Spatiotemporal patterns of urbanization in three Swiss urban agglomerations: insights from landscape metrics, growth modes and fractal analysis

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Abstract

Urbanization is currently a global phenomenon that has become the most important form of landscape change and is increasingly affecting biodiversity and ecosystem functions. In order to evaluate the impacts of urbanization and inform urban planning, it is important to understand the spatiotemporal patterns of land use change associated to urbanization. This paper exploits three different frameworks, namely landscape metrics, urban growth modes and fractal analysis to characterize the spatiotemporal patterns of urbanization of the Swiss urban agglomerations of Zurich, Bern and Lausanne. The land use inventory provided by the Swiss Federal Statistical Office was used to assemble four temporal snapshots from 1980 to 2016 at the extent of the urban agglomerations. The time series of landscape metrics generally supports the diffusion and coalescence model of urban growth, with Zurich exhibiting most characteristics of coalescence while Bern and Lausanne seem to be at the transition between diffusion and coalescence. Nevertheless, the analysis of the urban growth modes suggest that leapfrog development occurs at all periods, which contributes to an increasing fragmentation of natural patches and maintains the fractal configuration of the landscape. The discussion reviews potential explanations for the observed landscape changes, and concludes with some planning implications.

Keywords: urbanization; land use change; spatial pattern analysis; landscape metrics; diffusion and coalescence hypothesis; urban growth modes; fractals; scaling; complexity

Introduction   1

The last centuries have seen an unprecedented growth of urban areas, which has   2
resulted in dramatic conversion of natural land and profound changes in landscape   3
patterns and the ecosystem functions that they support [1]. The combination of current 4
demographic prospects and the observed trends of decreasing urban densities suggest 5
that the global amount of land occupied by cities might increase threefold [2].   6
Quantifying urban landscape patterns in space and time is an important and necessary 7
step to understand the driving forces and ecological impacts of urbanization [3].   8
    Recent decades have witnessed an increasing number of studies of the spatiotemporal 9
patterns of land use change associated to urbanization [4–11]. Initial attempts to   10
synthesis suggested that urbanization can be characterized as a two-step alternating 11

process of diffusion and coalescence [4,6], nonetheless, subsequent studies challanged the empirical validity of such hypothesis. On the one hand, Jenerette and Potere [7] examined the spatiotemporal patterns of land use change of a sample of 120 cities distributed throughout the world from 1990 to 2000, and determined that overall, urbanization leads to fragmented landscapes with more complex and heterogeneous structures. On the other hand, Li et al. [9] determined that the two-phase diffusion and coalescence model can be over-simplistic and that urbanization might be better characterized by means of three growth modes, namely infilling, edge expansion and leapfrogging, which operate simoultaneously while alternating their relative dominance.

Paralleling the above studies, approaches from the complexity sciences have provided novel insights into the spatial organization that underpins contemporary cities [12]. Like many other complex systems, cities exhibit morphological traits that are consistent with fractal geometry and reflect the self-organizing nature of the processes that occur upon them [13]. Although the scaling relationships of fractal geometry suggest the existence of strong morphological regularities over a wide variety of cities and regions [14–16], their meaning in the context of the spatiotemporal patterns of urbanization remains unclear [17–19].

This paper intends to evaluate the spatiotemporal patterns of land use change observed in three of the largest Swiss urban agglomerations from three different perspectives, namely landscape metrics, urban growth modes and fractal analysis. The objective of this paper is twofold. The first is to assess to test whether the spatiotemporal evolution of the three agglomerations conform to the diffusion and coalescence dichotomy, the second is to explore how the three adopted perspectives complement each other. The results will serve to discuss planning implications regarding the desirability of the recent densification policies adopted in Switzerland.

Materials and Methods

Study area

Switzerland is a highly developed country in central Europe with a population distributed into several interconnected mid-sized cities and a large number of small municipalities. Mainly because of the country's topography, most urban settlements are located in its Central Plateau region, which accounts for about one third of the total Swiss territory, The Central Plateau is characterized by elevations that range from 400 to 700m, a continental temperate climate with mean annual temperatures of 9-10 °C and mean annual precipitation of 800-1400 mm, and a dominating vegetation of mixed broadleaf forest.

