1   **Precise regulation of the relative rates of surface area and volume**

2   **synthesis in dynamic environments**

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Abstract

Bacterial cells constantly face complex environmental changes in their natural habitats. While steady-state cell size correlates with nutrient-determined growth rate, it remains unclear how cells regulate their morphology during rapid environmental changes. Here, we systematically quantified cellular dimensions throughout passage cycles of stationary-phase cells diluted into fresh medium and grown back to saturation, and found that cells exhibit characteristic dynamics in surface area to volume ratio (SA/V). SA/V dynamics were conserved across many genetic/chemical perturbations, as well as across species and growth temperatures. We developed a model with a single fitting parameter, the time delay between surface and volume synthesis, that quantitatively explained our SA/V observations, and showed that the time delay was indeed due to differential expression of volume and surface-related genes. The first division after dilution occurred at a tightly controlled SA/V, a previously unrecognized size-control mechanism highlighting the relevance of SA/V. Finally, our time-delay model successfully predicted the quantitative changes in SA/V dynamics due to altered surface area synthesis rates or time delays from translation inhibition. Our minimal model thus provides insight into how cells regulate their morphologies through differential regulation of surface area and volume synthesis and potentiates deep understanding of the connections between growth rate and cell shape in complex environments.

36   ## Introduction

37   In their natural habitats, bacterial cells constantly face dynamic environmental

38   conditions. To survive, cells alter their physiology to cope with stresses such as nutrient

39   depletion, chemical inhibition, and temperature shifts. During stressful conditions, cells

40   alter their gene expression profiles, often slowing down growth and proliferation and

41   instead allocating limited resources to genes critical for survival[1]. While certain genetic

42   perturbations do not have observable effects in fast-growing cells, they cause death in

43   stressed conditions[2] or impair survivability when cells resume growth after the

44   environment becomes favorable again[3,4], highlighting the unique physiological

45   challenges posed by dynamic environments.

46

47   Cell shape is intrinsically linked to physiology. During steady-state growth, fast-

48   growing cells in nutrient-rich media adopt larger volumes compared to isogenic cells in

49   minimal media[5], and systematic tuning of growth rate via medium composition dictates

50   steady-state cell size[6]. Gene expression is also modulated by steady-state growth rates:

51   faster-growing cells tend to have a higher fraction of their proteome devoted to

52   ribosomes, addressing the need for rapid protein synthesis[7,8]. In a batch culture, cell

53   shape can undergo transitions in both cell width and length within several minutes[9,10],

54   in part as cells adapt their transcriptional program to the new medium and also because

55   the growth of cells can alter the medium composition through nutrient depletion and

56   waste production. Previously, a top-down flux-balance model accurately depicted the

57   kinetics of gene expression and growth in *Escherichia coli* cells under nutrient shifts[11],

58   but it remains unclear how these environmental and gene expression changes are

59   transduced into cell-shape changes, and whether cell shape is actively optimized in a

60   dynamic environment or is simply a passive outcome of cellular physiology.

61

62   In most bacteria, cell shape and size are dictated by the cell wall, a rigid network of

63   peptidoglycan[12,13]. To grow and divide, cells synthesize new peptidoglycan precursors

64   in the cytoplasm, which are then transported to the periplasm and inserted to the

65   expanding cell wall[13]. In rod-shaped bacteria such as *Escherichia coli*, cell elongation and

66   division are regulated by distinct machineries. The actin homolog MreB dictates the

67   insertion pattern of new peptidoglycan material along the cylindrical cell body[14], which

68   elongates the cell and maintains steady-state cell width[15]. Cell division is regulated by

69   FtsZ, a tubulin homolog that localizes to the mid-cell and forms a ring-like structure

70   prior to division, which then constricts and guides septum formation[13]. Chemical or

71   genetic perturbations to the elongation or division machinery alter cell-shape

72   homeostasis through modified patterns of cell wall synthesis[9,10,15-18]. The extent to which

73   such perturbations disrupt the ability of bacterial cells to adjust to new environments

74   could provide insight into the cellular processes key to shape adaptation.

75

76   While cell width and length are thought to be regulated by distinct molecular

77   mechanisms, previous studies have also indicated that they are somewhat inter-

78   connected. In a non-essential gene knockout library, the mutants exhibited variation in

79   both mean cell width and length, with a positive correlation between width and

80   length[19]. Similarly, single point mutations in the MreB protein can alter both width and

81   length[20,21], yet a large library of mutants were found to all occupy a specific region of the

82   space of cell geometries during growth in LB in which both wider and thinner mutants

83   had longer mean lengths compared to wildtype[10]. Therefore, cell width and length seem

84   to be regulated by an upstream process which unifies the two aspects of cell shape. In a

85   previous study, it was shown that the regulation of surface area to volume ratio (SA/V)

86   is such a process upstream of cell width and length determination: switching cells at

87   steady-state to a condition in which only cell wall (i.e. surface area) synthesis is partially

88   inhibited increased both cell width and length, which lowers the SA/V[22]. Similarly,

89   SA/V changes during the different stages of growth, with log-phase cells having lower

90   SA/V compared to those in stationary phase[22]; those measurements were performed in

91   highly controlled microfluidic chambers, and cells took tens of minutes to several hours

92   to fully adapt to the new steady-state morphology after the almost instantaneous

93   medium switch. The more continuous changes that cells undergo in a dynamic

94   environment such as batch culture have yet to be fully understood, particularly from

95   the perspective of cellular dimensions.

96

97   In this study, based on precise and frequent experimental measurements of cellular

98   dimensions and growth rates of a batch culture constantly experiencing nutrient

99   compositional changes and waste accumulations, we develop a model that

100 quantitatively predicts SA/V dynamics. Our model predicts a time delay between

101 surface area and volume synthesis adaptation, and that cells outgrowing from

102 stationary phase will always experience a period of active width increase due to optimal

103 resource allocation to volumetric growth. This model focuses on global resource

104 constraints rather than specific molecular machineries, and therefore is broadly

105 applicable to other microbial batch cultures. Indeed, we found that the observed SA/V

106 dynamics are qualitatively universal across microbial species and growth conditions.

107 With only a single free parameter, our time-delay model predicts the SA/V changes due

108 to perturbations in cell-wall synthesis or protein translation. Our work highlights the

109 ability of bacterial cells to rapidly respond to changing environments by modifying

110 their physical growth.

111   # Results

112

113   **A time-delay model explains the relative dynamics of surface area and volume**

114   **synthesis in batch cultures**

115   In previous studies, we showed that as *Escherichia coli* cells transition from stationary

116   phase to log phase and back to stationary phase in a batch culture, cellular dimensions

117   vary along with the instantaneous growth rate[9,10]. After a 1:200 back-dilution of an

118   overnight culture grown in LB into fresh LB, cells resumed growth and reached their

119   maximum growth rate after ~1.5 h, after which growth rate gradually slowed down to

120   approximately zero by ~4-5 h (Figure 1A). To validate our previous measurements, we

121   extracted a small sample of cells every 15 min and quickly spotted them onto agarose

122   pads for single-cell imaging and quantification (Methods). Mean cell length increased

123   only slightly in the first 0.5 h. The peak in bulk growth rate at 1.5 h corresponded with

124   the peak in mean cell length across the population (Figure 1B), which increased by ~3-

125   fold relative to stationary phase cells. The mean cell width increased linearly

126   immediately after dilution, and reached its maximum after ~1 h, increasing by ~25%

127   relative to stationary phase cells (Figure 1B). Since both length and width initially

128   increase, the surface area-to-volume ratio (SA/V) decreased over this time; SA/V

129   reached its minimum at approximately the same time as the peak in growth rate and

130   mean length (1.5 h; Figure 1C). After 1.5 h, the dynamics of length, width, and SA/V

131   were more gradual, with all quantities reaching plateaus by 5 h. We term these

132   measurements of cell dimensions throughout a passage cycle as a "shape growth

133   curve," by analogy to absorbance measurements. Using such measurements, we can

134   accurately capture single-cell shape dynamics in a liquid batch culture over extended

135   time periods.

136

137   To confirm that the observed changes in cellular dimensions and SA/V were not due to

138   artifacts of sampling, we performed time-lapse imaging by diluting and spotting

139   stationary phase cells onto agarose pads containing fresh medium, and tracked the

140   same cells for 1.5 h as they resumed growth on pads. The growth rates of these cells

141   mimicked a population grown in liquid culture, and their shape dynamics recapitulated

142   the shape growth curves (Figure 1D). In particular, each single cell immediately

143   increased in width as soon as it was placed on the agarose pad with fresh medium,

144   while length did not increase noticeably until 20-30 min later (Figure 1D). Therefore,

145   our shape growth curves indeed reflect the morphological changes for each single cell

146   in the batch culture.

