use the `MCMCstat` package we require good first estimates of Θ_n and the mean
451 squared error, *mse*. To provide a good first estimate for Θ_n , we perform global optimisation using the
452 MATLAB `GlobalSearch` function with settings: `fmincon sqp` algorithm; `MaxTime` = 15 [minutes];
453 `NumTrialPoints` = 5000; and `lowerbounds` and `upperbounds` informed by fitted normal distributions
454 for $R_o(0)$, R_c , and \mathcal{R} and previous results [16]. To estimate the *mse* we use experimental measure-
455 ments as observations and simulate the deoxygenation model with the estimate of Θ_n from global
456 optimisation to obtain predicted values. Next we use the `MCMCstat` package to generate MCMC
457 chains with 100,000 samples and enable automatic sampling and estimation of the error standard
458 deviation. For other `MCMCstat` package options we use the default settings. Performing posterior

459 checks, using 25,000 samples from the chain to generate prediction intervals and comparing with the
460 experimental data, suggests the parameter estimates are reasonable. This process is repeated for the
461 hypoxia data to estimate Θ_h . The posteriors generated here are for s_n , s_h , λ_n and λ_h .

462 Next, we analyse the deoxygenation experimental data at each spheroid and time point indepen-
463 dently. To estimate \mathcal{R}_n , \mathcal{R}_h , $\tau_{\mathcal{R}}$ from Equation (8.8) we use global minimisation and the *MCMCstat*
464 package. For measurements of \mathcal{R} for each spheroid and at each time point independently we use
465 Equation (6.2) and measurements of $R_o(t)$ and $R_n(t)$. Similarly, to estimate α_n , α_h , τ_α from Equa-
466 tion (8.5) we use global minimisation and the *MCMCstat* package. For measurements of α we use
467 Equations (8.11) and (6.3) and measurements of $R_o(t)$, $R_n(t)$ and $R_i(t)$. Note that to estimate R_c
468 we assume that $R_n(t) = R_n^+(t)$. To estimate $R_o(0)$ we fit a normal distribution using the MATLAB
469 `fitdist` function to measurements of $R_o(t)$ at the first time point.

470 Next we perform a global minimisation to estimate Θ_d , using the estimates of $R_o(0)$, α_n , α_h ,
471 τ_α , \mathcal{R}_n , \mathcal{R}_h , $\tau_{\mathcal{R}}$, s_n , s_h , λ_n , λ_h to inform *lowerbounds* and *upperbounds*. Using the estimate of Θ_d
472 from global minimisation as a first guess, we then use the *MCMCstat* package to generate MCMC
473 chains with 200,000 samples and enable automatic sampling and estimation of the error variance.
474 Performing posterior checks, using 50,000 samples from the chain to generate prediction intervals
475 and comparing with the experimental data, suggests the parameter estimates are reasonable.

476 4.2.3 Re-oxygenation experiments

477 Parameter estimation for the re-oxygenation model formed by Equations (S.34.1)-(S.34.10), with
478 parameters $\Theta_r = (R_o(0), \alpha_n, \alpha_h, \tau_\alpha, \mathcal{R}_n, \mathcal{R}_h, \tau_{\mathcal{R}}, s_n, s_h, \tau_s, \lambda_n, \lambda_h, \tau_\lambda, \tilde{\lambda}, \tau_{\tilde{\lambda}}, \nu)$, is analogous to
479 the approach used for the deoxygenation model.