In line with the country's federalist government structure, the Swiss spatial planning system is distributed between the federal state, the 26 cantons and 2495 municipalities. The federal state specifies the framework legislation and coordinates the spatial planning activities of the cantons, while cantons check the compliance of municipal development plans with cantonal and federal laws. With some exceptions, municipal administrations are in charge of their local development plans, namely the land use plan and building ordinance, and might therefore be viewed as the most important spatial planning entities. While the Federal Statue on regional planning of 1979 limited the number of new buildings constructed outside the building zones, built-up areas have since increased continuously, mainly because the municipalities can designate new building zones almost entirely autonomously [20]. A major revision of the Federal Statue was accepted in 2013, which limits the amount of building zones that municipalities can designate and encourages infill development and densification by means of tax incentives. Forecasts based on the current urbanization trends predict

significant increases of urban land use demands over the next decades, mostly at the   61
expense of agricultural land located at the fringe of existing urban agglomerations [21].   62
  Given that a significant part of the cross-border urban agglomerations of Geneva and   63
Basel (the second and third largest in Switzerland) lie beyond the Swiss boundaries [22],   64
in order to ensure coherence of the land use/land cover data (see the section below),   65
this study comprises only three of the five largest Swiss urban agglomerations, namely   66
Zurich, Bern and Lausanne [23]. As shown in Figure 1, the three agglomerations have   67
undergone important population growth over the last 30 years, especially during the   68
most recent years and at the agglomeration extent. With a total population over 1.3   69
million and land area of 1305 km^2 (1038 hab/km^2), Zurich is the largest Swiss urban   70
agglomeration. As a leading global city and one of the world's largest financial centers,   71
Zurich has the country's largest airport and railway station, and also hosts the largest   72
Swiss universities and higher education institutions. Bern is the capital of Switzerland   73
and fourth most populous urban agglomeration in Switzerland, with a total population   74
of 410000 inhabitants and occupying a land area of 783 km^2 (531 hab/km^2). As the   75
fifth largest Swiss urban agglomeration and the second most important student and   76
research center after Zurich, the Lausanne agglomeration has a total population of   77
409000 inhabitants over a land area of 773 km^2 (537 hab/km^2). Given its larger   78
population growth rate, Lausanne is likely to soon surpass Bern and become the fourth   79
largest urban agglomeration in Switzerland. Overall, the three urban agglomerations are   80
characterized by a pervasive public transportation system and a highly developed   81
economy, with a 85% of the employment devoted to the tertiary sector.   82
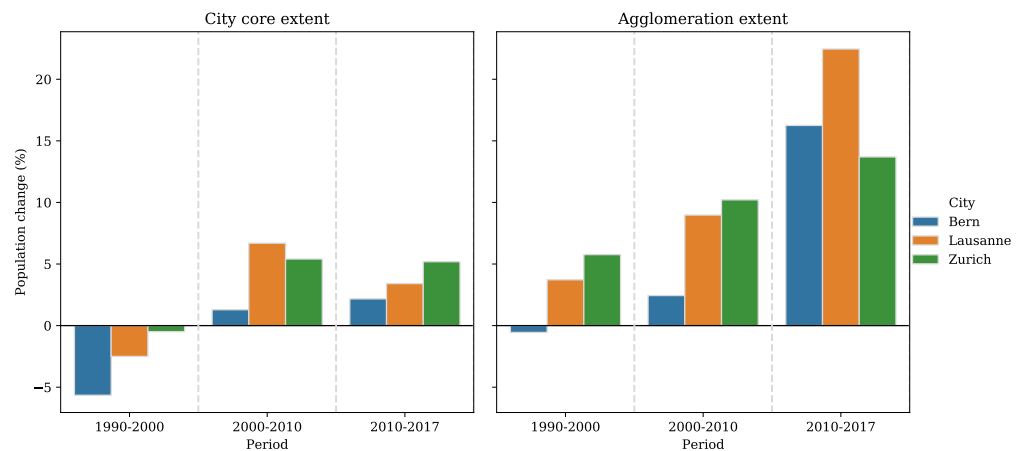
Figure 1. Population change of the three regions of study at the city core (left) and agglomeration extent (right) over the periods of 1990-2000, 2000-2010 and 2010-2017. Data from the Urban Audit collection [23].

