Microbial Species Abundance Distributions Guide Human Population Size Estimation from Sewage Metagenomes

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18 Abstract

The metagenome embedded in urban sewage is an attractive new data source to understand urban ecology and 19 assess human health status at scales beyond a single host. However, using census-based population size instead of 20 real-time population estimates can mislead the interpretation of data acquired from sewage, hindering assessment 21 of representativeness, inference of prevalence, or comparisons of taxa across sites. Here, we develop a new 22 method to estimate human population size in light of recent developments in species-abundance distributions of 23 microbial ecosystems. Using a population-scale human gut microbiome sample of over 1,100 people, we found that 24 taxon-abundance distributions of gut-associated multi-person microbiomes exhibited generalizable relationships in 25 response to human population size. We present a new non-parametric model, MicrobiomeCensus, for estimating 26 human population size from sewage samples. MicrobiomeCensus harnesses the inter-individual variability in 27 human gut microbiomes and performs maximum likelihood estimation based on simultaneous deviation of multiple 28 taxa's relative abundances from their population means. MicrobiomeCensus outperformed generic algorithms in 29 data-driven simulation benchmarks and detected population size differences in field data. This research provides a 30 mathematical framework for inferring population sizes in real time from sewage samples, paving the way for more 31 accurate ecological and public health studies utilizing the sewage metagenome. 32

33 Introduction

The metagenome embedded in urban sewage is an attractive new data source to understand urban ecology and assess 34 human health status at scales beyond a single host¹⁻³. Sewage microbiomes are found to share a variety of taxa with 35 human gut microbiomes, where the baseline communities are characterized by a dominance of human-associated 36 commensal organisms from the *Bacteroidetes* and *Firmicutes* phyla^{1,3,4}. Human viruses like SARS-CoV-2 and 37 polioviruses were detected in sewage samples during the pandemic and silent spreads, respectively, and found to 38 correlate to reported cases, suggesting that sewage samples could be useful for understanding the dynamics in the 39 human-associated symbionts at a population level^{5,6}. Sewage has several advantages as samples of the population's 40 collective symbionts. For instance, sewage samples are naturally aggregated, wastewater infrastructures are highly 41 accessible, and data on human symbionts can be collected without visits to clinics, thus utilizing sewage samples can 42 reduce costs and avoid biases associated with stigma and accessibility^{2,7}. Consequently, SARS-CoV-2 surveillance 43 utilizing sewage samples are underway globally and incorporated into the U.S. Centers for Disease Control and 44 Prevention surveillance framework⁸. 45

A pressing challenge in utilizing sewage for ecological and public health studies is the lack of methods to 46 directly estimate human population size from sewage. Specifically, virus monitoring at finer spatial granularity, e.g., 47 single university dorms and nursing homes, are informative for guiding contact tracing and protecting populations 48 at higher risk, but real-time population size estimations at such fine granularity arenot yet available. For a given 49 area, the census population (*de jure* population) can be larger than the number of people who contributed feces to 50 sewage at a given time (*de facto* population)⁹. Conversely, the de jure population can also be smaller than the de 51 facto population due to the presence of undocumented individuals¹⁰. Population proxies that are currently used for 52 monitoring at wastewater-treatment plants, such as the loading of pepper mild mottle viruses, likely have high error 53 at the neighborhood level because of their large variability in human fecal viromes (10⁶-10⁹ virions per gram of dry 54 weight fecal matter)¹¹. Consequently, it is difficult to assess the representativeness of a sewage sample, infer the 55 taxon abundance differences across time and space, or interpret errors. Lack of population size information could 56 lead to false negatives in assessing virus eradication, because an absence of biomarkers might be caused by a sewage 57 sample that under-represents the population size. Despite its importance, few studies have explicitly explored ways 58 to estimate real-time human population size from sewage samples independent from census estimates¹². 59

Macroecological theories of biodiversity may offer clues to decipher and even enumerate the sources of a sewage microbiome. While we are only beginning to view sewage as samples of human symbionts beyond one person, generating multi-host microbiomes resembles a fundamental random multiplicative process that can give rise to

