

1 **Sexual selection for rare beneficial mutations promotes the evolution of sexual**
2 **reproduction and adaptation**

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10

11 **Abstract**

12

13 The evolution and widespread maintenance of sexual reproduction remains a conundrum in
14 biology because asexual reproduction should allow twice the reproductive rate. One
15 hypothesis is that sexual selection lessens the negative impact on fitness of accumulating
16 deleterious mutations. However, for adaptation to occur, there must also be selection for
17 beneficial mutations. Here we show that sexual selection can help explain the evolution and
18 maintenance of sexual reproduction. In our model, females chose males with more beneficial
19 mutations (as opposed to just fewer harmful ones) even when these occurred much more
20 rarely. Sexual selection thereby increased fixation of beneficial mutations which increased
21 the absolute genetic quality of sexual offspring. This increase in fitness relative to asexual
22 offspring adds to the previously postulated effect of reduced mutation load in offsetting the
23 cost of sex. Analysing our simulations reveals that female choice among males raised the
24 fitness of reproducing males above that of females. We found that this effect could overcome
25 the decline in average fitness that occurs when mutation rate increases, allowing an
26 increase in the fixation of beneficial mutations. Sexual selection thereby not only facilitates
27 the evolution of sexual reproduction but maintains sex by leveraging its benefits and driving
28 adaptation.

29 **Introduction**

30

31 Any explanation for the evolution of sexual reproduction within groups must show how the
32 production of males, even when they do not care for offspring, increases the fitness of
33 sexually produced offspring, otherwise there is a 'two-fold cost of sex' [1, 2]. Sexual
34 reproduction entails variance in mating success, especially where females can choose
35 between males of varying quality and where a male can mate with more than one female [3,
36 4]. This differential mating success is integral to the process of sexual selection, which could
37 theoretically contribute to the maintenance of sex by the selective removal of low quality
38 males that effectively act as a sink for mutation load [5, 6]. Sexual selection could thereby
39 reduce the risk of population extinction [7], as has been demonstrated in flour beetles
40 *Tribolium castaneum* [8]. According to this theory, males become 'useful' in that females can
41 pick those males with the lowest load of deleterious mutations.

42

43 Mutation is the source of variation and the overwhelming majority of mutations are
44 deleterious [9] to the extent that models have ignored beneficial mutations, deeming them
45 too rare to be of interest. Nevertheless, adaptation depends upon those rare occasions when
46 mutations have a beneficial impact on fitness. Here, we investigate the role of sexual
47 selection in favouring beneficial mutations. Sexual selection can be a powerful process
48 resulting in strongly biased mating success [10]. This can even allow modifiers of the
49 mutation rate ('mutator genes', such as factors controlling DNA repair [11, 12]) to persist,
50 because female choice selects for those males with beneficial mutations [13, 14]. We
51 postulate here that female choice can be so potent that it not only promotes the maintenance
52 of genetic variation, but it allows beneficial mutations, despite their comparative rarity, to
53 have a significant impact on fitness. This means that the two-fold cost of sex may be
54 overcome not just by the lower reduction in fitness caused by deleterious mutation load [5,
55 6], but by the increase in fitness resulting from fixation of new beneficial mutations. We
56 further postulate that female choice can favour an increase in mutation rate, despite the
57 decline expected from the predominance of deleterious mutations, because female choice is
58 effective in selecting for those with an increased number of beneficial mutations.

59

60 We simulated the 'genetic quality' of individuals by examining the evolution of deleterious
61 and beneficial mutations in asexual and in sexual populations, and by varying the degree of
62 female choice in the latter. Implicit in our model is the assumption that, in addition to
63 determining survival, the mutations that a male accumulates determine the condition of
64 some trait, which is used by female subjects in mate choice. Thus, we assume that a male's
65 genetic quality is revealed in the trait and the female subjects use that information to select

