The inherent mutational tolerance and antigenic evolvability of influenza hemagglutinin

Bargavi Thyagarajan and Jesse D. Bloom

Division of Basic Sciences and Computational Biology Program,
Fred Hutchinson Cancer Research Center, Seattle, WA 98109, USA

E-mail: jbloom@fhcrc.org.

Abstract

Influenza is notable for its evolutionary capacity to escape immunity targeting the viral hemagglutinin. We used deep mutational scanning to examine the extent to which a high inherent mutational tolerance contributes to this antigenic evolvability. We created mutant viruses that incorporate most of the $\approx 10^4$ amino-acid mutations to hemagglutinin from A/WSN/1933 (H1N1) influenza. After passaging these viruses in tissue culture to select for functional variants, we used deep sequencing to quantify mutation frequencies before and after selection. These data enable us to infer the preference for each amino acid at each site in hemagglutinin. These inferences are consistent with existing knowledge about the protein’s structure and function, and can be used to create a model that describes hemagglutinin’s evolution far better than existing phylogenetic models. We show that hemagglutinin has a high inherent tolerance for mutations at antigenic sites, suggesting that this is one factor contributing to influenza’s antigenic evolution.
Introduction

Epidemic influenza poses an annual threat to human health largely because the virus rapidly evolves to escape the immunity elicited by previous infections or vaccinations. The most potent form of anti-influenza immunity is antibodies targeting the virus’s hemagglutinin (HA) protein (Yewdell et al., 1979; Wiley et al., 1981; Caton et al., 1982). The virus evades these antibodies primarily by accumulating amino-acid substitutions in HA's antigenic sites (Smith et al., 2004; Das et al., 2013; Koel et al., 2013; Bedford et al., 2014). Remarkably, HA undergoes this rapid evolution while retaining the ability to fold to a highly conserved structure that performs two functions essential for viral replication: receptor binding and membrane fusion (Wiley and Skehel, 1987; Russell et al., 2004). HA is therefore highly “antigenically evolvable” in the sense that it can accommodate rapid antigenic change without compromising its structural and functional properties.

Two factors that undoubtedly contribute to HA’s rapid antigenic evolution are influenza’s high mutation rate and the strong selection that immunity exerts on the virus. However, it is unclear whether these factors are sufficient to fully explain HA’s antigenic evolution. For instance, while some other error-prone viruses (such as HIV and hepatitis C) also exhibit rapid antigenic evolution of their surface proteins (Burton et al., 2012), other viruses with comparable mutation rates (such as measles) show little propensity for antigenic change (Duffy et al., 2008; Sheshberadaran et al., 1983), despite the fact that evasion of immunity would presumably confer a selective benefit. A variety of explanations ranging in scale from ecological to molecular can be posited to account for these differences in rates of antigenic evolution (Lipsitch and O’Hagan, 2007; Koelle et al., 2006; Heaton et al., 2013). One hypothesis is that HA has a high inherent tolerance for mutations in its antigenic sites, thereby conferring on influenza the evolutionary capacity to escape from anti-HA antibodies with relative ease.

Testing this hypothesis requires quantifying the inherent mutational tolerance of each site in HA. This cannot be done simply by examining variability among naturally occurring viruses, since the evolution of influenza in nature is shaped by a combination of inherent mutational tolerance and external immune selection. For example, the rapid evolution of HA's antigenic sites in nature could reflect the fact that these sites are especially tolerant of mutations, or it could be purely a consequence of strong immune selection. Traditional experimental approaches using site-directed mutagenesis or serial viral passage are also inadequate to quantify inherent mutational tolerance – while such experimental techniques have been used to determine the effect
of specific mutations on HA, they cannot feasibly be applied to all possible individual amino-acid mutations. Recently Heaton et al. (2013) used transposon mutagenesis to show that HA is tolerant to the random insertion of five to six amino-acid sequences at several locations in the protein. However, the relevance of this tolerance to insertional mutations is unclear, since HA's actual antigenic evolution involves almost entirely point substitutions, with only a very low rate of insertions and deletions.

Here we use the new high-throughput experimental technique of deep mutational scanning (Fowler et al., 2010; Araya and Fowler, 2011) to comprehensively quantify the tolerance of HA to amino-acid mutations. Specifically, we create mutant libraries of the HA gene from the H1N1 strain A/WSN/1933 (WSN) that contain virtually all of the \( \approx 4 \times 10^4 \) possible individual codon mutations, and therefore virtually all of the \( \approx 10^4 \) possible amino-acid mutations. We use these mutant libraries to generate pools of mutant influenza viruses, which we estimate incorporate at least 85% of the possible HA codon mutations and 97% of the possible amino-acid mutations. We then passage these viruses to select for functional variants, and use Illumina deep sequencing to determine the frequency of each HA mutation before and after this selection for viral growth. Since these experiments measure the impact of mutations in the absence of immune selection, they enable us to quantify HA’s inherent preference for each amino acid at each site in the protein. We show that these quantitative measurements are consistent with existing knowledge about HA structure and function, and can be used to create an evolutionary model that describes HA’s natural evolution far better than existing models of sequence evolution. Finally, we use our results to show that HA’s antigenic sites are disproportionately tolerant of mutations, suggesting that a high inherent tolerance for mutations at key positions targeted by the immune system is one factor that contributes to influenza’s antigenic evolvability.
Results

Strategy for deep mutational scanning of HA

Our strategy for deep mutational scanning (Fowler et al., 2010; Araya and Fowler, 2011) of HA is outlined in Figure 1. The wildtype WSN HA gene was mutagenized to create a diverse library of mutant HA genes. This library of mutant genes was then used to generate a pool of mutant viruses by reverse genetics (Hoffmann et al., 2000). The mutant viruses were passaged at a low multiplicity of infection to ensure a linkage between genotype and phenotype. The frequencies of mutations before and after selection for viral growth were quantified by Illumina deep sequencing of the mutant genes (the *mutDNA* sample in Figure 1) and the mutant viruses (the *mutvirus* sample in Figure 1). An identical process was performed in parallel using the unmutated wildtype HA gene to generate unmutated viruses in order to quantify the error rates associated with sequencing, reverse transcription, and virus growth (these are the *DNA* and *virus* samples in Figure 1). The entire process in Figure 1 was performed in full biological triplicate (the replicates are referred to as #1, #2, and #3). In addition, a repeat of the Illumina sample preparation and deep sequencing was performed for replicate #1 to quantify the technical variation associated with these processes.

Creation of HA codon-mutant libraries

The deep mutational scanning strategy in Figure 1 requires creating mutant libraries of the HA gene. We wanted to assess the impact of all possible amino-acid mutations. Most mutagenesis techniques operate at the nucleotide level, and so frequently introduce single-nucleotide codon changes (e.g. GGA → cGA) but only very rarely introduce multi-nucleotide codon changes (e.g. GGA → cat). However, several PCR-based techniques have recently been developed to introduce random codon mutations into full-length genes (Firnberg and Ostermeier, 2012; Jain and Varadarajan, 2014; Bloom, 2014). We used one of these techniques (Bloom, 2014) to create three replicate codon-mutant libraries of the WSN HA gene (Supplementary file 1).

Sanger sequencing of 34 individual clones indicated that the libraries contained an average of slightly over two codon mutations per gene, with a very low rate of insertions and deletions (less than 0.1 per gene). The number of mutations per clone was distributed around this average in an approximately Poisson fashion (Figure 2). The mutations consisted of a mix of one-, two-, and three-nucleotide codon changes, and were roughly uniform in their nucleotide composition.
and location in the gene (Figure 2).

The genes in each mutant library were cloned at high efficiency into a bidirectional influenza reverse-genetics plasmid (Hoffmann et al., 2000). Each of the library replicates contained at least six-million unique clones – a diversity that far exceeds the $10^4$ unique single amino-acid mutations and the $\approx 4 \times 10^4$ unique single codon mutations to the HA gene. The vast majority of possible codon and amino-acid mutations are therefore represented many times in each plasmid mutant library, both individually and in combination with other mutations.

**Generation of mutant viruses by reverse genetics**

The HA plasmid mutant libraries were used to generate pools of mutant influenza viruses by reverse genetics (Hoffmann et al., 2000). Briefly, this process involves transfecting cells with the HA plasmid mutant library along with plasmids encoding the other seven genes from the WSN strain of influenza. Although the cells were transfected with a very large diversity of HA plasmids, we were uncertain what fraction of the genes encoded on these plasmids would actually be productively packaged into a virus. In an attempt to maximize the diversity in the viral pools, the mutant viruses were generated by transfecting several dozen wells of cells. The logic behind this scheme was to maintain substantial diversity even if only a subset of viral mutants stochastically predominated in each individual well of cells. A different replicate virus pool was generated for each of the three HA plasmid mutant libraries.

The mutant viruses generated for each replicate were passaged at a relatively low multiplicity of infection (MOI) of 0.1 to reduce the probability of co-infection, thereby creating a link between viral genotype and phenotype. This genotype-phenotype link is essential to ensure that the sequenced HA gene matches the protein on the surface of the virus. Our previous work with NP (Bloom, 2014) indicates that one low MOI passage is sufficient to create a strong genotype-phenotype link, since that previous work found that the results obtained after one viral passage were extremely similar to the results obtained after two viral passages. In order to maintain a diversity of over two-million infectious viral particles, we performed the passaging in a total of $2.4 \times 10^7$ cells.