many universal patterns seen in ecology. It has been suggested that the approximately lognormal shape of the 63 Species-Abundance Distribution (SAD) might result from multiplicative processes¹³. Although ecological processes 64 such as growth and stochastic interactions have a multiplicative nature and could lead to a central limiting pattern, 65 Sizling et al. showed that lognormal SADs can be generated solely from summing the abundances from multiple 66 non-overlapping sub-assemblages to form new assemblages¹⁴. Likewise, adding multiple sub-assemblages can 67 also give rise to common Species-Area Relationships¹⁴. For microbial ecosystems, Shoemaker et al. examined the 68 abilities of widely known and successful models of SADs in predicting microbial SADs and found that Poisson 69 Lognormal distributions outperform other distributions across environmental, engineered, and host-associated 70 microbial communities, highlighting the underpinning role of lognormal processes in shaping microbial diversity¹⁵. 71 In this study, we conceptualize a sewage microbiome as a multi-person microbiome, where the number of human 72 contributors can vary. We hypothesize that the species abundance distribution in the multi-person microbiome will 73 vary as a function of the human population size, which would arise from summing taxon abundances from multiple 74 hosts analogous to the Central Limit Theorem. We use human gut microbiome data comprising over a thousand 75 human subjects and machine learning algorithms to explore these relationships. Upon discovering a generalizable 76 relationship, we develop MicrobiomeCensus, a nonparametric model that utilizes relative taxon abundances in 77 the microbiome to predict the number of people contributing to a sewage sample. MicrobiomeCensus utilizes 78 a multivariate T statistic to capture the simultaneous deviation of multiple taxa's abundances from their means 79 in a human population and performs maximum likelihood estimation. We provide proof on the validity of our 80 approach. Next, we examine model performance through a simulation benchmark using human microbiome data. 81 Last, we apply our model to data derived from real-world sewage. Our nonparametric method does not assume any 82 underlying distributions of microbial abundances and can make inferences with just the computational power of a 83 laptop computer. 84

85 Results

86 Species abundance distributions of multi-person microbiomes vary by population size

Here, we present MicrobiomeCensus, a nonparametric model that utilizes relative taxon abundances in the microbiome to predict the number of people contributing to a sewage sample. We establish MicrobiomeCensus in four steps. First, we demonstrate the usefulness of human microbiome features in estimating population size through a simulation mimicking an ideal mixing scenario in sewage. Then, we propose a T statistic to capture the simultaneous deviation of multiple taxa's abundances from their means in a human population, build a maximum likelihood model, and provide proof on the validity of our approach. Next, we examine model performance

through a simulation benchmark using human microbiome data. Last, we apply our model to real-world sewage.
Our nonparametric method does not assume any underlying distributions of microbial abundances and can make
inferences with just the computational power of a laptop computer.

We consider the fraction of microorganisms observed in sewage that are human-associated anaerobes as an 96 'average gut microbiome" sampled from residents of a catchment area. Hence, our task becomes to find the 97 underlying relationship between the number of contributors and the observed microbiome profiles in sewage samples. 98 We define an "ideal sewage mixture" scenario to illustrate our case, where the sewage sample consists only of 99 gut-associated microorganisms and is an even mix of n different individuals' feces (Figure 1). We denote the gut 100 microbiome profile of an individual as $X_i = (X_{i_1}, X_{i_2}, \dots, X_{i_n})^{\mathsf{T}}$, where each X_{i_i} represents the relative abundance of 101 individual i and operational taxonomic unit (OTU) j; hence, our ideal sewage mixture can be represented as a mean 102 from individuals 1,...,*n*: 103

$$\bar{X}_n = \sum_{i=1}^n X_i/n \tag{1}$$

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where X_1, X_2, \ldots, X_n are microbiome profiles from individuals $1, \ldots, n$. Under the ideal sewage mixture scenario, 105 if we can quantitatively capture the departure of the sewage microbiome profile from the population mean of the 106 human gut microbiomes of people constituting the catchment area, we will be able to estimate the population size. 107 Using a dataset comprised of 1,100 individuals' gut microbiome taxonomic profiles¹⁶, we created synthetic 108 mixture samples of different numbers of contributors through bootstrapping (Figure 1A). First, examined from an 109 ecological perspective, the shape of the ranked abundance curves of the gut microbiomes differed when the means 110 of multiple individuals were examined: when the number of contributors increased, dominance (Figure 1B). For 111 the single-person microbiomes, log-series and lognormal distributions explained 94% and 93% of the variations 112 in the SADs, respectively, compared with 89% for Poisson lognormal, 87% for Zipf multinomial and 80% for the 113 broken-stick model. Multi-person microbiomes were best predicted by log-series or lognormal models, but as the 114 population increased to over a hundred, the multi-person SADs were best described by only lognormal SADs (Table 115 S1). The predictive performance of the lognormal is expected to be good for the gut microbial communities across 116 different sizes because they can reflect processes of a multiplicative nature¹⁵. 117

We explored the distributions of the relative abundances of gut bacteria as a function of population size. As expected, the distribution of a taxon's relative abundance changes with population size (Figure 1C). For instance, for OTU-2397, a *Bifidobacterium* taxon, the relative abundance distribution was approximately log-normal when the relative abundance in single-host samples was considered, yet converged to a Normal distribution when mixtures of multiple hosts were considered. Although the means of the distributions of the same taxon under different population sizes were close, the variation in the data changed. A smaller variance was observed when the number of contributors increased (Figure 1D). Notably, different taxa varied in the rates at which their variances decreased with population size (Figure 1E), suggesting that a model that considers multiple features would be useful in predicting the number of contributors.

Classifiers utilizing microbial taxon abundance features alone detects single-person and multi-person microbiomes

Next, we set up a classification task using the taxon relative abundances to separate synthetic communities constituting one, ten, and a hundred people. With algorithms of varying complexity, namely Logistic Regression (LR), Support Vector Machine (SVM), and Random Forest (RF) classifier, classification accuracies of 29.6%, 97.2%, and 100% were achieved (Figure 2). Between RF and SVM, RF showed higher sensitivity and specificity in classifying all population groups (Table S2). This experiment suggests the usefulness of microbiome features in predicting human population counts from mixture samples.