Data sources   83

The Swiss Federal Statistical Office (SFSO) provides an inventory of land statistics   84
datasets [24], namely a set of land use/land cover maps for the national extent of   85
Switzerland, which comprise 72 base categories. Four datasets have been released for   86
1979/85, 1992/97, 2004/09 and 2013/18[1], at a spatial resolution of one hectare per pixel.   87
The pixel classification is based on computer-aided interpretation of satellite imagery,   88

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[1]The exact dates of each surveying period 1979/85, 1992/97, 2004/09 and 2013/18 are determined according to the production process of the national maps and vary accross the Swiss territory [24]

which includes special treatment and field verification of pixels where the category attribution is not clear.

The SFSO land statistics datasets have been used to produce a series of categorical maps for each urban agglomeration and time period. In order to process the SFSO datasets in an automated and reproducible manner, an open source reusable toolbox to manage, transform and export categorical raster maps has been developed in Python [25]. The boundaries of each urban agglomeration have been adopted from the definitions provided also by the SFSO [22], which comprise multiple municipalities and have been established in consideration of population density, proximity between centers, economic activities and commuting behavior. As stated above, Geneva and Basel are excluded from this study because a significant portion of their urban agglomeration lies beyond the extent covered by the SFSO land statistics inventory, namely the administrative boundaries of Switzerland. The spatiotemporal evolution of the urban footprint for the three selected urban agglomerations (i.e., Bern, Lausanne and Zurich) over the study period (i.e., 1980-2016[1]) is displayed in Figure 2.

Quantifying spatiotemporal patterns of urbanization

While a plentiful collection of landscape metrics can be find in the literature, many of them are highly correlated with one another. As a matter of fact, Riitters et al. [26] found that the characteristics discerned by 55 prevalent landscape metrics could be reduced to only 6 independent factors. On the other hand, landscape metrics can be very sensitive to the resolution and the extent of the maps. However, several metrics empirically exhibit consistent responses to changing scales that conform to predictable scaling relations [27, 28]. Based on such remarks, and in order to enhance comparability with other studies, ten landscape metrics have been selected for the present study, whose details are listed in Table 1. While complying with the FRAGSTATS v4 definitions [29], the landscape metrics have been computed with the open source library PyLandStats [30]. Like in most of the related studies, the categorical maps have been reclassified into urban and natural classes, and the metrics have computed at the urban class level, namely aggregating their values across all the urban patches of the landscape. The only exceptions are the contagion (CONTAG) and Shannon's diversity index (SHDI), which can only be computed at the landscape level, namely considering all the landscape classes (urban and natural in the this study). Pixels that correspond to land unavailable for development, such as water bodies, have been excluded from the computation of the metrics.

Modes of urban growth

In addition to the conventional landscape metrics, which are computed over a single snapshot of a landscape, Liu et al. [31] proposed a quantitative method to classify the types of urban growth occurring between two time points. To that end, for each new urban patch, the Landscape Expansion Index (LEI) is computed as[2]:

$$LEI = \frac{L_c}{P} \tag{1}$$

where L_c denotes the length of the interface between the new urban patch and pre-existing urban patches, and P is the perimeter of the new urban patch. Then, the type urban growth attributed to a new urban patch will be identified as infilling when $LEI > 0.5$, edge-expansion when $0 < LEI \leq 0.5$ and leapfrog when $LEI = 0$. As suggested by Li et al. [9], the relative dominance of each growth mode between two

