Title: Factors contributing to the accumulation of reproductive isolation: a mixed model approach

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Abstract
Studies utilizing large data sets that characterize reproductive isolation (the ability to cross and produce hybrids) across species with varying degrees of relatedness have been extremely influential in the study of speciation. However several limitations have made it difficult to test specific hypothesis about factors that predict the evolution of reproductive isolation. In particular, the statistical methods typically used are limited in their ability to test complex hypotheses involving more than one predictor variable; at least one method, the Mantel Test, has also been found to be unreliable. In this paper I describe a framework to determine which factors contribute to the evolution of reproductive isolation using phylogenetic linear mixed models. Phylogenetic linear mixed models do not suffer from the same statistical limitations as other methods and I demonstrate the flexibility of this framework to analyze data collected at different evolutionary scales, to test both categorical and continuous predictor variables, and to test the effect of multiple predictors simultaneously, all of which cannot be achieved using any other single statistical method. I do so by re-analyzing several classic data sets and explicitly testing hypotheses that had previously been untested directly, including differences in accumulation of reproductive isolation between sympatric and allopatric species pairs.
**Introduction**

The divergence of lineages (speciation) is only complete after gene flow is highly reduced due to the evolution of reproductive isolation. Two general modes of reproductive isolation are prezygotic and postzygotic barriers to reproduction. Patterns of reproductive isolation inferred from comparative analyses of crossability (species willingness/ability to mate and produce viable and fertile offspring) have generated important and influential observations about the rate of evolution of reproductive isolation, especially comparing allopatric and sympatric species pairs, or prezygotic and postzygotic barriers to reproduction (Coyne and Orr 1989, Presgraves 2002, Mendelson 2003, Moyle et al. 2004, Funk et al. 2006, Malone and Fontenot 2008, Meiners and Winkelmann 2012). These analyses have produced iconic patterns/rules of speciation including that reproductive isolation accumulates more quickly between sympatric species pairs compared to allopatric species pairs and, specifically, that in sympatry prezygotic reproductive isolation appears more quickly than postzygotic reproductive isolation. Nonetheless, the contemporary methods used to analyze these data are known to suffer from both statistical errors and analytical limitations that prevent a more robust simultaneous assessment of the factors that most strongly influence the accumulation of reproductive isolation.

The two methods most typically relied upon to analyze crossability data are Mantel tests, including partial mantel tests (Mantel 1967, Smouse et al. 1986), and phylogenetic regression based on generalized least squares or independent contrasts (Felsenstein 1985, Grafen 1989). These two methods (Mantel/matrix regression vs. PICs) also typically reflect differences in the scale of relationships between lineages that are being tested. Studies that use PICs, or node based averages (Fitzpatrick and Turelli 2006), generally have some information about phylogenetic or exact sister species relationships such that they can accurately calculate contrasts. The use of PICs or methods that assume independence of lineages are not appropriate for intraspecies data.
(Slatkin et al. 2002, Stone et al. 2011). Thus, Mantel tests are often applied when specific phylogenetic relationships are unknown (if few molecular markers are used) and/or lineages being tested include extensive sampling from only a few species. The main limitations of these approaches are threefold: lack of statistical power, failure to deal adequately with non-independence, and the inability to test categorical variables and/or multiple variables simultaneously. The first two limitations have been discussed in detail for the Mantel test (Legendre 2000, Harmon and Glor 2010) and it has been determined that Mantel tests can have unacceptably high type-I error rates (Legendre 2000, Harmon and Glor 2010). The last limitation results in the inability to test biologically interesting hypotheses, and applies equally to both Mantel test and PIC type tests. For example, in many of the classic studies the comparisons between sympatric vs. allopatric rates of evolution were never formally tested with a statistical model. Recent attempts to refine the patterns of the accumulation of reproductive isolation have also included other explanatory variables, including ecological differences, range size overlap, and other traits (Yukilevich 2012, Turelli et al. 2014), but have not tested multiple variables simultaneously or the interaction between these variables.

Categorical variables are of particular interest to most researchers as they can describe geographic relationships (allopatry vs. sympatry), mating systems (animals: monogamy vs. polygamy, plants: outcrossing vs. selfing), or phenotypic traits (e.g., pigmentation/patterning) that could have very strong influence on the rate and strength of isolation accumulation. Categorical variables can be difficult to implement in Mantel tests because they rely on pairwise distance matrices that require no missing data (Mantel 1967). When these variables can be represented as distances, multiple matrix regression can be used, but most typically are only used on binary categorical variables (Legendre and Fortin 2010, Wang 2013) because the extension
becomes more difficult when comparing categorical variables with multiple levels. Mantel tests based on pairwise distance cannot accommodate these hypotheses. Regression models are the most promising for incorporating categorical variables, but the analysis is not simple when the regression is carried out using PICs. Continuous variables can be accommodated because they are assumed to evolve under Brownian motion; this is what enables node values to be estimated and contrasts to be evaluated. However an analogous model does not exist for categorical variables, unless all daughter taxa (taxa derived from a common ancestor) share the same categorical value (Burt 1989). Even with this conservative approach the number of contrasts would be reduced tremendously in studies of crossability, and may not be applicable to most systems. One way of circumventing this issue would be to analyze the cross product of a categorical and continuous variable (Garland et al. 1992); however, although it takes these models a step further by analyzing differences in slope (assuming genetic distance is a covariate), it cannot be used to estimate mean crossability because regression in PICS is constrained to pass through the origin.

