1   # The Multispecies Coalescent Model Outperforms

2   # Concatenation across Diverse Phylogenomic Data Sets

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23   ABSTRACT

24   A statistical framework of model comparison and model validation is essential to

25   resolving the debates over concatenation and coalescent models in phylogenomic data

26   analysis. A set of statistical tests are here applied and developed to evaluate and compare the

27   adequacy of substitution, concatenation, and multispecies coalescent (MSC) models across

28   47 phylogenomic data sets collected across tree of life. Tests for substitution models and the

29   concatenation assumption of topologically concordant gene trees suggest that a poor fit of

30   substitution models (44% of loci rejecting the substitution model) and concatenation models

31   (38% of loci rejecting the hypothesis of topologically congruent gene trees) is widespread.

32   Logistic regression shows that the proportions of GC content and informative sites are both

33   negatively correlated with the fit of substitution models across loci. Moreover, a substantial

34   violation of the concatenation assumption of congruent gene trees is consistently observed

35   across 6 major groups (birds, mammals, fish, insects, reptiles, and others, including other

36   invertebrates). In contrast, among those loci adequately described by a given substitution

37   model, the proportion of loci rejecting the MSC model is 11%, significantly lower than those

38   rejecting the substitution and concatenation models, and Bayesian model comparison strongly

39   favors the MSC over concatenation across all data sets. Species tree inference suggests that

40   loci rejecting the MSC have little effect on species tree estimation. Due to computational

41   constraints, the Bayesian model validation and comparison analyses were conducted on the

42   reduced data sets. A complete analysis of phylogenomic data requires the development of

43   efficient algorithms for phylogenetic inference. Nevertheless, the concatenation assumption

44   of congruent gene trees rarely holds for phylogenomic data with more than 10 loci. Thus, for

45   large phylogenomic data sets, model comparison analyses are expected to consistently and

46   more strongly favor the coalescent model over the concatenation model. Our analysis reveals

47   the value of model validation and comparison in phylogenomic data analysis, as well as the

48   need for further improvements of multilocus models and computational tools for

49   phylogenetic inference.

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51   Keywords: congruent gene trees, Bayesian model validation, Bayes factor, posterior

52   predictive simulation, coalescent prior, independent prior, Metazoa

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54   Due to the increasing growth in dimensionality and complexity of multilocus

55   sequence data, accurate phylogenetic inference for understanding the evolutionary history of

56   species faces substantial computational and modeling challenges (RANNALA AND YANG 2008;

57   LIU *et al.* 2015; EDWARDS *et al.* 2016). With the assumption of topologically congruent (TC)

58   genealogies across loci, a phylogenetic tree estimated from concatenated sequences is often

59   used as the estimate of the species tree, despite the fact that the concatenation model

60   oversimplifies the complexity inherent in the diversification of species by ignoring many

61   biological phenomena, such as deep coalescence, hybridization, recombination, and gene

62   duplication and loss, that are commonly observed during the history of species (MADDISON

63   1997; RANNALA AND YANG 2003; BRAVO *et al.* 2019). Since the advent of multilocus

64   sequence data, there has been ongoing effort toward building stochastic models for handling

65   gene tree variation. Given that incomplete lineage sorting (ILS) is likely the most common

66   biological source of gene tree variation (EDWARDS 2009), some of the earliest efforts

67   included parsimony and Bayesian multispecies coalescent models based on a coalescence

68   process running along the lineages of the species tree (PAGE 1998; LIU AND PEARL 2007; LIU

69   2008; HELED AND DRUMMOND 2010). Subsequently, multispecies coalescent (MSC) model

70   has been updated by adding biological parameters, such as gene flow, rate variation among

71   lineages, recombination and hybridization (KUBATKO 2009; HEY 2010; WANG *et al.* 2014).

72   In other developments, methods have been proposed to ask whether a tree is the best model

73   for a given data set, or whether reticulations in the form of gene flow or lineage merging are

74   more appropriate (see below) (MORET et al. 2004; JACKSON et al. 2017; BURBRINK AND

75   GEHARA 2018). Meanwhile, skeptics of the MSC and advocates for simpler models,

76   particularly concatenation models, have raised critical questions about appropriateness of the

77   MSC and argued that observed gene tree variation is often not caused by ILS, but instead by

78   gene tree estimation errors (SPRINGER AND GATESY 2016; SCORNAVACCA AND GALTIER 2017;

79   RICHARDS et al. 2018). Given the inconsistency of concatenation methods under some

80   regions of tree space in which coalescent methods of tree building are still consistent (LIU et

81   al. 2010), to many researchers it is the convincing evidence to choose coalescent over

82   concatenation methods for species tree inference. However, since the mathematical proofs or

83   simulations for inconsistency of concatenation methods assume that the MSC model is true

84   (KUBATKO AND DEGNAN 2007; ROCH AND STEEL 2015), it is important to show empirical

85   evidence for validating and comparing the concatenation and MSC models. . Resolution of

86   debates over concatenation and coalescent models requires a statistical framework of model

87   comparison and model validation on a variety of empirical and simulated data.

88   *Model fit and model adequacy in phylogenomics*

89   Discussions about the necessity or adequacy of MSC models versus concatenation

90   have taken three principle forms. One form involves questioning the phylogenetic signal in

91   data sets designed for application of the MSC. For example, several authors have suggested

92   that gene tree error (whether deriving from alignment artifacts, low signal, or gene tree

93   estimation error), rather than ILS, is responsible for most if not all observed gene tree

94   variation (GATESY AND SPRINGER 2014; ARCILA et al. 2017). If demonstrable gene tree

95   variation can be ruled out for a given data set, this logic goes, then concatenation is a

96   reasonable fallback model for analysis. This logic reasonably implies that the simpler model

97   inherent in concatenation is favored, especially when gene tree variation can be shown to be

98   low or negligible. The problem with this logic, however, is that gene tree variation is only

99   one motivation for MSC models. The other, more fundamental, motivation for MSC models

100   is the conditional independence of loci in the genome, wherein recombination and random

101   drift render the topologies, but more often the branch lengths of different loci independent of

102   one another, conditional on the species tree, which necessarily influences the shape of all

103   gene trees in the genome (EDWARDS *et al.* 2016). This point leads to the second common

104   argument against MSC models: that violation of MSC model assumptions, such as evidence

105   for recombination within loci or lack of recombination between loci or violations of

106   neutrality, render MSC models poor descriptors of actual data sets, again recommending

107   concatenation or other approaches as more robust alternatives (GATESY AND SPRINGER 2014;

108   SCORNAVACCA AND GALTIER 2017). Again, however, demonstration of violation of a model's

109   assumptions does not necessarily imply that that model is not a reasonable, or even the best

110   available, description of the data. Indeed, we know of no violation of assumptions of an MSC

111   model that is not also a violation of the concatenation model, especially since the

112   concatenation model is best described as a special case of the MSC model, wherein all gene

113   trees are topologically identical (LIU *et al.* 2015).

114   A third approach to deciding whether MSC, concatenation or other models might best

115   apply to a given data set is testing for model fit and model adequacy (BROWN AND THOMSON

116   2018). Only a few papers have explicitly tested the fit and adequacy of the MSC, and,

117   crucially, in doing so, have usually neglected to compare the fit of the major alternative

118   model, concatenation, to that of the MSC. Reid et al. (REID *et al.* 2014) applied posterior

119   predictive simulation (PPS), a Bayesian modeling approach, to a series of moderately sized

120   data sets and concluded that a "poor fit to the multispecies coalescent is widely detectable in

121   empirical data." Although this study was a major advance in our understanding of the MSC

122   as applied to real data sets, we wonder whether the sweeping nature of this conclusion is

123   reasonable and suggest that it may have been overly pessimistic. First, they definitively

124   rejected the fit of the MSC at the level of gene trees for only 4 out of 25 data sets, and only 7

125   total loci (2.9%), hardly suggesting that poor fit at the level of the coalescent is "widespread".