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[2]The LEI definition of (1) is taken from Nong et al. [11] and is equivalent to the initial formula proposed by Liu et al. [31]
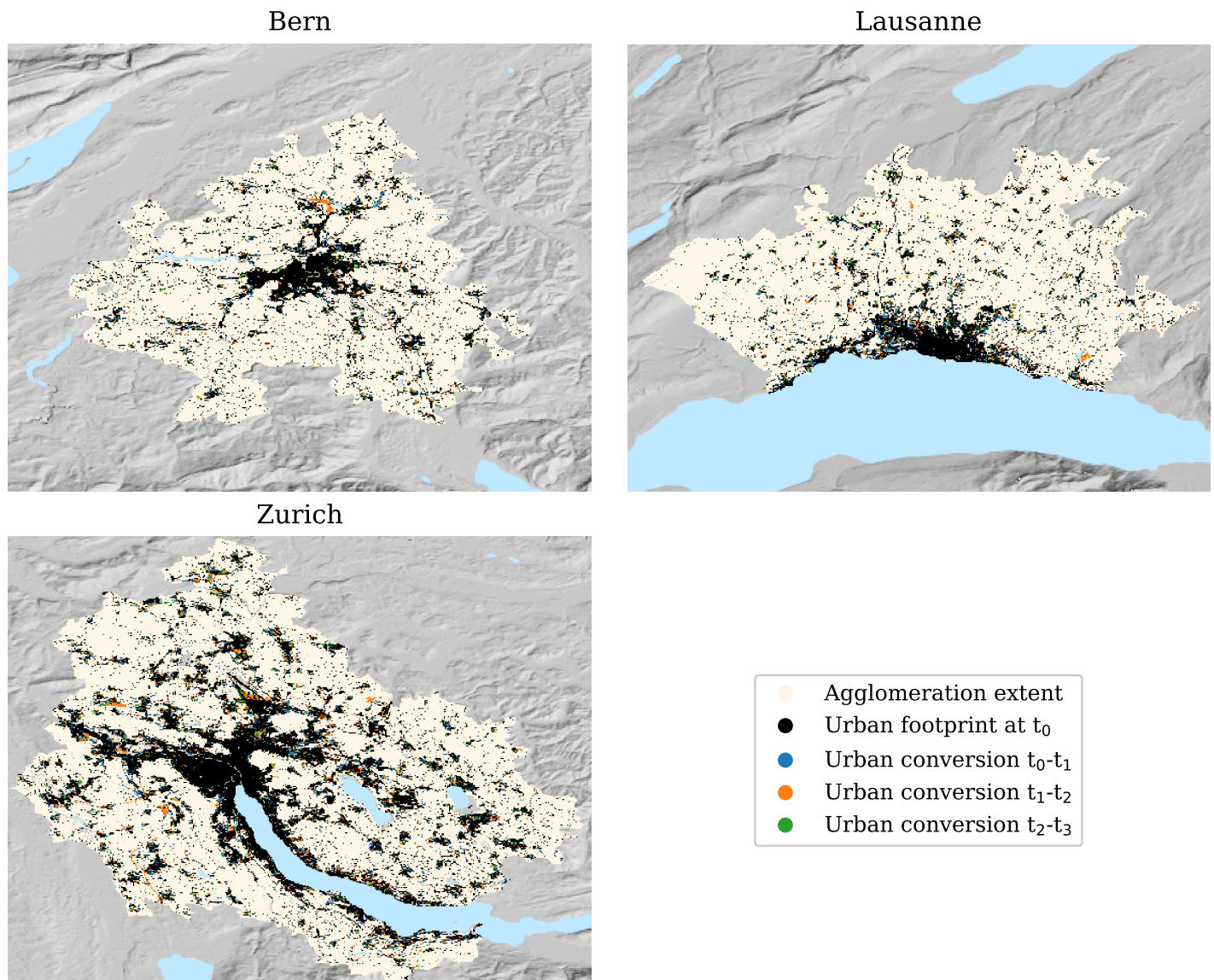
Figure 2. Evolution of urban patches of the three urban agglomerations throughout their respective periods of study. The times t_0, t_1, t_2 and t_3 correspond to 1981, 1993, 2004 and 2013 for Bern; 1980, 1990, 2005 and 2014 for Lausanne and 1982, 1994, 2007 and 2016 for Zurich

landscape snapshots can be evaluated both in terms of number and the area of new urban patches that are attributed to each growth mode.