**Deep sequencing reveals purifying selection against many mutations**

We used Illumina sequencing to quantify the frequencies of mutations before and after selection for viral growth. For each replicate, we sequenced HA from the unmutated plasmid, the plasmid
mutant library, virus produced from the unmutated plasmid, and mutant virus produced from the plasmid mutant library – these are the DNA, mutDNA, virus, and mutvirus samples in Figure 1. For the DNA and mutDNA samples, the HA gene was amplified directly from the plasmids by PCR. For the virus and mutvirus samples, the HA gene was first reverse-transcribed from viral RNA and was then amplified by PCR. In all cases, template quantification was performed prior to PCR to ensure that > 10^6 initial HA molecules were used as templates for subsequent amplification.

In order to reduce the sequencing error rate, the HA molecules were fragmented to roughly 50 nucleotide fragments using Illumina’s transposon-based Nextera kit, and then sequenced with overlapping paired-end reads (Figure 3 – figure supplement 1). We only called codon identities for which both paired reads concur – this strategy substantially increases the sequencing fidelity, since it is rare for the same sequencing error to occur in both reads. For each sample, we obtained in excess of 10^7 overlapping paired-end reads that could be aligned to HA (Figure 3 – figure supplement 2). As shown in Figure 3 – figure supplement 3, the read depth varied somewhat along the primary sequence, presumably due to known weak biases in the insertion sites for the Nextera transposon (Adey et al., 2010). However, these biases were fairly mild, and so we obtained well over 2 × 10^5 unique paired reads for nearly all HA codons.

Figure 3 shows the frequency of mutations in each sample as quantified by deep sequencing. The DNA samples derived from unmutated HA plasmid show a low frequency of apparent mutations which are almost exclusively composed of single-nucleotide codon changes – the frequency of these apparent mutations reflects the rate of errors from the PCR amplification and subsequent deep sequencing. The virus samples created from the unmutated plasmid show only a slightly higher frequency of mutations, indicating that reverse-transcription and viral replication introduce only a small number of additional mutations. As expected, the mutDNA samples derived from the plasmid mutant libraries show a high rate of one-, two-, and three-nucleotide mutations, as all three types of mutations were introduced during the codon mutagenesis. The mutvirus samples derived from the mutant virus pools exhibit a mutation rate that is substantially lower than that of the mutDNA samples. Most of the reduction in mutation frequency in the mutvirus samples is due to decreased frequencies of nonsynonymous and stop-codon mutations; synonymous mutations are only slightly depressed in frequency. As stop-codon and nonsynonymous mutations are much more likely than synonymous mutations to substantially impair viral fitness, these results are consistent with purifying selection purging deleterious mutations during viral growth.
Inspection of Figure 3 also demonstrates an important advantage of introducing the mutations at the codon rather than the nucleotide level. While there is a low but non-zero rate of errors (from sequencing, PCR, or reverse-transcription) that lead to single-nucleotide codon changes (as judged by the DNA and virus samples), errors that lead to multi-nucleotide codon changes are negligible because it is extremely rare for a single codon to experience two errors. We similarly expect that any do novo mutations or reversions that arise during viral growth should be limited to single-nucleotide changes given the short duration of viral passage in our experiments. The fact that our mutant libraries were constructed at the codon rather than the nucleotide level means that the vast majority (54 of 63) possible mutations to each codon involve multiple nucleotide changes, and so the sequencing results for these mutations can be analyzed essentially at face value, without having to worry about confounding errors. For the remaining (9 of 63) possible mutations that only involve a single-nucleotide codon change, we have attempted to statistically correct for the error rates estimated from our controls as described in the Methods.

Most mutations are sampled by the experiments

It is important to assess the completeness with which the experiments sampled all possible HA mutations. Several problems could limit mutational sampling: mutations might be absent from the plasmid mutant libraries due to biases in the codon mutagenesis, mutations that are present in the plasmid mutants might fail to be incorporated into viruses due to stochastic bottlenecks during virus generation by reverse genetics, or the sequencing read depth might be inadequate to sample the mutations that are present. The most straightforward way to assess these issues is to quantify the number of times that each possible multi-nucleotide codon mutation is observed in the mutDNA and mutvirus samples. Restricting the analysis to multi-nucleotide codon mutations avoids the confounding effects of sequencing and reverse-transcription errors, which cause almost exclusively single-nucleotide changes.

Figure 4 shows the number of times that each mutation was observed in the combined sequencing data for the three biological replicates; Figure 4 – figure supplement 1 shows the same data for the replicates individually. More than 99.5% of multi-nucleotide codon mutations are observed at least five times in the combined sequencing data from the plasmid mutant libraries (mutDNA samples), and ≈ 97.5% of all such mutations are observed at least five times in sequencing of the mutDNA for each individual replicate. These results indicate that the vast
majority of codon mutations are represented in the plasmid mutant libraries.

In contrast, only 53% of multi-nucleotide codon mutations are observed at least five times in the combined sequencing data for the mutant viruses (mutvirus samples), and only ≈ 26% of such mutations are observed at least five times in sequencing of the mutvirus for each individual replicate (Figure 4, Figure 4 – figure supplement 1). However, these numbers are confounded by the fact that many mutations are deleterious, and so may be absent because purifying selection has purged them from the mutant viruses. A less confounded measure is the frequency of synonymous multi-nucleotide mutations, since synonymous mutations are less likely to be strongly deleterious. About 85% of such mutations are observed at least five times in the combined mutvirus samples, and ≈ 51% of such mutations are observed at least five times in the mutvirus samples for the individual replicates (Figure 4, Figure 4 – figure supplement 1). Note that these numbers are only a lower bound on the fraction of codon mutations sampled by the mutant viruses – even synonymous mutations to influenza are sometimes strongly deleterious (Marsh et al., 2008), and so some of the missing synonymous codon mutations may have been introduced into mutant viruses but then purged by purifying selection. Furthermore, the redundancy of the genetic code means that the fraction of possible amino-acid mutations sampled is substantially higher than the fraction of codon mutations sampled. Specifically, if 85% of possible codon mutations are sampled at least five times in the combined libraries (as Figure 4 indicates), then our simulations suggest that ≈ 97% of possible amino-acid mutations will have also been sampled at least five times (see Methods).

Overall, these results indicate that nearly all mutations are represented in the plasmid mutant libraries. Virus generation by reverse genetics does introduce a bottleneck – but fortunately, this bottleneck is sufficiently mild that at least half of all possible codon mutations are still sampled at least five times by the mutant viruses in each individual replicate. Combining the data for the three replicates brings the coverage of possible codon mutations to around 85%, and the coverage of possible amino-acid mutations to 97%. Therefore, the sampling of mutations is sufficiently complete to provide information on the effects of most amino-acid mutations when the data from the three experimental replicates are combined.

**Estimation of the effects of each amino-acid mutation to HA**

We quantified the effects of mutations in terms of site-specific amino-acid “preferences.” These preferences are the expected frequency of each amino acid at each site in the mutant viruses in
a hypothetical situation in which all amino acids are introduced at that site at equal frequency in the initial plasmid mutant library (Bloom, 2014). Because many of the HAs in our libraries contain several mutations, these preferences do not simply correspond to the fitness effect of each individual mutation to the WSN HA – rather, they represent the average effect of each mutation in a collection of closely related HA mutants. Mutations to amino acids with high preferences are favored by selection, while mutations to amino acids with low preferences are disfavored. The amino-acid preferences are inferred from the deep sequencing data using a Bayesian statistical framework in which the observed counts are treated as draws from multinomial distributions with unknown parameters representing the initial mutagenesis rate, the various error rates, and selection as represented by the preferences (see Methods for details).

Figure 5 shows the amino-acid preferences for the entire HA gene inferred from the combined data from all three biological replicates. As can be seen from this figure, some sites have strong preferences for one specific amino acid, while other sites are tolerant of a variety of different amino acids. As described in Table 1, the inferred amino-acid preferences are consistent with existing knowledge about mutations and residues affecting HA stability, membrane fusion, proteolytic activation, and receptor binding (Nakajima et al., 1986; Qiao et al., 1999; Stech et al., 2005; Martin et al., 1998). This concordance suggests that the deep mutational scanning effectively captures many of the structural and functional constraints on HA.

Despite the general concordance between the inferred amino-acid preferences and existing knowledge, it is important to quantify the experimental error associated with the deep mutational scanning. We sought to quantify two factors: technical variation due to inaccuracies and statistical limitations during Illumina sample preparation and deep sequencing, and biological variation due to stochasticity in the viral mutants that were generated and enriched during each replicate of the experiment. Figure 6A shows the correlation between biological replicate #1 and a technical repeat of the Illumina sample preparation and deep sequencing for this biological replicate. There is a very high correlation between the preferences inferred from these two repeats, indicating that technical variation has only a very minor influence on the final inferred amino-acid preferences. Figure 6B-D show the correlation among the three different biological replicates. Although the biological replicates are substantially correlated, there is also clear variation. Most of this variation is attributable to amino acids which in one replicate are inferred to have preferences near the a priori expectation of 0.05 (there are 20 amino acids, which in the absence of data are all initially assumed to have an equal preference of $\frac{1}{20}$), but in another replicate are inferred to have a much higher or lower preference. Such variation arises because the
mutant viruses for each biological replicate only sample about 50% of the possible codon mutations (see previous section), meaning that there is little data for some mutations in any given replicate. Fortunately, combining the three biological replicates greatly increases the coverage of possible mutations (see previous section). Therefore, inferences made from the combined data (as in Figure 5) should be substantially more accurate than inferences from any of the individual replicates. This idea is supported by the results below, which quantify the extent to which the inferred preferences accurately describe natural HA evolution.