126   Reid et al. (2014) also suggest that a large percentage of partitions or loci in data sets,

127   sometimes as high as 50%, violate the MSC; but the largest data set in their analysis

128   consisted of only 20 loci, with 15 out of 25 data sets consisting of less than 10 loci, thereby

129   possibly exaggerating the extent of violations of the MSC. Many of these rejections were

130   based not on a poor fit of coalescent assumptions but on deviations of the loci from assumed

131   substitution models, which is hardly a direct rejection of the MSC itself. In several cases,

132   Reid et al (REID et al. 2014) were unable to distinguish whether the MSC was a poor fit due

133   to analyses at the level of estimating gene trees and substitution models or at the level of the

134   coalescent model itself. Additionally, their use of a χ^2 test for comparing the observed site

135   patterns with those expected from the assumed substitution models could not accommodate

136   missing data, making this aspect of their model testing problematic and raising the possibility

137   that different substitution models could improve model fit. Moreover, several of the data sets

138   in their analysis can be reasonably thought of as phylogeographic data sets (e.g., Leache

139   (2009) and Walstrom et al. (2012)), in which gene flow is likely or expected, rather than

140   phylogenomic data sets, in which gene flow is less expected or unexpected. Arguably, none

141   of the data sets they analyzed could be called robustly phylogenomic in the modern sense:

142   only 5 of the data sets interrogated relationships above the level of genus and none of them

143   examined relationships among families suborders or orders, where, again, gene flow among

144   lineages is less expected. It is therefore perhaps not surprising that such data sets do not

145   conform well to the MSC. Jackson et al. (2017) recently applied a novel model fitting

146   algorithm, Phrapl, to a series of multilocus phylogeographic data sets, concluding that a pure

147   isolation model, such as the MSC, is rejected in favor of models including gene flow and

148   other reticulate events. Here, again, however, the data sets analyzed are explicitly termed

149   phylogeographic, and, although the MSC was often applied to these data sets in the original

150   papers, it is unsurprising that this model is a poor fit compared to models that include gene

151   flow. Like all models, the MSC has a particular domain of application, one that we suggest is

152   even wider than that in which concatenation is appropriate, but not so wide as to be

153   applicable to data sets that demonstrably include gene flow or hybridization.

154   Most arguments in favor of concatenation, such as those summarized above, assert the

155   superiority of concatenation by noting widespread perceived violations of the MSC or lack of

156   demonstrable gene tree variation, and there have only been a few scattered examples of

157   statistical comparisons of model fit and model adequacy between the MSC and concatenation.

158   To our knowledge, only Liu and Pearl (2007) and Edwards et al. (2007) have explicitly

159   compared the fit of MSC and concatenation models to the same data set, and asked which is a

160   better fit (model comparison) and whether either model can account for the details of the

161   multilocus data (model adequacy). Tests of model fit and model adequacy have been

162   conspicuously absent from discussions about the relative merits of the MSC versus

163   concatenation, although they have begun to appear in discussions of the relative merits of

164   simple and more elaborate MSC models (WEN *et al.* 2016; JACKSON *et al.* 2017). Testing

165   whether the MSC or concatenation can adequately describe multilocus data sets, and which

166   model can describe those data better, will go a long way towards addressing concerns about

167   the MSC and towards delimiting its appropriate domain of application.

168   In this paper, we will address several questions regarding the MSC and its application

169   to empirical data sets: (1) is gene tree variation primarily caused by estimation error? (2) how

170   well do the assumed substitution models fit multilocus sequence data and how does this fit

171   drive the overall fit of the MSC? (3) how well does the multispecies coalescent model,

172   divorced from shortcomings of the substitution model, fit empirical data? and (4) which

173   model fits empirical multilocus data sets better, concatenation or the MSC? Question 1 can be

174   addressed by a likelihood ratio test (LRT), where the null hypothesis is that all loci have the

175   same tree topology (but possibly different branch lengths) versus the alternative hypothesis

176   that allows gene tree variation across loci (testing TC gene trees; Figure 1). We addressed

177   question 2 with the same χ^2 test used by Reid et al. (REID *et al.* 2014), comparing the

178   observed and expected frequencies of site patterns, but this test cannot be applied to

179   sequences with missing characters. We therefore modified this χ^2 test to handle missing

180   characters (goodness of fit of substitution models; Figure 1). To evaluate the effect of

181   substitution models on the fit of the MSC, model validation analysis was conducted with

182   different substitution models for the same data sets. Question 3, the adequacy of the MSC,

183   can be addressed using posterior predictive simulation (PPS) in a Bayesian framework (REID

184   *et al.* 2014) implemented in a Bayesian phylogenetic program BEAST (SUCHARD *et al.* 2018).

185   Unlike previous studies utilizing sequence data simulated under the MSC model to validate

186   coalescent methods (KUBATKO AND DEGNAN 2007), PPS directly evaluates the fit of the MSC

187   model by comparing the posterior gene trees and the gene trees simulated from the MSC

188   (REID *et al.* 2014). However, the posterior gene trees generated with a coalescent prior are

189   biased towards the MSC, especially when the alignments lack phylogenetic signal and

190   Bayesian inference of gene trees is primarily driven by the coalescent prior. Validation

191   analysis should instead compare the simulated gene trees with empirical gene trees estimated

192   from multilocus sequence data without any influence of the MSC (i.e., the posterior gene

193   trees generated independently across loci). Additionally, to reduce the influence of

194   substitution models on the fit of the MSC, we perform the model validation only for loci that

195   fit the substitution model (Bayesian model validation; Figure 1). Question 4, model

196   comparison between the concatenation and MSC models, can again be addressed in a

197   Bayesian framework, using Bayes factors (Bayesian model comparison; Figure 1) or other

198   posterior predictive approaches (LEWIS *et al.* 2014). By addressing these questions, we aim to

199   directly compare competing models, especially as they apply to phylogenomic data sets

200   where concatenation might plausibly be applied.

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202   <div align="center">MATERIALS AND METHODS</div>

203   <div align="center">*Phylogenomic data sets*</div>

204   This study consists of 47 empirical data sets, including 25 data sets from Reid et al

205   (REID *et al.* 2014) and 22 phylogenomic data sets across the tree of life. We chose

206   phylogenomic data sets primarily based on their having been sampled from multiple species,

207   usually more than 10 at the level of family or above, for their coverage of at least 50 loci and

208   for their availability in already aligned nexus or phylip format on an easy accessible open

209   access data base. We also eased our search by focusing primarily although not exclusively on

210   data sets from the journal Molecular Phylogenetics and Evolution. The 22 phylogenomic data

211   sets were downloaded from the data links available in the original papers (Table 1). The

212   genetic markers of 22 phylogenomic data sets are highly diversified, including CDS matrices,

213   exons, and UCEs (Table 1). There are 12 to 207 species in the 22 additional data sets, and the

214   number of loci ranges from 110 to 30,636 (Table 1). Due to computational limits of Bayesian

215   phylogenetic analyses, each of the 22 phylogenomic data sets was reduced to only include the

216   alignments of the 10 most fully populated species across loci, and loci with missing

217   sequences were removed from further analysis. Removing species from alignments will, if

218   anything, increase gene tree similarity across loci as compared with data sets with the full

219   complement of species, and therefore increase the fit of the concatenation model to the data.

220   After data reduction, the data sets contained alignments of 36 (AITKEN *et al.* 2017) to 4709

221   (WU *et al.* 2018) loci, each with 10 species (Table 1).