¹³⁵ MicrobiomeCensus is a statistical model that estimates population size from microbial taxon abundances

While the classification tasks described above demonstrated the usefulness of taxa's relative abundances in predicting the population size, a complex model like RF provides little explanatory power. We then ask, since the variance in the relative abundance of a given taxon decreases with population size, can we devise a statistic that captures the simultaneous deviation of several taxa's abundances from their means, and estimate population size utilizing the statistic? Further, will this new method perform well despite inter-personal variation in gut microbiomes?

Our new method, MicrobiomeCensus, involves a T statistic to capture the simultaneous deviation of multiple taxa's abundances from their means in relation to the variance of those taxa in the population (Figure 3A):

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$$T = ||\Lambda_0^{-1}(\bar{X}_n - u)||_2^2,$$
(2)

where $\bar{X}_n = \sum_{i=1}^n X_i/n$ denotes the observed microbiome profile in ideal sewage, u denotes the population mean for the catchment area, and Λ_0 denotes the diagonal of the covariance matrix, $\Sigma_0 = (\sigma_{ij})_{1 \le i,j \le p}$, i.e., where $\sigma_i = \sigma_{ii}^{1/2}, 1 \le i \le p$.

In developing this new method, we utilize the variance change by population, but without an *a priori* assumption about the gut bacterium species taxon abundance distributions and the covariance between species. Our analysis showed that the *T* statistic changed monotonically with increasing population size, indicating the promise of a

population estimation model (Figure 3B). While our *T* statistic is based on Hotelling's T-squared statistic¹⁷, which is often used in multivariate T-tests, we extend its application beyond the problem of the significance of the multivariate means.

Leveraging our T statistic, we build a maximum likelihood model to estimate population size from an unseen 154 sample. Here, the parameter of interest is the population size, the test statistic is our T statistic, and a point estimate is 155 made by maximizing the likelihood of the observed T statistic in that sample. We performed training and validation 156 using 50% of the human microbiome data and held out the rest of the data for testing. Our model achieved a training 157 error as low as 0.13 (mean absolute percentage error, MAPE) when up to 250 features are included. The model's 158 training performance increased when more features were included, yet the validation error did not profoundly change 159 with an increasing number of features (Figure 3C). Upon training and validation, we chose the top 120 OTUs and 160 tested the performance of the tuned model on a test set held out during training/validation. The model's MAPE was 161 0.21 (Figure 3D and E, testing errors at each population size evaluated are provided in Table S3), indicating that our 162 model generalized well across different hosts. We then used all data and tuned hyperparameter to acquire a final 163 model. When applying the final model on the same testing data, our model achieved a testing error of 0.162 (Figure 164 3D). 165

It is worth noting that in this algorithm, for each population size, we need to calculate the sampling distribution of the *T* statistic only once, hence it is not time-consuming, regardless of the true population size. We also note that an RF regression model could not be trained in a reasonable time on the same dataset, even with high-performance computing (Methods). Our model performed remarkably better than a ten-fold cross-validated RF regression model utilizing a reduced dataset, which gave an MAPE of 0.320, while the training time for our model was only a fraction of that of the RF regression model (Figure S1).

172 MicrobiomeCensus detects human population size differences in sewage samples

With the newly developed population model, we set out to apply our model to sewage samples. Ideally, we 173 would like to apply the model to samples generated from a fully controlled experiment with known human hosts 174 contributing at a given time, yet such an experiment presents logistic challenges beyond the field's current abilities. 175 Instead, we applied our model to sewage samples taken using one of two methods, either a snapshot (grab sample) 176 sample taken from the sewage stream over 5 minutes, or an accumulative (composite sample) taken at a constant rate 177 over 3 hours during morning peak human defecation¹⁸ (Figure S2). We hypothesized that the composite samples 178 would represent more people than snapshot samples. Taking grab samples, we sampled at 1-hr intervals at one 179 manhole (n=25); using the accumulative method, we sampled at three campus buildings (classroom, dormitory, and 180

family housing) multiple times over three months (n=76). To remove sequences possibly contributed by the water, we applied a taxonomic filter to retain families associated with the gut microbiome and normalized the species abundance by the retained sequencing reads (Methods, Table S4). We applied our final model to the sewage data set. Our model estimated 1-9 people's waste was captured by the snapshot samples (mean=3, s.d.=3), and 3-27 people were represented by the composite samples (mean=9, s.d.=7), where the composite samples represented significantly more people (p < 0.0001) (Figure 3F). The hypothesis that composite samples represent more people is well supported by our model results.