To accommodate more complex hypotheses, a more appropriate and powerful analytical framework should be: 1) flexible to test explicit hypothesis with multiple variables (both continuous and categorical) and 2) able to handle different data types to cover differences in taxonomic scale. Here I describe a framework that overcomes several limitations of current approaches to analyzing these data. Specifically this framework can be used to test whether geographical context, and/or any other trait hypothesized to be important to speciation, contribute to patterns of crossability using comparative crossing data and phylogenetic linear mixed effect models (similar to phylogenetic least squares, PGLS). Using linear models allows flexibility in the hypothesis being tested and can include categorical predictors and multiple
predictors simultaneously. The advantage over PICs is that the phylogenetic structure is modeled as a covariance matrix, and thus contrasts for categorical predictors do not have to be calculated. The use of this covariance matrix allows/accounts for phylogeny by either using a pairwise distance matrix or a phylogeny. I use this framework to reanalyze classic data sets (Drosophila, Bufonidae, Silene) making explicit statistical comparisons between allopatric and sympatric conditions as an example of how categorical variables can be included in these types of analyses. In addition I test two new hypotheses about the relationship between floral differences and crossability in each of the plant genera Silene and Nolana.

Methods

Description of Linear Mixed Model Approach

In their most basic form, linear mixed models include a response variable (y), fixed effects (XB), random effects (Zu), and residuals (e), where X is the fixed effect design matrix, B is the vector of estimated coefficients, Z is the random effect design matrix, and u is a vector of random effect estimators.

\[ y = X\beta + Zu + \varepsilon \]  

(1)

Relatedness either via pedigree or phylogeny is incorporated into a structured matrix (typically A, the additive genetic relatedness matrix, see (Hadfield 2010, Hadfield and Nakagawa 2010)) that is considered known and contributes to defining the variance structure of random effects in the model. In equation (2) the random effect estimators are distributed normally with mean=0 and variance matrix G. This matrix can be decomposed into a standard variance/covariance matrix V, and the structured matrix A (Equation 3)
\[ u \sim N(0, G) \]  
\[ G = V \times A \]  

In this modeling framework I also include a pair-wise genetic distance matrix \( D \) because of its similarities to the additive genetic relatedness matrix. Each element of \( A \), in the absence of inbreeding, represents the expected proportion of genes shared by two individuals. Values range from 0 (completely unrelated individuals) to 1 (completely identical individuals). Whereas some measures of genetic distance are not bound by 0 and 1, (Euclidean distances, Nei’s standard genetic distance (Nei 1972)), others formally meet this requirement (Nei’s \( D_A \) distance (Nei et al. 1983), Wier and Cockerham \( \theta \) (Weir and Cockerham 1984)), and in most actual studies values are rarely seen above 1. In these distance measures values of 0 represent more closely related populations, so for my analysis that uses the \( D \) matrix, I use \( 1-D \) to be analogous to the structured \( A \) matrix.

The datasets I analyze include *Drosophila* (Coyne and Orr 1989, Yukilevich 2012, Nosil 2013, Turelli et al. 2014), Bufonidae (Malone and Fontenot 2008), *Silene* (Moyle et al. 2004), and *Nolana* (Jewell et al. 2012). All of these datasets have been analyzed previously for patterns of crossability and are explained in detail below.

**Model Descriptions**

The method used can be applied to any case where the goal is to analyze the effect of a categorical variable and/or multiple variables on reproductive isolation between different taxa. I illustrate this with several examples. In one set of analyses I estimate the effects of a continuous trait (genetic distance) and categorical trait (allopatry vs. sympatry; or trait presence vs. absence)
and their interaction. In another analysis I analyze three continuous variables simultaneously (genetic distance, geographic distance, and a phenotypic/morphological distance).

**Model incorporating relatedness and categorical biogeography:**

A specific model that can be analyzed to determine if reproductive isolation accumulates more quickly in crosses between sympatric species compared to allopatric species will incorporate the ability of two species to cross with one another (Reproductive isolation (reproductive isolation): pre-zygotic isolation, post-zygotic isolation, or total isolation) as a function of genetic distance and geographic context (sympatry vs. allopatry) while controlling for phylogenetic relatedness (Eq. 4).

\[
y_{RI} = \mu + x_1 \beta_{gen.dist.} + x_2 y_{sym} + (x_1 \times x_2) \beta_{int} + Z_f f + Z_m m + e \tag{4}
\]

The first term (\(\mu\)) is the intercept of the linear model, and can be thought of as the baseline level of reproductive isolation if there is no significant relationship between reproductive isolation and genetic distance. The intercept also represents the reproductive isolation between closely related species pairs when genetic distance is significant. The variable \(x_1\) is a vector of genetic distance between species that are crossed and \(\beta_{gen.dist.}\) is the slope of the relationship between reproductive isolation and genetic distance. The variable \(x_2\) is a dummy variable (0 when the pair is allopatric and 1 when the pair is sympatric) and \(y_{sym}\) is the additional reproductive isolation that is attributable to the species occurring in sympatry. \(\beta_{int}\) is the increase in the slope of describing the relationship between reproductive isolation and genetic distance for sympatric species crosses. Lastly there are two \(Z\) matrices; they represent the identity of the female parent species and male parent species used in the cross (or can be designated species 1 and species 2). I use a separate effect for each parent in the cross, because not all species are used as both a male parent and female parent, depending on the data set. Recent studies use interactions between
phylogenetic effects for species interactions (Hadfield et al. 2014), but I have not used this approach because in most datasets there are very few interactions outside of very closely related species so the interactions would be very sparse. Using this model I was able to test for differences in the rate of reproductive isolation for three data sets: *Drosophila*, *Bufonidae*, and *Silene* (described below). The *Drosophila* data set has previously been shown to have increased levels of prezygotic reproductive isolation between sympatric pairs compared to allopatric pairs (Coyne and Orr 1989), but these rates were never directly compared in a single model.