222   The sequence divergence (i.e., the average pairwise p-distance) of the 22 reduced

223   phylogenomic data sets was significantly higher (p-value < 0.01) than that of 25 Reid et al.

224   data sets (Figure A1), indicating that these new data sets are more classically 'phylogenomic'

225   than those of Reid et al. (2014). Indeed, several of the data sets we analyze are at very high

226   taxonomic levels, such as those of metazoans (WHELAN *et al.* 2015; SIMION *et al.* 2017) or

227   mammals (SCORNAVACCA AND GALTIER 2017; WU *et al.* 2018). Some of these data sets, such

228   as those from metazoans, are at such high taxonomic levels, that MSC models have to our

229   knowledge never been applied, perhaps in the mistaken idea that ILS is extremely unlikely to

230   occur among such deep lineages. However, as pointed out by many authors, even if ILS is

231   harder to detect among deep lineages, it is no less likely to occur among deeply diverging

232   than recently diverging lineages, since it is the length of internodes, rather than their depth in

233   time, that is most relevant to MSC processes.

Goodness of fit of substitution models

235   Let $X = \{x_1, ..., x_k\}$ be the counts of k site patterns in a locus alignment. The random

236   variables $X = \{x_1, ..., x_k\}$ have a multinomial distribution with $\sum_{i=1}^{k} x_i = l$, where l denotes

237   the length of the alignment. Let M be the pre-selected substitution model. When there is no

238   missing data, the χ^2 goodness of fit test can evaluate adequacy of model M by comparing the

239   observed and expected counts of site patterns (REEVES 1992; GOLDMAN 1993; JHWUENG

240   2013). The test statistic is $\chi^2 = \sum_{i=1}^{k} \frac{(x_i - lp_i)^2}{lp_i}$, in which p_i is the probability of site pattern i,

241   which can be estimated under the null hypothesis using the maximum likelihood (ML)

242   estimates of the tree topology, branch lengths, and the parameters in model M.

243   Asymptotically, the test statistic has the χ^2 distribution with (k-1) degrees of freedom. Since

244   this χ^2 test statistic is based on the frequencies of sites for fully populated characters, sites

245   with missing characters (gaps, ambiguous nucleotides, and unidentified regions) are excluded

246   from analysis, even though only a small portion of nucleotides are missing in each site. To

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247   incorporate partially missing sites, a modified χ^2 test was developed to calculate the

248   observed and expected counts of site patterns in the presence of missing data (WADDELL

249   2005). We instead calculate the marginal proportion of a site with missing characters and

250   then compare the marginal proportion of the site with its expectation. For example, there are

251   two missing characters in a site {??AC} of 4 species (S_1, S_2, S_3, S_4), i.e., the nucleotides from

252   species S_1 and S_2 are missing. The marginal proportion y_{AC} of {AC} in the alignment of S_3

253   and S_4 is given by $y_{AC} = x_{AC}/z$, in which x_{AC} is the count of {AC} and z is the number of

254   sites without missing characters in the alignment of S_3 and S_4. Since a small z indicates a

255   large amount of missing data in the alignment, we ignore the sites for which $z/l \leq 0.8$. The

256   test statistic $t = \sum_{j=1}^{n} |y_j - p_j|$, in which y_j is the observed proportion of a site pattern with

257   or without missing characters, and p_j is the probability of the site pattern under the null

258   hypothesis, and n is the number of site patterns for which $z/l > 0.8$. The null distribution of

259   the test statistic is estimated by parametric bootstrap samples generated from the ML

260   estimates of the tree topology, branch lengths, and the parameters in model M.

261   Marginal tests of base compositions between pairs of taxa (TAVARE 1986) have been

262   found to be more powerful than the χ^2 goodness of fit test of the substitution models to

263   phylogenetic data (WADDELL *et al.* 2009). We therefore perform two marginal tests. The first

264   test is to detect heterogeneity of base compositions across species, when the observed base

265   frequencies of individual species deviate significantly from the overall average base

266   frequencies across species. Let $\{x_A, x_C, x_G, x_T\}$ be the observed frequencies of nucleotides A,

267   C, G, and T of a species. The frequency of nucleotide i ($i = A, C, G, T$) is equal to $x_i = N_i/N$,

268   where N_i is the number of nucleotide i and N is the total number of nucleotides excluding

269   missing characters in the sequence. Under the null hypothesis of homogeneous substitution

270   models, all species are expected to have the same base frequencies and thus the expected base

271   frequencies under the null hypothesis are estimated by the overall average frequencies

272 $\{p_A, p_C, p_G, p_T\}$ of A, C, G, and T across species. The χ^2 test of the observed frequencies

273 $\{x_A, x_C, x_G, x_T\}$ against the expected frequencies $\{p_A, p_C, p_G, p_T\}$ is carried out for each

274 species to detect those species whose base frequencies significantly deviate from the null

275 hypothesis that all species have the same base frequencies. Similarly, the second marginal

276 test is applied to the frequencies of double-nucleotides (doublets) between pairs of species to

277 find pairs of species for which doublet frequencies are inconsistent with the pre-selected

278 substitution model. The frequency of doublet ij $(i = A, C, G, T \ and \ j = A, C, G, T)$ is equal to

279 $x_{ij} = N_{ij}/N$, where N_{ij} is the number of doublet ij and N is the total number of doublets

280 excluding those with missing characters.

281 The bootstrap and two marginal tests were conducted to evaluate goodness of fit of

282 the GTRGAMMA model to 47 empirical data sets (Figure 1). We chose the GTRGAMMA

283 model because the most parameter-rich model (GTRGAMMA in RAxML) is sufficient for

284 reliable phylogenetic inference (Abadi et al. 2019) and a more complex model tends to be a

285 better fit to phylogenomic data (LIU *et al.* 2017). For each locus, the ML estimates of the

286 phylogenetic tree and other parameters were obtained by RAxML v8.2.3 (STAMATAKIS 2014)

287 using the GTRGAMMA model. Then, 100,000 base pairs of sequence were simulated from

288 the estimated phylogenetic tree using Seq-Gen v1.3.2x (RAMBAUT AND GRASSLY 1997). The

289 expected frequencies of site patterns were estimated by the corresponding frequencies in the

290 simulated sequences. In addition, 100 bootstrap samples were generated by simulating DNA

291 sequences from the concatenation tree for each locus. If taxa were missing from the loci,

292 they were pruned from the concatenation tree and DNA sequences were simulated from the

293 pruned concatenation tree. The test statistic was calculated for each bootstrap sample, and the

294 observed test statistic t* was compared with the bootstrap test statistics $\{t_1, \dots, t_{100}\}$ and p-

295 value = (# of $t_i > t^*$) / 100. For the marginal test of base frequencies, the sequence of a

296 species was considered significant if its p-value was less than 0.05 divided by the number of

297 species. A locus was significant if it had at least one significant species. Similarly, for the test

298 of doublet frequencies between pairs of species, a pair of species was significant if its p-value

299 was less than 0.05 divided by the number of pairs. A locus was significant if it has at least

300 one significant pair. The bootstrap and two marginal tests were applied to each locus of the

301 47 data sets. A locus waas significant if any of above three tests was significant for the locus.

302 *Testing for topologically congruent gene trees*

303 We ask the question whether a single gene tree topology can adequately explain a

304 given multilocus data set, using a variant of the LRT. Similar types of LRTs were developed

305 to test if alternative trees are congruent with the maximum likelihood (ML) tree for a single

306 locus (SHIMODAIRA AND HASEGAWA 1999; SHIMODAIRA 2002). McVay and Carstens (2013)

307 proposed a parametric bootstrap approach to assess the extent to which gene tree variation

308 can be attributed to phylogenetic estimation error. Here, we develop a LRT to evaluate the

309 concatenation assumption of congruent gene trees for multiple loci. Let $D = (D_1, D_2, ..., D_K)$

310 be the concatenated alignments of a multilocus sequences data set, in which D_i represents the

311 alignments of locus i and K is the count of loci. The tree topology of locus i is denoted by τ_i.