147

148   Previous work showed that if surface area synthesis, like volume synthesis, is

149   dependent on cell volume (rather than surface area), SA/V will equilibrate at a steady-

150   state value corresponding to the ratio of surface and volume synthesis rates[22] (Figure

151   1E). Our measurements for cells transitioning out of and into stationary phase are

152   clearly not at steady state as growth rate is constantly changing, and indeed mean SA/V

153   varied by ~25%. If we extend the exponential growth laws[22] for volume V, $\frac{dV}{dt} = \alpha V(t)$,

154   and surface area A, $\frac{dA}{dt} = \beta V(t)$, to now cover non-exponential growth through time-

155   dependent functions $\alpha(t)$ and $\beta(t)$, we can derive (Figure 1E) an equation for the

156   dynamics of A/V:

$$\frac{d\left(\frac{A}{V}\right)}{dt} = \frac{1}{V}\frac{dA}{dt} - \frac{A}{V^2}\frac{dV}{dt} = \beta(t) - \alpha(t)\frac{A}{V}. \quad (3)$$

158   At steady-state, $\frac{d\left(\frac{A}{V}\right)}{dt} = 0$, and therefore $\frac{A}{V} = \frac{\beta}{\alpha}$. Previous studies have measured these

159   steady-state SA/V values across media that support different growth rates α, showing

160   that steady-state SA/V was approximately linear (with negative slope) as a function of

161   α[6]. Hence, we approximated β as a hyperbolic function of α based on our steady-state

162   SA/V measurements (Methods), providing an empirical relationship $\beta(t) = f(\alpha(t))$.

163   With our measured value of initial SA/V at t=0, the dynamics of α (calculated from

164   optical density readouts), and the function f, we obtained a prediction for the SA/V

165   dynamics during a shape growth curve (Figure S1A), and found that the model poorly

166   predicted our experimental measurements. Specifically, the model predicted a slower

167   initial decrease in SA/V, and the minimum value was higher and occurred at a later

168   time than our experimental measurements. The final SA/V value never recovered to the

169   initial value, even though the growth rate α was 0 at the beginning and end. Thus, the

170   model based on a quasi-steady state assumption does not capture some key factor(s)

171   contributing to the SA/V changes during batch culturing.

172

173   Studies focused on the *E. coli* proteome have shown that conditions that support higher

174   growth rate require a reallocation of protein synthesis toward ribosomes[7,8]. We

175   hypothesized that the transition from stationary phase to log growth would require a

176   similar shift in proteome composition more heavily weighted toward cytoplasmic

177   components than surface area components (Figure 1F), which could lead to different

178   temporal dynamics between α and β contrary to the quasi-steady state hypothesis. To

179   explore such a possibility, we analyzed our single-cell time-lapse trajectories (Figure

180   1D) to measure α and β for each cell. From our measurements of α, we calculated $f(\alpha)$,

181   the expected value of β during steady-state growth at rate α. We found that $f(\alpha)$

182   increased more quickly than β, with a roughly constant time delay of ~10 min between

183   the two curves (Figure 1G). Thus, we modified our model in Eq. 3 by substituting the

184   function between α and β to be $\beta(t) = f\big(\alpha(t - \Delta t)\big)$, where Δt is a constant that

185   characterizes the time delay between β and α. Fitting our experimental data with the

186   time-delay model yielded almost perfect agreement with a time delay $\Delta t = 11$ min

187   (Figure 1H). Thus, the minimal time-delay model with a single free parameter is able to

188   almost entirely recapitulate the quantitative features of SA/V dynamics.

189

190   To confirm that such a delay actually occurs, we utilized a library of *E. coli* strains with

191   GFP reporting the expression from various promoters[23] and sought to directly quantify

192   the dynamics of cytoplasmic and surface-related proteins as cells emerge from

193   stationary phase. We tested two strains representing ribosomal proteins (P_{rplL}-GFP, P_{rpsU}-

194   GFP), two representing other cytoplasmic proteins (P_{lacI}-GFP, P_{gyrB}-GFP), and two

195   representing enzymes related to cell-wall synthesis (P_{mrcB}-GFP, P_{murA}-GFP). We grew

196   each strain in LB overnight to saturation, then placed the cells directly into a

197   microfluidic device surrounded by the supernatant from the overnight culture. We then

198   switched the spent medium to fresh LB and monitored cell morphology and gene

199   expression. In all six strains, GFP levels increased during growth, signifying increased

200   expression. Consistent with our model prediction, the promoters of cytoplasmic

201   proteins increased expression faster than those of the cell-wall genes (Figure 1I). We

202   quantified the expression dynamics by calculating t_{10}, the time for each promoter to

203   increase their relative expression by 10% (a proxy for promoter activation). The

204   promoters for cytoplasmic proteins had $t_{10} \sim 10$ min, whereas the promoters for cell-wall

205   enzymes had $t_{10} \sim 20$ min, a delay of $\Delta t \sim 10$ min. Therefore, our direct measurement of

206   gene expression dynamics confirmed a delay between α and β, indicating differential

207   regulation of the proteome (Figure 1F).

208

209   Our ability to fit the complex SA/V dynamics during batch culture with a simple model

210   involving only the introduction of a time delay to the steady-state relationship between

211   β and α suggests a simple picture of the initial stages of growth: as cells emerge from

212   stationary phase, they devote more resources to synthesizing cytoplasmic components

213   such as ribosomes than to surface components such as the cell wall. While the cell still

214   must expand to allow space for these new cytoplasmic components, it does so with a

215   minimal amount of surface growth by expanding predominantly in width rather than

216   length, as volume scales approximately quadratically with width but only linearly with

217   length. Indeed, in a typical rod-shaped cell, a two-fold change in volume requires only a

218   47% increase in surface area if cells only increase in width, but 91% if cells increase only

219   in length (Figure 1J, Methods). To test this reasoning, from our single-cell time-lapse

220   results (Figure 1D), we directly calculated the possible range of β at each time point

221   using the observed width, length and growth rate α (Methods). At $t = 0$, the measured β

222   was close to its minimal possible value, characterizing a widening-dominant growth

223   mode. By $t = 60$ min, the measured β approximately reached its maximum under those

224   growth conditions, consistent with the canonical elongation-dominant growth mode

225   (Figure 1K). Thus, during outgrowth from stationary phase, cells transition their growth

226   mode from widening to elongation.

227

228   **Cell widening during exit from stationary phase occurs even if width decreases at**

229   **steady-state**

230   To further validate that the initial increase in width during outgrowth from stationary

231   phase (Figure 1B,D,K) is governed by the delay between α and β, rather than

232   determined solely by the current nutrient condition after back dilution, we took

233   stationary-phase cells grown in LB and diluted them into M9 glucose medium. Cells

234   grown in LB always had widths larger than 0.94 μm (Figure 1B), whereas cell widths

235   during passage exclusively in M9 glucose never exceeded 0.94 μm (Figure S1B). Thus, if

236   the medium cells are diluted into dictated cell shape, cell width in M9 glucose would

237   only decrease to below 0.94 μm. However, we observed that by 30 min after dilution

238   into M9 glucose from a stationary-phase LB culture, cell width increased by ~8% and

239   reached ~1.03 μm (Figure 1L), a value that was not achievable for cells always passaged

240   in M9 glucose (Figure S1B). Afterward, cell width dropped to ~0.9 μm, as expected for

241   cells passaged in M9 glucose (Figure S1B), which we presume is mainly dictated by the

242   M9 medium. Therefore, the initial widening of cells during outgrowth is not

243   determined by external nutrients.

244

245   Outgrowth from stationary phase also involves changes such as altered expressions of

246   stress-response genes, initiation of DNA replication, and different osmolalities of fresh

247   versus stationary phase media. We tested these possibilities by repeating shape growth

248   curve measurements in a ppGpp^0 strain and a $\Delta thyA$ strain. The ppGpp^0 strain is unable

249   to synthesize ppGpp, a small nucleotide regulating stress-related genes[1]. The $\Delta thyA$

250   strain does not replicate DNA in the absence of external thymine[24]. In both strains,

251   shape growth curves still exhibited similar outgrowth dynamics (Supplementary Text,

252   Figure S1C-J). Systematically tuning the osmolality of media caused much smaller

253   shape changes than those observed in the shape growth curves (Supplementary Texts,

254   Figure S1K). Taken together, we conclude that the initial increase in width is likely

255   governed by proteome re-allocation rather than external factors or other biological

256   processes.

257

258   **Cells exiting from stationary phase reach a critical SA/V at their first division**

259   Previous work suggested that exponentially growing cells accumulate excess surface

260   area material during the cell cycle, which then triggers division[22]. For a rod-shaped cell,

261   division adds two hemispheric poles and increases SA by 4% without changing volume

262   (Figure S2A). Since cells decrease their SA/V during outgrowth (Figure 1D), we thus

263   asked whether the first division after cells exit from stationary phase was also related to

264   their SA/V.