66 the best male. This assumption is supported by the literature on ‘good genes’ effects in
67 sexual selection [15, 16] and by the demonstration that sexual traits can reveal genetic
68 quality [17, 18]. It is also consistent with other sexual selection models [19]. We compared
69 sexual and asexual populations in the presence of varying levels of sexual selection and a
70 modifier of mutation rate. We hypothesized that increasing mutation rate above a baseline
71 would leverage the effects of sexual selection making it more likely for sexual types to have
72 higher genetic quality than asexual types. The rationale for this is that an increase in
73 mutation rate feeds variation in genetic quality (and hence attractiveness), and that this
74 variation promotes choice between males [4]. We consider that sexually reproducing
75 individuals will vary in mating success [5] and that a key driver of this variation is female
76 choice for high quality and attractive mates that will provide females with high viability and
77 attractive offspring. We propose that females can actually get ‘good genes’ rather than
78 ‘fewer bad genes’ as in the models of how sexual selection facilitates the evolution of sex [5,
79 6]. As such, we predicted that variability in mutation rate should facilitate the effect of sexual
80 selection in overcoming the two-fold cost of sex.

81

82 **Results**

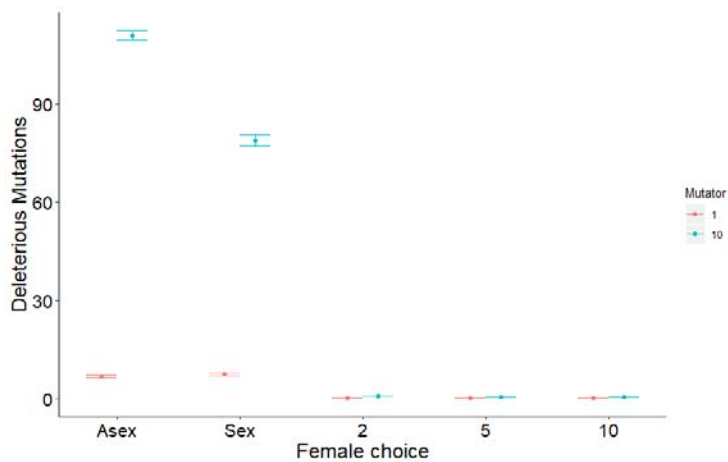
83

84 Looking at deleterious mutations first, we found that in populations with asexual reproduction
85 and in those with sexual reproduction but no sexual selection, deleterious mutation load
86 increased dramatically when mutation rate increased (Figure 1a). However, female choice,
87 even between just two males, reduced deleterious mutations to very low levels. Female
88 choice was so effective that even with a high mutation rate, the numbers of deleterious
89 mutations were reduced to substantially below those found in asexual populations or in
90 sexual populations lacking female choice. Conversely, numbers of beneficial mutations were
91 low, even with a ten-fold increase in mutation rate in asexual populations and sexual ones
92 without female choice (Figure 1b). However, with female choice, beneficial mutations were
93 much more common, and increased mutation rate accentuated this effect. Summing these
94 effects, overall genetic quality decreased with increasing mutation rate in asexual
95 populations and sexual ones lacking female choice, yet it increased with increasing mutation
96 rate in populations with female choice (Figure 1c). Thus, sexual selection was so powerful
97 that it overcame the 1000-fold disadvantage of the beneficial mutation rate and allowed an
98 increase in genetic quality with increased mutation rate. This increase in genetic quality
99 occurred because sexual selection was effective at keeping numbers of deleterious
100 mutations low despite an increase in mutation rate, yet was also effective in selecting for
101 beneficial mutations, and could do this most effectively when mutation rate was high.

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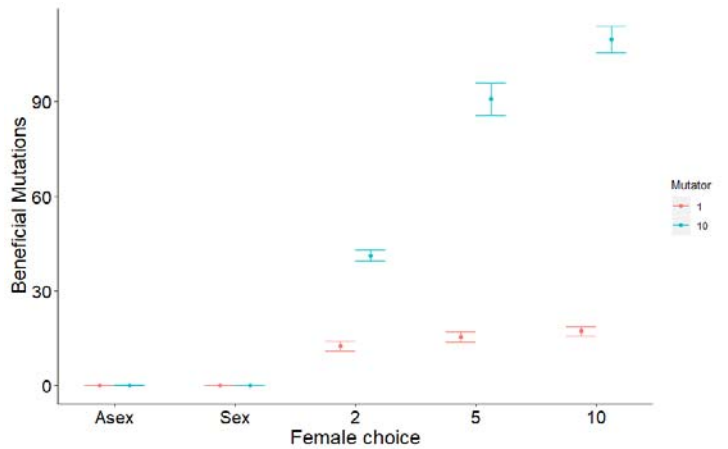
103 **Figure 1**