¹⁸⁸ Sub-species diversity in sewage samples reflects adding microbiomes from multiple people

Independent from our MicrobiomeCensus model, we found that certain human gut-associated species were frequently detected in sewage samples by using shotgun metagenomics, e.g., *Bacteroides vulgatus*, *Provotella copri*, and *Eubacterium rectale*. Further, their sub-species diversity, as indicated by nucleotide diversity and the number of polymorphic sites in housekeeping genes, was dramatically higher in sewage samples than in the gut microbiomes of individual human subjects (Figure 4A-F and Supplementary Results).

To examine the effect of increasing population size on sub-species genetic variation in representative gut-194 associated microbial species, we simulated aggregate human gut samples using a sample without replacement 195 procedure and computed the nucleotide diversity and numbers of polymorphic sites for the aggregate samples at 196 different population sizes. This resulted in SNV profiles from 64 species. Our simulation showed increases in both 197 nucleotide diversity and the number of polymorphic sites as more human gut samples were aggregated (Figure 3 G 198 and H). For instance, the nucleotide diversity and number of polymorphic sites in *Eubacterium rectale* increased 199 from 0.029 (s.d. 0.026) to 0.149 (s.d. 0.002) and 64 (s.d. 54.33) to 1274 (s.d. 18.41), respectively, when the 200 population size increased from 1 to 300. Further, the number of polymorphic sites strongly correlated with the 201 population size (Pearson correlation coefficient > 0.8) in 49 of the 64 species (Table S7), suggesting the potential that 202 the SNV profiles of a wide range of gut species could be developed into feature space for population size estimation. 203 Our simulation further shows that the number of polymorphic sites increased with population size more slowly than 204 nucleotide diversity, indicating its potential to reflect more subtle changes in population size (Figure 4G and H). 205 Despite the need for further model developments, the analysis here shows the potential of the sub-species diversity 206 of gut anaerobes as a feature space to be developed into a population size estimation model, independent from the 207 taxon abundance-based model described here. 208

209 Discussion

MicrobiomeCensus showed excellent performance in our simulation benchmark. In particular, the study subjects 210 that we utilized in the training and testing sets are random samples out of 1.110 men and women across a wide range 211 of age without any stratification, hence the model's testing performance indicates its generalizability. Our study is 212 founded on the observations that healthy gut microbiomes are resilient, with inter-individual variability outweighing 213 variability within individuals over time^{19–21}. There are caveats to our approach; potentially, diets and regional effects 214 on human microbiome composition could introduce noises to the prediction^{?,22}. In applications to sewage, future 215 studies on water matrix effects should be performed to understand and further account for noises from the sewage 216 collection network. In further validating and applying the model, we recognize that both the responsible engagement 217 of citizen scientists and privacy protection are crucial for advancing sewage-based ecological and public health 218 studies. 219

Utilizing sewage to understand population-level dynamics of human symbionts presents an interesting scenario 220 of sampling meta-communities. The gut microbiomes of humans can be viewed as local communities, and gut 221 microbiomes of people living in a neighborhood could be viewed as a kind of regional meta-communities, because 222 these communities are linked by dispersal that can take place among people connected by social networks and 223 through a shared built environment. The meta-community framework is considered to provide useful new conceptual 224 tools to understand the largely unexplained inter-personal variability in gut microbiomes, with expansions of the 225 theory to consider biotic interactions suggested by Miller, Svanbäck, and Bohannan²³ In considering a sample of 226 meta-communities, Leibold and Chase asked provocatively "what is a community?" and observed that the definition 227 of a community is usually "user-defined and could be context-dependent" - "one community ecologist might explore 228 the patterns of coexistence and species interactions among species within a delimited area, the other might ask the 229 same question but define a community that encompasses more area and thus types of species, as well as different 230 degrees of movements and heterogeneity patterns"²⁴. The ambiguity between samples of meta-communities and 231 local communities is particularly challenging for samples of microbial communities, because dispersal boundaries are 232 difficult to delineate. Despite the conceptual importance, empirical methods that explicitly test whether a microbiome 233 sample is a sample of a meta-community or a local community has not been available. MicrobiomeCensus directly 234 distinguishes samples of meta-communities and local communities by enumerating the number of hosts contributing 235 to a microbiome. While MicrobiomeCensus is trained on gut microbiome data, the procedure may have wide 236 applications in other microbial ecosystems. 237

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In response to the COVID-19 pandemic now affecting the human population globally, sewage-based virus

monitoring is underway(Bivins et al. 2020). Our analysis calls for attention to the denominator used in normalizing 239 the biomarker measurements. While in practice, loading-based population proxies such as the copy numbers of 240 pepper mild mottle viruses are used to normalize data generated from sewage, such proxies would likely have high 241 error at the neighborhood level because of their variability in human fecal viromes (10⁶-10 virions per gram of dry 242 weight in fecal matters)¹¹, while they likely have reasonable performance when the population size is sufficiently 243 large and the means of biomarker loadings converge under the Central Limit Theorem. Thus, the relationships 244 between sewage measurements and true viral prevalence in small populations are hard to establish despite the 245 need for sentinel population studies. Our model has immediate application in detecting false negatives, because it 246 alerts us to the possibility that an absence of biomarkers might be caused by a sewage sample that under-represents 247 a population. With further developments incorporating local training data, the model can potentially generate a 248 denominator that can help turn biomarker measurements into estimates of prevalence and enable the application of 249 epidemiology models at finer spatio-temporal resolutions. 250