265

266   We diluted stationary-phase cells and placed them onto an agarose pad containing fresh

267   LB, tracked single cells until their first division, and quantified their cellular

268   dimensions. Several models have been proposed for cell-size control during steady-

269   state growth: the "sizer" model, in which cells divide at a fixed size; the "adder" model,

270   in which cells add a fixed volume before division; and the "timer" model, in which cells

271   grow for a fixed time before division[25]. The "sizer" model predicts that the volume at

272   division is independent of initial volume, while the "adder" model predicts a slope of

273   +1 between volume at division and initial volume. During outgrowth from stationary

274   phase, we found that the volume at the first division negatively correlated with the

275   initial volume (Figure 2A), deviating from both the sizer and adder models. Similar

276   negative correlations were observed for cell length and surface area (Figure S2B,C). The

277   timer model also failed to explain the data, with time to first division negatively

278   correlated with initial cell volume (Figure 2B). However, the SA/V at division was

279   approximately constant and independent of the initial SA/V (Figure 2C). Moreover, the

280   normalized distribution of SA/V at division was much narrower compared to other

281   cellular dimensions (Figure 2C,D), suggesting that the first division after stationary-

282   phase exit is linked to a critical SA/V.

283

284   We further asked how division-related proteins were regulated during stationary-phase

285   exit by tracking the dynamics of the key division protein FtsZ. We selected four *E. coli*

286   strains, each containing a mutation in the actin homolog MreB that exhibited different

287   mean widths and lengths during log-phase growth [10]. These mutants allowed us to

288   analyze division dynamics in cells of different widths. These strains also contained a

289   chromosomally-integrated internal fusion of FtsZ to monomeric Venus (FtsZ^{sw}-mVenus)

290   at the native FtsZ locus[10,26], allowing quantification of FtsZ abundance using

291   fluorescence microscopy (Methods). All strains exhibited qualitatively similar cell shape

292   dynamics as wild-type *E. coli*, despite their altered lengths and widths (Figure S2D,E,F).

293   Total FtsZ fluorescence remained constant in the first 45 min post-dilution before

294   starting to increase (Figure 2E), indicating that FtsZ synthesis started much later

295   compared to other genes (Figure 1I). We also measured FtsZ dynamics in a time-lapse

296   experiment with GFP fused to the FtsZ promoter (P$_{ftsZ}$-GFP)[23] and confirmed that FtsZ

297   expression started ~50 min post-dilution (Figure S2G). Although the four MreB mutants

298   had different levels of total FtsZ (Figure 2E), FtsZ concentration was quantitatively

299   similar across the different strains (Figure 2E, inset), suggesting a conserved mechanism

300   of FtsZ regulation independent of cell shape, consistent with previous measurements in

301   exponential-phase cells[10]. In all strains, no FtsZ rings were observed until ~50 min post-

302   dilution. Virtually all cells contained one FtsZ ring by ~100 min post-dilution (Figure

303   2F), consistent with the observed timing of the first division after stationary-phase exit

304   (Figure 2B). Taken together, these data indicate that FtsZ levels are upregulated

305   concurrent with the need for division.

306

307   **SA/V dynamics are broadly conserved across width and length perturbations**

308   Since SA/V is dependent on both cell width and length, we asked whether chemically or

309   genetically tuning cell width or length would affect SA/V dynamics. We first treated

310   wild-type *E. coli* cells with a range of concentrations of cephalexin, a β-lactam antibiotic

311   that inhibits the division-specific cell-wall synthesis enzyme PBP3[27]. Importantly, lower

312   cephalexin concentrations (2.5 μg/mL and 5 μg/mL) did not affect bulk growth rate for

313   at least the first 10 h of growth. For the highest cephalexin concentration used (10

314   μg/mL), cells started to lyse after 2 h, but growth was not affected prior to lysis (Figure

315   S2H). Thus, cephalexin treatment does not directly affect any parameters in our model,

316   despite the obvious perturbations in cell length. Shape growth curves showed that cells

317   became longer due to inhibition of cell division in a concentration-dependent manner

318   (Figure 2G). However, as cephalexin concentration was increased, cell width peaked at

319   a lower value and began to decrease at an earlier time point (Figure 2H). As a result,

320   SA/V was maintained throughout the first 3 h (Figure 2I) despite the marked changes in

321   cell length. Therefore, cells collectively regulate width and length to maintain SA/V

322   during growth.

323

324   We further studied cell shape changes in a library of *E. coli* mutants with a wide range

325   of mean cell lengths and widths[10]. While the strains had different morphologies, they all

326   exhibited similar SA/V dynamics as observed in wild-type *E. coli* (Supplementary Text,

327   Figure S2I-N), further indicating that the SA/V dynamics (Figure 1C) are conserved

328   across genetic perturbations to cellular dimensions.

329

330   **SA/V dynamics are conserved across species and growth temperatures in rich media**

331   The basis of our interpretation of SA/V dynamics during batch culture should be

332   generally applicable to species other than *E. coli*, as it does not make any assumptions

333   about *E. coli*-specific pathways. Hence, we predicted that a similar initial decrease in

334   SA/V upon outgrowth from stationary phase should generally occur. We thus expanded

335   our shape growth curve measurements to a variety of other species and conditions. We

336   quantified shape growth curves for the Gram-negative bacteria *Vibrio cholerae* and

337   *Caulobacter crescentus*, both of which form slightly curved rods, the rod-shape Gram-

338   positive bacterium *Bacillus subtilis*, and the eukaryote fission yeast *Schizosaccharomyces*

339   *pombe*. In all species we tested, SA/V dynamics were similar to those in *E. coli*, with

340   SA/V decreasing when cells resumed growth, and then gradually recovering when cell

341   growth slowed down again (Supplementary Text, Figure S3A-E).

342

343   Bacterial cell size during steady-state growth is thought to be relatively constant as

344   growth rate changes across temperatures[5]. Nonetheless, we still found that *E. coli* cells at

345   30, 37, and 42 °C had different cellular dimensions and SA/V values. At all

346   temperatures, cells still obeyed similar SA/V dynamics (Supplementary Text, Figure

347   S3F,G). Taken together, the initial decreases of SA/V appear to be general across

348   microbial species, growth temperatures, and cell shapes and sizes, indicating that as

349   cells accelerate in growth, volume synthesis always increases more quickly than surface

350   synthesis.

351

352   **SA/V regulation is dependent on nutrient conditions**

353   We next asked whether medium composition affects SA/V dynamics, considering that

354   steady-state cell shape is nutrient-dependent[6]. We quantified shape growth curves in

355   M9 media supplemented with different carbon/nitrogen sources that support different

356   growth rates. Overall, in low-nutrient conditions with slower growth rates, Δt was close

357   to zero and SA/V remained largely constant, despite substantial changes in cell width

358   and length (Supplementary Text, Figure S4A-E). Richer nutrient conditions supported

359   faster growth rates and led to larger changes in SA/V and non-zero Δt values

360   (Supplementary Text, Figure S4F-H). Since cell shape changes occurred even in defined

361   media with a single carbon source (Figure S4C,D), the observed cellular dimension

362   changes across shape growth curves are not likely due to diauxic shifts caused by

363   nutrient consumption, but rather related to the dynamics of proteome composition as

364   growth rate changes. A more complex panel of nutrients that support faster growth

365   likely requires a larger shift in proteome composition (Figure 1F), driving a larger range

366   of SA/V changes (Figure S4I).

367

Time-delay model quantitatively predicts SA/V decreases due to inhibiting cell-wall

synthesis

We next sought to test predictions of our time-delay model experimentally. In our

model, reducing β (without changing α) predicted that the shape growth curve would

exhibit larger SA/V decreases during the first 2 h, with a final SA/V when cells returned

to stationary phase lower than the initial value (Figure 3A). The *E. coli* cytoplasm is

surrounded by the cell envelope, constituted of three layers: the cell wall, and two

membranes on either side of the cell wall. The cell wall mainly consists of

peptidoglycan, and the membranes are constituted by lipids, proteins, and

lipopolysaccharides. Since in most conditions the synthesis of peptidoglycan is more

energetically costly compared to lipids[28], we hypothesized that that altering cell-wall

synthesis would have a larger effect on β.

380

To validate our model prediction, we treated cells with multiple antibiotics that inhibit

cell-wall synthesis and asked whether the SA/V changes were consistent with the model

predictions. We first treated MG1655 cells grown in LB with A22[29], a small molecule

inhibiting the actin homolog MreB and therefore affecting the spatial pattern of new cell

wall incorporation. Sub-lethal concentrations of A22 did not affect growth rate during

the first 3 h of growth, but cells treated with A22 exhibited dose-dependent increases in

387 cell width compared to the non-treated control (Figure S5A), as previously shown [30].

388 Interestingly, the increase in cell width was accompanied by relatively lower increases

389 in cell length (Figure S5B), which partially compensated for the decrease in SA/V.