312 Under the concatenation model, all loci are assumed to have the same tree topology, i..e,

313 $\tau_1 = \cdots = \tau_K$. We develop an LRT to evaluate the null hypothesis that all gene trees have the

314 same topology, i.e., $\tau_1 = \cdots = \tau_K$ versus the alternative hypothesis that not all gene trees are

315 topologically identical. The test statistic is defined as $t = \log(l_1) - \log(l_0)$, in which l_0 and

316 l_1 are the likelihoods of the null and alternative hypotheses. Under the null hypothesis, the

317 ML tree is built from the concatenated alignments across loci using RAxML v8.2.3

318 (STAMATAKIS 2014) with the GTRGAMMA model (TAVARE 1986; YANG 1994). Using the

319 ML tree instead of the true concatenation tree for the null hypothesis may lead to a biased test.

320 However, since the concatenated sequences of phylogenomic data consist of millions of base

321 pairs, the ML tree is very similar, if not identical, to the true concatenation tree. hus, the bias

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322   induced by the topologcial difference between the ML and true concatenation tree is

323   negaligible for phylogenomic data. Let w_i be the log-likelihood of locus i by refitting branch

324   lengths and substitution model parameters to the concatenation tree with missing taxa being

325   removed. The log-likelihood under the null hypothesis is equal to the sum of the log-

326   likelihoods of individual loci, i.e., $\log(l_0) = \sum_{i=1}^{K} w_i$. Refitting branch lengths and model

327   parameters on a fixed tree topology was performed in RAxML using the command line

328   "*raxml-HPC-AVX –s datafile –m GTRGAMMA –n outputfile –f e –t fixtree*". To find the log-

329   likelihood of the alternative hypothesis, maximum likelihood trees were independently built

330   for individual loci using RAxML. Since model parameters include tree topologies, the χ^2

331   distribution is not a good approximation to the null distribution of the test statistic (JHWUENG

332   *et al.* 2014). Therefore, the null distribution of the test statistic was approximated by a

333   parametric bootstrap. Bootstrap samples were generated under the null hypothesis by

334   simulating DNA sequences from the concatenation tree pruned for available species at each

335   locus. Since the original alignments include missing characters (gaps, ambiguous nucleotides,

336   and unidentified regions), bootstrap samples should involve a similar pattern of missing

337   characters. Thus, corresponding nucleotides in bootstrap samples were replaced by missing

338   characters. Let t_i be the value of the test statistic t for the bootstrap sample $i = 1, …, B$. The

339   loglikelihoods of the null and alternative hypothesis in the test statistic t were generated using

340   RAxML. The values $\{t_i, i = 1, …, B\}$ of the test statistic for B bootstrap samples were used to

341   approximate the null distribution of the test statistic t. The p-value was estimated by the

342   proportion of $\{t_i, i = 1, …, B\}$ that were greater than or equal to the test statistic t calculated

343   from real data. Rejection of the null hypothesis indicates that some gene trees are incongruent

344   with the concatenation tree. Then, the LRT was further applied to each locus to identify

345   alignments that reject the null (concatenation) tree. Let τ be the concatenation tree and τ_i is

346   the gene tree i. The null and alternative hypotheses are $H_0: \tau_i = \tau$ and $H_1: \tau_i \neq \tau$. The test

347   statistic is $t = \log(l_1) - \log(l_0)$, in which $\log(l_0)$ and $\log(l_1)$ are the log-likelihoods of

348   locus i under the null and alternative hypotheses. The null distribution of the test statistic was

349   approximated by the bootstrap samples generated under the null hypothesis and the p-value

350   was equal to the proportion of bootstrap test statistics that are greater than or equal to the

351   observed test statistic. A locus was significant if its p-value was less than or equal to 0.05

352   divided by the number of loci (Bonferroni correction for multiple comparisons).

353   *Bayesian validation of the multispecies coalescent model*

354   Like Reid et al. (2014), the Bayesian MSC model is here validated by Bayesian

355   predictive simulation. Reid et al. recommended comparing the posterior coalescent gene

356   trees to the gene trees simulated from the posterior species trees. However, the posterior

357   coalescent gene trees have been influenced by the multispecies coalescent prior, which is

358   implemented in packages such as BEST (LIU 2008) or *BEAST (HELED AND DRUMMOND

359   2010). The posterior gene trees with an MSC prior are biased towards the MSC model to

360   some extent, compared to gene trees generated without an MSC prior, making this test

361   conservative (i.e., in favor of the MSC). Thus, here, simulated gene trees are compared to

362   posterior gene trees generated without the MSC prior. We validate the MSC model using two

363   tests. The first test, as in Reid et al. (2014), involves two comparisons - comparing the

364   multispecies coalescent likelihoods of the simulated and posterior coalescent gene trees and

365   comparing the number of deep coalescences of the simulated and posterior coalescent gene

366   trees. The first test is rejected if either or both of two comparisons reject the MSC model. In

367   the second test, not used by Reid et al. (2014), the posterior gene trees are first estimated

368   independently across loci in BEAST by unlinking the substitution models, clock models, and

369   trees. If the 99.9% posterior credible regions of the log-likelihoods of the independent model

370   and the MSC model are not overlapped, we conclude that there is a significant difference

371   between the posterior independent and coalescent gene trees. We infer a poor fit of the MSC

372   model to the data if either or both of the two tests are rejected. Both tests can also be applied

373   to each locus in the data to identify gene trees that significantly deviate from the MSC model.

374   To alleviate the impact of poorly fitting substitution models on the fit of the MSC, the

375   model validation and comparison analyses were only performed on the loci that fit the

376   assumed substitution model (GTRGAMMA). Since the number of loci in 25 Reid et al. data

377   sets is insufficient for filtering out the unfit loci, selection of loci that fit the substitution

378   model was only performed on 22 reduced phylogenomic data sets. After locus selection, 9 of

379   22 data sets had ≤ 3 loci that fit the substitution model and thus they were removed from

380   further analysis. We then randomly selected 50 loci from the remaining 14 phylogenomic

381   data sets, resulting in a total of 39 data sets (25 Reid et al. data sets + 14 phylogenomic data

382   sets with 50 loci) for the model validation analysis (Figure 1). The xml input files of the 25

383   data sets from Reid et al. were available in the data package provided by the authors. Reid et

384   al. (2014)'s *BEAST analyses of those data sets assumed HKY and TN93 (+GAMMA)

385   substitution models for individual loci and a multispecies coalescent prior for gene trees. To

386   evaluate the effect of substitution models on the fit of the MSC model, Bayesian model

387   validation of 25 Reid et al. data sets was reconducted with the GTRGAMMA model. For 14

388   phylogenomic data sets, to reduce the effect of substitution models on the overall fit of the

389   MSC, the validation analysis was conducted only for loci for which the GTRGAMMA model

390   was a good fit. Consequently, rejections of the MSC imply a poor fit of coalescent

391   assumptions rather than a poor fit of the assumed substitution model. The xml input files of

392   14 data sets were generated using BEAUti v1.8.4, assuming the GTRGAMMA substitution

393   model for all loci.

394   Two independent runs were carried out for each analysis and convergence was

395   checked by comparing the outputs from two runs. The first 50% of MCMC samples were

396   discarded as burn-in. Then, 1000 samples were selected from the remaining MCMC samples

397   and used as input for Bayesian model validation. The first test of Bayesian model validation

398   was conducted using the R package starbeastPPS (2014). To perform the second test, 39

399   input data sets were re-analyzed by unlinking the substitution models, clock models, and trees

400   across loci in BEAST, which produced posterior gene trees independently across loci without

401   the MSC prior. The 99.9% credible region of the difference between the log-likelihoods of

402   the independent and coalescent models was calculated in R. The two tests were also applied

403   to each locus to identify gene trees that significantly deviate from the MSC model.