**Model incorporating relatedness and categorical trait differences:**

As a second example of examining the contributions of a categorical variable, but in this case focusing on categorical trait variation, the basic model above can be used but with flower color substituted for geographic context (allopatry vs. sympatry).

\[
y_{RI} = \mu + x_1 \beta_{gen.dist.} + x_2 \gamma_{color} + (x_1 \times x_2) \beta_{int} + Z_f f + Z_m m + e
\]  

Here the \(x_2\) variable can have two levels, similar to the model above, or multiple levels. For example, \(x_2\) will have two levels if one level represents crosses between species that share the same state for floral color (red x red and white x white) and the other represents crosses between species with different floral colors (red x white and the reciprocal). Alternatively the \(x_2\) variable could have multiple levels: crosses between species with red flowers, crosses between species with white flowers, and crosses between red and white flowered species. This model would allow one to test if specific floral colors/morphologies have increased speciation rates compared to other floral morphologies.

Using the *Silene* dataset I set out to test the hypothesis that floral differences may contribute to post-mating and postzygotic isolation. Flower color and shape (together making up
a pollination syndrome) are often thought to contribute to premating reproductive isolation through pollinator preference (Schemske and Bradshaw 1999, Kay and Sargent 2009) and mechanical isolation, including pollen placement (Grant 1992, Hodges and Arnold 1994, Smith and Rausher 2007). Additionally pollination syndromes can contribute to post-mating isolation if there are differences in the ability of pollen to reach the ovary depending on differences in style length (Lee et al. 2008). Moreover, genes that control floral development are active throughout several developmental processes including gametogenesis and embryonic development (Smaczniak et al. 2012), so that post-zygotic isolation may evolve as a byproduct of floral divergence (Haak et al. 2014).

Model incorporating multiple continuous variables with potential correlations:

Often geographical context may not be captured by a categorical variable (allopatry vs. sympatry) but instead by a continuous variable such as geographic distance. When spatial variation is included in analyses we expect correlations between geographic/spatial variables and other variables of interest including genetic distance (lineages that are more geographically isolated are also more genetically differentiated). Further correlations may exist in aspects of morphology that can contribute to reproductive isolation, such as quantitative floral traits, and this model allows multiple continuous variables to be analyzed simultaneously (Equation 5). In the example illustrated below, I include genetic distance, geographic distance, and the difference in corolla tube length, which is one measure that captures the difference in floral size between species.

\[
y_{RI} = \mu + x_1 \beta_{gen.dist} + x_2 \beta_{geo.dist} + x_3 \beta_{corolla} + Z_f f + Z_m m + e \tag{6}
\]

If these variables are correlated with one another it will be difficult to make inferences on any given parameter estimate since mutlicollinearty can cause variance inflation (increased estimates
of variance parameters compared to model where variables are not correlated). To address this
issue I explicitly allow for covariance between these variables in the model by changing the
variance structure from being independent (Equation 6), to being correlated (Equation 7).

\[ X \sim N(\beta, V) \quad V = I \sigma^2 = \begin{pmatrix} \sigma^2_1 & 0 & 0 \\ 0 & \sigma^2_2 & 0 \\ 0 & 0 & \sigma^2_3 \end{pmatrix} \] (7)

\[ X \sim N(\beta, V) \quad V = \begin{pmatrix} \sigma^2_1 & \sigma^2_{1,2} & \sigma^2_{1,3} \\ \sigma^2_{2,1} & \sigma^2_2 & \sigma^2_{2,3} \\ \sigma^2_{3,1} & \sigma^2_{3,2} & \sigma^2_3 \end{pmatrix} \] (8)

This model can be applied to the *Nolana* dataset, for example, to disentangle the effects of multiple correlated variables. In the original analysis of the *Nolana* dataset (Jewell et al. 2012) there was evidence that genetic distance and/or geographic distance predicted reproductive isolation. However, since these two variables were highly correlated that analysis lacked power to disentangle this pattern using partial mantel tests. Using the approach here, I directly modeled the correlation between the continuous variables by including a covariance/correlation matrix between the three continuous variables (described above).

**Model incorporating genetic distance matrix:**

Another way to correct for relatedness in this framework is to use a pairwise genetic distance matrix. This method would be most suitable for closely related species for which constructing a phylogenetic tree is inappropriate. As an example, I analyzed the *Nolana* data using information from a pairwise genetic distance matric (specifically 1-D, where D is the genetic distance matrix) in the place of the structured \( A \) matrix, to see if the inferences varied between the two methods. The package MCMCglmm (Hadfield 2010) requires the inverse of the structured matrix and has built in functions to take the inverse of the relatedness matrix from either pedigree or phylogeny
information. To use the genetic distance matrix, I used the ginv function from the MASS (Venables and B.D 2002) package to find the generalized inverse of the 1-D matrix.