Comparison to another high-throughput study of mutations to HA

As our paper was under review, Wu et al. (2014) published the results of using a similar strategy to examine the effects of mutations to the WSN HA. In their study, the HA gene was mutated at the nucleotide level, so their experiments surveyed only amino-acid mutations accessible by single-nucleotide codon changes. As a result, they provide data on the effects of only about 20% of the $19 \times 564 = 10716$ amino-acid mutations examined in our study. Despite this limitation, their study provides a large dataset of mutational effects to which we can compare our results.

Figure 7 compares the mutational effects determined in our study to those from Wu et al. (2014). There is a highly significant correlation between the results of the two studies. However, the correlation is weaker than between any pair of replicates of our experiments (Figure 6). Unfortunately, Wu et al. (2014) did not provide raw data for replicates of their experiment, so we cannot determine the extent to which the imperfect correlation between the studies reflects interesting differences in the experimental selection pressures (for instance, they use A549 cells while we use MDCK-SIAT1 cells) versus simple noise in the experimental measurements. This inability to pinpoint the reason for variation between the studies highlights a limitation of the high-throughput experimental methodology employed by ourselves and Wu et al. (2014): while such experiments provide a wealth of data, numerous factors can create noise in these data (sequencing errors, population bottlenecks, epistasis among mutations, etc.). Realizing the full potential of such studies will therefore require the availability of raw data from experimental controls and biological replicates to quantify errors and noise to enable comparisons across data sets.

Nonetheless, Figure 7 shows that there is a highly significant correlation between the results of these two high-throughput studies, despite differences in experimental methodology and unquantified sources of experimental noise. This fact suggests that both studies capture
fundamental constraints on HA’s mutational tolerance. In the remaining sections, we apply the more comprehensive data generated by our study to address questions about HA’s natural evolution and antigenic evolvability.

**Experimental inferences are consistent with HA’s natural evolution**

Do the results of our deep mutational scanning experiment accurately reflect the real constraints on HA? Table 1 uses an anecdotal comparison to a small number of existing experimental studies to suggest that they do. However, a more systematic way to address this question is to compare the inferred amino-acid preferences to the actual patterns of HA evolution in nature.

To make such a comparison, we created an alignment of HA sequences from human and swine influenza viruses descended from a common ancestor closely related to the virus that caused the 1918 influenza pandemic. Figure 8 shows a phylogenetic tree of these sequences. The WSN HA used in our deep mutational scanning falls relatively close to the root of this tree.

The crudest comparison is simply to correlate amino-acid frequencies in the natural sequences to the experimentally inferred amino-acid preferences. Figure 9 shows that the inferred preferences are substantially although imperfectly correlated with the natural amino-acid frequencies. However, this comparison is problematic because it fails to account for the contingent and limited sampling of mutations by natural evolution. While the deep mutational scanning is designed to sample all possible mutations, only a fraction of theoretically tolerable mutations have fixed in natural H1 HAs due to the finite timespan during which evolution has been exploring possible sequences (in other words, evolution is not at equilibrium; see Povolotskaya and Kondrashov, 2010). Therefore, an amino-acid frequency of close to one among the natural HA sequences in Figure 8 might imply an absolute functional requirement for that amino acid – or it might simply mean that natural evolution has not yet happened to fix a mutation to another tolerable amino acid at that site.

A better approach is therefore to treat natural evolution as a non-equilibrium dynamic process, and ask whether the inferred amino-acid preferences accurately describe this process. This type of analysis can be done using the likelihood-based statistical framework for phylogenetics developed by Felsenstein (1973, 1981). Specifically, we fix the phylogenetic tree topology to that shown in Figure 8 and then assess the likelihood of the natural sequences given a specific evolutionary model after optimizing the branch lengths of the tree. Evolutionary models that more accurately describe HA sequence evolution will have higher likelihoods, and the rela-
The accurate accuracy of models can be quantified by comparing their likelihoods after correcting for the number of free parameters using AIC (Posada and Buckley, 2004). Previous work has described how experimental measurements of amino-acid preferences can be combined with known mutation rates to create a parameter-free phylogenetic evolutionary model from deep mutational scanning data (Bloom, 2014).

Table 2 compares the fit of evolutionary models based on the experimentally inferred amino-acid preferences with several existing state-of-the-art models that do not utilize this experimental information (Goldman and Yang, 1994; Kosiol et al., 2007). The model based on amino-acid preferences inferred from the combined experimental data from the three replicates describes the evolution of the naturally occurring HA sequences far better than the alternative models, despite the fact that the latter have a variety of free parameters that are optimized to improve the fit. Models based on amino-acid preferences inferred from the individual experimental replicates also fit the data better than existing models – however, the fit is poorer than for the model that utilizes the data from all three replicates. This result is consistent with the fact that the individual replicates are incomplete in their sampling of the mutational effects, meaning that aggregating the data from several replicates improves the accuracy of inferred preferences. Overall, these comparisons show that the deep mutational scanning reflects the actual constraints on HA evolution substantially better than existing quantitative evolutionary models.

The inherent evolvability of antigenic sites on HA

The amino-acid preferences inferred from the deep mutational scanning reflect the inherent mutational tolerance of sites in HA. In contrast, the evolution of HA in nature is shaped by a combination of HA's inherent mutational tolerance and external selection pressures. Specifically, the evolution of HA in humans is strongly driven by selection for mutations that alter antigenicity (Yewdell et al., 1979; Wiley et al., 1981; Caton et al., 1982; Smith et al., 2004; Das et al., 2013; Koel et al., 2013; Bedford et al., 2014). The fact that such antigenic mutations fix at high frequency implies some degree of mutational tolerance at antigenic sites, since no mutations would fix if these sites were under absolute structural or functional constraint. However, it is not possible to tell from natural sequences alone whether antigenic sites are unusually mutationally tolerant compared to the rest of HA, or whether their rapid evolution is solely because they are under strong external immune selection.

To address this issue, we used the results of the deep mutational scanning to compare the
inherent mutational tolerance of antigenic sites to the rest of the HA protein. Caton et al. (1982) mapped the antigenic sites of the H1 HA from A/Puerto Rico/8/1934 (PR8), which is closely related to the WSN HA used in our experiments. We therefore defined the “Caton et al. antigenic sites” as the WSN residues homologous to those mapped by Caton et al. (1982) with the exclusion of a single site that has gained glycosylation in the WSN HA relative to the PR8 HA (see Methods for details). One possible concern is that Caton et al. (1982) mapped antigenic sites largely by selecting monoclonal-antibody escape mutants, and so these sites might be biased towards being more mutationally tolerant. We therefore also made a broader classification of “antigenic sites and contacting residues” consisting of the Caton et al. antigenic sites plus all surface-exposed residues in contact with these sites (see Methods for details). This broader classification includes all residues in regions of the HA surface targeted by antibodies, and so should not be biased by whether sites are amenable to the selection of monoclonal-antibody escape mutants. We hypothesized that both sets of antigenic sites would have unusually high mutational tolerance.

For comparison, we used two classifications of receptor-binding residues (see Methods). The first classification consists of residues that have important roles in receptor binding (Martin et al., 1998) and are conserved in H1 HAs; these residues are mostly deep in the binding pocket. The second classification consists of all residues that contact the sialic-acid receptor in the crystal structure, regardless of their level of conservation. We hypothesized that the core set of conserved receptor-binding residues would have unusually low mutational tolerance, but that the set of all receptor-binding residues would have typical levels of mutational tolerance since influenza routinely escapes from antibodies that target the periphery of the receptor-binding pocket (Koel et al., 2013).

The positions of the Caton et al. antigenic sites and the conserved receptor-binding residues in the primary sequence are indicated by the top overlay bar in Figure 5. Visual inspection suggests that the conserved receptor-binding residues are indeed relatively intolerant of mutations (have a strong preference for one specific amino acid), whereas the Caton et al. antigenic sites are relatively tolerant of mutations (have roughly equivalent preferences for many amino acids).

For a more quantitative analysis, we computed a site entropy from the inferred amino-acid preferences – larger site entropies indicate a higher inherent tolerance for mutations. The site entropies of all residues are displayed on the HA protein structure in Figure 10. Visual inspection suggests that both classifications of antigenic sites have unusually high mutational tolerance, whereas the conserved receptor-binding residues have unusually low mutational tolerance.
We next tested whether these visual observations were supported by a rigorous statistical analysis. A confounding factor in comparing mutational tolerance across different sets of residues is that sites with higher solvent accessibility are typically more tolerant of mutations (Ramsey et al., 2011; Bustamante et al., 2000). To correct for this fact, we computed the relative solvent accessibility (RSA) for all residues in the HA crystal structure. Residues with RSAs close to zero are buried and are expected to be fairly intolerant of mutations, whereas residues with RSAs substantially greater than zero are surface exposed and are expected to be fairly tolerant of mutations. Figure 10 plots site entropy as a function of RSA for HA1 residues. This figure shows that sites with higher RSA are more mutationally tolerant as expected. However, the figure also suggests that both classifications of antigenic sites are more mutationally tolerant than other residues with equivalent RSA. The figure also suggest that the conserved receptor-binding residues are less mutationally tolerant than other residues with equivalent RSA, whereas the set of all receptor-binding residues have fairly typical mutational tolerance. These observations are supported by the statistical analyses in Table 3: even after correcting for RSA, there is a significant trend for antigenic sites to have high mutational tolerance, and for conserved receptor-binding residues to have low mutational tolerance.