251 Methods

Proof. Recall $X_1, X_2, ..., X_n$ are independent and identically distributed (i.i.d) random vectors in \mathbb{R}^p with mean $u \in \mathbb{R}^p$ and variance $\operatorname{Var}(X_i) = \Sigma_0 \in \mathbb{R}^{p \times p}$. (Note $X_i = (X_{i1}, ..., X_{ip})^{\mathsf{T}}$ and in our application, each X_{ij} represents the value for person *i* and bacteria *j*.) Denote $\Sigma_0 = (\sigma_{ij})_{1 \le i,j \le p}$ and $\sigma_i = \sigma_{ii}^{1/2}, 1 \le i \le p$. Let $\Lambda = \operatorname{diag}(\sigma_i, 1 \le i \le p)$. If both Σ_0 and *u* are given, then we can construct our statistic:

256
$$T_n = \|\Lambda_0^{-1}(\bar{X}_n - u)\|_2^2,$$

where $\bar{X}_n = \sum_{i=1}^n X_i/n$. For notation's simplicity, consider $Y_i = \Lambda_0^{-1}(X_i - u)$, the normalized version of X_i . Then

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$$T_n = \|\bar{Y}_n\|_2^2,$$

where $\bar{Y}_n = \sum_{i=1}^n Y_i/n$. Then the covariance matrix Σ for Y_i is the correlation matrix of X_i , with expression $\Sigma = \Lambda^{-1}\Sigma_0 \Lambda^{-1}$.

We need the following condition on Y_i for the main theorem.

ASSUMPTION 1 Let $\delta > 0$. Assume

$$K_{\delta}^{2+\delta} = \mathbb{E} \left| \frac{\|Y_1\|_2^2 - p}{\|\Sigma\|_F} \right|^{2+\delta} < \infty, \quad \text{and} \quad D_{\delta}^{2+\delta} = \mathbb{E} \left| \frac{Y_1^\top Y_2}{\|\Sigma\|_F} \right|^{2+\delta} < \infty.$$
(3)

REMARK 1 Above conditions naturally hold if Y_{1i} , $1 \le i \le p$, are independent and $\max_{1 \le i \le p} ||Y_{1i}||_{2+\delta} \le M < \infty$. Actually under this setting, $\Sigma = I_p$ and thus $||\Sigma||_F = p^{1/2}$. By Lemma 1,

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$$\mathbb{E}\Big(\big|\|Y_1\|_2^2 - p\big|^{2+\delta}\Big) \le (1+\delta)^{2+\delta}\Big(\sum_{i=1}^p \|Y_{1i}^2 - 1\|_{2+\delta}^2\Big)^{(2+\delta)/2} \lesssim p^{(2+\delta)/2},$$

where the constant in \leq only depends on δ . This justifies K_{δ} part in condition (3). Similarly by Lemma 1,

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$$\mathbb{E}\Big(|Y_1^\top Y_2|^{2+\delta}\Big) \le (1+\delta)^{2+\delta} \Big(\sum_{i=1}^p \|Y_{1i}Y_{2i}\|_{2+\delta}^2\Big)^{(2+\delta)/2} \lesssim p^{(2+\delta)/2}$$

269 And thus D_{δ} part in condition (3) holds.

Theorem 1 Assume Assumption 1 holds with some $\delta > 0$, also assume

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$$K_0^2/n + K_{\delta}^q/n^{q-1} + D_{\delta}^q/n^{\delta/2} \to 0,$$
 (4)

where $q = 2 + \delta$. Then for $Z \sim N(0, \Sigma)$, we have

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$$\sup_{t\in\mathbb{R}} \left| \mathbb{P}(nT_n \le t) - \mathbb{P}(\|Z\|_2^2 \le t) \right| \to 0.$$

It is worth noticing that under settings in Remark 1, condition (4) holds. The proof follows from Theorem 2.2 in Xu et al.²⁵.

Based on above theorem, we would have the following result for justification of our sub-sampling approach. Let A_1, A_2, \dots, A_J be i.i.d uniformly sampled from the class $\mathscr{A}_m = \{A : A \subset \{1, 2, \dots, n\}, |A| = m\}$. Assume the sampling process are independent from our data $(X_i)_i$.