**Interpreting model outputs**

In the Bayesian framework used in MCMCglmm, there is no formal distinction between fixed and random effects, but for ease of explanation I will call all parameters to be estimated (except for phylogenetic variances) fixed effects. I can test any specific hypothesis of fixed effects by examining the highest posterior density (HPD) of the parameter from a given model. For example, to test whether there is a difference in average reproductive isolation between allopatric and sympatric species pairs, the test evaluates if the regression coefficient ($\gamma_{sym}$) overlaps 0. If it does not than there is evidence for significant differences in reproductive isolation between the two groups. Similarly, evaluating whether the rate of accumulation of reproductive isolation differs between two groups (e.g. sympatric and allopatric pairs), involves evaluating the slope $\beta_{int}$ to again assess whether the HPD does not include 0. For all analyses I set the prior distributions for random effect covariances and residuals as follows. MCMCglmm uses inverse Wishart distributions for random effects, with scale parameter $V$, and degrees of freedom parameter $n$. For each model I set $V$ to be $1/3$ the total variance in the response variable because there were three covariance matrices (two matrices for male and female parent, and the residual covariance matrix).

For each model I ran two MCMC chains; this enabled me to determine lack of convergence by examining within and between chain properties. The trace plots (iteration number vs. value of the draw) were visually inspected for all variables/chains, to see if chains were mixing well or if there was high auto-correlation (which would signify chain being stuck on
a local maximum and thereby give a false signal of convergence). Along with visual inspection, the primary tool used to determine if the MCMC chains failed to converge was the Gelman-Rubin Diagnostic (Gelman and Rubin 1992). This test uses information from the variance of the mixture of both chains, and the variance within a single chain to calculate a potential reduction factor (Gelman and Rubin 1992, Brooks and Gelman 1998). A value of 1 indicates that the chains have converged because the ratio of variance between and within chains is identical. In practice chains are typically run until the reduction factor for all variables is less than 1.1 (Brooks and Gelman 1998). I used coda package (Plummer et al. 2006) in R to calculate the convergence diagnostics. I considered a model to have converged if the all scale reduction factors for all variables (both fixed and random effects) were less than or equal to 1.1 and the trace plots indicate good mixing (actual scale reduction factors were generally less than 1.06, and the multivariate scale reduction factors were less than 1.02.) Code for all analyses are available through Dryad digital repository.

Data Sets

Four different data sets were used here and are explained in detail below; as outlined, in several cases these were enriched with additional tree construction, biogeographical information, and/or trait data prior to performing analyses. All data sets and phylogenies are available Dryad digital repository.

Drosophila

The Drosophila dataset is an expansion of the original data set used by Coyne and Orr (Coyne and Orr 1989) and was accessed from http://www.drosophila-speciation-patterns.com/. In this dataset, prezygotic isolation estimates are based on choice and no-choice mating assays, depending on specific species pair. Post-zygotic isolation is a combination of hybrid sterility and
inviability. To include phylogenetic information in my model, I combined data from two phylogenies that had complementary information and largely agreed on phylogenetic relationships. The first phylogeny (van der Linde et al. 2010) (VL) provides a useful backbone for different species groups, but lacks species richness within some groups. The second phylogeny (Morales-Hojas and Vieira 2012) (MH) has more species represented for particular clades. The VL tree includes more groups in total so I used this tree as a skeleton for the major groups. Since this tree was already formed from a supermatrix I was able to combine the two trees as follows. After scaling both trees so that they were ultrametric I could substitute relationships from the MH tree into the VL tree, by simply transforming the branch length from ML, so they were proportional to the branch length VL tree (see example: Supplementary Fig 1). For some clades, races or subspecies were used. I represented these as polytomies. After constructing the phylogeny I only retained crossing data where both members were represented in the phylogeny, leaving me with 182 crosses total to include in analyses.

Bufonidae

The primary dataset analyzed in the original study was post-zygotic isolation estimated from in vitro crosses (Malone and Fontenot 2008). Several phenotypes were used to calculate a reproductive isolation index including: fertilization rate, hatching rate, the number of tadpoles produced, percentage of tadpoles metamorphosed, fertility in backcross analysis, and the stage at which eggs ceased to develop. The reproductive isolation index was then calculated similarly to (Coyne and Orr 1989, Presgraves 2002). To evaluate the sensitivity of the inferences to this index, I also conducted analyses on an additional reproductive isolation index that takes into
account that these barriers are sequential (Ramsey et al. 2003). This made the response variable more continuous instead of considering only a fixed number of values.

I used the original sequence alignment to construct a neighbor-joining tree that corresponded to the tree used in the original analysis (Malone and Fontenot 2008). In addition, I also enriched this dataset by determining allopatry/sympathy relationships, by downloading shape files (vector storing geometric information) for each species from the IUCN Red List Database (IUCN 2014.). These files were reprojected (changed from 3D to 2D objects) to Albers Equal areas using rgdal (Bivand et al. 2013) and maptools (Bivand and Lewin-Koh 2013) in R with parameters specific for the region where they were located (Asia, Africa, Europe, or North America). I then determined whether species ranges overlapped using PBSmapping (Schnute et al. 2012) in R. Species that had no overlap were designated as allopatric.