104 **a**



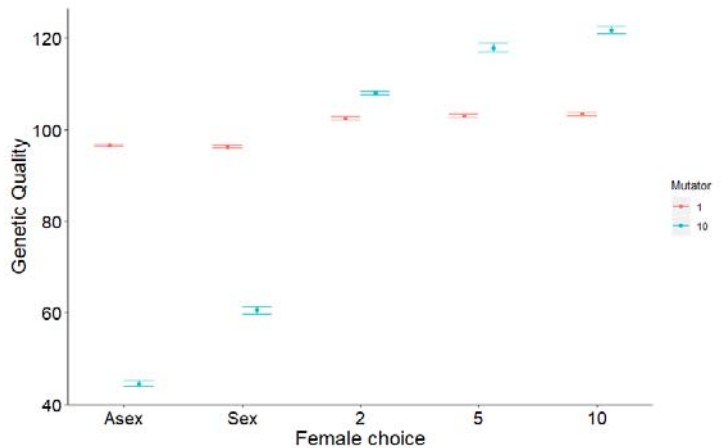
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106 **b**



107

108 **c**



109

110

111 **Figure 1 Legend**

112

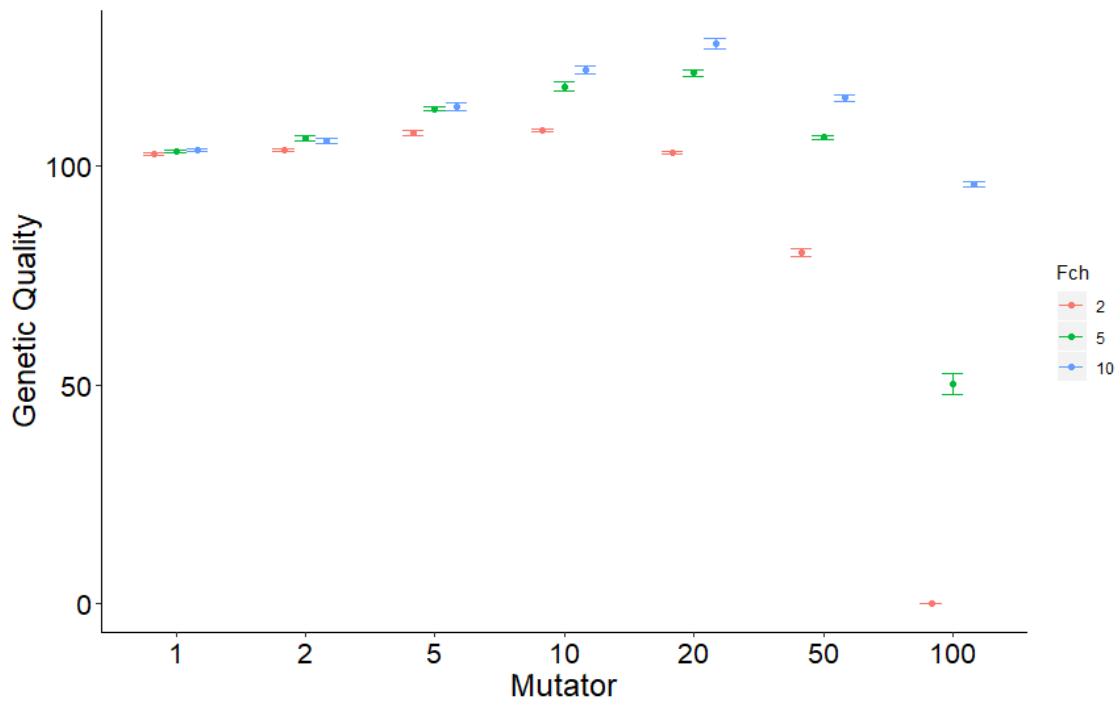
113 The figure shows how the numbers of mutations per individual vary with mode of
114 reproduction and strength of female choice where “Asex” is asexual reproduction; “Sex” is
115 sexual reproduction without female choice; and where “2”, “5” and “10” are sexual
116 reproduction with female choice between the given number of males . Figures a and b show
117 the numbers of mutations per individual; c shows ‘genetic quality’ calculated as baseline
118 fitness (100) minus the number of deleterious mutations per individual multiplied by the
119 effect of each (0.5); plus the number of beneficial mutations multiplied by the effect of each
120 (0.2). The rate of deleterious mutations per gene per individual per generation was 1000x
121 that of beneficial mutations. Plotted are the means and standard errors computed across 10
122 simulations for each set of parameters, taken at generation 1000. Plotted in red are the
123 results where the mutator gene $M = 1$; blue is where $M = 10$, i.e. the rates of both deleterious
124 and beneficial mutations are at 10x the baseline mutation rates, which were 10^{-3} and 10^{-6}
125 respectively. Other parameters: population size $N=1000$, equally divided between males and
126 females in simulations with sexual reproduction; cost of female choice = $0.02 \times$ female choice.
127
128