390 Together, the inhibition of cell-wall synthesis by A22 caused SA/V to drop in a dose-

391 dependent fashion (Figure 3B), as predicted by our model (Figure 3A). Fitting the A22

392 shape growth curves to our model was indeed consistent with a dose-dependent

393 decrease β (Figure 3B). Δt was not affected except at the highest A22 concentration,

394 which resulted in a ~50% longer time delay (Table S2), presumably because higher A22

395 concentrations require further proteome redistribution. We also tested two other cell-

396 wall synthesis inhibitors, fosfomycin and mecillinam. Fosfomycin inhibits MurA, the

397 enzyme catalyzing the first committed step of peptidoglycan biosynthesis[31,32], and

398 mecillinam specifically targets PBP2, a transpeptidase that crosslinks new cell-wall

399 material[33]. In both cases, we observed similar changes to shape growth curves as with

400 A22 treatment (Figure S5C,D).

401

402 Since cells grown in M9 glucose exhibited largely constant SA/V and virtually no time

403 delay (Figure S4A), we asked whether inhibiting SA synthesis would affect their SA/V

404 dynamics by treating cells grown in M9 glucose with A22. In this case, A22 also caused

405 a similar drop in SA/V (Figure 3C) and mean length (Figure S5E), and cell width now

406 increased as opposed to the slight decrease in the A22-free control (Figure S5F). Thus,

407   the relatively small range of SA/V changes observed in M9 glucose (Figure S4A) was

408   indeed because the proteome composition for surface area and volume synthesis was

409   largely balanced in M9 glucose. Nonetheless, perturbations such as A22 treatment can

410   still break this proteome balance and alter SA/V more substantially. Fitting the A22

411   SA/V dynamics to our model also showed that at high A22 concentrations, in addition

412   to decreased β (Table S2), Δt became non-zero (Figure 3C), suggesting that cells have to

413   re-allocate their proteome composition to accommodate inhibition of cell-wall synthesis.

414

415   Cell wall synthesis can also be altered genetically. In *V. cholerae*, activation of a histidine

416   kinase/response regulator two-component system, WigK/WigR, increases expression of

417   many cell-wall synthesis genes and elevates cell-wall synthesis[34]. We therefore

418   quantified the shape growth curves of *V. cholerae* strains with a range of cell-wall

419   synthesis capacities. Compared to wildtype, overexpression of WigR increased SA/V

420   (Figure 3D), mainly through decreased cell width. Overexpression of WigR[D78E], a

421   phosphomimetic version of WigR, further increases cell wall synthesis[34], and SA/V

422   increased even more as expected (Figure 3D), accompanied by further decreases in cell

423   width. By contrast, deletion of WigR slows down cell wall synthesis, and we observed

424   decreases in SA/V similar to those during treatment of *E. coli* with wall-acting

425   antibiotics (Figure 3D). Therefore, genetically perturbing cell-wall synthesis affects β

426   and therefore SA/V dynamics as predicted by our model.

427

428   We next tested whether inhibiting lipid synthesis would have similar effects on SA/V

429   dynamics. While it has been previously shown that inhibiting fatty acid synthesis via

430   treatment with cerulenin alters cell morphology[35], those experiments were performed in

431   a regime (cerulenin concentration >50 μg/mL) in which growth rates were strongly

432   affected (Figure S5G). In the context of our model, at lower concentrations of cerulenin

433   (<10 μg/mL) where growth rates remained unaffected (Figure S5G), we did not observe

434   noticeable changes in cellular dimensions after 2 h of growth (Figure S5H). Similarly, in

435   cell wall-deficient spheroplasts[36], surface area was only limited by lipid synthesis, and

436   those cells exhibited increased, rather than decreased, SA/V during outgrowth from

437   stationary phase (Supplementary Text, Figure S5I). We further analyzed previously

438   published proteome datasets[11,37], and found that levels of lipid synthesis proteins, but

439   not peptidoglycan synthesis proteins, increased monotonically with growth rate

440   (Supplementary Text, Figure S5J-L). Taken together, lipid biosynthesis protein levels are

441   likely directly linked to growth rate, and cell envelope growth is limited by cell wall

442   rather than membrane synthesis.

443

444   **Inhibiting translation increases the time delay between volume and surface growth**

445   The addition of the time delay Δt was a critical modification to our model in order to fit

446   our experimental shape growth curve data (Figure 1H, Figure S1A). We therefore asked

447   whether modifying Δt would have observable effects on SA/V dynamics. By increasing

448   Δt from 11 to 25 min, our model predicted that the minimal SA/V reached in log phase

449   would decrease, while the final SA/V when cells enter stationary phase would increase

450   (Figure 4A). Such non-monotonic changes to SA/V dynamics are somewhat counter

451   intuitive, highlighting the biological relevance of the time delay. The initial SA/V drop

452   after exiting stationary phase is primarily due to the quick increase in α. While β also

453   increases, the time delay between α and β causes V to grow faster than A, leading to

454   decreased SA/V. Therefore, a larger Δt means that V increases more before A growth

455   catches up, resulting in an even lower SA/V in log phase. As for the terminal SA/V, it is

456   dependent on $\frac{\int dA/dt}{\int dV/dt}$, an integral effect that depends on the entirety of the growth

457   dynamics. $\frac{dV}{dt}$ only depends on α and remains unaffected, while $\frac{dA}{dt} = \beta V(t) =$

458    $f\big(a(t - \Delta t)\big)V(t)$. Increasing Δt leads to increased $\int dA/dt$ and eventually a higher

459   terminal SA/V.

460

461   We tested these predictions by treating cells with low levels of chloramphenicol, a

462   translational inhibitor, based on our inference that Δt is mainly determined by rates of

463   proteome re-allocation (Figure 1F). Although inhibiting protein translation inevitably

464   affected both α and β, at very low chloramphenicol concentrations (~0.01-0.05X minimal

465   inhibitory concentration), cell growth was largely unaltered, and the SA/V dynamics

466   matched our model predictions: increasing chloramphenicol concentrations increased

467 Δt by ~70%, while β only changed <5% across conditions (Figure 4B). In these cases, the

468 changes in SA/V were largely dictated by the relatively larger cell widths under

469 chloramphenicol treatment (Figure S6A), as cell length followed very similar trends

470 across concentrations (Figure S6B). Higher chloramphenicol concentrations

471 substantially reduced growth rate and led to even lower SA/V in log phase (Figure

472 S6C). Model fitting found that the reduced SA/V was also mainly due to increased Δt

473 (Figure S6C), as β changed less than 10% (Table S2). Thus, our shape growth curves

474 with chloramphenicol treatment provide further validation of our model predictions,

475 and demonstrate that tuning Δt has observable effects, rather than merely acting as a

476 fitting parameter.

477

478 **Discussion**

479

480 Although much work has been done to unveil the molecular players determining cell

481 morphology at steady states, an approach unifying cell morphology and growth rates in

482 dynamic environments is still lacking. In this study, our time-delay model of SA/V

483 dynamics accurately predicted how cell size responded to growth rate changes, and

484 was generally applicable across many species and growth conditions. The minimal

485 assumption of a single, constant time delay between volume and surface area synthesis

486 quantitatively recapitulated the complex SA/V dynamics (Figure 1C, S3, S4), and

487 predicted SA/V changes under perturbations (Figure 3, 4). While previous studies have

488 shown that cells adopt different steady-state SA/V values across growth conditions[6,22],

489 our work further reveals that the quantitative dynamics of SA/V under environmental

490 perturbations are based on global resource allocation and the temporal dependence

491 between surface area and volume growth (Figure 1I). Our model thus has the potential

492 to quantitatively describe other dynamic biological processes that scale with cell

493 volume[38].

494

495 While we obtained the time delay between surface area and volume synthesis (Δt) via

496 model fitting, systematically tuning Δt conferred non-monotonic changes in SA/V

497 dynamics (Figure 4A,B), highlighting its biological relevance. Indeed, we were able to

498   quantify the delay of surface area growth compared to volumetric growth by directly

499   tracking protein expression in single cells (Figure 1G), and the delay was observed

500   previously when cells were switched from one steady state to another[22]. Inhibiting

501   protein translation increased Δt (Figure 4B), suggesting that surface area synthesis was

502   delayed due to a slower regulation of surface area synthesis-related enzymes. The

503   connection between Δt and changes in growth rate is complex, since higher growth

504   rates may require larger shifts in proteome, but also speeds up proteome turnover. Thus,

505   Δt does not necessarily have a simple correlation with growth rates. Other factors, such

506   as cell-wall precursor synthesis and insertion, could also alter Δt in addition to

507   proteome changes. It remains to be explored why and how surface area and volume

508   synthesis rates are differentially modulated, and the ways in which such a delay can be

509   beneficial for cells.