Overall, these results show that antigenic sites in HA have unusually high inherent mutational tolerance, suggesting that this property combines with external immune selection to contribute to HA’s rapid antigenic evolution. These results also show that while a core group of conserved residues deep in the receptor-binding pocket have unusually low mutational tolerance, the bulk of residues that contact the receptor are not under exceptional constraint. This fact probably explains why HA is able to escape from antibodies targeting the periphery of the receptor-binding pocket (Koel et al., 2013), and why only rare antibodies that penetrate deep into this pocket are broadly neutralizing (Whittle et al., 2011).

**HA’s antigenic evolvability is not shared by all influenza proteins**

The foregoing results show that the antigenic sites in HA have an unusually high inherent tolerance for mutations. Is this antigenic evolvability an exceptional feature of HA, or is it commonly shared by other viral proteins? Ideally one would compare HA to the major surface antigens of other viruses with high (e.g., HIV) and low (e.g., measles) rates of antigenic evolution – but unfortunately comparable data sets for these other viruses are not yet available. Therefore, we instead compared the antigenic evolvability of HA to that of influenza nucleoprotein (NP),
a protein for which we have recently performed a similar deep mutational scanning experiment (Bloom, 2014).

The adaptive immune system targets NP via cytotoxic T-lymphocytes (CTLs) (Valkenburg et al., 2011). Although the selection exerted by these CTLs is believed to be weaker than the antibody-mediated selection on HA’s antigenic sites (Bhatt et al., 2011), influenza does benefit from mutations in NP that promote escape from CTLs (Berkhoff et al., 2007; Valkenburg et al., 2013). However, whereas HA rapidly evolves to escape from antibodies, NP does not appear to have any special propensity for rapid evolution of the epitopes targeted by CTLs. Instead, mutations in NP’s CTL epitopes are often deleterious and require secondary permissive or compensatory mutations to fix without a fitness cost (Rimmelzwaan et al., 2004; Berkhoff et al., 2005, 2006; Gong et al., 2013). Therefore, we hypothesized that unlike HA’s highly evolvable antigenic sites, NP’s CTL-antigenic sites would not possess unusually high inherent mutational tolerance.

To test this hypothesis, we used a previously described delineation of epitopes in NP from the human H3N2 strain A/Aichi/2/1968 with experimentally validated human CTL responses (Gong and Bloom, 2014). In this delineation, less than a quarter of NP’s sites participate in multiple CTL epitopes. We used the results of our previous deep mutational scanning of NP to compare the inherent mutational tolerance of sites that participate in multiple CTL epitopes to all other sites in NP. As shown in Figure 11 and Table 4, the NP sites involved in multiple CTL epitopes have an inherent mutational tolerance that is indistinguishable from other sites in the protein. Therefore, NP does not possess any special inherent mutational tolerance in its CTL epitopes. This finding implies that a high level of antigenic evolvability is not a general feature of all viral proteins, but is instead at least somewhat unique to HA.
Discussion

A fundamental challenge in studying the natural evolution of influenza is separating the effects of external selection pressures from inherent structural and functional constraints. The evolutionary patterns observed in natural sequences are shaped by a combination of inherent mutational tolerance and external pressures such as immune selection, and the analysis of such sequences is further confounded by the fact that influenza is not at evolutionary equilibrium.

Here we have quantified the inherent mutational tolerance of influenza HA by using deep mutational scanning (Fowler et al., 2010; Araya and Fowler, 2011) to simultaneously assess the impact on viral growth of the vast majority of the \( \approx 10^4 \) possible amino-acid mutations to influenza HA. The information obtained from the deep mutational scanning is consistent with existing knowledge about the effects of mutations on HA function and structure. For instance, the deep mutational scanning shows strong selection for specific amino acids known to play important roles in HA’s receptor-binding activity, fusion activity, and proteolytic activation (Qiao et al., 1999; Stech et al., 2005; Martin et al., 1998). Similarly, at the sites of known temperature-sensitive mutations to HA (Nakajima et al., 1986), the deep mutational scanning identifies the more stabilizing amino-acid as more favorable. Broader trends from the deep mutational scanning are also in agreement with current thinking about mutational effects. For example, the deep mutational scanning finds that there is strong purifying selection against stop-codon mutations and many nonsynonymous mutations, but that there is only weak selection against synonymous mutations. All of these results suggest that the deep mutational scanning faithfully captures both the specific and general effects of mutations on HA.

The comprehensive information generated by the deep mutational scanning can be used to create quantitative evolutionary models for analyzing HA sequence phylogenies. Here we have shown that an evolutionary model constructed from our deep mutational scanning data describes the evolution of human and swine H1 HAs far better than existing state-of-the-art models for sequence evolution. We anticipate that separating HA’s inherent mutational tolerance from external selection should also eventually allow the external selection pressures to be studied in greater detail. For example, one might imagine that sites in HA that exhibit evolutionary patterns that deviate from the quantitative model created from our deep mutational scanning are likely to be under external selection. Future work that augments deep mutational scanning with specific experimentally defined selection pressures (such as antibodies against HA) could aid in further elucidation of the forces that shape influenza evolution. It also may be possible to
utilize high-throughput experimental data on mutational effects to better estimate the fitness of naturally occurring strains in a way that aids in prediction of the year-to-year strain dynamics of influenza (Łuksza and Lässig, 2014).

The deep mutational scanning also enabled us to assess the extent to which HA’s inherent mutational tolerance contributes to influenza’s antigenic evolvability. It remains a mystery why error-prone RNA viruses differ so widely in their capacity for evolutionary escape from immunity, with some (e.g. influenza and HIV) undergoing rapid antigenic evolution while others (e.g. measles) show little antigenic change on relevant timescales (Lipsitch and O’Hagan, 2007; Koelle et al., 2006; Heaton et al., 2013). Our data demonstrate that the antigenic sites in HA are unusually tolerant to mutations, implying that inherent evolutionary plasticity at sites targeted by the immune system is one factor that contributes to influenza’s rapid antigenic evolution. This high mutational tolerance at antigenic sites could itself be a property that influenza has evolved to aid in its antigenic escape – or it might simply be an unfortunate coincidence that the immune system focuses on especially plastic portions of HA. In either case, it is intriguing to speculate whether a high inherent mutational tolerance in antigenic sites is also a feature of other antigenically variable RNA viruses. Application of the deep mutational scanning approach used here to additional viruses should provide a means to address this question.
Methods

Availability of data and computer code


HA sequence numbering

A variety of different numbering schemes for HA are used in the literature. Unless noted otherwise, residues are numbered here using sequential numbering of the WSN HA protein sequence (Supplementary file 1) starting with one at the N-terminal methionine. In some cases, the number of the corresponding residues in the widely used H3 numbering scheme is also indicated. These numbering systems can be interconverted using the Python script available at https://github.com/jbloom/HA_numbering.

Generation of HA codon mutation library

The HA codon-mutant library was generated using the oligo-based PCR mutagenesis protocol described previously by Bloom (2014). The only differences from that protocol were that HA was used as the template rather than NP, and that only two overall rounds of mutagenesis were performed, rather than the three rounds used by Bloom (2014). This reduction in the number of rounds of mutagenesis reduced the average number of codon mutations from the ≈ three per clone in Bloom (2014) to the ≈ two per clone shown in Figure 2. The libraries were created in full biological triplicate, meaning that each experimental replicate was derived from an independent plasmid mutant library.

The end primers for the mutagenesis were 5’-cgatcacgtctctggagcaggagaagggaaataaaacaac-3’ and 5’-gatacacgtctcatattagtagaaacaagggtttttctatatatttctg-3’ (these primers include BsmBI restriction sites). The mutagenic primers were ordered from Integrated DNA Technologies, and
are listed in Supplementary file 2.

The final products from the codon mutagenesis PCR were gel purified and digested with BsmBI (New England Biolabs, R0580L). The BsmBI-digested HA was ligated into a dephosphorylated (Antarctic Phosphatase, New England Biolabs, M0289L) and BsmBI-digested preparation of the bidirectional reverse-genetics plasmid pHW2000 (Hoffmann et al., 2000) using T4 DNA ligase (New England Biolabs, M0202S). Column-purified ligations were electroporated into ElectroMAX DH10B T1 phage-resistant competent cells (Invitrogen, 12033-015) and plated on LB plates containing 100 µg/ml of ampicilin. A 1:4000 dilution of each transformation was plated in parallel to enable estimation of the number of unique transformants – we obtained at least two-million unique colonies per transformation. For each replicate of the codon-mutant library, we performed three transformations to generate approximately six-million independent clones per replicate library. Control ligations lacking an insert yielded at least 100 times fewer colonies, indicating a very low rate of background self-ligation of the pHW2000 plasmid. The transformants from each HA mutant library replicate were pooled, cultured in LB supplemented with ampicillin, and mini-prepped to generate the HA codon mutant plasmid libraries.

For the Sanger sequencing analysis shown in Figure 2, we picked and prepped 34 independent colonies for sequencing. The full analysis of this Sanger sequencing is available at https://github.com/jbloom/SangerMutantLibraryAnalysis/tree/v0.2.