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$$\hat{F}_m(t) = J^{-1} \sum_{j=1}^J \mathbf{1}_{m \| \Lambda_0^{-1}(\bar{X}_{A_j} - \bar{X}_n) \|_2^2 \le t(1 - m/n)},$$

- where $\bar{X}_{A_i} = \sum_{i \in A_i} X_i / m$. Following result comes from Theorem 3.5 in Xu et al.²⁵.
- **Theorem 2** Assume Assumption 1 holds with some $\delta > 0$, also assume $m \to \infty$, m = o(n) and (4) is satisfied with n replaced by m. Then for $J \to \infty$, we have

$$\sup_{t\in\mathbb{R}}|\hat{F}_m(t)-\mathbb{P}(\|Z\|_2^2\leq t)|\to 0.$$

²⁸² Therefore under conditions in Theorems 1 and 2, we have

$$\sup_{t\in\mathbb{R}}|\hat{F}_m(t)-\mathbb{P}(mT_m\leq t)|\to 0.$$
(5)

Note T_m is an infeasible estimator since u and Λ_0 are typically unknown. Therefore we need to estimate u and Λ_0 , using our data X_1, \ldots, X_{n_0} where n_0 is the number of observations we have. Consider the estimate

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$$\hat{u} = \bar{X}_{n_0}, \text{ and } \hat{\Lambda}_{0,j}^2 = \sum_{i=1}^{n_0} (X_{i,j} - \bar{X}_{n_0,j})^2 / n_0, \quad 1 \le j \le p,$$

where $\Lambda_{0,j}$ is the *j*th entity of Λ_0 . If X_i has heavy tail, we can also consider robust m-estimator for \hat{u} and $\hat{\Sigma}_0$, see for example, Catoni²⁶.

LEMMA 1 (BURKHOLDER²⁷, RIO²⁸) Let q > 1, $q' = \min\{q, 2\}$. Let $D_T = \sum_{t=1}^T \xi_t$, where $\xi_t \in \mathscr{L}^q$ are martingale differences. Then

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$$||D_T||_q^{q'} \le K_q^{q'} \sum_{t=1}^T ||\xi_t||_q^{q'}, \text{ where } K_q = \max\left\{(q-1)^{-1}, \sqrt{q-1}\right\}.$$

Bootstrap procedure. Below we describe the bootstrap procedure we use to approximate the distribution of *T* for different census counts. Recall that $X_1, ..., X_m$ represents arrays of taxon relative abundances in the gut microbiome of human subject 1, ..., m, and *T* is defined in (Eq. 2).

Step 1. Estimate the population mean, \hat{u} , and diagonal matrix, $\hat{\Lambda}_0$, from a sample human gut microbiome.

Step 2. For each census count *N*, generate X_1^*, \ldots, X_m^* which is equivalent to drawing a simple random sample with replacement from $\{X_1^*, \ldots, X_m^*\}$. Compute \hat{T}_1^* on the resulting bootstrap sample.

Step 3. Repeat Step 2 many times, B, (herein 10,000 times) to get $\hat{T}_1^*, \ldots, \hat{T}_B^*$.

Step 4. Estimate the distribution of \hat{T}^* at census count N, using a Gaussian kernel.

Step 5. Repeat Steps 2-4 for all the census counts $1, \ldots, N$ considered, herein integers from 1 to 300. It should be noted that per Theorem 2 we require bootstrap sample size much smaller than total sample size, thus up to 300-person samples were simulated here because the gut microbiome dataset we utilized consisted of a total of 1010 people. The range can be expanded if a larger dataset is available.

Maximum Likelihood Estimation. We use a maximum likelihood estimation (MLE) procedure to achieve point estimates of the population size from a new mixture sample, X_0 . The MLE procedure first computes T_0 from X_0 , and then computes the likelihoods that T_0 was drawn from population sizes from 1 to *B*, respectively, using the

sampling distributions generated from the bootstrap procedures described above. Next, the population size that yields the highest likelihood is chosen. For a point estimate N, the confidence interval for the population size, N, is [1,N].

Model training, validation, and testing. We synthesized a mixed data set from a gut microbiome dataset of 309 1,135 healthy human hosts from the Lifelines Deep study¹⁶, which was the largest single-center study of population-310 level human microbiome variations from a single sequencing center at the time of this study. The data set consisted of 311 661 women and 474 men. We considered OTUs defined by 99% similarity of partial ribosomal RNA gene sequences 312 (Methods of OTU clustering are described in detail in Supplementary Methods). After quality filtering, we retained 313 1,110 samples that had more than 4,000 sequencing reads/sample. We split the entire dataset approximately in half, 314 using 550 subjects to generate the training/validation set and the other 550 subjects to generate the test set. We then 315 used the aforementioned ideal sewage mixture approach to generate synthetic populations of up to 300 individuals, 316 which is the relevant range for population estimation in upstream sewage. The training error was computed using the 317 entire training data set. Five repeated holdout validations using a 50-50 split in the training set were performed to 318 tune the hyperparameter for feature selection. The training and cross-validation errors were evaluated at integers 319 from 1 to 100, using the error definition: 320

$$\delta = \left|\frac{N_{predicted} - N_{actual}}{N_{actual}}\right| \times 100\%,\tag{6}$$

and the model's performance across all the population sizes was characterized by the mean absolute percentage error
 (MAPE):

$$MAPE = \frac{1}{n} \sum_{n=1}^{100} \left| \frac{N_{predicted} - N_{actual}}{N_{actual}} \right| \times 100\%.$$
(7)

After training and validation, the hyperparameter (in this case, the top k abundant OTUs) that yielded the best performance in the validation step was used in the model. The tuned model was then tested on the test set. Our synthetic sewage microbiome approach captured the actual microbiome variation among individual hosts and demonstrated the model's generalizability.