129 We further investigated the interaction between female choice and mutation rate (Figure 2).
130 Genetic quality increased with mutation rate and female choice to an intermediate maximum
131 before declining rapidly. High levels of female choice improved genetic quality; but there
132 came a point where even the highest level of female choice shown was insufficiently
133 powerful not to be overwhelmed by the surge in deleterious mutations caused by a
134 substantially increased mutation rate.

135

136 **Figure 2.**

137



138

139 **Figure 2 Legend.**

140 The figure shows how 'genetic quality' varies with a 'Mutator' and with sexual selection by
141 female choice. Genetic quality was calculated as given in Fig. 1. The mutator was a
142 multiplier of the default mutation rates. Female choice was between 2, 5 and 10 males.
143 Plotted are the means and standard errors computed across 10 simulations for each set of
144 parameters, taken at generation 1000. Other parameters were as in Fig. 1.

145

146

147 We investigated the robustness of our results by varying key parameters whilst maintaining a
148 moderate degree of female choice ($F = 5$). First, we varied the ratio of deleterious to
149 beneficial mutation around the default ratio of 1000:1 respectively. As intuitively expected,
150 genetic quality increased as beneficial mutations became relatively more common, and
151 especially when this factor combined with a higher mutation rate (Figure S1). Looking at the
152 effect on genetic quality of each beneficial mutation, we can again see that the results are
153 intuitive (Figure S2): increasing the effect of beneficial mutations increases genetic quality,
154 especially when mutation rate is high. Varying the cost of female choice within the range
155 shown has no effect on genetic quality in either mutation rate condition (Figure S3).
156 Increasing the population size, P , increased the effect size, as expected from the increased
157 potential for genetic change across more individuals (Figure S4). Varying recombination rate
158 had a little quantitative effect, with increased recombination allowing an increase in genetic
159 quality, presumably through allowing favourable genetic combinations (Figure S5). All in all,
160 varying key parameters suggested that the main effect we describe was robust.

161

162 The benefit of simulations is that they can help us predict processes that are difficult to
163 comprehend intuitively or mathematically; the corollary is that they can be hard to interpret.
164 To better understand the processes in the model we hypothesized that female choice selects
165 for a breeding population that results in offspring that are s standard deviations above the
166 mean of the underlying population. To test whether males that were chosen to breed were
167 indeed of higher genetic quality than the population from which they were drawn, we
168 aggregated across the first 1000 generations for all 1000 reproducing pairs and calculated
169 the mean difference in genetic quality between females and their chosen males. Where
170 female choice was absent and mutation was at the default rate, the mean difference was
171 $0.01 \pm <0.005$ (standard error of the mean); with females choosing the best of 10 males and
172 mutation rate at 10x the default, the difference was $0.22 \pm <0.005$. Therefore, females were
173 choosing males that had a genetic quality equivalent to approximately 1 beneficial mutation
174 above the average (recall that we modelled only a few genes, not the entire genome). In this
175 way, sexual selection appears to be able to exploit increasing variation caused by increased
176 mutation rate and actually produce an increase in genetic quality out of a background that
177 one would otherwise expect to be dominated by increased deleterious mutation load.