404   To evaluate the effect of loci rejecting the MSC on species tree estimation, species trees

405   were built from all loci and only loci that did not reject the MSC for each of the 14

406   phylogenomic data sets using NJst (LIU AND YU 2011) implemented in an R package Phybase

407   (LIU AND YU 2010). This analysis was not performed for 25 Reid et al. data sets due to their

408   small numbers of loci for species tree estimation. We calculated the Robinson-Foulds (RF)

409   distance (ROBINSON AND FOULDS 1981) of two species trees reconstructed for each data set

410   using the function dist.topo in an R package APE (PARADIS AND SCHLIEP 2019). For the

411   species trees with a positive distance, to evaluate statistical significance of the difference

412   between two species trees, bootstrap support values of the incongruent branches were

413   calculated using bootstrap gene trees estimated from alignments. Specifically, bootstrap gene

414   trees were built for each locus and then used as input data to calculate bootstrap NJst trees.

415   The bootstrap support value of a branch was equal to the count of bootstrap NJst trees

416   supporting the clade indicated by the branch. Romiguier et al. (2013) suggested that high GC

417   content may cause problems for phylogenetic inference under the MSC model, and that

418   selecting AT-rich loci can improve the resolution of estimated phylogenies. To investigate

419   the association between GC content and poor fit of the MSC, we calculated GC content for

420   loci rejecting and accepting the MSC, respectively. A two-sample t-test was used to find

17

421   significant difference in GC content between loci rejecting the MSC and those accepting the

422   MSC.

Bayesian model comparison for MSC versus concatenation

424   Bayesian model comparison for concatenation versus the MSC was evaluated using

425   Bayes factors (BF) (KASS AND RAFTERY 1995), the ratio of marginal likelihoods $BF =$

426    $P(D|M_1)/P(D|M_2)$, in which D denotes data and M_1 and M_2 are two competing models.

427   Here, M_1 is the MSC model and M_2 is the concatenation model. The Bayesian concatenation

428   analyses assumed a partition model by unlinking substitution models and clock models across

429   loci. The marginal log-likelihoods of the Bayesian multispecies coalescent and concatenation

430   models were estimated using path sampling / stepping-stone sampling with 100 path steps

431   implemented in BEAST. A value of log(BF) > 10 indicates that the Bayesian multispecies

432   coalescent model M_1 is strongly favored by the data versus the Bayesian concatenation model

433   M_2.). The model comparison analysis was applied to the (39) data sets used in the Bayesian

434   model validation analysis. Since the model comparison analysis implemented in BEAST does

435   not allow missing taxa in any locus, 8 data sets with missing data were removed, further

436   reducing the number of input data for the model comparison analysis to 31 (Figure 1).

437   To demonstrate that model assumptions may influence species tree inference, we

438   reconstructed species trees for 5 phylogenomic data sets using concatenation and a coalescent

439   method (NJst). In addition, we subsampled 25%, 50%, and 75% of loci from the original

440   phylogenomic data, and compared the species trees built from the subsamples with those for

441   the full phylogenomic data. The concatenation trees were estimated by RAxML with the

442   GTRCAT model. The NJst trees were built using the function sptree.njst() in an R package

443   Phybase. We calculated the bootstrap support values for each estimated species tree. Two

444   estimated species trees are said to be significantly incongruent if two trees have a conflict

445   branch with a bootstrap support value > 70. The subsampling analysis was repeated 10 times

446   and we reported the proportion of subsamples (out of 10) for which the estimated species tree

447   was significantly incongruent with the species tree built from the full phylogenomic data.

448

449   RESULTS

450   *Goodness of fit of substitution models*

451   There was a total of 20,032 loci (CDS, UCEs or exons) throughout the 47 empirical

452   data sets; 241 loci from the 25 Reid et al. data sets and 19,791 loci from the 22 phylogenomic

453   data sets. The marginal test of base frequencies identified a total of 1,362 (7%)

454   loci/alignments (or 9% loci per data set in Figure 2a) for which at least one sequence

455   significantly deviates from the average base frequencies expected from the GTRGAMMA

456   model. The doublet test indicated that 6,990 (35%) loci/alignments (or 51% loci per data set

457   in Figure 2a) have at least a pair of species whose doublet patterns are significantly different

458   from the patterns expected from the GTRGAMMA model. The marginal test favors complex

459   substitution models, because a complex model has a higher likelihood than a simple model,

460   indicating that the expected frequencies under the complex model are more consistent with

461   the observed frequencies of site patterns in the alignments. Thus, rejection of the

462   GTRGAMMA model suggests that a more complex substitution model should be fit to the

463   data. In the bootstrap test for site patterns, the GTRGAMMA model fails to fit the alignments

464   of 5,718 (24%) loci across the 47 data sets (or 34% of loci per data set in Figure 2a). The

465   doublet test appears to be more likely than the bootstrap test for site patterns to reject the

466   GTRGAMMA model (Figure 2a), indicating the necessity of marginal tests for goodness of

467   fit of substitution models. Because the doublet test is more likely to reject the GTRGAMMA

468   model than the other two tests, the intersection test (the intersection of three tests, i.e., at least

469   one of two marginal tests and the bootstrap test reject the GTRGAMMA model) appears to

470   be primarily driven by the doublet test (Figure 2a). Overall, nearly half of the alignments

471   (8,775 loci or 44%) were found significant (p-value < 0.05) in the intersection test, and the

472   proportion of significant loci identified by the intersection test ranges from 6% to 100%

473   across the 47 data sets (Figure 2a). A two-sample t-test finds no significant difference in the

474   proportion of loci rejecting the GTRGAMMA model between the 25 Reid et al. data sets and

475   the 22 phylogenomic data sets (Figure 2b).

476   To understand the causes of poor substitution model fit, we investigated the

477   relationship between GC content (and proportion of informative sites) and the rejection of the

478   GTRGAMMA model. A two-sample t-test suggests that the proportions of GC content and

479   informative sites of loci rejecting the GTRGAMMA model are significantly higher (p-value

480   < 0.05) than those for loci that fit the GTRGAMMA model (Figure 2c-d). We fitted a logistic

481   regression for all loci across the 47 data sets, where non-significance (0) or significance (1)

482   of a locus in the intersection test is the binary response variable, and the proportions of GC

483   content and informative sites are two explanatory variables. In the fitted logistic regression,

484   the coefficients of two explanatory variables are significantly negative with p-value < 0.01.

485   We further fit a logistic regression to each of the 47 data sets. The coefficient of GC content

486   is negative/positive for 29/18 data sets, among which 6/1 negative/positive coefficients are

487   significant at the α level of 5% (Figure 2e). Similarly, the coefficient for the number of

488   informative sites is negative/positive for 33/14 data sets, among which 14/0 negative/positive

489   coefficients are significant (Figure 2e). The preponderance of significantly negative

490   coefficients indicates that GC content and the number informative sites are both negatively

491   correlated with the probability of a locus rejecting the GTRGAMMA model, i.e., a higher GC

492   content and/or proportion of informative sites tends to increase the chance of a poor fit of the

493   GTRGAMMA substitution model.

494   *Testing topologically congruent gene trees*

495   The LRT for TC gene trees rejected the null hypothesis of tree congruence for all 47

496   empirical data sets with p-value < 0.05. Thus, all empirical data sets in this study strongly

497   favor the alternative hypothesis of incongruent gene trees, a pattern that cannot be adequately

498   explained by gene tree estimation errors. The p-values of the data sets with 10 or more loci

499   are very close to 0, indicating that the assumption of TC gene trees is rarely satisfied for

500   phylogenomic data, which often involve thousands of loci.