510

511   Our model predicts that upon growth resumption, cells should always increase in

512   width, as surface area synthesis is limiting and increasing width rather than length

513   poses a lower demand for surface area material (Figure 1J). We observed such width

514   increases after diluting stationary-phase cells into fresh media across all species and

515   experimental conditions (Figure 1B,D,L, S3, S4). Similar changes in width have been

516   reported in growth-inhibited cells due to the presence of an antibiotic, in which *E. coli*

517   cells resumed growth after washing out the antibiotic and cell width increased prior to

518   length increase[39]. The initial widening of cells is likely related to active growth and the

519   subsequent imbalance between surface area and volume synthesis. In *E. coli*, such

520   widening has been linked to altered cell wall insertion patterns governed by changes in

521   MreB localization patterns[9,10], providing a potential molecular mechanism in response to

522   limited surface area synthesis. While DNA replication is a central process in cell

523   proliferation and has implications in cell-size determination[6,40], we have shown that cell

524   shape remodeling can be independent of DNA replication (Figure S1G-J), at least in the

525   initial 2 h of shape growth curves, indicating that the effect of DNA abundance on cell

526   shape potentially manifests on a different time scale or is growth dependent. Regardless,

527   our findings strongly suggest that the dynamic coordination between surface area and

528   volume growth dictates cell shape.

529

530   *E. coli* cell division at steady state is well described by the adder model[41]. However, for

531   cells growing out of stationary phase, we observed that cells did not add a constant

532   volume, surface area, or length (Figure 2A, Figure S2B,C), nor did they divide at a fixed

533   size or after a fixed time interval (Figure 2A,B). Instead, cell division occurred at a given

534   SA/V (Figure 2C,D), highlighting the biological relevance of SA/V regulation. The key

535   division protein, FtsZ, was upregulated concurrently with the need for cell division

536   (Figure 2E,F, S2G), consistent with previous work showing that a threshold of FtsZ is

537   required for cell division[42,43]. The dynamics of FtsZ were further delayed compared to

538   other cell-wall synthesis genes (Figure 1I, S2G), reinforcing the idea that gene

539   expression during growth resumption is temporally regulated to allow cells to prioritize

540   volumetric growth over surface area synthesis or division.

541

542   Our model of SA/V dynamics links cell width and length, even though the two

543   dimensions are regulated by distinct molecular machineries[14,15,33]. Interestingly,

544   perturbations known to increase cell width or length also led to decreases in the other

545   dimension (Figure 2G,H, S5A,B,E,F). Larger cell width and length both decrease SA/V,

546   and a corresponding decrease in cell length or width can compensate for an increase in

547   the other to maintain SA/V. Therefore, despite the seemingly disjoint nature of cell

548   width and length regulation in rod-shaped cells, the global resource limitation on

549   surface area growth poses constraints on the two dimensions. From an evolutionary

550   perspective, bacterial cells constantly encounter feast or famine conditions, and

551   therefore optimize the resource allocation strategies through regulations between

552   surface area and volume growth. Rod-like shapes allow cells to efficiently tune SA/V via

553   two disparate growth modes (Figure 1J), which potentially confers evolutionary

554   benefits compared to other shapes. In eukaryotic cells, a nuclear transporter receptor

555   serves as a sensor of SA/V[44], and it remains to be discovered whether similar global

556   SA/V sensors exist in bacterial cells, which would provide opportunities to reveal new

557   connections between cell physiology, size, and fundamental mechanisms of

558   morphogenesis.

559

560   # Methods

561

562   **Strains and media**

563   Strains used in this study are described in Table S1. For routine culturing, all cells were

564   grown in lysogeny broth (LB) at 37 °C unless otherwise specified. *C. crescentus* cells

565   were grown in PYE (peptone-yeast extract) media at 30 °C as previously described[22],

566   and *S. pombe* cells were grown in YES255 media at 30 °C. Antibiotics (Sigma Aldrich, St.

567   Louis, MO, USA) were used at the concentrations noted in the text. IPTG was used at a

568   final concentration of 1 mM for *V. cholerae* cells. Thymine was added at a final

569   concentration of 500 μg/mL for the *E. coli* Δ*thyA* strain. For minimal media, glucose or

570   other carbon sources were added at final concentration of 0.4%, six amino acids (L-

571   methionine, L-histidine, L-arginine, L-proline, L-threonine, and L-tryptophan) were

572   added to final concentrations of 500 μg/mL each, and casamino acids were added to a

573   final concentration of 3% (w/v).

574

575   Strains were inoculated from freezer stocks into test tubes with 3 mL of media and

576   supplemented with the appropriate antibiotics. The tubes were incubated overnight,

577   except for cells grown in M9 acetate, which were incubated for 48 hours. Overnight

578   cultures were back-diluted 1:200 into the same fresh medium for shape growth curves

579   and growth curves measurements.

580

581   Spheroplasts were grown in LFLB (LB with additional 3.6% sucrose and 10 mM MgSO$_4$)

582   at 30 °C, with 60 μg/mL cefsulodin added to inhibit cell wall growth[45]. For shape

583   growth curve measurements, overnight spheroplast cultures with cefsulodin were

584   washed three times in fresh LFLB, and diluted 1:10 into LFLB with or without

585   cefsulodin.

586

587   **Single-cell imaging**

588   For imaging, samples were taken from test tubes and placed on 1% agarose pads every

589   15 min, and then imaged within 5 min. For membrane staining, a small aliquot of cells

590   was incubated with FM 4-64 (Invitrogen) at a final concentration of 5 μg/mL for 5 min

591   and spotted on agarose pads without washing. Phase-contrast images and

592   epifluorescence images were acquired with a Nikon Ti-E inverted microscope (Nikon

593   Instruments) using a 100X (NA 1.40) oil immersion objective and a Neo 5.5 sCMOS

594   camera (Andor Technology). The microscope was outfitted with an active-control

595   environmental chamber for temperature regulation (HaisonTech, Taipei, Taiwan).

596   Images were acquired using μManager v.1.4[46].

597

598   **Morphological analyses**

599   The MATLAB (MathWorks, Natick, MA, USA) image processing code *Morphometrics*[19]

600   was used to segment cells and to identify cell outlines from phase-contrast or

601   fluorescence microscopy images. A local coordinate system was generated for each cell

602   outline using a method adapted from *MicrobeTracker*[47]. Cell widths were calculated by

603   averaging the distances between contour points perpendicular to the cell midline,

604   excluding contour points within the poles and sites of septation. Cell length was

605   calculated as the length of the midline from pole to pole. Cell volume and surface area

606   were estimated from the local meshing results.

607

608   **FtsZ fluorescence quantification**

609   Cells with a sandwich fusion of mVenus to FtsZ[26] were imaged in phase contrast and

610   fluorescence using an ETGFP filter. FtsZ fluorescence was quantified by summing the

611   intensity values of each pixel within the cell contour. FtsZ rings were identified as the

612   peak of fluorescence intensity along the cell contour.

613

614   **Population-level growth analyses**

615   To measure growth dynamics, overnight cultures were inoculated into 200 μL of fresh

616   media supplemented with the appropriate antibiotics in a clear 96-well plate. The plate

617   was covered with an optical film, with small holes poked at the side of each well to

618   allow aeration. Incubation and OD measurements were performed with an Epoch 2

619   plate reader (BioTek) at appropriate temperatures with continuous shaking and OD_{600}

620   measured at 7.5-min intervals. The growth rate was calculated as the slope of ln(OD)

621   with respect to time after smoothing using a moving average filter of window size five.

622

623   **β as a function of α at steady state**

624   Based on previous steady-state growth rate and SA/V measurements, steady-state SA/V

625   linearly correlates with growth rate[6]. Since steady-state SA/V equals β/α, and growth

626   rate is α, β/α is a linear function of α. Therefore, based on SA/V measurements at two

627   different growth rates, we can fit the function relating β to α. In our measurements in LB,

628   *E. coli* cells approaching stationary phase correspond to $\alpha \sim 0$ and $\beta/\alpha = 5.7$ μm^{-1}. By

629   diluting cells repeatedly, cells reached steady-state morphologies[10] for which $\beta/\alpha = 3.8$

630   μm^{-1}, and the corresponding $\alpha = 1.7$ h^{-1}. Thus, in LB, we have $\beta/\alpha = 5.7 - 1.12\alpha$, or $\beta = $

631   $\alpha(5.7 - 1.12\alpha)$.

632

633   **SA/V as a function of width and length changes**

634   For calculations in Figure 1J and S2E, a cell with width w and length l was

635   approximated by a cylindrical cell body with radius $r = w/2$ and length $l - 2r$, and

636   hemispherical caps on each end with radius $r = w/2$. In this scenario, the corresponding

637   surface area of the cell is $SA = 2\pi r(l - 2r) + 2 \times 2\pi r^2 = \pi w l$, and the volume is $V = \pi r^2(l - 2r)$

638   $+ 4\pi r^3/3 = \pi w^2 l/4 - \pi w^3/12$. For the initial cell, $w = 1$ μm and $l = 5$ μm.