178

179 As a simple analytical approximation, consider that female choice between males results in
180 offspring that are s standard deviations above the mean. For the cost of sex to be overcome
181 we then need:

$$\bar{x} + s\sigma > 2\bar{x}$$

$$s > \frac{\bar{x}}{\sigma}$$

182

Equation 1

183

184 This equation will most readily be satisfied when the standard deviation of the genetic quality
185 is high relative to the mean. That is, there should be high variability within the population.

186 Variability results from mutation, and we can show when an increase in mutation rate can be

187 favoured. This can occur when the decrease in the mean genetic quality in the population

188 that necessarily results from an increase in mutation rate (assuming there is a strong

189 predominance of deleterious over beneficial mutations) is more than compensated for by the

190 effect of female choice in selecting for males of high genetic quality. If subscripts 1 and 2

191 indicate the means and standard deviations before and after the change in mutation rate,

192 then:

$$\bar{x}_2 + s\sigma_2 > \bar{x}_1 + s\sigma_1$$

193

$$s > \frac{\bar{x}_1 - \bar{x}_2}{\sigma_2 - \sigma_1}$$

194

Equation 2

195

196 This analytical approach has the benefit that it considers the whole genome, something we

197 do not attempt in our simulations, which allow us to include stochastic factors at the level of

198 the gene. As a hypothetical numerical example, consider that increasing the mutation rate

199 lowers the mean genetic quality from 1 to 0.9 whilst increasing the variance in genetic quality

200 from 0.2 to 0.4. Consider also that female choice selects for males that produce offspring 1

201 standard deviation above the mean. Entering these hypothetical values into Equation 2

202 demonstrates that an increase in mutation rate combined with female choice can indeed

203 lead to an increase in the genetic quality of offspring. To aid understanding, this example is

204 illustrated in Figure S6. Whilst simplified, this makes the point that an increase in mutation

205 rate can be favoured under sexual selection and can thereby contribute to overcoming the

206 two-fold cost of sex.

207

208 **Discussion**

209

210 We have shown here that an increase in mutation rate works with sexual selection to

211 increase genetic quality and thereby assist in overcoming the two-fold cost of sex. Crucially,

212 our simulations reveal that sexual selection not only leads to the maintenance of variation

213 [13, 20], but also leads to an adaptive increase in genetic quality. This is counterintuitive

214 given that any increase in mutation rate brings 1000 times as many deleterious as beneficial
215 mutations in our model. This result highlights just how powerful the effect of female choice
216 can be, even when just choosing between 2 males. We believe this is the first time that this
217 effect has been reported. Its significance is that if mutation rate is elevated above a typically
218 postulated minimum level then this would increase the benefits of sex relative to asexual
219 reproduction, helping to overcome what has been termed the ‘two-fold cost of sex’ [1, 2]. It
220 therefore seems that the role of sexual selection in the promotion of heritable genetic
221 variation is key to understanding the evolution of sexual reproduction.

222

223 Our model assumes that mutation can be controlled genetically. One mechanism for this is
224 through selection on those genes that are responsible for DNA repair [11]. We predict a
225 greater mutation rate in genes that influence sexually selected phenotypes and in more
226 sexually selected species. Across non-human species, particularly in birds, which differ in
227 within population variance in mating success [21], and thus the level of sexual selection,
228 there is some evidence of a positive correlation with the rate of mutation, measured by
229 variance in minisatellite mutation rate [22, 23]. Given that sexual selection can often result in
230 greater variance in mating success in males, our results are also consistent with male-
231 biased mutation rates [24]. Our results may also be consistent with the finding that sexual
232 selection interacts with mutation rates in seed beetles [25].