501   A two-sample t-test finds no significant difference (p-value $= 0.10$) in the proportion

502   of loci rejecting the null hypothesis of TC gene trees between the 22 phylogenomic data sets

503   and the 25 Reid et al. data sets (Figure 3a). The topological congruence LRT on individual

504   loci suggests that 38% of gene trees across 47 data sets are statistically incongruent with the

505   concatenation tree (Figure 3b). When the 47 data sets are grouped into 6 categories –

506   mammals (11), birds (11), insects (6), fish (5), reptiles (5), and others (9), an ANOVA

507   analysis finds no significant difference in the proportion of loci rejecting the hypothesis of

508   TC gene trees among 6 groups (Figure 3c). Both the two-sample t-test and ANOVA indicate

509   that the proportion of loci rejecting the hypothesis of gene tree congruence is similar across

510   groups and data sets. A linear regression line was fit for the log scale of the number of

511   incongruent loci rejecting the hypothesis of TC gene trees (y) versus the log scale of the

512   number of loci (x), i.e., $\log(y) = 0.87 \times \log(x) - 0.08$ with a significant (p-value < 0.01)

513   positive correlation between $\log(x)$ and $\log(y)$ (Figure 3d). This result is consistent with the

514   previous conclusion that phylogenomic data sets with more loci are more likely to reject the

515   assumption of TC gene trees; namely, the observed gene tree variation cannot be adequately

516   explained by gene tree estimation error. Moreover, both ANOVA and linear regression

517   analyses suggest a constant and high proportion (38%) of loci rejecting the assumption of TC

518   gene trees across 47 data sets, providing strong evidence for violation of the concatenation

519   assumption of congruent gene trees in phylogenomic data across the tree of life. When the 22

520 phylogenomic data sets are grouped by data types – CDS (10), EXON (4), UCE (8), the t-

521 tests for pairwise comparisons find no significant difference (p-value = 0.1) for the

522 proportion of loci rejecting the assumption of TC gene trees between the CDS and Exon

523 groups, but the proportions of both groups are significantly (p-value < 0.01) higher than that

524 of the UCE group (Figure 2e). This result indicates that the congruent gene tree assumption

525 of the concatenation model is more likely to hold for the UCE data than for the CDS and

526 Exon data.

527   To reduce the potential bias caused by an unfit substitution model, the LRT was only

528 applied to the loci that fit the GTRGAMMA model. We filtered out 27 data sets with < 5 loci

529 that fit the GTRGAMMA model and applied the LRT to the remaining 20 data sets. The null

530 hypothesis of tree congruence was rejected for all 20 data sets with p-value < 0.05. The LRT

531 on individual loci suggests that 46% of gene trees across 20 data sets are statistically

532 incongruent with the concatenation tree, which is lower (but not significantly) than the

533 proportion (48%) when the LRT was applied to all loci of the 20 data sets (Figure A2).

534   *Bayesian model validation*

535   The coalescent methods have been widely used for estimating species trees from

536 phylogenomic data. Due to computational constraints, however, few studies have evaluated

537 the fit of the MSC to the multilocus sequences. Here, we validate the MSC model using two

538 tests based on Bayesian predictive simulation. The first test (i.e., PPS proposed by Reid et al.

539 (2014)) compares the simulated gene trees with the posterior coalescent gene trees generated

540 with the MSC prior, whereas the second test (i.e., the independent test) compares the

541 posterior coalescent gene trees with the posterior independent gene trees generated with the

542 independent prior. The analysis of 25 Reid et al. data sets found that 8 (32%) data sets failed

543 either or both of two tests (Figure 4a), among which 3 data sets were also found to poorly fit

544 to the MSC by Reid et al (2014; *Certhiidae, Tamias, Aliatypus*). However, the xml input

545 files provided by Reid et al (2014) assumed the HKY and TN93 (+GAMMA) substitution

546 models for all loci. When the *BEAST analyses were rerun with the GTRGAMMA model,

547 only two data sets provided were rejected by either or both of two tests (Table 2). Thus, the

548 choice of substitution models has major effects on the fit of the MSC. In addition, Bayesian

549 model validation for the 14 phylogenomic data sets for which the GTRGAMMA model was a

550 good fit found that 12 data sets failed the first test and all 14 data sets failed the second test.

551 Thus, the MSC model failed to fit all 14 phylogenomic data sets (Figure 4a). Since these 14

552 data sets have more loci than the Reid et al. data sets, it implies that phylogenomic data with

553 more loci are more likely to reject the MSC. In addition, Bayesian model validation for

554 individual loci of the 14 phylogenomic data sets found that 10.88% of loci rejected the MSC

555 (Figure 4b), significantly higher (p-value < 0.01) than the proportion (4.17%) for the 25 Reid

556 et al. data sets, indicating that the probability of a locus rejecting the MSC increases as the

557 number of loci grows.

558 To evaluate the effect of loci rejecting the MSC on species tree estimation, two

559 species trees were reconstructed from all loci and only loci that fit to the MSC for each of 14

560 phylogenomic data sets. A majority (9) of 14 data sets produced two identical species trees

561 (i.e., RF = 0), whereas RF = 2 for 4 data sets (Ant, Cracid, Mammal2017, Squirrel) and RF =

562 4 for 1 data set (Figure 4c). Note that RF = 2 or 4 indicates only 1 or 2 conflicting branches in

563 two species trees. Since the incongruent branches are not strongly supported (bootstrap

564 support values < 60), the conflict between two different species trees is not significant. This

565 analysis suggests that including loci that fail to fit the MSC has little impact on species tree

566 estimation, when a small portion (10.88%) of loci rejects the MSC.

567 To investigate the association between GC content and poor fit of the MSC, we

568 calculated the average GC content of loci rejecting or accepting the MSC for two

569 phylogenomic data sets for which the number of loci rejecting the MSC is large (Birds and

23

570   mammal2017, in which the number of loci rejecting the MSC is 10 and 17, respectively;

571   Figure 4d). Other phylogenomic data sets contain insufficient number of loci rejecting the

572   MSC for the analysis. A two-sample t-test for the overall average GC content (combining two

573   data sets) and the average GC content of each of two data sets unanimously found that the

574   difference in GC content between loci rejecting the MSC and loci accepting the MSC was not

575   significant (Figure 4d), showing little evidence for a positive association between high GC

576   content and poor fit of the MSC.

577   *Bayesian model comparison for MSC versus concatenation*

578   Bayesian model comparison was applied to 31 data sets for which there was no

579   missing data, including 17 Reid et al. data sets and 14 phylogenomic data sets. The BFs (on

580   logarithmic scale) of 22 data sets are greater than 100 and the BFs of the remaining 9 data

581   sets are between 10 and 100. Overall, the high BFs imply that all 31 data sets strongly favor

582   the MSC rather than the concatenation model (Figure 5). This Bayesian model comparison

583   analysis is consistent with the LRT results for congruent gene trees, which reject the

584   concatenation assumption of congruent gene trees and thus favor the MSC for all 47 data sets.

585   To demonstrate the impact of model assumptions on species tree inference, species

586   trees were estimated for 4 phylogenomic data sets (Cracids 23 species and 430 loci,

587   Gallophesants 18 species and 1479 loci, Lizard 29 species and 1852 loci, Shrews 19 species

588   and 1112 loci, Table 1) using concatenation and a coalescent method NJst. We found 3 data

589   sets (Cracids, Gallophesants, Lizard) for which the concatenation trees were significantly

590   incongruent with the corresponding NJst trees (Figure A3), indicating that different models

591   may yield conflict species trees. In the subsampling analysis, the average proportion of

592   significantly incongruent concatenation trees across 4 data sets is 0.19, much higher than the

593   average proportion (0.008) of significantly incongruent NJst trees (Figure A4), suggesting

594 that concatenation is more likely than coalescent methods in producing wrong relationships

595 with high bootstrap support values.