639

Calculation of permissible range of β

641 In rod-shaped cells, given the above equations for V and A, $\frac{dV}{dt} = \left(\frac{\pi}{2} wl - \frac{\pi}{4} w^2\right) \frac{dw}{dt} +$

642 $\frac{\pi}{4} w^2 \frac{dl}{dt} = \alpha \left(\frac{\pi}{4} w^2 l - \frac{\pi}{12} w^3\right)$, and $\frac{dA}{dt} = \pi l \frac{dw}{dt} + \pi w \frac{dl}{dt} = \beta \left(\frac{\pi}{4} w^2 l - \frac{\pi}{12} w^3\right)$. During growth,

643 $\frac{dw}{dt} \geq 0$ and $\frac{dl}{dt} \geq 0$. Solving for the linear optimization with the above constraints gives a

644 permissible range of β that is dependent on w, l, and α, with minimum β corresponding

645 to $\frac{dl}{dt} = 0$, and maximum β corresponding to $\frac{dw}{dt} = 0$.

646

DAPI staining and fluorescence quantification

648 Cells were grown in the same conditions as in single-cell imaging experiments. At each

649 time point, 1 mL of each sample was taken, pelleted at 6,500 rcf for 1 min, and fixed via

650 resuspension in 500 μL 70% ethanol and incubation for 15 min at room temperature.

651 Cells were then pelleted at 6,500 rcf for 1 min, resuspended in 500 μL PBS, with 4',6-

652 diamidino-2-phenylindole (DAPI) added to a final concentration of 1 μg/mL, and

653 incubated in the dark for 15 min. Cells were washed with PBS twice by pelleting at

654 6,500 rcf for 1 min followed by resuspension. Cells were spotted onto 1% agarose pads

655 and imaged in phase contrast and fluorescence using a DAPI filter. DAPI fluorescence

656 was quantified by summing the intensity values of each pixel within the cell contour,

657 and then normalizing to the corresponding intensity in the control.

658

659   **qPCR**

660   To estimate the relative replication rate of the chromosome, we quantified the copy

661   numbers of 16 genetic loci via qPCR and fitted their log(relative abundance) to their

662   corresponding distances to *terC*, as previously described[18]. The cells were harvested at

663   six different time points (in the overnight culture, and 30, 60, 90, 120, and 150 min after

664   1:200 dilution), and the DNA was extracted using the genomic DNA purification kit

665   (Qiagen). The relative abundances of chromosomal loci were quantified by qPCR, using

666   the EvaGreen qPCR kit (Bio-rad). The qPCR probes used were as previously described[47].

667

668   **Figures**

669
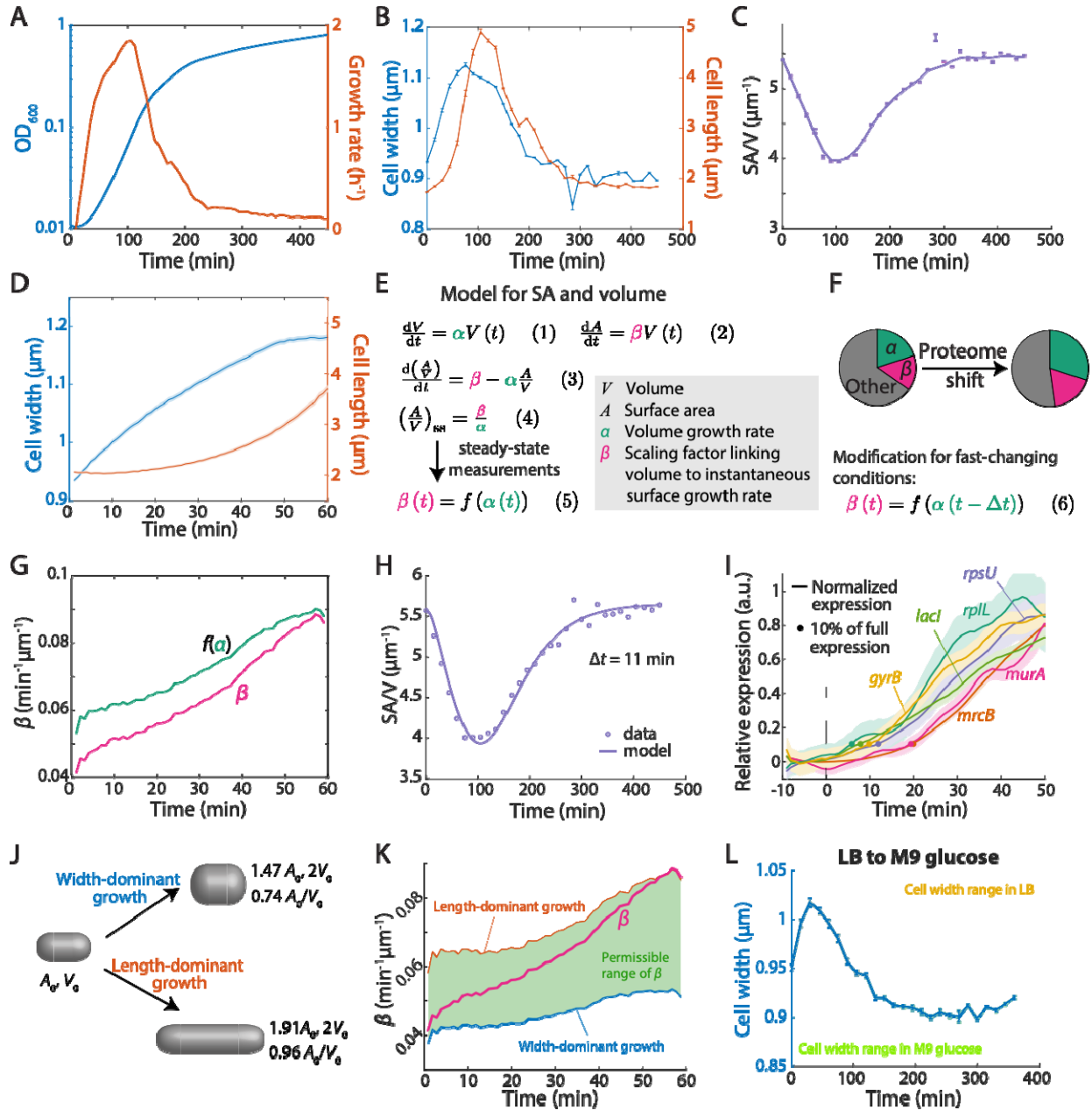
671   Figure 1: A time-delay model explains the relative dynamics of surface area and

672   volume synthesis in batch cultures.

673   A) Growth curve and the corresponding growth rate of an *E. coli* MG1655 batch

674   culture after diluting the overnight culture 1:200 into fresh LB. Growth rate peaks

675   at ~100 min post-dilution, and then slowly decreases.

676   B) Shape growth curves (cell width and length as a function of time) for the same

677   culture in (A). Cell width starts to increase earlier compared to length. Data

678   points are mean ± standard error of mean (s.e.m.) for $n > 200$ single cells.

679   C) SA/V as a function of time for the same culture in (B). SA/V decreased as cells

680   resume growth, and then slowly increased back to the initial value when cell

681   growth slowed down. Data points are mean ± s.e.m. with $n > 200$ single cells, and

682   the line is smoothed as a guide to the eye.

683   D) Single-cell time-lapse imaging of stationary-phase MG1655 cells diluted onto an

684   agarose pad containing fresh LB. Each cell exhibited similar width and length

685   dynamics as in the bulk culture in (B). Solid lines and the corresponding shaded

686   areas are mean ± s.e.m. with $n > 100$ single cells.

687   E) A conceptual model for SA/V regulation in cells. The synthesis rates of both

688   surface and volume scale with current cell volume (Eq. 1,2), predicting that the

689   time derivative of A/V depends on α, β, and the current A/V (Eq. 3). Steady state

690   A/V is therefore dictated by the ratio between β and α (Eq. 4). Using previous

691   experimental steady-state SA/V measurements, β can be parameterized as a

692   function of α in steady state (Eq. 5).

693   F) Given that changes in growth rate (α) are accompanied by shifts in proteome

694   composition, our model assumes that the shift is more heavily weighted toward

695   cytoplasmic components than surface area components, thereby causing a

696   delayed change in β, which can be approximated by introducing a constant time

697   delay in the function relating β to α (Eq. 6).

698   G) From the single-cell data in (D), the experimentally measured β exhibited a delay

699   of approximately 10 min compared to the steady-state β determined by Eq. 5 (i.e.

700       $f(\alpha)$).

701   H) Fitting our time-delay model to the experimental data in (C) with $\Delta t = 11$ min

702   yielded an excellent fit.