Fractal aspects of urban patterns

Despite their complex and irregular appearance, cities comply with well-defined order principles that can be characterized quantitatively by means of fractal geometry [14, 15]. Two main characteristics of fractal structures are of particular interest in the context of the study of urbanization and land use change [16]: the area-radius scaling and the size-frequency distribution of urban patches.

Table 1. Selected landscape metrics to quantify the spatiotemporal patterns of urbanization. A more thorough description can be found in the documentation of the software FRAGSTATS v4 [29]

Metric name (abbrev.)	Level	Category	Description
Percentage of landscape (PLAND)	Class	Area and edge	Percentage of landscape, in terms of area, occupied by patches of a given class
Mean patch size (MPS)	Class and landscape	Area and edge	Mean patch size
Largest patch index (LPI)	Class and landscape	Area and edge	Percentage of the landscape occupied by the largest patch
Patch density (PD)	Class and landscape	Aggregation	The number of patches per area unit
Edge density (ED)	Class and landscape	Area and edge	Sum of the lengths of all edge segments per area unit
Area-weighted mean fractal dimension (AWMFD)	Class and landscape	Shape	Mean patch fractal dimension weighted by relative patch area
Mean euclidean nearest neighbor distance (ENN)	Class and landscape	Aggregation	Mean patch shortest edge-to-edge distance to the nearest neighboring patch of the same or different class
Landscape shape index (LSI)	Class and landscape	Aggregation	Standardized ratio of edge length to area
Contagion (CONTAG)	Landscape	Aggregation	Metric that measures the extent to which patches of the same class are spatially aggregated in the landscape
Shannon's diversity index (SHDI)	Landscape	Diversity	Metric that measures the diversity of patch types determined by both the number of different patch types and the proportional distribution of area among patch classes.

Area-radius scaling   The relationship between the built-up area of an urban agglomeration and the distance from the main city center has been shown (e.g., Frankhauser [14]) to empirically conform to relationships of the form:

$$A(r) \sim r^D \tag{2}$$

where A denotes the total area of the urban built-up extent that lays within a distance r from the city center, and D corresponds to the radial dimension, analogous to the fractal dimension of two-dimensional complex objects such as Sierpinski carpets. Although the measure might not be appropriate for urban agglomerations with multiple important centers, Frankhauser [14] found extensive evidence that most contemporary cities could be approximated through (2), with the value of D consistently falling between 1.9 and 2.0. On the other hand, following initial observations by Frankhauser [32], White and Engelen [13] suggested that the area-radius scaling could be better approximated throguh two values of D, a first steeper one for small values of r, reflecting an inner zone where urbanization was essentially complete, and a second lower slope for the outer zone that is still undergoing urbanization.

Size-frequency distribution of urban patches   Contemporary urban agglomerations are configured by numerous patches of urban land use. If such configuration is fractal, there must be no characteristic patch size, and thus the relationship between the size of an urban patch and the number of patches of that size found in the agglomeration must follow a power-law scaling relationship of the form:

$$N(s) \sim s^{-\alpha} \tag{3}$$

where $N(s)$ is the number of patches of size s, and the scaling exponent α is the patch size-frequency dimension [13].