**Virus rescue and passage in cells**

The HA mutant plasmid libraries were used to generate pools of mutant influenza viruses by reverse genetics (Hoffmann et al., 2000). Cocultures of 293T and MDCK-SIAT1 cells were transfected with equal amounts of HA (either unmutated or one of the plasmid mutant libraries) cloned into pHW2000 as described above, plus the seven other WSN genes in bidirectional reverse-genetics plasmids (pHW181-PB2, pHW182-PB1, pHW183-PA, pHW185-NP, pHW186-NA, pHW187-NA, pHW188-NS), which were kind gifts from Robert Webster of St. Jude Children’s Research Hospital. Overall, six viral rescues and passages were performed, each using a different HA plasmid preparation: the three HA mutant library replicates (eventually yielding the mutivirus samples in Figure 1) and three independent unmutated HAs (eventually yielding the virus samples in Figure 1).

Each of the viral rescues was performed by transfecting multiple wells of cells in an effort to
increase the diversity of the rescued viruses. Specifically, two 12-well dishes were transfected per rescue. Cells were plated at $2 \times 10^5$ 293T cells and $5 \times 10^4$ MDCK-SIAT1 cells per well in D10 (DMEM supplemented with 10% heat-inactivated FBS, 2 mM L-glutamine, 100 U of penicillin/ml, and 100 $\mu$g of streptomycin/ml), and then each well was transfected with 1 $\mu$g of total plasmid DNA (125 ng of each of the eight plasmids) using the BioT transfection reagent (Bioland B01-02). At 12 to 18 hours post-transfection, the medium was changed to our WSN viral growth media: Opti-MEM supplemented with 0.5% heat-inactivated FBS, 0.3% BSA, 100 U of penicillin/ml, 100 $\mu$g of streptomycin/ml, and 100 $\mu$g of calcium chloride/ml. This media does not contain trypsin since viruses with the WSN HA and NA are trypsin independent (Goto and Kawaoka, 1998). Viral supernatants were collected 72 hours post-transfection, and the supernatants from the different wells were pooled for each viral rescue. These pooled supernatants were then clarified by centrifugation at $2000 \times g$ for five minutes, aliquoted, and frozen at -80°C. Aliquots were then thawed and titered by TCID50 (see below).

For viral passage, each viral rescue replicate was passaged in four 10-cm dishes. Briefly, $6 \times 10^6$ MDCK-SIAT1 cells per 10-cm dish in WSN viral growth media were infected with $6 \times 10^5$ infectious particles (multiplicity of infection of 0.1). Since there are four dishes for each replicate, this maintains a diversity of $2.4 \times 10^6$ TCID50 units per replicate. The passaged viral supernatants were collected at 50 hours post-infection, and the supernatants for the four plates were pooled for each replicate. These pooled supernatants were clarified at $2000 \times g$ for five minutes, aliquoted, and frozen at -80°C. Aliquots were then thawed and titered by TCID50.

**Virus titering by TCID50**

The viruses were titered by TCID50 (50% tissue culture infectious dose). In this assay, 10 $\mu$l of a 1:10 dilution of the viral supernatant to be titered was added to the first row of a 96-well tissue culture plate containing 90 $\mu$l of WSN viral growth media. At least one no-virus control supernatant was included on each plate as a negative control. The virus was then serially diluted 1:10 down the rows of the plates, and then $5 \times 10^3$ MDCK-SIAT1 cells were added to each well. The plates were then incubated at 37°C, and scored for cytopathic effects caused by viral growth after for 65-72 hours. Virus titers were calculated by the method of Reed and Muench (1938) implemented via the Python script at https://github.com/jbloom/reedmuenchcalculator.
Generation of samples for Illumina deep sequencing

The deep sequencing samples were prepared from PCR amplicons that were generated exactly as described for the DNA, mutDNA, virus, and mutvirus samples in Bloom (2014). The viral RNA template for the virus and mutvirus were isolated using freshly purchased Trizol reagent (Life Technologies; 15596-026) in order to avoid any oxidative damage associated with old reagents. After performing reverse transcription as described in Bloom (2014), quantitative PCR (qPCR) was used to quantify the number of HA cDNA molecules to ensure that there were at least $10^6$ unique template molecules before beginning the subsequent PCR amplification. The qPCR primers were designed based on those described by Marsh et al. (2007), and were 5’-taacctgctcgaagacagcc-3’ and 5’-agagccatccggtgatgtta-3’.

The PCR amplicons were fragmented and barcoded using the custom modification of Illumina’s Nextera kit using the protocol described in Bloom (2014). Samples were barcoded as follows: DNA - N701, mutDNA - N702, virus - N704, and mutvirus - N705. For each of the three biological replicates, these four samples were pooled and sequenced on their own Illumina lane with 50-nucleotide paired-end reads as described in Bloom (2014). For the technical sequencing repeat of biological replicate #1, the library preparation and sequencing were repeated from the same viral RNA templates. This technical repeat therefore only quantifies variation associated with sample preparation and sequencing, whereas the biological replicates also quantify variation associated with the processes of codon-mutant library creation, virus generation, and virus passage.

Analysis of deep sequencing data

The deep sequencing data was analyzed using the mapmuts computer program (Bloom, 2014). A description of the analysis approach and the resulting data files and figures produced are available at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.

Briefly, paired reads were overlapped as illustrated in Figure 3 – figure supplement 1 and then aligned to HA. Reads were retained only if both reads in the pair passed the default Illumina filter, had average Q-scores of at least 25, overlapped for at least 30 nucleotides with no more than one mismatch, and the overlap aligned to the HA gene with no more than six mismatches. Figure 3 – figure supplement 2 shows the number of reads for each sample that met these criteria. Most reads that did not meet these criteria failed to do so because they could not be
paired with at least 30 nucleotides of overlap – a situation that arises when the HA fragment produced by the Nextera fragmentation produces a fragment smaller than 30 nucleotides or larger than 70 nucleotides. Codon identities were called only if both overlapped paired reads agreed on the identity of the codon. This requirement reduces the error rate, because it is rare for both paired reads to independently experience the same sequencing error.

As shown in Figure 4, we estimated that 85% of possible codon mutations were sampled at least five times by the mutant viruses. To estimate the fraction of amino-acid mutations that would have been sampled, we simulated randomly selecting 85% of the mutant codons from the HA sequence, and determined that these codons encoded \( \approx 97\% \) of the amino-acid mutations.

**Inference of amino-acid preferences and site entropies**

The counts of each codon identity in the deep sequencing data was used to infer the “preference” of each site for each amino acid as described in Bloom (2014). This inference was also done using the mapmuts computer program as detailed at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.

Briefly, the preference \( \pi_{r,a} \) of site \( r \) for amino-acid \( a \) represents the expected frequency of that amino acid in a hypothetical library where each amino-acid is introduced at equal frequency. Specifically, the expected frequency \( f_{r,x}^{\text{mutvirus}} \) of mutant codon \( x \) at site \( r \) in the mutvirus sample is related to the preference for its encoded amino-acid \( A(x) \) by

\[
f_{r,x}^{\text{mutvirus}} = \epsilon_{r,x} + \rho_{r,x} + \frac{\mu_{r,x} \times \pi_{r,A(x)}}{\sum_y \mu_{r,y} \times \pi_{r,A(y)}},
\]

where \( \epsilon_{r,x} \) is the rate at which site \( r \) is erroneously read to be codon \( x \), \( \rho_{r,x} \) is the rate at which site \( r \) is erroneously reverse-transcribed to codon \( x \), and \( \mu_{r,x} \) is the rate at which site \( r \) is mutagenized to codon \( x \) in the mutant DNA sample. These unknown error and mutation rate parameters are inferred from the DNA, virus, and mutvirus samples using the Bayesian approach described in Bloom (2014). Inferences of the posterior mean preferences \( \pi_{r,a} \) were made separately for each replicate of the experiment, and the correlations among these inferences from different replicates are in Figure 6. The final “best” inferred preferences from the combined data of the three biological replicates were obtained by averaging the preferences obtained from the three biological replicates. These final inferred preferences are provided in Supplementary file 3 and displayed graphically in Figure 5.
The site entropies in Figure 10 and Table 3 were calculated from the amino-acid preferences as
\[ h_r = \sum_a \pi_{r,a} \times \log_2 \pi_{r,a}. \]
These site entropies are therefore in bits. Higher site entropies indicate a higher inherent mutational tolerance.

Alignment of naturally occurring HAs and phylogenetic tree

The inferred amino-acid preferences were compared to amino-acid frequencies in an alignment of naturally occurring H1N1 HAs from swine and human lineages descended from a close relative of the 1918 virus. Briefly, all full-length H1 HAs from these hosts were downloaded from the Influenza Virus Resource (Bao et al., 2008). Up to three sequences per host and year were randomly subsampled and used to build a phylogenetic tree. Clear outliers from the molecular clock (typically lab artifacts or mis-annotated sequences) were iteratively excluded and the trees were rebuilt. The final sequence alignment is in Supplementary file 4. This alignment was used to build the phylogenetic trees in Figure 8 and Figure 8 – figure supplement 1 with codonPhyML (Gil et al., 2013) using the codon-substitution model of (Goldman and Yang, 1994) or (Kosiol et al., 2007) with empirical codon frequencies determined using the CF3x4 method (Pond et al., 2010) or the F method, respectively. In both cases, the nonsynonymous-synonymous ratio (\( \omega \)) was drawn from four gamma-distributed categories (Yang et al., 2000). A description of this process is at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.