<div align="center">DISCUSSION AND CONCLUSIONS</div>

597   Model validation and comparison are essential to accurate phylogenetic inference for

598 genome-scale sequence data. Many recent disputes about the utility of the MSC model in

599 phylogenomics have rested on perceived model violations of the MSC, rather than direct tests

600 of the explanatory power of the MSC versus concatenation. Here we developed and

601 implemented a set of statistical tests to evaluate the adequacy of substitution models, the

602 concatenation model, and the MSC model. In particular, we tried to distinguish two possible

603 sources of rejection of the MSC in empirical data sets: rejection due to violation of the

604 substitution model and rejection due to violation of the MSC. The LRT results for congruent

605 gene trees reveals strong evidence in 47 data sets against the concatenation assumption of

606 congruent gene trees across loci. Crucially, this test suggests that the gene tree variation is

607 real and cannot be explained simply by gene tree estimation error, a point of increasing

608 concern among skeptics of the MSC model (RICHARDS *et al.* 2018). This result is consistent

609 with the subsequent Bayesian model comparison analysis, which unanimously favored the

610 MSC over concatenation for all phylogenomic data sets under consideration. Moreover, the

611 proportion of gene trees significantly deviating from the concatenation tree (38%) is

612 consistently high across taxonomic groups (bird, fish, mammal, insect, reptile, and others),

613 and our linear regressions suggest that the concatenation assumption of congruent gene trees

614 is more seriously violated as the number of loci continues to grow in phylogenomic data

615 across the tree of life (BRAVO *et al.* 2019).

616   The fact that Bayesian model comparison strongly favors the coalescent over

617 concatenation does not necessarily validate the use of the MSC model for analyzing

618 phylogenomic data. In our Bayesian model validation, the MSC model is a good fit for the

<div align="center">25</div>

619   majority data sets in Reid et al. (REID *et al.* 2014), but the choice of substitution models has a

620   strong influence on the fit of the MSC model. To alleviate the effect of substitution models,

621   we applied Bayesian model validation to the loci of 14 phylogenomic data sets that fit the

622   assumed substitution model. The MSC failed to fit all 14 phylogenomic data sets, but the

623   proportion of loci rejecting the MSC was only 11%, significantly smaller than those for

624   substitution models (44%) and concatenation models (38%). Thus, deficiencies in the fit of

625   data to substitution models and to concatenation models appear to be much more severe than

626   fit to the MSC model, suggesting that more attention should be given to appropriately

627   modeling the evolution of single nucleotides (i.e., substitution models) and gene tree

628   variation, though continuous efforts for improving models at the level of both sequences and

629   gene trees are ultimately desirable.

630   An empirical study of placental mammals (ROMIGUIER *et al.* 2013) suggested that

631   GC-rich regions are associated with high recombination rates which may be problematic for

632   species tree inference under the MSC model. Our analysis, however, finds no convincing

633   evidence for the positive association between high GC content and poor fit of the MSC.

634   Instead, we find that high GC content is strongly associated with poor fit of substitution

635   models. Thus, the shifting phylogenetic relationships of placental mammals for GC-rich

636   regions found by Romiguier et al. (2013) may be caused not by poor fit of the MSC, but the

637   conflicts among gene trees due to poorly fitted substitution models.

638   Stochastic models for phylogenomic data should consider the cumulative effect of the

639   mutation process of nucleotides (molecular evolution) and biological processes rooted in

640   population genetics that have played important roles in the evolution of species. Some have

641   argued (Edwards 2009; Liu et al. 2015) that, among the relevant biological processes, the

642   coalescence process, which assumes random drift, should serve as the null model, and other

643   biological factors, such as gene flow and hybridization, can be added to the null model if the

644   null model cannot adequately explain the observed gene tree variation. As the number of loci

645   continues to increase, some loci are bound to reject the MSC model. Brown and Thomson

646   (2017) suggests that a small number of extremely influential loci can significantly change the

647   estimates of phylogenetic trees. Our analysis indicates that if the loci rejecting the MSC (or

648   concatenation) only account for a small proportion of the empirical data (e.g. 11% in this

649   study), the MSC model (or concatenation) can still be applied to entire data sets or to data

650   sets purged of the loci that violate the MSC. On the other hand, a large number of loci

651   rejecting the MSC (or concatenation) suggests that additional biological phenomena may

652   have occurred and must be added to the stochastic model when analyzing such data sets.

653   Mathematical models are variably robust to assumption violations. Several authors

654   have identified numerous putative biological violations of the MSC in empirical data sets,

655   including recombination within loci, pseudo-concatenation of loci such as occurs in

656   transcriptome data as well as natural selection (GATESY AND SPRINGER 2014; SCORNAVACCA

657   AND GALTIER 2017). However, even in these data sets, despite numerous putative violations

658   of the MSC, the MSC is a better fit than concatenation, suggesting that violations of the MSC

659   may not recommend falling back on concatenation as an alternative method of analysis (LIU

660   *et al.* 2015; EDWARDS *et al.* 2016). The analysis of empirical data in this study suggests that,

661   although 11% of loci reject the MSC, there is no significant difference between the species

662   trees estimated from all loci and only loci that fit the MSC model. Thus, gene-tree-based

663   coalescent methods are robust to a certain degree of violation of coalescent assumptions. In

664   this study, model validation and species tree analyses were conducted on reduced

665   phylogenomic data sets of 50 loci and 10 species each. Our analyses suggest that the

666   concatenation assumption of congruent gene trees rarely holds for phylogenomic data with

667   more than 10 loci. Thus, for large phylogenomic data sets, model comparison analyses are

668   expected to consistently and more strongly favor the coalescent model over the concatenation

669   model. As the number of loci increases, model validation analysis is more likely to reject the

670   MSC. Adding species above the level of genus in phylogenomic data, however, will

671   introduce additional gene tree variation caused by gene flow, gene duplication/loss, etc. Thus,

672   unlike increasing numbers of loci, growth in the number of taxa in phylogenomic data is

673   likely to increase the proportion of loci rejecting the MSC. When the majority of loci do not

674   support the MSC, the coalescent methods will eventually fail to accurately reconstruct

675   species trees from the full phylogenomic data, even though model comparison is still in favor

676   of the MSC over the concatenation model. In such cases, MSC network models, in which

677   gene flow and lineage merging are incorporated, may better fit phylogenomic data sets than

678   the standard MSC model (WEN *et al.* 2016; BASTIDE *et al.* 2018).

679   SUPPLEMENTARY MATERIAL

680   The alignments of the input data sets for the substitution model, TC gene trees, model

681   validation, and model comparison analyses are available from the Dryad Digital Repository:

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906 TABLE 1: Summary of 22 phylogenomic data sets analyzed here. In the columns OTUs and

907 Loci, the bottom number is the count of taxa (or loci) in the original data set; the top number

908 is the count of taxa (or loci) after data reduction.