703   I) Protein expression levels were measured using GFP fused to the respective

704   promoters and normalized from 0 to 1. The cytoplasmic proteins increased in

705   expression ~10 min earlier than the cell-wall synthesis proteins. Dots represent

706   the time points at which expression had increased by 10%. Data are mean ±

707   standard deviation (S.D.) with $n > 100$ cells.

708   J) For a rod-shaped cell starting with surface area A_0 and V_0, doubling its volume

709   by expansion in width costs 47% increase in surface area (top), whereas

710   expansion in length requires a 91% increase in surface area (bottom). Therefore,

711   an increase in width minimizes the surface area requirement for a given amount

712   of volumetric growth.

713   K) Given the geometry and instantaneous growth rate (α) of cells in (D), to maintain

714   rod-like shapes, only a certain range of β values are permissible (green;

715   Methods). The actual value of β started close to its minimal possible value,

716   characterizing a widening-dominant growth mode; by 60 min, β reached its

717   maximum possible value, transitioning to an elongation-dominant growth mode.

718   L) Dilution of stationary-phase cells grown in LB into M9 glucose caused increased

719   cell width, despite the fact that cells continuously passaged in M9 glucose always

720   had lower cell width than the LB-grown stationary-phase cells. Data are mean ±

721   s.e.m. with $n > 100$ cells.
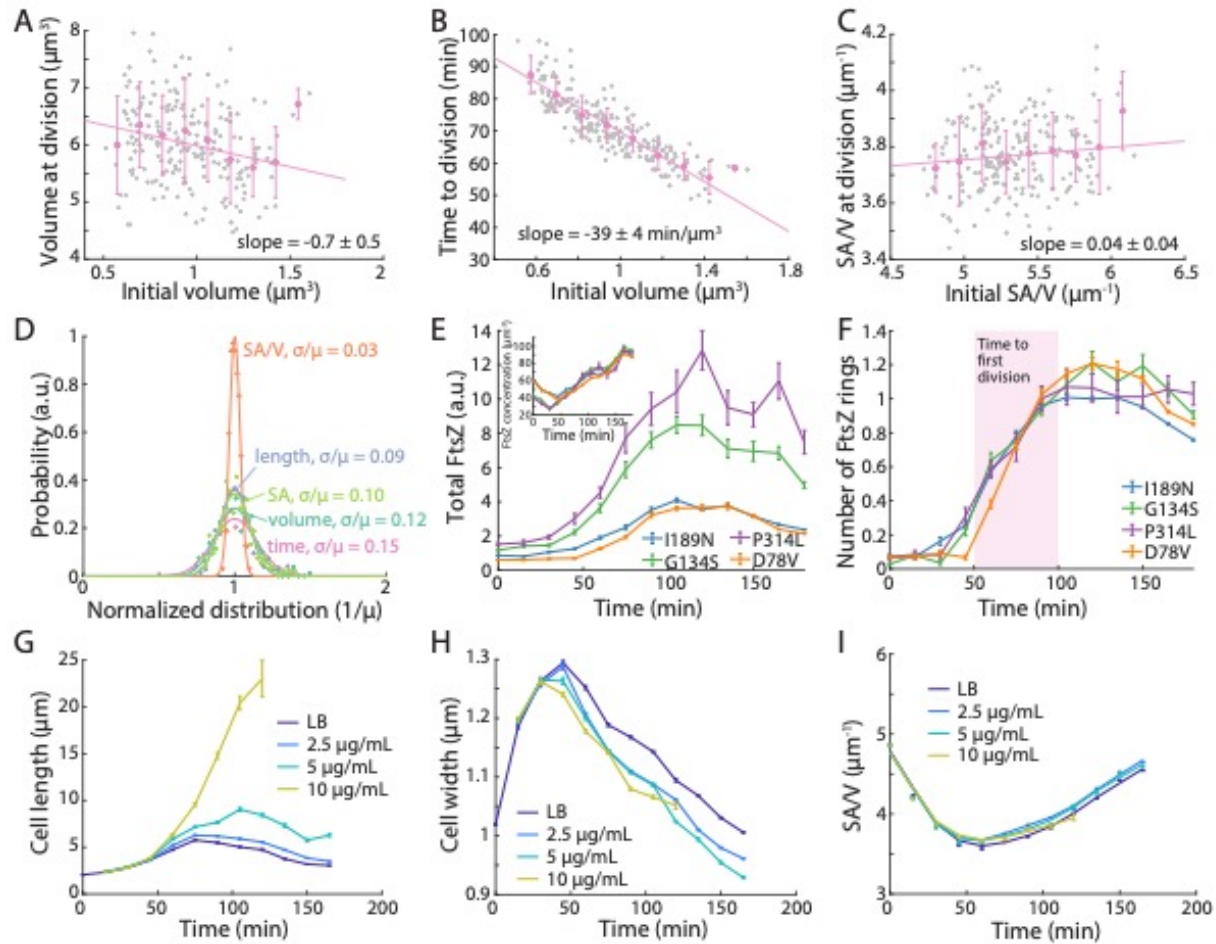
Figure 2: SA/V dynamics are correlated with cell division, and are conserved across cell morphologies.

A) For cells exiting stationary phase, the volume at the first division was negatively correlated with the starting volume, deviating from the "sizer" and "adder" models. Gray dots are data points for n = 209 individual cells, and pink data points are binned mean and S.D. values, which were fit to a linear model, leading to a slope of -0.7 ± 0.5 (mean ± s.e.m., Pearson's r = -0.22, p = 0.001, Student's t-test).

731   B) The time to first division after stationary-phase exit was negatively correlated

732   with the initial cell volume with a slope of -39 ± 4 min/μm^3 (mean ± s.e.m.,

733   Pearson's r = -0.86, $p < 10^{-5}$, Student's t-test), indicating that the first division was

734   not regulated by time spent in fresh media. Gray dots are data points for $n = 209$

735   individual cells, and pink data points are binned mean and S.D. values.

736   C) The SA/V at the first division was largely constant and independent of the initial

737   SA/V of the stationary-phase cell. Gray dots are data points for $n = 209$ individual

738   cells, and pink data points are binned mean and S.D. values, which were fit to a

739   linear model, leading to a slope of -0.04 ± 0.04 (mean ± s.e.m., Pearson's r = 0.11, p

740   = 0.12, Student's t-test).

741   D) Normalized distributions of cell length, SA, volume, SA/V, and time at first

742   division after stationary-phase exit. SA/V had by far the narrowest distribution,

743   suggesting that the first cell division after exiting stationary phase occurs

744   precisely at a fixed SA/V.

745   E) FtsZ abundance was measured as total fluorescence intensity inside cells. The

746   dynamics of FtsZ regulation were similar across mutants. FtsZ abundance did

747   not change in the first ~50 min, then increased to a maximum at ~100 min. Inset:

748   While larger cells tended to have lower SA/V and higher FtsZ levels, FtsZ

749   concentrations were highly similar across shape mutants. Data points are mean ±

750   s.e.m. with $n > 200$ cells.

751   F) All strains started without FtsZ rings and did not possess a ring until ~50 min

752   post-dilution, consistent with the onset of first divisions after stationary phase

753   exit (B). By 100 min, virtually all cells had ~1 FtsZ ring. Data points are mean ±

754   s.e.m. with $n > 200$ cells.

755   G-I) Shape growth curves of *E. coli* MG1655 cells treated with sub-lethal

756   concentrations of cephalexin. Cephalexin causes a dose-dependent increase in

757   cell length (G), accompanied by decreased cell width (H). The increased lengths

758   and decreased widths precisely maintain SA/V for all conditions (I), suggesting

759   that SA/V is robust to perturbations in cellular dimensions. Data points are mean