Comparison of evolutionary models

We compared the accuracy with which the naturally occurring HA phylogeny was described by an evolutionary model based on the experimentally measured amino-acid preferences versus several standard codon-substitution models. These comparisons were used made using HY-PHY (Pond et al., 2005) and phyloExpCM (Bloom, 2014). A description of this analysis is at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.

Briefly, the phylogenetic tree topology was fixed to that shown in Figure 8 or Figure 8 – figure supplement 1. The branch lengths and any free parameters of the evolutionary model were then optimized by maximum likelihood. The experimentally determined evolutionary models were constructed from the inferred amino-acid preferences reported here and the experimentally measured mutation rates reported in Bloom (2014). The “fixation probabilities” were computed
using either the Metropolis-like relationship described in Bloom (2014) or the relationship proposed by Halpern and Bruno (1998). The results of these comparisons are in Table 2, Table 2 – table supplement 1, Table 2 – table supplement 2, and Table 2 – table supplement 3. All of these comparisons show that the experimentally determined evolutionary models are far superior to the various standard models.

**Structural analyses**

The WSN HA studied here has a high degree of sequence identity to the HA crystallized in PDB 1RVX (Gamblin et al., 2004). It is this HA structure that is shown Figure 10. The relative solvent accessibilities (RSA) values in Figure 5 and Figure 10 were calculated by first determining the absolute solvent accessibilities of the residues in the full trimeric HA in PDB 1RVX with the DSSP (Joosten et al., 2011) webserver at http://www.cmbi.ru.nl/hsspsoap/, and then normalizing by the maximum solvent accessibilities given by Tien et al. (2013).

**Classification of antigenic sites and conserved receptor-binding residues**

Several sub-classifications of HA residues were performed.

Conserved receptor-binding sites were any residues listed in the first table of Martin et al. (1998) that are also conserved in at least 90% of H1 HAs. These residues are listed in Table 1.

All receptor-binding residues were any residues with any atom within 5 Å of the substrate in PDB 1RVX (Gamblin et al., 2004). No constraint is placed on whether or not these residues are conserved in natural sequences. The residues that fall into this classification are (in sequential numbering of the WSN HA): 108, 147, 148, 149, 150, 151, 158, 166, 168, 196, 198, 199, 203, 207, 238, 239, and 241.

The Caton et al. (1982) antigenic-site residues are classified based on antigenic mapping of the A/Puerto Rico/8/1934 (H1N1) HA. Specifically, these are any residues listed in the third table of Caton et al. (1982) with the following exceptions: residue 182 (H3 numbering) is not considered for the reason explained on page 421 of Caton et al. (1982), residue 273 (H3 numbering) is not considered for the reason explained on page 422 of Caton et al. (1982), and residue 129 (H3 numbering) is not considered because it has gained a glycosylation site in the WSN HA that is not present in the A/Puerto Rico/8/1934 (H1N1) HA and mutation of this WSN glycosylation site can strongly affect viral growth (Deom et al., 1986). Overall, this gives the following set of antigenic residues, listed by sequential numbering of the WSN HA with the H3
number in parentheses: 171 (158), 173 (160), 175 (162), 176 (163), 178 (165), 179 (166), 180 (167), 169 (156), 172 (159), 205 (192), 206 (193), 209 (196), 211 (198), 182 (169), 186 (173), 220 (207), 253 (240), 153 (140), 156 (143), 158 (145), 237 (224), 238 (225), 87 (78), 88 (79), 90 (81), 91 (82), 92 (83), and 135 (122).

A second classification is done that includes the Caton et al. (1982) plus any surface-exposed residues that are in contact with these residues, using an α-carbon to α-carbon distance of \( \leq 6.0 \text{Å} \) as the threshold for being in contact and classifying residues are solvent-exposed if they have an RSA of at least 20%. The rationale for this second classification is that the mapping by Caton et al. (1982) may have been biased towards inherently variable sites, and so other surface-exposed residues that contact these sites could also be antigenic. This classification adds the following 28 residues (listed by sequential numbering of the WSN HA) to the 29 Caton et al. (1982) residues: 85, 86, 89, 126, 132, 136, 137, 138, 142, 148, 150, 154, 155, 157, 170, 184, 185, 187, 202, 203, 207, 210, 212, 221, 235, 236, 239, and 252.
References


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**Figure 1:** Schematic of the deep mutational scanning experiment. The Illumina deep-sequencing samples are shown in yellow boxes (DNA, mutDNA, virus, mutvirus). Experimental steps and associated sources of mutations are shown in blue text, while sources of error during Illumina sample preparation and sequencing are shown in red text. This entire process was performed in biological triplicate.
Figure 2: Properties of the HA codon-mutant library as assessed by Sanger sequencing of 34 individual clones drawn roughly evenly from the three experimental replicates. (A) There are an average of 2.1 codon mutations per clone, with the number per clone following a roughly Poisson distribution. (B) The codon mutations involve a mix of one-, two-, and three-nucleotide mutations. (C) The nucleotide composition of the mutant codons is roughly uniform. (D) The mutations are distributed uniformly along HA’s primary sequence. (E) There is no tendency for mutations to cluster in primary sequence. Shown is distribution of observed pairwise distances between mutations in multiply mutated clones versus the expected distribution when the mutations are placed independently in the clones. All plots show results only for substitution mutations; insertion / deletion mutations are not shown. However, only two insertion / deletion mutations (0.06 per clone) were identified. The data and computer code used to generate this figure are at https://github.com/jbloom/SangerMutantLibraryAnalysis/tree/v0.2.
**Figure 3:** The per-codon frequencies of mutations in the samples. The samples are named as in Figure 1, with the experimental replicate indicated with the numeric label. The DNA samples have a low frequency of mutations, and these mutations are composed almost entirely of single-nucleotide codon changes – these samples quantify the baseline error rate from PCR and deep sequencing. The mutation frequency is only slightly elevated in virus samples, indicating that viral replication and reverse transcription introduce only a small number of additional mutations. The mutDNA samples have a high frequency of single- and multi-nucleotide codon mutations, as expected from the codon mutagenesis procedure. The mutvirus samples have a lower mutation frequency, with most of the reduction due to fewer stop-codon and nonsynonymous mutations – consistent with purifying selection purging deleterious mutations. The data and code used to create this plot is available via http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html; this plot is the file parsesummary_codon_types_and_nmuts.pdf described therein. The sequencing accuracy was increased by using overlapping paired-end reads as illustrated in Figure 3 – figure supplement 1. The overall number of overlapping paired-end reads for each sample is shown in Figure 3 – figure supplement 2. A representative plot of the read depth across the primary sequence is shown in Figure 3 – figure supplement 3.
Figure 3 – figure supplement 1: The overlapping paired-end Illumina sequencing strategy. 

(A) Sequencing accuracy was increased by fragmenting the HA gene to pieces roughly 50 nucleotides in length, and then using overlapping paired-end 50 nucleotide Illumina sequencing reads. Codon identities were only called if the reads overlapped and concurred on the codon identity. 

(B) The distribution of actual HA fragment lengths for a representative sample. The plot in (B) is the file replicate_3/DNA/replicate_3_DNA_insertlengths.pdf described at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.
Figure 3 – figure supplement 2: The total number of reads for each sample. For all samples, the majority of reads could be paired and aligned to the HA sequence. However, the exact fraction of reads that could be paired varied somewhat among samples due to variation in the efficiency with which the HA gene was fragmented to the target length of 50 nucleotides. This plot is the file alignmentsummaryplot.pdf described at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.
**Figure 3 – figure supplement 3:** The per-codon read depth as a function of primary sequence. This plot is typical of the samples. The read depth varied fairly consistently as a function of primary sequence, presumably due to biases in the positions at which the HA gene tended to fragment. This plot is the file `replicate_3/DNA/replicate_3_DNA_codondepth.pdf` described at [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html).
**Figure 4:** The number of times that each possible multi-nucleotide codon mutation was observed in each sample after combining the data for the three biological replicates. Nearly all mutations were observed many times in the mutDNA samples, indicating that the codon mutagenesis was comprehensive. Only about half of the mutations were observed at least five times in the mutvirus samples, indicating either a bottleneck during virus generation or purifying selection against many of the mutations. If the analysis is restricted to synonymous multi-nucleotide codon mutations, then about 85% of mutations are observed at least five times in the mutvirus samples. Since synonymous mutations are less likely to be eliminated by purifying selection, this latter number provides a lower bound on the fraction of codon mutations that were sampled by the mutant viruses. The redundancy of the genetic code means that the fraction of amino-acid mutations sampled is higher. The data and code used to create this figure are available via [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html); this plot is the file `countparsedmuts_multi-nt-codonmutcounts.pdf` described therein. Similar plots for the individual replicates are shown in Figure 4 – figure supplement 1.
Figure 4 – figure supplement 1: Plots like those in Figure 4 for the individual biological replicates: (A) replicate 1, (B) replicate 2, and (C) replicate 3. These plots are the files replicate_1/countparsedmuts_multi-nt-codonmutcounts.pdf, replicate_2/countparsedmuts_multi-nt-codonmutcounts.pdf, and replicate_3/countparsedmuts_multi-nt-codonmutcounts.pdf described at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.
Figure 5: The amino-acid preferences inferred using the combined data from the three biological replicates. The letters have heights proportional to the preference for that amino acid, and are colored by hydrophobicity. The first overlay bar shows the relative solvent accessibility (RSA) for residues in the HA crystal structure. The second overlay bar indicates Caton et al. antigenic sites or conserved receptor-binding residues. The sequence is numbered sequentially beginning with 1 at the N-terminal methionine – however, this first methionine is not shown as it was not mutagenized. Figure 5 – figure supplement 1 shows the same data with H3 numbering of the sequence. The data and code used to create this figure are available via http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html; this plot is the file sequentialnumbering_site_preferences_logoplot.pdf described therein.
**Figure 5 – figure supplement 1:** A plot matching that shown in Figure 5 except that the HA sequence is numbered using the H3 numbering scheme. This plot is the file `H3numbering_site_preferences_logplot.pdf` described at [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html).
**Figure 6:** Correlations among the amino-acid preferences inferred using data from the individual biological replicates. (A) The preferences from two technical repeats of the sample preparation and deep sequencing of biological replicate #1 are highly correlated. (B)-(D) The preferences from the three biological replicates are substantially but imperfectly correlated. Overall, these results indicate that technical variation in sample preparation and sequencing is minimal, but that there is substantial variation between biological replicates due to stochastic differences in which mutant viruses predominate during the initial reverse-genetics step. The Pearson correlation coefficient ($R$) and associated $P$-value are shown in the upper-left corner of each plot.