Human gut microbiome 16S rRNA amplicon data source. The single-person and multi-person microbiome data were drawn from a gut microbiome dataset of 1,135 healthy human hosts from the Lifelines Deep study¹⁶, which was the largest study of population-level human microbiome variations from a single sequencing center at the time of this study. The data set consisted of 661 women and 474 men. We considered operational taxonomic

units defined by 99% similarity of partial ribosomal RNA gene sequences. After quality filtering, we retained 1,100
 samples that had more than 4,000 sequencing reads/sample. The rarefaction depth was chosen to balance sample
 size and sequencing depth.

16S rRNA gene amplicon sequencing data analysis. Operational taxonomic units defined at 99% sequencing similarity were generated from the combined dataset by first denoising the samples with DADA2²⁹, and then clustering the outputted exact sequence variants with the q2-vsearch plugin of QIIME2³⁰. Taxonomic assignments were performed using a multinomial naïve Bayes classifier against SILVA $132^{31,32}$. All 16S rRNA gene amplicon analyses were performed in the QIIME2 platform (QIIME 2019.10)³³.

Species Abundance Distribution. We examined the relationships between the performances of several widely 341 used SAD models and the number of contributors (population size) to a multi-person microbiome. Multi-person 342 microbiomes were generated by sampling N individuals from the quality-filtered gut microbiome 16S rRNA dataset 343 and summing the abundances of the same taxa. At each population size, 10,000 repeats were performed. The repeats 344 were chosen according to the constraints of computational efficiency. The SADs evaluated included the Lognormal, 345 Poisson Lognormal, Broken-stick, Log series and the Zipf model, which were shown to have varied successes 346 in predicting microbial SADs¹⁵. We examined the fit using a rank-by-rank approach as previously described by 347 Shoemaker et al.¹⁵. First, maximum-likelihood coefficients for each of the SADs described above were estimated 348 using the R package sads³⁴. Next, SADs were predicted using each model, and tabulated as RADs. Then, we used 349 a least-squares regression to assess the relationship between the performance of the predicted SADs against the 350 observations and recorded the coefficient of determination (R-squared). Last, R-squared values from model fits of 351 each SAD model were summarized as the means, and the models that resulted in the highest R-squared values for 352 each simulated community were recorded. 353

Field data. We conducted a field sampling campaign, collecting sewage samples daily at manholes near three 354 buildings (two dormitory buildings and one office building) on the campus of Massachusetts Institute of Technology. 355 Seventy-six sewage samples were collected through a continuous peristaltic pump sampler operated at the morning 356 peak (7-10 a.m. near the dormitory buildings and 8-11 a.m. near the office building) at 4 mL/min for 3 hours. 357 Wastewater was filtered through sterile 0.22-µm mixed cellulose filters to collect microbial biomass. Environmental 358 DNA was extracted with a Qiagen PowerSoil DNA extraction kit according to the manufacturer's protocol. The 359 DNA was amplified for the V4 region of the 16S rRNA gene and sequenced in a Miseq paired-end format at 360 the MIT BioMicro Center, according to a previously published protocol³⁵. Included as a comparison are a set of 361 snapshot sewage samples taken using a peristaltic pump sampler at 100 mL/min for 5 minutes over a day (10 a.m. 362

on Wednesday April 8, 2015, to 9 a.m. on Thursday April 9, 2015). The sampling methods for snapshot samples are described in detail by Matus et al.⁴

Application to sewage data. 1he 16S rRNA gene amplicon sequencing data from the field sewage samples 365 were trimmed to the same region, 16S V4 (534-786) with the LifeLines Deep data using Cutadapt 1.12^{36} . Forward 366 reads were trimmed to 175bps, and reverse reads were first trimmed to 175bps and then further trimmed to 155bps 367 during quality screening. We created a taxonomic filter based on the composition of the gut microbiome data set, 368 which consisted of the abundant family-level taxa that accounted for 99% of the sequencing reads in the human gut 369 microbiome data set, and excluded those that might have an ecological niche in tap water (Enterobacteriaceae and 370 Burkholderiaceae). This exclusion resulted in 25 bacterial families and one archaeal family in our taxonomic filter, 371 including Lachnospiraceae, Ruminococcaceae, Bifidobacteriaceae, Erysipelotrichaceae, Bacteroidaceae, and others 372 (Table S4). We applied our taxonomic filter to the sewage sequencing data, which retained 73.9% of the sequencing 373 reads. This retention rate is consistent with our previous report of the human microbiome fraction in residential 374 sewage samples⁴. We then normalized the relative abundance of taxa against the remaining sequencing reads in each 375 sample. Welch's two-sample t-tests were performed to retain the OTUs whose means did not differ significantly 376 from the human microbiome data set (p > 0.05). 377