233

234 Our model reveals a positive feedback effect whereby a high mutation rate can favour sexual
235 reproduction over asexual reproduction, while sexual reproduction with sexual selection can
236 favour a high mutation rate. We speculate that this creates a ratchet effect in that once
237 sexual reproduction is established, it becomes harder to switch back to asexual
238 reproduction. Paradoxically, natural selection will tend to favour a low mutation rate [9], yet
239 adaptation requires mutation. Our model shows how a faster rate of adaptation can occur
240 with sexual selection. This is consistent with the finding that sexual selection (measured as
241 the degree of polygyny) interacts with the rate of molecular evolution and with body mass to
242 predict species richness at the genus level [26]. We argue that evolvability itself is under
243 selection [27], and that through sexual reproduction with sexual selection, evolution can lead
244 to greater evolvability.

245

246

247 **Methods**

248

249 We simulated the ‘genetic quality’ of individuals by examining the evolution of deleterious
250 and beneficial mutations in asexual and in sexual populations, and by varying the degree of
251 female choice in the latter. A simplified flow diagram of the simulations is given in Figure S6
252 and a Visual C program is provided as supplementary information. Our simulation methods
253 were based on models of the evolution of mutation rate [11, 13]. As in those simulations, the
254 parameters reflected literature estimates where available [28], subject to the constraint that
255 the model was intended as a simple abstraction of reality and not an attempt to simulate an
256 entire genome.

257

258 The simulations began by setting up a population of P individuals. In simulations of sexual
259 populations, half were male and half female. Individuals were given a pair of homologous
260 ‘chromosomes’ (i.e., we assumed diploidy) each bearing a ‘mutator gene’ and an associated
261 string of 10 ‘viability genes’. We did not assume that these genes constituted the entire
262 genome; only that there were no interactions between the genes of interest and those at
263 other sites and that for the purposes of comparison between simulations, all other things
264 were equal.

265

266 Each viability gene was subjected to a mutation process in which the rates of deleterious
267 and beneficial mutations varied between simulations. The absolute rates of mutation were
268 determined by the mutator gene, which increased the rates of beneficial and of deleterious
269 mutation by a factor M . We assumed that the mutator gene affected DNA repair only in a
270 relatively small region of the genome [29], namely the set of viability genes referred to
271 above; that it was adjacent to the first of the row of viability genes; and that the crossover
272 rate between the mutator and the first viability gene was the same as between each other
273 viability gene.

274

275 Individuals were subjected to a mortality process, whereby their probability of survival was a
276 function of their genetic quality. Deleterious mutations were assumed to have larger
277 phenotypic effects than beneficial mutations: deleterious mutations reduced the wild type
278 fitness of 100 by 0.5; beneficial mutations increased it by 0.2. The model assumed co-
279 dominance with additive fitness effects, so the effects of mutations were summed to give
280 ‘genetic qualities’, which determined individual survivorship in a mortality process.

281

282 Surviving individuals reproduced, either by asexual or by sexual reproduction, the latter with
283 or without female choice. Asexual reproduction was by selecting an individual at random and

284 copying its chromosomes into an individual in the next generation. Sexual reproduction
285 without female choice involved selecting a male and a female subject at random. In the case
286 of female choice, a female subject was selected at random, and a set of F male subjects
287 was selected at random. The female then bred with the male of highest genetic quality from
288 that set of F males. This ‘best of n ’ rule is the most widely used rule in modelling female
289 choice [30, 31] and has some empirical support from lekking species [32]. For each sexual
290 mating, one offspring was produced by bringing together chromosomes contributed by both
291 parents. This was carried out by selecting a chromosome at random from each parent and
292 allowing crossover between each adjacent gene with probability 0.01. The process of
293 selecting parents and producing offspring was repeated until the population was replaced by
294 a new generation of P individuals.

295

296 Unless otherwise stated, parameters used were as given in Table S1.

297

298 **Author contributions:** GR devised the computer simulations and analysis and wrote the
299 paper. MP conceived the original idea of relating sexual selection and mutation rate, and
300 contributed to the theoretical background.

301

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303

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