The data and code used to create this figure are available via [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html); these plots are the files `correlations/replicate_1_vs_replicate_1_repeat.pdf`, `correlations/replicate_1_vs_replicate_2.pdf`, `correlations/replicate_1_vs_replicate_3.pdf`, and `correlations/replicate_2_vs_replicate_3.pdf` described therein.
Figure 7: Correlation of the site-specific amino-acid preferences determined in our study with the “relative fitness” (RF) values reported by Wu et al. (2014). Wu et al. (2014) report RF values for 2350 of the $564 \times 19 = 10716$ possible amino-acid mutations to the WSN HA examined in our study (they only examine single-nucleotide changes and disregard certain types of mutations due to oxidative damage of their DNA). To compare across the data sets, we have normalized their RF values by the RF value for the wildtype amino-acid (which they provide for only 2264 of the 2350 mutations). We then correlate on a logarithmic scale these normalized RF values with the ratio of our measurement of the preference for the mutant amino acid divided by the preference for the wildtype amino acid, using the preferences from our combined replicates. For mutations for which Wu et al. (2014) report an RF of zero, we assign a normalized RF equal to the smallest value for their entire data set. There is a significant Pearson correlation of 0.48 between the data sets, indicating that both our experiments and those of Wu et al. (2014) are capturing many of the same constraints on HA. However this correlation is lower than that between our individual experimental replicates (Figure 6). Because Wu et al. (2014) do not provide raw data from replicates to enable quantification of the variability of their measurements, it is impossible to assess whether the reduced correlation reflects differences in selection pressures in their experiment versus our own, or simply reflects a higher inherent level of noise in their measurements (i.e., we cannot compute the expected correlation between two independent replicates of their measurements). The data and code used to create this figure are available via http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html; this plot is the file correlation_with_Wu_et_al.pdf described therein.
**Figure 8:** A phylogenetic tree of human and swine H1 HA sequences descended from a common ancestor closely related to the 1918 virus. The WSN virus used in the experiments here is a lab-adapted version of the *A/Wilson Smith/1933* strain. Human H1N1 that circulated from 1918 until 1957 is shown in blue. Human seasonal H1N1 that reappeared in 1977 is shown in purple. Swine H1N1 is shown in red. The 2009 pandemic H1N1 is shown in green. This tree was constructed using *codonPhyML* (Gil et al., 2013) with the substitution model of Goldman and Yang (1994). This plot is the file *CodonPhyML_Tree_H1_HumanSwine_GY94.annotated_tree.pdf* described at [http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html](http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html). *Figure 8 – figure supplement 1* shows a tree estimated for the same sequences using the substitution model of Kosiol et al. (2007).
Figure 8 – figure supplement 1: A phylogenetic tree of the same sequences shown in Figure 8, this time inferred using the substitution model of Kosiol et al. (2007). This tree is extremely similar to that in Figure 8, indicating the inferred topology is robust to the exact choice of codon-substitution model. This plot is the file Codon-PhyML_Tree_H1_HumanSwine_KOSI07.annotated_tree.pdf described at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.
Figure 9: The frequencies of amino acids among the naturally occurring HA sequences in Figure 8 versus the amino-acid preferences inferred from the combined replicates (Figure 5). Note that a natural frequency close to one or zero could indicate absolute selection for or against a specific amino acid, but could also simply result from the fact that natural evolution has not completely sampled all possible mutations compatible with HA structure and function. The Pearson correlation coefficient ($R$) and associated $P$-value are shown on the plot. This plot is the file natural_frequency_vs_preference.pdf described at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.
Figure 10: Inherent mutational tolerance of HA’s receptor-binding residues and antigenic sites. (A) Surface of HA with one monomer colored by site entropy as determined by the deep mutational scanning; blue indicates low mutational tolerance and red indicates high mutational tolerance. (B) The structure shows residues classified as antigenic sites by Caton et al. (1982) in colored spheres; the plot shows site entropy versus relative solvent accessibility (RSA) of these residues (red triangles) and all other HA1 residues in the crystal structure (blue circles). (C) Antigenic sites of Caton et al. (1982) plus all other surface-exposed residues that contact these sites. (D) Conserved receptor-binding residues. (E) All receptor-binding residues. Table 3 shows that residues in (B) and (C) have unusually high mutational tolerance, residues in (D) have unusually low mutational tolerance, and residues in (E) do not have unusual mutational tolerance. The data and code to create all panels of this figure is provided via http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html. The structure is PDB 1RVX (Gamblin et al., 2004).
**Figure 11:** The inherent mutational tolerance of NP’s CTL epitopes is indistinguishable from that of non-epitope sites in NP. The plot shows the site entropy versus relative solvent accessibility (RSA) of NP residues that participate in multiple CTL epitopes (red triangles) and all other NP residues in the crystal structure (blue circles). Visual inspection suggests that the epitope sites have mutational tolerance comparable to other sites, and this result is supported by the statistical analysis in Table 4. Note that unlike for HA, there is no trend for RSA to correlate with site entropy – this could be because many of NP’s surface-exposed sites are constrained by interactions with viral RNA. The CTL epitopes are those delineated in the first supplementary table of Gong and Bloom (2014). The site entropies are computed from a previously described deep mutational scan of NP, and are the values in the first supplementary file of Bloom (2014); the RSA values are also taken from that reference. The data and code used to generate this plot is available via [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html); the plot itself is the file `NP_CTL_entropy_rsa_correlation.pdf` described therein.
### Table 1

<table>
<thead>
<tr>
<th>Site in sequential numbering</th>
<th>Site in H3 numbering</th>
<th>Existing knowledge</th>
<th>Inferred amino-acid preferences</th>
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<tbody>
<tr>
<td>127</td>
<td>117 (HA1)</td>
<td>Mutation from S to P creates a temperature-sensitive defect (Nakajima et al., 1986)</td>
<td>The preference for S is 30 times higher than the preference for P</td>
</tr>
<tr>
<td>174</td>
<td>161 (HA1)</td>
<td>Mutation from Y to H creates a temperature-sensitive defect (Nakajima et al., 1986)</td>
<td>The preference for Y is 25 times higher than the preference for H</td>
</tr>
<tr>
<td>344</td>
<td>1 (HA2)</td>
<td>Mutation from G to E abolishes HA fusion activity (Qiao et al., 1999)</td>
<td>The preference for G is 11 times higher than for E</td>
</tr>
<tr>
<td>343</td>
<td>327 (HA1)</td>
<td>A basic residue (R or K) is required for HA proteolytic activation (Stech et al., 2005)</td>
<td>The combined preferences for R and K (0.87) far exceed those of all other amino acids combined</td>
</tr>
<tr>
<td>108</td>
<td>98 (HA1)</td>
<td>Receptor-binding residue, is Y in &gt; 99% of natural H1 HAs</td>
<td>The preference for Y (0.61) exceeds those of all other amino acids combined</td>
</tr>
<tr>
<td>166</td>
<td>153 (HA1)</td>
<td>Receptor-binding residue, is W in &gt; 99% of natural H1 HAs</td>
<td>The preference for W (0.65) exceeds those of all other amino acids combined</td>
</tr>
<tr>
<td>196</td>
<td>183 (HA1)</td>
<td>Receptor-binding residue, is H in &gt; 99% of natural H1 HAs</td>
<td>The preference for H (0.69) exceeds those of all other amino acids combined</td>
</tr>
<tr>
<td>203</td>
<td>190 (HA1)</td>
<td>Receptor-binding residue, is D in 90% of natural H1 HAs</td>
<td>The highest preference is for the chemically similar E</td>
</tr>
<tr>
<td>207</td>
<td>194 (HA1)</td>
<td>Receptor-binding residue, is L in 97% of natural H1 HAs</td>
<td>The preference for L (0.55) exceeds those of all other amino acids combined</td>
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<tr>
<td>208</td>
<td>195 (HA1)</td>
<td>Receptor-binding residue, is Y in &gt; 99% of natural H1 HAs</td>
<td>The preference for Y (0.72) exceeds those of all other amino acids combined</td>
</tr>
<tr>
<td>239</td>
<td>226 (HA1)</td>
<td>Receptor-binding residue, is Q in ≈ 99% of natural H1 HAs</td>
<td>Q is one of three amino acids with a high preference</td>
</tr>
<tr>
<td>241</td>
<td>228 (HA1)</td>
<td>Receptor-binding residue, is G in &gt; 99% of natural H1 HAs</td>
<td>The preference for G (0.57) exceeds those of all other amino acids combined</td>
</tr>
</tbody>
</table>