Data set	OTUs	Loci	Markers
Ant (BLAIMER *et al.* 2018b)	10/153	1509/1763	UCE
Bee (SANN *et al.* 2018)	10/95	193/195	CDS
Bird (PRUM *et al.* 2015)	10/198	259/259	CDS
Lizard (BLOM *et al.* 2017)	10/29	1831/1852	Exon
Brittlestar (O'HARA *et al.* 2019)	10/46	407/416	CDS
Butterfly (ESPELAND *et al.* 2018)	10/207	325/352	Exon
CarpenterBee (BLAIMER *et al.* 2018a)	10/179	597/753	UCE
Cichlid (MCGEE *et al.* 2016)	10/50	924/1043	UCE
Clupeocephalan (STRAUBE *et al.* 2018)	10/52	48/829	Exon
Cracids (HOSNER *et al.* 2016)	10/23	430/430	UCE
Darter (MACGUIGAN AND NEAR 2018)	10/112	363/30636	Exon
Diplostomoidea (LOCKE *et al.* 2018)	10/12	324/517	UCE
Gallopheasant (MEIKLEJOHN *et al.* 2016)	10/18	1479/1479	UCE
Hemimastigophora (LAX *et al.* 2018)	10/61	239/351	CDS
Lepanthe (BOGARÍN *et al.* 2018)	10/33	334/433	CDS
Mammal2018 (WU *et al.* 2018)	10/90	4709/5162	CDS
Mammal2017 (SCORNAVACCA AND GALTIER 2017)	10/97	108/110	CDS
Metazoan2015 (WHELAN *et al.* 2015)	10/76	36/115	CDS
Shrew (GIARLA AND ESSELSTYN 2015)	10/19	966/1112	UCE
Squirrel (COOK *et al.* 2018)	10/74	3209/3951	UCE
Weevil (AITKEN *et al.* 2017)	10/67	318/521	CDS
Fish (CUI *et al.* 2013)	10/27	1183/1183	CDS

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910   TABLE 2: Bayesian model validation for the 25 data sets in Reid et al. (2014). The validation

911   analysis involves two tests - starbeastPPS and the independent test. Significance symbols

912   *<0.05, **<0.025, ***<0.01, ****<0.001, and ns denotes nonsignificant. The last column

913   GTRGAMMA indicates that the Bayesian model validation analyses assuming HKY and

914   TN93 + GAMMA were reconducted with the GTRGAMMA model.

Data set	starbeastPPS	Independent test	GTRGAMMA	
			starbeastPPS	Independent test
Aliatypus	***	***	ns	ns
Certhiidae	**	***	****	***
Cheirogaleidae	ns	***	ns	ns
Liolaemus	ns	***	ns	ns
Malurus	ns	***	ns	ns
Sceloporus	ns	***	ns	ns
Sitta	ns	***	ns	ns
Tamias	****	ns	****	ns

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925 **Figure legends**

926

927 Figure 1: The flowchart of phylogenetic analyses in this study. The alignments of 47 data sets

928 were used to test the hypothesis of topologically congruent (TC) gene trees and goodness of

929 fit of substitution models. The model validation and comparison analyses were only

930 performed for the loci that fit the GTRGAMMA model, reducing the number of input data

931 for model validation to 39 (25 Reid et al. data sets and 14 phylogenomic data sets). Because

932 the model comparison analysis implemented in BEAST does not allow missing taxa in any

933 locus, 8 Reid et al. data sets were removed, further reducing the number of input data for the

934 model comparison analysis to 31 (17 Reid et al. data sets and 14 phylogenomic data sets).

935

936 Figure 2: Goodness of fit of substitution models for 47 data sets. a) The violin boxplot of the

937 proportion of loci rejecting the GTRGAMMA model in 47 data sets by the base frequency

938 test, doublet test, bootstrap test, and the intersection of three tests (i.e., the intersection test),

939 respectively. b) The violin boxplot of the proportion of loci rejecting the GTRGAMMA

940 model for the 25 Reid et al. data sets and the 22 phylogenomic data sets. A two-sample t-test

941 shows no significant difference between two sets of data with p-value = 0.96. c) Boxplots of

942 GC content of loci rejecting or accepting the GTRGAMMA model. d) Boxplots of

943 informative sites of loci rejecting or accepting the GTRGAMMA model. e) Logistic

944 regression of whether a locus rejects the GTRGAMMA model (response variable) versus GC

945 content and informative sites (two explanatory variables). The y-axis is the count of data sets

946 with a negative or positive coefficient of GC content (or number of informative sites)

947 estimated in the logistic regression. The bars in dark grey denote the count of data sets for

948 which the coefficient (negative or positive) of GC (or informative sites) is significant (p-

949 value < 0.05) in the logistic regression.

40

950   Figure 3: LRT for topologically congruent gene trees. a) A scatter plot of the p-value versus

951   the number of loci rejecting the hypothesis of TC gene trees across 47 data sets. b) Boxplots

952   of the proportion of loci rejecting the hypothesis of TC gene trees for 25 Reid et al. data sets

953   and 22 phylogenomic data sets. A two-sample t-test shows no significant difference (p-value

954   = 0.10) in the proportion of loci rejecting the hypothesis of TC gene trees between the 25

955   Reid et al. data sets and the 22 phylogenomic data sets. c) Proportion of loci rejecting the

956   hypothesis of TC gene trees across 47 data sets. d) Proportion of loci rejecting the hypothesis

957   of TC gene trees in 6 groups. The 47 data sets fall into 6 groups (bird, mammal, insect, fish,

958   reptile, and others). The filled black diamond represents the average proportion of loci

959   rejecting the hypothesis of TC gene trees in each group. ANOVA finds no significant

960   difference (pvalue = 0.71) in the proportion of loci rejecting the hypothesis of TC gene trees

961   among 6 groups. e) A linear regression line fitted for the log of the number of loci rejecting

962   the hypothesis of TC gene trees (y) versus the log of the number of loci (x). The regression

963   line is $log\ (y)\ =\ 0.87\ \times\ log\ (x) - 0.08$, where the coefficient 0.87 is significantly greater

964   than 0 with pvalue < 0.01.

965

966   Figure 4: Bayesian model validation. The MSC model is validated by two tests. The first test

967   proposed in Reid et al. (2014) compares the simulated and posterior coalescent gene tree. The

968   second test compares the gene trees estimated with the coalescent prior and those estimated

969   with independent prior. The MSC model is a poor fit to the data if either or both of the two

970   tests are rejected. a) The proportion of data sets rejecting the MSC model. 32% of 25 Reid et

971   al. data sets and 100% of 14 phylogenomic data sets reject the MSC model. b) The tests were

972   applied to each locus to find the proportion of loci rejecting the MSC model. The proportion

973   (10.88%) of loci rejecting the MSC for 22 phylogenomic data sets is significantly (p-value $<$

974   0.01) higher than the proportion (4.17%) of loci in 25 Reid et al. data sets that reject the MSC

975   model. c) A scatter plot of the RF distance versus the proportion of loci rejecting the MSC

976   model. The RF distance between two species trees built from all loci and only loci that fit to

977   the MSC is calculated for 14 phylogenomic data sets; RF = 0 for 9 data sets, RF = 2 for 4, RF

978   = 4 for 1 data set. The number below each point is the bootstrap support value on the

979   corresponding incongruent branch in two species trees. Note that two points with RF = 2 are

980   overlapping, and two values below the point with RF = 4 (i.e., two incongruent branches) are

981   the bootstrap support values on two incongruent branches. d) Testing the association between

982   GC content and poor fit of the MSC. We calculated the average GC content of loci rejecting

983   or accepting the MSC for two phylogenomic data sets with large numbers of loci rejecting the

984   MSC (Birds and mammal2017). We performed a two-sample t-test for the overall average

985   GC content (combining two data sets) and the average GC content of each of two data sets,

986   respectively. All three tests found no significant difference (p-value > 0.3) in GC content

987   between loci rejecting the MSC and loci accepting the MSC.

988

989   Figure 5: Bayesian model comparison. The log-scale Bayes factors of coalescent vs

990   concatenation (unlinking substitution model parameters) for 31 data sets, including 17 Reid et

991   al. data sets and 14 phylogenomic data sets.

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Figure 2

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Figure 5