760   ± s.e.m. with $n > 200$ cells.
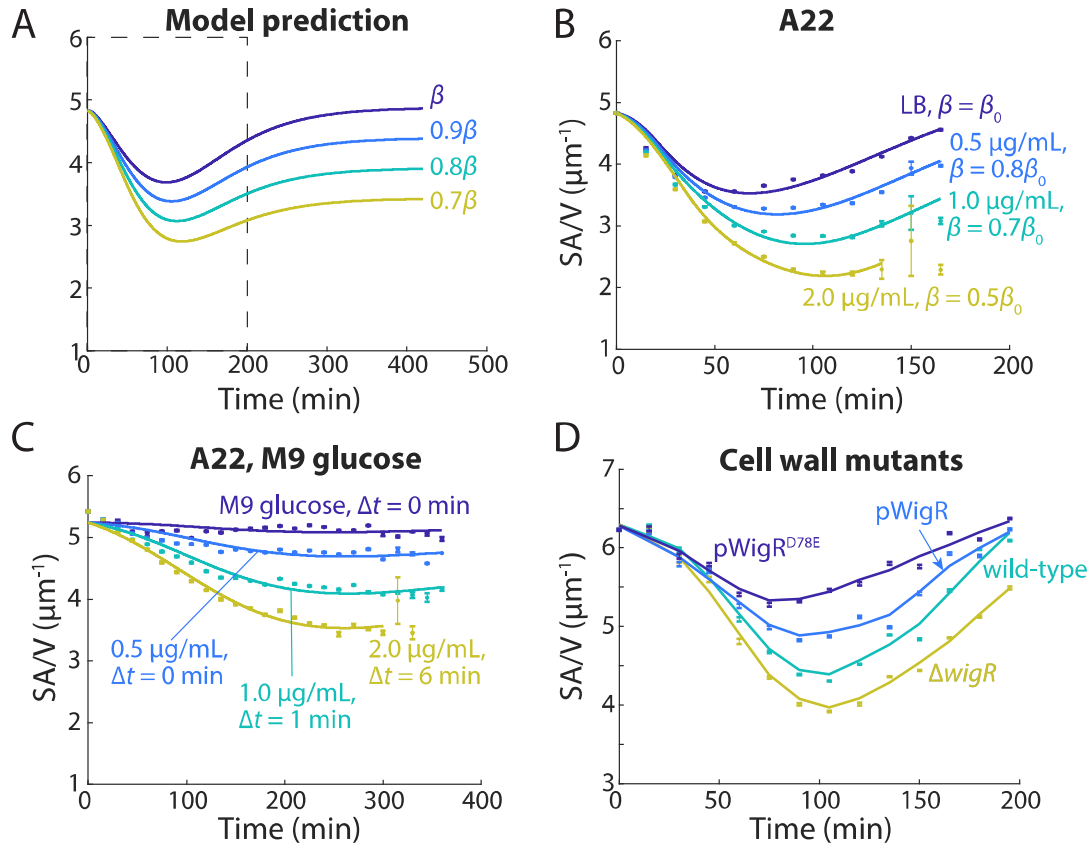
Figure 3: Time-delay model quantitatively predicts SA/V decreases due to inhibiting cell-wall synthesis.

A) The model predicts that decreasing β results in decreased SA/V over time.

B) Shape growth curves during A22 treatment in LB exhibited similar SA/V dynamics as predicted in (A).

C) Shape growth curves with A22 treatment in M9 glucose also exhibited decreases in SA/V, even though SA/V remained largely constant without A22. Higher A22 concentrations also led to non-zero Δt, indicating that cells must adjust their proteome under inhibition of cell-wall synthesis.

771   D) Shape growth curves for *V. cholerae* cell-wall synthesis mutants. Overexpression

772   of WigR (pWigR, pWigR^{D78E}), which up-regulates cell wall synthesis without

773   affecting growth, increased SA/V. By contrast, Δ*wigR* cells have down-regulated

774   cell-wall synthesis and exhibited lower SA/V.
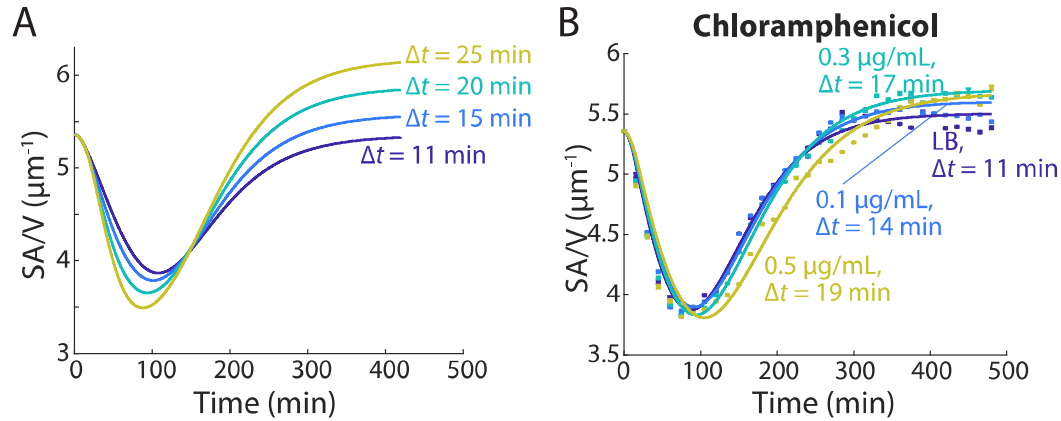
Figure 4: Inhibiting translation increases the time delay between volume and surface growth.

A) The model predicts that higher Δt leads to lower SA/V in log phase, but higher SA/V when cells enter stationary phase again.

B) Shape growth curves of MG1655 cells treated with low levels of chloramphenicol. The dose-dependent SA/V dynamics were consistent with model predictions, and model fitting resulted in longer Δt at higher doses. Data points are mean ± s.e.m., with $n > 200$. Solid lines are best fits to the time-delay model.

795

796 **Data availability statement**

797 The datasets generated during and/or analysed during the current study are available

798 from the corresponding author on reasonable request.

799   **References**

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917

A — OD$_{600}$ (blue) and Growth rate (h^{-1}) (orange) vs Time (min)

B — Cell width (μm) (blue) and Cell length (μm) (orange) vs Time (min)

C — SA/V (μm^{-1}) vs Time (min)

D — Cell width (μm) (blue) and Cell length (μm) (orange) vs Time (min)

E — Model for SA and volume

$$\frac{\mathrm{d}V}{\mathrm{d}t} = \alpha V(t) \quad (1) \qquad \frac{\mathrm{d}A}{\mathrm{d}t} = \beta V(t) \quad (2)$$

$$\frac{\mathrm{d}\left(\frac{A}{V}\right)}{\mathrm{d}t} = \beta - \alpha\frac{A}{V} \quad (3)$$

$$\left(\frac{A}{V}\right)_{\mathrm{ss}} = \frac{\beta}{\alpha} \quad (4)$$

steady-state measurements

$$\beta(t) = f(\alpha(t)) \quad (5)$$

V	Volume
A	Surface area
α	Volume growth rate
β	Scaling factor linking volume to instantaneous surface growth rate

F — Proteome shift

Modification for fast-changing conditions:

$$\beta(t) = f(\alpha(t - \Delta t)) \quad (6)$$

G — β (min^{-1}μm^{-1}) vs Time (min); $f(\alpha)$, β

H — SA/V (μm^{-1}) vs Time (min); $\Delta t = 11$ min; data, model

I — Relative expression (a.u.) vs Time (min); Normalized expression, 10% of full expression; *rpsU*, *rplL*, *lacI*, *gyrB*, *mrcB*, *murA*

J — Width-dominant growth: 1.47 A_0, 2V_0, 0.74 A_0/V_0; Length-dominant growth: 1.91A_0, 2V_0, 0.96 A_0/V_0; A_0, V_0

K — β (min^{-1}μm^{-1}) vs Time (min); Length-dominant growth, β, Permissible range of β, Width-dominant growth

L — LB to M9 glucose; Cell width (μm) vs Time (min); Cell width range in LB, Cell width range in M9 glucose

A slope = -0.7 ± 0.5

B slope = -39 ± 4 min/μm³

C slope = 0.04 ± 0.04

D SA/V, σ/μ = 0.03; length, σ/μ = 0.09; SA, σ/μ = 0.10; volume, σ/μ = 0.12; time, σ/μ = 0.15

E I189N, G134S, P314L, D78V

F Time to first division; I189N, G134S, P314L, D78V

G LB, 2.5 μg/mL, 5 μg/mL, 10 μg/mL

H LB, 2.5 μg/mL, 5 μg/mL, 10 μg/mL

I LB, 2.5 μg/mL, 5 μg/mL, 10 μg/mL

A — **Model prediction**

β
0.9β
0.8β
0.7β

B — **A22**

LB, $\beta = \beta_0$
0.5 µg/mL, $\beta = 0.8\beta_0$
1.0 µg/mL, $\beta = 0.7\beta_0$
2.0 µg/mL, $\beta = 0.5\beta_0$

SA/V (μm^{-1})

C — **A22, M9 glucose**

M9 glucose, $\Delta t = 0$ min
0.5 µg/mL, $\Delta t = 0$ min
1.0 µg/mL, $\Delta t = 1$ min
2.0 µg/mL, $\Delta t = 6$ min

SA/V (μm^{-1})

D — **Cell wall mutants**

pWigR^{D78E}
pWigR
wild-type
$\Delta wigR$

SA/V (μm^{-1})

Time (min)

A

SA/V (μm^{-1}) vs Time (min)

$\Delta t = 25$ min
$\Delta t = 20$ min
$\Delta t = 15$ min
$\Delta t = 11$ min

B **Chloramphenicol**

SA/V (μm^{-1}) vs Time (min)

0.3 μg/mL, $\Delta t = 17$ min
LB, $\Delta t = 11$ min
0.1 μg/mL, $\Delta t = 14$ min
0.5 μg/mL, $\Delta t = 19$ min