480 4.3 Experimental methods

481 *Cell culture.* The human melanoma cell lines established from primary (WM793b) and metastatic
482 cancer sites (WM983b, WM164) were provided by Prof. Meenhard Herlyn, The Wistar Institute,
483 Philadelphia, PA, [50]. All cell lines were previously transduced with fluorescent ubiquitination-
484 based cell cycle indicator (FUCCI) constructs [13, 14]. Cell lines were previously genotypically
485 characterised [13, 51–53], and authenticated by short tandem repeat fingerprinting (QIMR Berghofer
486 Medical Research Institute, Herston, Australia). The cells were cultured in melanoma cell medium
487 (“Tu4% medium”): 80% MCDB-153 medium (Sigma-Aldrich, M7403), 20% L-15 medium (Sigma-
488 Aldrich, L1518), 4% fetal bovine serum (ThermoFisher Scientific, 25080-094), 5 mg mL⁻¹ insulin
489 (Sigma-Aldrich, I0516), 1.68 mM CaCl₂ (Sigma-Aldrich, 5670) [14]. Cell lines were checked routinely
490 for mycoplasma and tested negative using the MycoAlert MycoPlasma Detection Kit (Lonza) and
491 polymerase chain reaction [54].

492 *Spheroid generation, culture, and experiments.* Spheroids were generated in 96-well cell culture
493 flat-bottomed plates (3599, Corning), with 5000 total cells/well, using 50 µL total/well non-adherent
494 1.5% agarose to promote formation of a single spheroid per well [30]. From previous work we
495 expect that different seeding densities, in the range 1250-10000 total cells/well, will provide similar
496 results [15, 16]. For all experiments spheroids formed after 2 days for WM793b, WM164 and WM983b.
497 On day 3 and 7 of each experiment 50% of the medium in each well was replaced with fresh medium
498 (200 µL total/well). Each experiment was performed for 8 days, informed by previous experiments
499 with these cell lines so that necrotic and inhibited region form prior to the end of the experiments [16].

500 For normoxia experiments, cells and spheroids were grown and formed in an incubator with
501 standard settings: 37 °C, 5% CO₂ [13, 14]; referred to as the normoxia incubator. For hypoxia exper-
502 iments, cells were cultured in the normoxia incubator and then spheroids were grown in a hypoxia
503 incubator with settings: 37 °C, 5% CO₂, 2% O₂. For deoxygenation experiments, cells and spheroids
504 were formed and grown in the normoxia incubator. At the time of deoxygenation, the relevant
505 plate(s) of spheroids were manually transferred from the normoxia incubator to the hypoxia incu-
506 bator. Similarly, for the re-oxygenation experiments spheroids were grown in the hypoxia incubator
507 then at the time of re-oxygenation the relevant plate(s) of spheroids were manually transferred to
508 the normoxia incubator. The time to move plates was 1-2 minutes.

509 To estimate the outer, necrotic, inhibited, and hypoxic radii, we use a high-throughput method of
510 mounting, clearing and imaging [55]. Spheroids maintained in the relevant incubator were harvested,
511 fixed with 4% paraformaldehyde (PFA), and stored in phosphate buffered saline solution (PBS),
512 sodium azide (0.02%), Tween-20 (0.1%), and DAPI (1:2500) at 4 °C, on days 2, 3, 4, 6 and 8
513 after seeding. For hypoxia measurements, spheroids were stained with 100mM pimonidazole for
514 three hours, prior to fixation. Spheroids were then permeabilized with 0.5% Triton X-100 in PBS
515 for one hour; blocked in antibody dilution buffer (Abdil) [56] for 24 hours; stained with a 1:50
516 anti-pimonidazole mouse IgG1 monoclonal antibody (Hypoxyprobe-1 MAb1) in Abdil for 48 hours;

517 washed in PBS with 0.1% Tween-20 for 6 hours; placed in a 1:100 solution of goat anti-mouse Alexa
518 Flour 647 in Abdil for 48 hours; and, finally washed for 6 hours in PBS. Then for imaging, fixed
519 spheroids were set in place using low melting 2% agarose and optically cleared in 500 μ L total/well
520 high refractive index mounting solution (Quadrol 9 % wt/wt, Urea 22 % wt/wt, Sucrose 44 % wt/wt,
521 Triton X-100 0.1 % wt/wt, water) for 2 days in a 24-well glass bottom plate (Cellvis, P24-1.5H-N)
522 before imaging to ensure accurate measurements [55, 57, 58]. Images were then captured using an
523 Olympus FV3000 confocal microscope with the 10 \times objective focused on the equatorial plane of
524 each spheroid.