Deployment of generic machine learning models. Logistic regression, support vector machine, and random 378 forest classifiers were employed to perform the classification task for population sizes of 1, 10, and 100. Model 379 training, cross-validation, and testing were performed using the R Caret platform with the default setting³⁷. For 380 the support vector machine, the radial basis function kernel was employed. Ten-fold cross-validation and five 381 repeats were performed for all the models considered. Model performance was evaluated using accuracy, sensitivity, 382 and specificity. Based on the classifier performance, the RF regression model was used for comparison with 383 our new model's performance. Initially, we trained the model using the same training data set used in training 384 our maximum likelihood model, however, the computation was infeasible, even with a 36-thread, 3TB-memory 385 computing cluster. We then introduced gaps in the population size range, using populations from the vector 386 $(1, 5, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 150, 180, 240, 300)^T$ while maintaining the same sample size at 387 each population size (10,000 samples). The training was performed in R Caret, using 10-fold cross-validation. Ten 388 variables were randomly sampled as candidates at each split, mtry=10. The performance was evaluated using the 389 same testing set that was used to evaluate the maximum likelihood model. 390

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482 Author contributions statement

F.L. and E.J.A. designed the study; F.L. performed simulation; L.C. performed mathematical proofs; F.L., X.Y. and
L.Z. performed sequence analysis; F.L., S.I., C.Dai., and S.P. performed sewage experiments; C. Duvallet, K. F-M,
F.D. C.R. and E.J.A. coordinated the acquisition of sequencing data; F.L., L.C., and E.J.A wrote the manuscript.

486 Competing interests

487 E.J.A has an equity stake in Biobot Analytics. C. Duvallet is employed by Biobot Analytics.

488 Code and data availability

Source code will be made available through https://github.com/linglab-washu/population-model upon publication.
 Sewage metagenomic data will be made available at National Center for Biotechnology Information Short Read
 Archive at BioProject PRJNA683921 upon the time of publication.

492 Figure Legends

Figure 1. An ideal sewage mixture simulation shows the potential of microbiome taxon abundance profiles as population census information sources. (A) We generated an "ideal sewage mixture" consisting of gut microbiomes from different numbers of people. (B) Ranked abundance curves for gut microbiomes of one person and mixtures of multiple people exhibit different levels of dominance and diversity. Blue lines show the rank abundance curves in stool samples (one person), red lines show 10-person mixtures, and saffron lines show 100-person mixtures. In each scenario, ten examples are shown. All samples were rarefied to the same sequencing depths (4,000 seqs/sample). (C)

The probability density function of the relative abundance of one taxon for different population sizes. OTU-2379, a *Bifidobacterium* taxon, was used as an example. Maroon dashed lines indicate the sample means. (D) Multiple taxa's abundance variances in one-person samples and 100-person samples. The dominant taxa are shown (top100) and are sorted by their ranks in variance. (E) The ratios of the variances of one-person samples and 100-person samples across dominant gut microbial taxa.

Figure 2. Classifier performance of models utilizing gut microbiome taxon abundances.

Figure 3. MicrobiomeCensus statistic definition, model training, validation, and application. (A) Example of 505 computing the T statistic. (B) Simulation results for T with different population sizes. Grey points are simulation 506 results. Red bars are means of 10,000 repeats performed for each population size. (C) Model training and tuning. 507 We built the MicrobiomeCensus model using our T statistic and a maximum likelihood procedure. The training 508 set consisted of 10,000 samples for population sizes ranging from 1-300, and 50% of the data were used to train 509 and validate the model. Training and validation errors from different feature subsets are shown. Training errors are 510 shown as red lines, and validation errors are shown as blue lines. (D) Model performance on simulation benchmark. 511 After training and validation, the model utilized the top 120 abundance features. Model performance was tested on 512 synthetic data generated from 550 different subjects not previously seen by the model. The training set consisted of 513 10,000 samples with population sizes from 1-300, and the testing set consisted of 10,000 repeats at the evaluated 514 population sizes. The training error, testing error, and the error of the final model are shown. (E) Model performance 515 evaluated using a testing set. Black solid dots indicate the means of the predicted values, and error bars indicate 516 the standard deviations of the predicted values. (F) Application of the microbiome population model in sewage. 517 Seventy-six composite samples (blue) were taken from three manholes on the MIT campus, and each sample was 518 taken over 3 hours during the morning peak water usage hours. Twenty-five snapshot samples (grey) were taken 519 using a peristaltic pump for 5 minutes at 1-hour intervals throughout a day. 520

Figure 4. Sub-species diversity in gut-associated bacterial species as a potential marker for human population size. (A-F) Comparison of sub-species diversity of gut-associated bacteria in human gut microbiome samples (LifelinesDeep) and MIT sewage samples. Nucleotide diversity and numbers of polymorphic sites were computed from ten phylogenetic marker genes. (G) and (H) Simulation results showing intra-species diversity in response to increasing population size, as represented by the number of polymorphic sites (G) and nucleotide diversity (H).

Figure 1.



Figure 2.



Figure 3.



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Figure 4.