Table 1: The amino-acid preferences inferred from the combined experimental replicates are consistent with existing knowledge about HA structure and function. The conserved receptor-binding residues listed in this table are those delineated in the first table of Martin et al. (1998) that also have at least 90% conservation among all naturally occurring H1 HAs in the Influenza Virus Resource (Bao et al., 2008).
<table>
<thead>
<tr>
<th>model</th>
<th>ΔAIC</th>
<th>log likelihood</th>
<th>parameters (optimized + empirical)</th>
</tr>
</thead>
<tbody>
<tr>
<td>combined</td>
<td>0.0</td>
<td>-24088.7</td>
<td>0 (0 + 0)</td>
</tr>
<tr>
<td>replicate 3</td>
<td>303.2</td>
<td>-24240.3</td>
<td>0 (0 + 0)</td>
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<tr>
<td>replicate 1</td>
<td>535.4</td>
<td>-24356.4</td>
<td>0 (0 + 0)</td>
</tr>
<tr>
<td>replicate 2</td>
<td>876.2</td>
<td>-24526.8</td>
<td>0 (0 + 0)</td>
</tr>
<tr>
<td>GY94, gamma ω, gamma rates</td>
<td>882.6</td>
<td>-24517.0</td>
<td>13 (4 + 9)</td>
</tr>
<tr>
<td>GY94, gamma ω, one rate</td>
<td>1109.7</td>
<td>-24631.5</td>
<td>12 (3 + 9)</td>
</tr>
<tr>
<td>KOSI07, gamma ω, gamma rates</td>
<td>1620.5</td>
<td>-24834.9</td>
<td>64 (4 + 60)</td>
</tr>
<tr>
<td>GY94, one ω, gamma rates</td>
<td>1859.4</td>
<td>-25006.4</td>
<td>12 (3 + 9)</td>
</tr>
<tr>
<td>KOSI07, one ω, one rate</td>
<td>1883.0</td>
<td>-24967.2</td>
<td>63 (3 + 60)</td>
</tr>
<tr>
<td>KOSI07, one ω, gamma rates</td>
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<td>63 (3 + 60)</td>
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<tr>
<td>GY94, one ω, one rate</td>
<td>2544.5</td>
<td>-25350.0</td>
<td>11 (2 + 9)</td>
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<tr>
<td>KOSI07, one ω, one rate</td>
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<td>62 (2 + 60)</td>
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<tr>
<td>combined, randomized</td>
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<td>replicate 3, randomized</td>
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<tr>
<td>replicate 2, randomized</td>
<td>6477.8</td>
<td>-27327.6</td>
<td>0 (0 + 0)</td>
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</table>

**Table 2:** An evolutionary model derived from the experimentally inferred amino-acid preferences describes the HA sequence phylogeny in Figure 8 far better than a variety of existing state-of-the-art models. The model is most accurate if it utilizes data from the combined experimental replicates, but it also outperforms existing models even if the data are only derived from individual replicates. Models are ranked by AIC (Posada and Buckley, 2004). GY94 indicates the model of Goldman and Yang (1994), and KOSI07 indicates the model of Kosiol et al. (2007). The nonsynonymous / synonymous ratio (ω) and the substitution rate are either estimated as a single value or drawn from a four-category gamma distribution. Randomizing the experimentally inferred preferences among sites makes the models far worse. The fixation probabilities are computed from the preferences using the first equation proposed in Bloom (2014). This table shows data from the file H1_HumanSwine_GY94_summary.tex described at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html. Table 2 – table supplement 1 shows the results when the fixation probabilities are instead computed using the model of Halpern and Bruno (1998). Table 2 – table supplement 2 shows the results when the tree topology is instead estimated using the substitution model of Kosiol et al. (2007). Table 2 – table supplement 3 shows the results when the fixation probabilities are instead computed using the model of Halpern and Bruno (1998) and the tree topology is instead estimated using the model of Kosiol et al. (2007).
Table 2 – table supplement 1: An evolutionary model derived from the experimentally inferred amino-acid preferences also outperforms existing models when the fixation probabilities are estimated using the equation of Halpern and Bruno (1998). This table shows data from the file H1_HumanSwine_GY94_summary.txt described at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.

<table>
<thead>
<tr>
<th>model</th>
<th>ΔAIC</th>
<th>log likelihood</th>
<th>parameters (optimized + empirical)</th>
</tr>
</thead>
<tbody>
<tr>
<td>combined</td>
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<td>0 (0 + 0)</td>
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<tr>
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<td>13 (4 + 9)</td>
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<td>GY94, one ω, gamma rates</td>
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<td>KOSI07, gamma ω, one rate</td>
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<tr>
<td>KOSI07, one ω, gamma rates</td>
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<td>GY94, one ω, one rate</td>
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<td>11 (2 + 9)</td>
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<td>0 (0 + 0)</td>
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<td>replicate 2, randomized</td>
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<td>parameters (optimized + empirical)</td>
</tr>
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<td>-----------------------------------</td>
</tr>
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</tr>
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</tr>
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</tr>
<tr>
<td>GY94, gamma $\omega$, one rate</td>
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<tr>
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<td>-24953.1</td>
<td>63 (3 + 60)</td>
</tr>
<tr>
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<td>-25203.4</td>
<td>63 (3 + 60)</td>
</tr>
<tr>
<td>GY94, one $\omega$, one rate</td>
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<td>-25345.6</td>
<td>11 (2 + 9)</td>
</tr>
<tr>
<td>KOSI07, one $\omega$, one rate</td>
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<td>6475.2</td>
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**Table 2 – table supplement 2:** An evolutionary model derived from the experimentally inferred amino-acid preferences also outperforms existing models for the tree topology in Figure 8 – figure supplement 1. This table shows data from the file *H1_HumanSwine_KOSI07_summary.tex* described at [http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html](http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html).
### Table 2 – Table Supplement 3:

An evolutionary model derived from the experimentally inferred amino-acid preferences also outperforms existing models for the tree topology in Figure 8 – figure supplement 1 when fixation probabilities are estimated using the equation of Halpern and Bruno (1998). This table shows data from the file *H1_HumanSwine_KOSI07_summary.tex* described at [http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html](http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html).

<table>
<thead>
<tr>
<th>Model</th>
<th>ΔAIC</th>
<th>Log Likelihood</th>
<th>Parameters (Optimized + Empirical)</th>
</tr>
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<td>64 (4 + 60)</td>
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<tr>
<td>GY94, One ω, Gamma Rates</td>
<td>1856.2</td>
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<td>KOSI07, Gamma ω, One Rate</td>
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<td>11 (2 + 9)</td>
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<tr>
<td>Combined, Randomized</td>
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<td>Replicate 1, Randomized</td>
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<tr>
<td>Replicate 3, Randomized</td>
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<tr>
<td>Replicate 2, Randomized</td>
<td>8496.0</td>
<td>-28330.5</td>
<td>0 (0 + 0)</td>
</tr>
</tbody>
</table>
Table 3: The antigenic sites are more significantly mutationally tolerant than other HA1 residues with similar relative solvent accessibility (RSA), the conserved receptor-binding residues are significantly less mutationally tolerant than other similar residues, and sites in the more expansive set of all receptor-binding residues have typical levels of mutational tolerance. The sets of residues analyzed here are those shown in Figure 10. Shown here are the results of multiple linear regression of the continuous dependent variable of site entropy (as computed from the amino-acid preferences) versus the continuous independent variable of RSA and the binary variable of being a receptor-binding residue or being an antigenic site. The data and code used to perform these analyses are available via http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.
**Model:** \[ \text{NP site entropy} \sim \text{RSA} + (\text{multiple CTL epitopes}) + \text{intercept} \]

<table>
<thead>
<tr>
<th>Property</th>
<th>Estimate</th>
<th>Standard error</th>
<th>(P)-value</th>
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</thead>
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<td>0.07</td>
<td>0.52</td>
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<tr>
<td>multiple CTL epitopes</td>
<td>-0.04</td>
<td>0.04</td>
<td>0.31</td>
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</table>

**Table 4:** There is no statistically significant difference between the inherent mutational tolerance of NP sites involved in multiple CTL epitopes and all other NP residues. The table shows the result of multiple linear regression of the continuous dependent variable of site entropy (as computed from the amino-acid preferences) versus the continuous independent variable of RSA and the binary variable of participating in multiple CTL epitopes. The data set analyzed here is plotted in Figure 11. The data and code used to perform this analysis are available via [http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html](http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html).
Supplementary file 1: The coding sequence of the WSN HA gene used in this study is provided in FASTA format.

Supplementary file 2: An Excel file listing the oligonucleotides used for the codon mutagenesis.

Supplementary file 3: The site-specific amino-acid preferences as computed from the averages of the three unique replicates are provided in this supplementary file in text format. This is the file combined_equilibriumpreferences.txt described at http://jbloom.github.io/mapmuts/example_WSN_HA_2014Analysis.html.
Supplementary file 4: The alignment of human and swine HA sequences used to build the phylogenetic trees are provided in this supplementary file in FASTA format. This is the file H1_HumanSwine_alignment.fasta described at http://jbloom.github.io/phyloExpCM/example_2014Analysis_Influenza_H1_HA.html.