525 As the unexpected necrotic core movement for WM983b cell line was observed in the re-oxygenation
526 experiments, the re-oxygenation experiments were repeated for all cell lines alongside a control nor-
527 moxia condition. Spheroids were cultured into three 96-well plates (3599, Corning): plate (i) control
528 for normoxia; plate (ii) re-oxygenation 2.5 days after seeding; and, plate (iii) re-oxygenation 5.5 days
529 after seeding. Each plate consisted of 32 spheroids of each cell line. The plates were placed inside the
530 IncuCyte S3 live cell imaging system (Sartorius, Goettingen, Germany) incubator (37 $^{\circ}$ C, 5% CO₂).
531 IncuCyte S3 settings were chosen to image with the 4 \times objective. For plate (i) images were captured
532 every 2 hours for the first three days and then every 4 hours for the remainder of the experiment.
533 For plate (ii) and (iii) images were captured every hour for three and seven days, respectively.

534 *Image processing.* Confocal microscopy images were converted to TIFF files in ImageJ and then
535 processed with custom MATLAB scripts that use standard MATLAB image processing toolbox
536 functions. Area was converted to an equivalent radius ($r^2 = A/\pi$). These scripts are freely available
537 on Zenodo with DOI:10.5281/zenodo.5121093 [59], with modifications to account for pimonidazole
538 staining and blurred central regions due to hypoxia and deoxygenation discussed in Supplementary
539 Discussion B. Images captured with the IncuCyte S3 were processed with custom MATLAB scripts
540 that use standard MATLAB image processing toolbox functions and are detailed in Supplementary
541 Discussion D.3.1.

542 *Statistics and Reproducibility.* Details of practical parameter identifiability analysis and the
543 Bayesian inference are presented in Section 4.2. Each radial measurements is represented as an
544 individual data point in relevant figures, with non-filled circles representing outliers (Section 4.2),
545 and are summarised using box charts. Supplementary Table S1 details the number of measurements
546 at each time point for each cell line and experimental data analysed during the study are available on
547 a GitHub repository (<https://github.com/ryanmurphy42/Murphy2022SpheroidOxygenAdaptation>).
548 We note that some measurements could not be obtained primarily due to blurring of the automated
549 imaging, spheroids not forming properly, or spheroids losing their structural integrity at late times.
550 Data for these spheroids was excluded. In a previous study we assess experimental designs [16] and
551 use this to inform that our sample size is sufficient in this study. Randomisation and blinding was
552 not possible.

553 **Data Availability**

554 The datasets generated during and analysed during the current study are available on a GitHub repos-
555 itory (<https://github.com/ryanmurphy42/Murphy2022SpheroidOxygenAdaptation>) and are summarised
556 in the electronic supplementary material.

557 **Code Availability**

558 Key computer code and all experimental data used to generate computational results are available on
559 a GitHub repository (<https://github.com/ryanmurphy42/Murphy2022SpheroidOxygenAdaptation>)
560 repository. The computer code for the mathematical modelling and statistical identifiability anal-
561 ysis was written in MATLAB R2021b (v9.11) with the Image Processing Toolbox (v11.4), Op-
562 timization Toolbox (v9.2), Global Optimization Toolbox (v4.6), and the Statistics and Machine
563 Learning Toolbox (v12.2), and uses the *MCMCstat* package available on the GitHub repository
564 (<https://mjlane.github.io/mcmcstat/>).

565 **Author Contributions**

566 All authors conceived and designed the study. R.J.M. performed the research and drafted the article.
567 G.G. and R.J.M. performed experimental work. All authors provided comments and approved the
568 final version of the manuscript. N.K.H. and M.J.S. contributed equally.

569 **Competing Interests**

570 The authors declare no competing interests.

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