Silene

The original crossing dataset was compiled in Moyle et al. (2004). Prezygotic isolation was a measure of the total number of failed pollinations (likely due to pollen pistil interactions) in interspecific crosses, compared to the crossability of the parental species. Postzygotic isolation was estimated from pollen sterility of F1 hybrids. These data already had sympatric and allopatric relationships designated but I additionally included flower color for each species. Floral color data were summarized from the available literature, online flora projects, and personal observations. The phylogeny comes from a super tree (Jenkins and Keller 2011). Similar to the Drosophila data I only retained taxa for analysis that could be placed into the phylogeny, and I allowed polytomies for certain taxa where different subspecies were used in crosses. This yielded 65 crosses in total, for analyses.
Nolana

The *Nolana* data were originally presented in Jewell et al. (2012). Since the authors found no measurable prezygotic isolation, I focused on total post-zygotic isolation that was a combination of fruit set, mericarp size, and seed set. The phylogeny used in the original study had several large polytomies. To resolve these polytomies I used the original sequence data to construct a new phylogeny in Raxml (Stamatakis 2014), by allowing each gene (genes on chloroplast were concatenated and treated as one unit) to have its own substitution model. These data also contained a complete pairwise genetic distance matrix, pairwise measures of geographic distance, and pairwise measures of differences in specific aspects of floral morphology, all three of which are significantly correlated with one another. In my analyses I used corolla diameter differences to quantify floral distance, though similar results were achieved with another measure of floral divergence (corolla depth difference) likely because these measures were highly similar (data not shown).

Results

*Drosophila*

Using data on *Drosophila* crossability I analyzed a model where I could compare differences between allopatric and sympatric species pairs in their baseline levels of reproductive isolation ($\mu=$baseline for allopatry and $\gamma_{sym}=$ change in RI for sympatry) and in their rate of isolation accumulation (i.e. slope; $\beta_{gen.dist} =$relationship between genetic distance and RI for allopatric pairs and $\beta_{int.} =$change in slope for sympatric pairs). To interpret these models it is often easiest look at which coefficients contribute to reproductive isolation in allopatric vs. sympatric species.
pairs. The overall model has many coefficients but only a few differentiate the allopatric vs.
sympatric species pairs. The overall model has the following form:

\[ y_{RI} = \mu + x_1 \beta_{gen.dist.} + x_2 \gamma_{sym} + (x_1 \times x_2) \beta_{int} + Z_f f + Z_m m + e \]  \hspace{1cm} (9)

The variable \( x_1 \) is a continuous variable, but the variable \( x_2 \) is binary and is equal to 0 for
allopatric pairs and 1 for sympatric pairs. Thus for allopatric pairs the model simplifies to:

\[ y_{RI} = \mu + x_1 \beta_{gen.dist.} + Z_f f + Z_m m + e \]  \hspace{1cm} (10)

For sympatric pairs the model simplifies to

\[ y_{RI} = \mu + \gamma_{sym} + x_1 (\beta_{gen.dist.} + \beta_{int}) + Z_f f + Z_m m + e \]  \hspace{1cm} (11)

This highlights that the coefficient \( \beta_{int} \) represents the change in slope for sympatric pairs and
that the total slope for sympatric species pairs is the sum of the two beta coefficients.

For prezygotic isolation the intercept (baseline level of reproductive isolation) was
significantly different than zero, and reproductive isolation was significantly elevated in
sympatric pairs \( (\gamma_{sym} = (0.2533, 0.4764), \text{ (Lower 95\% HPD interval, Upper 95\% HPD interval)}; \)
Table 1). There was also a significant relationship between genetic distance and reproductive
isolation, as detected in the original study (Coyne and Orr 1989), but only for allopatric species
pairs. In comparison, the overall relationship between genetic distance and reproductive isolation
is non-significant for sympatric pairs (Table 1). In this model the coefficients are additive
(Equation 11), and the relationship between genetic distance and reproductive isolation is not
significantly different from zero (HPD for \( \beta_{gen.dist} + \beta_{int}=(-0.1250, 0.3571) \)). The effect of
sympathy on reproductive isolation \( (\gamma_{sym}) \) is so strong that most of the reproductive isolation
values are near 1 across all genetic distances (completely isolated; Supplemental Fig 1).

For post-zygotic isolation the intercept and increase in reproductive isolation in sympathy
were not significantly different than zero \( (\mu \text{ and } \gamma_{sym} \) had HPD overlapping zero; Table 1). This
indicates that there is little to no postzygotic isolation in recently diverged species regardless of geographical context. The relationship between genetic distance and reproductive isolation ($\beta_{gen,\text{dist}}$) was significant and the rate of increase of reproductive isolation with genetic distance was greater in sympatric pairs ($\beta_{int} = 0.1326, 0.5247$). This suggests that reproductive isolation may accumulate more quickly between sympatric pairs of species than allopatric pairs, and the difference increases as divergence time (genetic distance) increases.

Bufonidae

Results of analyses of the Bufonidae data using the two alternative indices of reproductive isolation were qualitatively the same (Table 2), so I only discuss results using the original index of reproductive isolation. The model intercept was significantly different than zero ($\mu = 0.2980, 0.6945$) and the effect of sympatry was to actually decrease the level of reproductive isolation ($\gamma_{sym} = -0.2816, -0.0427$) though the overall level of reproductive isolation was still non-zero (the HPD for $\mu + \gamma_{sym} = (0.0164, 0.6518)$). The relationship between genetic distance and reproductive isolation was quite steep ($\beta_{gen,\text{dist}} = 3.6212, 5.8819$), and the increased rate of accumulation in sympatric pairs was also significant ($\beta_{int} = 0.4679, 3.5163$). In combination, these coefficients suggest that even though there is little reproductive isolation for very recently diverged sympatric pairs (those separated by small genetic distances), reproductive isolation accumulates more quickly for sympatric pairs than allopatric pairs.

Silene

Sympatry had no effect on the baseline prezygotic reproductive isolation ($\gamma_{sym} = -0.3643, 0.1510$) or on the rate of accumulation of reproductive isolation ($\beta_{int} = -1.5671, 3.5080$), which is consistent with the original results from Moyle et al (2004). There was a significant relationship
between genetic distance and reproductive isolation ($\beta_{gen\text{-}dist}$), which did not differ between sympatry and allopatry (Table 3). The lack of allopatric pairs for the postzygotic and total reproductive isolation measurements precluded analysis of the effects of geographical context on these measures (though the general relationship between reproductive isolation and genetic distance was positive and significant consistent with (Moyle et al. 2004); data not shown).

For all three measures of reproductive isolation, floral color differences did not increase reproductive isolation. Regardless of whether considering crosses between vs. within floral colors, or further separating the within class crosses into crosses among red species vs. crosses among white species, there was no effect of floral color on the average levels of reproductive isolation or on the accumulation of reproductive isolation over time (Table 3; prezygotic model shown).

**Nolana**

When genetic distance, geographic distance, and measures of flower size differences were considered jointly, the only significant predictor of reproductive isolation was geographic distance ($\beta_{geo\text{-}dist}$=0.0001, 0.0004; note, the small coefficient is due to the scale of reproductive isolation/kilometers), signifying that there is more reproductive isolation between pairs of species that are more geographically distant. This is consistent with the original study in the sense that only geographical distance was significant using the Mantel test (Jewell et al. 2012). The analysis using the genetic distance matrix also indicated that geographic distance was the only significant predictor of reproductive isolation (Table 4) and the coefficients were similar to the previous analysis. The main difference was there was no significant intercept ($\mu=\{ -1.0166, 1.4672 \}$). This is likely caused by the differences in inferred relatedness between the phylogeny.
and the genetic distance matrix (Supplemental Fig. 2), as this was the only difference in the two models. In a phylogeny relatedness is based on shared ancestry, whereas a distance matrix includes all nucleotide changes without context of whether they are shared with other taxa or phylogenetically informative. The result of using the genetic distance matrix to infer relatedness may have been to infer that more closely related species had little reproductive isolation, so the intercept was not significantly different than zero.

**Discussion**

Understanding how reproductive isolation accumulates over time in different geographic contexts (allopatry vs. sympatry) or according to specific trait differences requires analyzing the interaction between genetic distance and these factors and their joint effects on reproductive isolation. These comparisons cannot be made using PICs or Mantel tests, so in many classical studies the effects of these factors are instead indirectly compared (Coyne and Orr 1989, 1997, Moyle et al. 2004, Jewell et al. 2012). Using a phylogenetic mixed model framework, and classic data sets on species ability to cross with one another, I was able to formally test these relationships. I explicitly tested for interactions between categorical and continuous variables and accounted for correlations between predictor variables, something that is not possible in the standard PICs framework (Burt 1989, Garland et al. 1992) and difficult to implement using Mantel tests when there are more than two levels of the categorical variable. Additionally Mantel tests only evaluate the correlation between two variables but not average effects (i.e. intercepts), which must be tested with other methods, whereas estimates of mean differences between two groups are simultaneously generated using a mixed model approach.
In addition, in the mixed modeling framework specific variance matrices for independent variables can model correlations between these variables, which enables several predictors to be tested simultaneously (as demonstrated in the analysis of Nolana). In comparison, current approaches to evaluating the effect of multiple variables on reproductive isolation have clear limitations. Partial Mantel tests do not examine multiple effects simultaneously, but instead evaluate what additional variance a variable may explain after accounting for variance due to other variables (Smouse et al. 1986). Although multiple variables can be accommodated in a standard regression using PICs, it is difficult to determine the significance/validity of coefficients when the analysis involves correlated independent variables because multicollinearity causes spurious variance inflation (Mundry 2014). This is especially troubling, given that the nature of the data used in these studies will often contain correlations between the variables that may explain the accumulation of reproductive isolation.

The phylogenetic mixed effect model is also flexible in that relationships between taxa can be conveyed either through a phylogenetic relatedness matrix or a genetic distance matrix. In contrast, often the use of PICs vs. Mantel test reflects the scale of relatedness that researchers are examining: PICs typically examine interspecific data using phylogenies while Mantel tests can focus on intraspecific data using genetic distance matrices. The mixed model approach is a natural way to apply these analyses across different phylogenetic scales.

*New insights from phylogenetic mixed model framework*

Given the advantages of the phylogenetic mixed model framework I discuss the inferences from the hypotheses I examined, both in the context of how they compared to the original results and what additional inferences can be made.
For the *Drosophila* and Bufonidae analyses I specifically tested whether geographic context (allopatry or sympatry) influences the rate of accumulation of reproductive isolation. These data were both originally analyzed using linear regression (similar to PICS), however the difference in the rate of accumulation (represented by the slope relating genetic distance to reproductive isolation) could not be tested directly because of the inability to calculate contrasts for binary variables and therefore the interaction between geographic context and genetic distance could not be evaluated. Using the phylogenetic mixed model enabled direct tests of the differences in the rate of isolation accumulation, and doing so produced new insights into these previously analyzed datasets. In particular, I found that in both *Drosophila* and Bufonidae there was an increase in the rate of accumulation of postzygotic reproductive isolation in sympatric species pairs compared to allopatric species pairs. This result contrasts with the analysis by (Coyne and Orr 1997) and likely reflects the fact that (Coyne and Orr 1997) used a subset of the data that only included recently diverged species (D<0.25), whereas analyses here included the entire dataset. Other studies that have included data from both sympatric and allopatric pairs in Lepidoptera (Presgraves 2002) and birds (Price and Bouvier 2002) failed to find differences between sympatry and allopatry in the level of reproductive isolation, although the inferences were based on informal analyses.

For prezygotic isolation, the presence of stronger prezygotic isolation among closely related species pairs in sympathy is often assumed to be a product of reinforcement (Yukilevich 2012), but reinforcement is an unlikely force directly contributing to increased accumulation of postzygotic isolation in sympathy (Servedio 2000; Servedio and Saetre 2003). An alternative hypothesis, called the Templeton Effect or differential fusion effect, proposes that strong reproductive isolation in sympathy is a consequence of a systematic bias among species pairs that
are able to maintain their integrity in sympatry, whereby weakly isolated species fail to maintain
species boundaries (and therefore undergo species collapse), leaving only species pairs with
strong reproductive isolation. This hypothesis has previously been proposed to explain patterns
of strong prezygotic isolation in sympatry (Templeton 1981, Noor 1999, Yukilevich 2012),
however (unlike reinforcement) the effect may be equally applicable to postzygotic isolation.
The Templeton/differential fusion effect may be reinterpreted and applied to postzygotic
isolation such that the level of postzygotic isolation that exists between species will determine
the likelihood of species coexistence. This is because sexual isolation alone is often not strong
enough to maintain species barriers (Lande 1982; Payne and Krakauer 1997; Servedio and
Burger 2014), and reinforcement is sensitive to gene flow. If the strength of postzygotic isolation
between sympatric lineages drives reinforcement and ultimately the strength of prezygotic
isolation (Servedio 2000; Servedio and Saetre 2003), we should observe stronger postzygotic
isolation in sympatry (as observed for both the Drosophila and Bufonidae data sets) and a
correlation between postzygotic and prezygotic isolation in sympatry. Interestingly, postzygotic
and prezygotic isolation are correlated in sympatry in the Drosophila dataset (Yukelivich 2012).

The mixed model approach can also be used to evaluate the effect of categorical trait
variation on the strength and accumulation of reproductive isolation, to address additional
mechanistic questions. In my analyses of whether floral divergence can contribute to post-mating
and postzygotic reproductive isolation, independent of effects on pollinator visitation, I found no
support in Silene for the hypothesis that floral divergence could also influence these reproductive
isolation phenotypes through pleiotropic effects (Haak et al. 2014). Specifically, floral
divergence in the form of flower color differences did not contribute to either prezygotic
isolation (most likely via pollen-pistil interactions) or postzygotic isolation (F1 pollen sterility).
It is possible that the pleiotropic effects of floral traits on reproductive isolation could manifest in a different traits (seed sterility, F1 germination/viability) or floral divergence could contribute to extrinsic post zygotic isolation (Ramsey et al. 2003a, Lowry et al. 2008), all of which were not captured in this analysis. Alternatively (or in addition), differentiation in floral traits other than color might be more important in this context. In Silene, for example, there is some evidence that floral traits other than red vs. white flower color, including flower display height and orientation (Brothers and Atwell 2014, Fenster et al. 2015) and floral scent (Waelti et al. 2008, Castillo et al. 2014) may contribute to reproductive isolation via pollinator visitation.

Trait variation like floral variation might also be correlated with other factors that contribute to reproductive isolation. For example, if floral shape has phylogenetic signal then floral divergence would be correlated with genetic distance; similarly, if there is selection for different flower sizes in different environments, floral divergence would be associated with geographical distance. Under these scenarios floral divergence might seem to be contributing to reproductive isolation, merely because it shares a main driving factors with the accumulation of isolation, so it is important to be able to distinguish these potential mechanisms. In the original Nolana analysis (Jewell et al. 2012), floral, geographical, and genetic distance measures were all observed to be correlated. In the reanalysis here, I did not observe an independent effect of floral divergence (floral size difference) on reproductive isolation. Indeed, I was able to explicitly rule out the possibility of floral changes contributed to reproductive isolation while simultaneously testing the effects of genetic distance and geographic distance, and found geographical distance alone contributed to reproductive isolation in this system. This result might reflect both reduced gene flow between geographically distant species and/or differences in habitats, both of which could contribute to reproductive isolation. Regardless, it is clear that, differences in flower size
do not appear to relay into pleiotropic effects on reproductive isolation in this system, as has been hypothesized for differences in traits associated with pollinator preference (Haak 2014).

**Conclusion**

The phylogenetic mixed model framework utilized in this study remedies difficulties for Mantel tests and PICs in testing hypothesis about factors contributing to the evolution of reproductive isolation. To demonstrate the utility of this framework, I performed several analyses to evaluate the roles of categorical geographic and trait variation, and quantitative divergence measures, on the accumulation and strength of isolation in four published datasets. I tested the role of geography in the evolution of reproductive isolation and was able to show that reproductive isolation accumulates more quickly in sympatry not only for prezygotic isolation but also for postzygotic isolation. In the datasets examined, floral traits did not contribute to the pattern or strength of reproductive isolation measures included in the original studies. This framework can enable future studies to test complex hypothesis, test the effects of multiple variables simultaneously (even if they are correlated), and use a generalized framework to examine reproductive isolation between species or at the intraspecies level.

**Literature Cited**


IUCN. 2014. The IUCN Red List of Threatened Species.


Table 1. Summary of coefficients estimated for the analysis of prezygotic (left) and postzygotic (right) reproductive isolation from the *Drosophila* data. The confidence intervals are for 95% Highest posterior density (HPD) and are significant if they do not include zero (in bold).

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Biological meaning</th>
<th>Prezygotic</th>
<th>Postzygotic</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower</td>
<td>Upper</td>
</tr>
<tr>
<td>(\mu) (intercept)</td>
<td>average RI</td>
<td>0.1975</td>
<td>0.6033</td>
</tr>
<tr>
<td>(\beta_{gen.dist.})</td>
<td>slope relating genetic distance and RI</td>
<td>0.1959</td>
<td>0.4164</td>
</tr>
<tr>
<td>(\gamma_{sym})</td>
<td>additional RI in sympatry</td>
<td>0.2533</td>
<td>0.4764</td>
</tr>
<tr>
<td>(\beta_{int})</td>
<td>increase in slope for sympatry</td>
<td>-0.3209</td>
<td>-0.0593</td>
</tr>
</tbody>
</table>

Table 2. Summary of coefficients estimated for the analysis of postzygotic reproductive isolation from the *Bufonidae* data. The original index of reproductive isolation (left) was calculated by Malone and Fotenont (2008) following the procedure of Coyne and Orr (1989) and Presgraves (2002). The new index (right) takes into account that reproductive barriers are sequential following Ramsey et al. (2003) The confidence intervals are for 95% Highest posterior density (HPD) and are significant if they do not include zero (in bold).

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Biological meaning</th>
<th>Postzygotic (Original)</th>
<th>Postzygotic (New)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower</td>
<td>Upper</td>
</tr>
<tr>
<td>(\mu) (intercept)</td>
<td>average RI</td>
<td>0.2980</td>
<td>0.6945</td>
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<tr>
<td>(\beta_{gen.dist.})</td>
<td>slope relating genetic distance and RI</td>
<td>3.6212</td>
<td>5.8819</td>
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<tr>
<td>(\gamma_{sym})</td>
<td>additional RI in sympatry</td>
<td>-0.2816</td>
<td>-0.0427</td>
</tr>
<tr>
<td>(\beta_{int})</td>
<td>increase in slope for sympatry</td>
<td>0.4679</td>
<td>3.5163</td>
</tr>
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</table>

Table 3. Summary of coefficients estimated for the analysis of prezygotic reproductive isolation when considering geographical context (left) or floral divergence (right) from the *Silene* data. The confidence intervals are for 95% Highest posterior density (HPD) and are significant if they do not include zero (in bold).

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Biological meaning</th>
<th>Prezygotic (Geographic model)</th>
<th>Prezygotic (Floral differences model)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower</td>
<td>Upper</td>
</tr>
<tr>
<td>(\mu) (intercept)</td>
<td>average RI</td>
<td>-1.2138</td>
<td>1.9094</td>
</tr>
<tr>
<td>(\beta_{gen.dist.})</td>
<td>slope relating genetic distance and RI</td>
<td>0.9126</td>
<td>7.1054</td>
</tr>
<tr>
<td>(\gamma_{sym})</td>
<td>additional RI in sympatry</td>
<td>-0.3643</td>
<td>0.1510</td>
</tr>
<tr>
<td>(\beta_{int})</td>
<td>increase in slope for sympatry</td>
<td>-1.5671</td>
<td>3.5080</td>
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</table>
Table 4. Summary of coefficients estimated for the analysis of total reproductive isolation when using the phylogeny (left) or genetic distance matrix (right) from the *Nolana* data. The confidence intervals are for 95% Highest posterior density (HPD) and are significant if they do not include zero (in bold).

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Biological meaning</th>
<th>Total reproductive isolation (phylogenetic matrix)</th>
<th>Total reproductive isolation (genetic distance matrix)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower</td>
<td>Upper</td>
</tr>
<tr>
<td>$\mu$ (intercept)</td>
<td>average RI</td>
<td>0.1166</td>
<td>0.6249</td>
</tr>
<tr>
<td>$\beta_{gen.dist.}$</td>
<td>slope relating genetic distance to RI</td>
<td>-0.3149</td>
<td>0.4861</td>
</tr>
<tr>
<td>$\beta_{geo.dist.}$</td>
<td>slope relating geographic distance (km) to RI</td>
<td>0.0001</td>
<td>0.0004</td>
</tr>
<tr>
<td>$\beta_{corolla}$</td>
<td>slope relating differences in corolla diameter to RI</td>
<td>-0.0071</td>
<td>0.0140</td>
</tr>
</tbody>
</table>
Figure S1. The relationship between genetic distance and prezygotic isolation for *Drosophila* species pairs that are either allopatric or sympatric, demonstrating that most sympatric species pairs show almost complete isolation, resulting in no relationship between genetic distance and reproductive isolation. The best fit lines were constructed using the mode of the parameters from the MCMCglmm analysis.
Figure S2. Comparison of relationships in the genus *Nolana* when either a phylogeny made from several loci or matrix of pairwise genetic distances are used. The topology on the left represents the maximum likelihood tree based on sequence from the *ADH2, atpB, ndhF, psbA-trnH, rps16* genes. The topology on the right was generated using Ward’s hierarchical clustering method for pairwise genetic distances reported in Jewell et al (2012).