Results   162

Time series of landscape metrics   163

The computed time series of landscape metrics for the agglomerations of Bern,   164
Lausanne and Zurich are displayed in Figure 3 (see also Code S1). As suggested by Wu   165
et al. [27, 28], the chosen landscape metrics show predictable responses to changes to the   166
map extent (see Code S2). Therefore, the reminder will only consider the values   167
computed at the extent of the urban agglomeration.   168
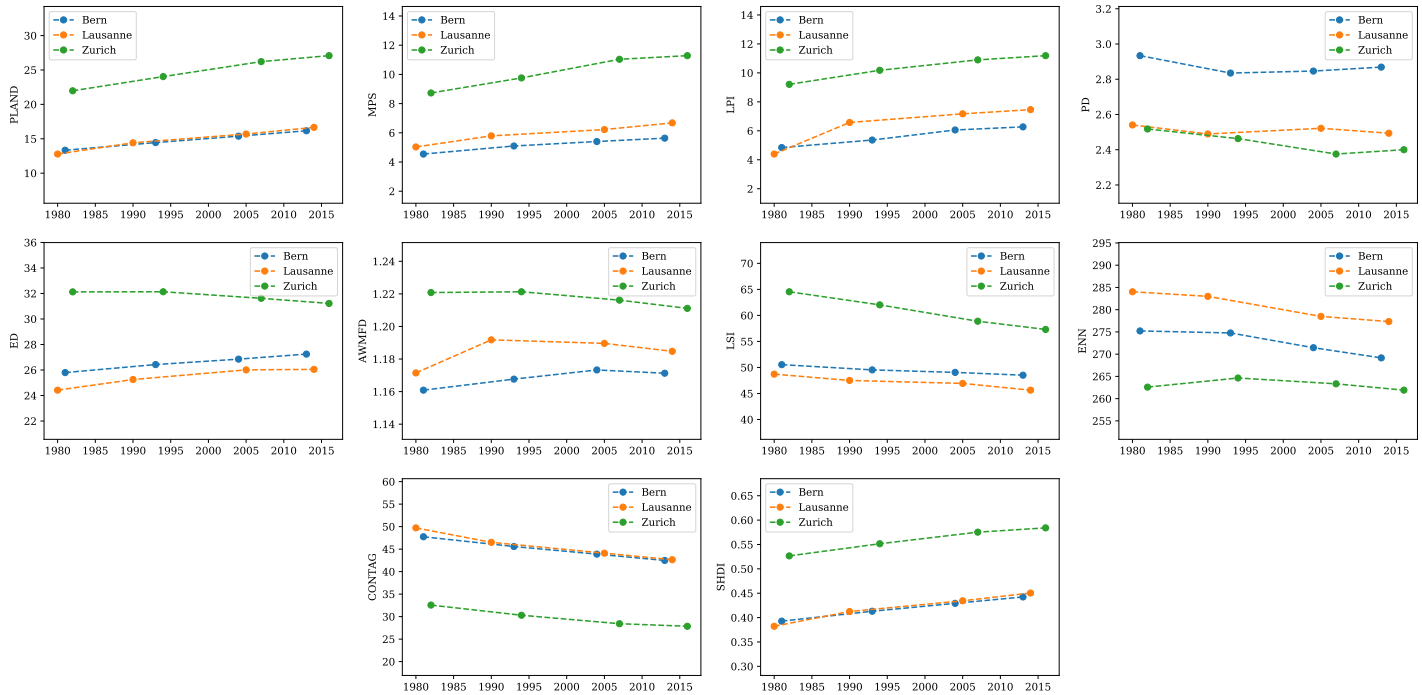
Figure 3. Time series of landscape metrics. The eight metrics of the two upper rows are computed at the urban class level, that is, aggregating the values computed for each urban patch. The two metrics of the lower row are computed at the landscape level, that is, considering the patches of all the classes present within the landscape (urban and natural in this case)

The proportion of landscape occupied by urban patches, represented by PLAND has   169
increased monotonically for the three agglomerations. Bern and Lausanne show almost   170
indistinguishable trends, starting from a 13% in the early 1980s and surpass the 16% in   171
the last snapshot of 2013 and 2014 respectively. Zurich shows a parallel tendence with   172
the percentage of urbanized land increasing from 22% in 1982 to a 27% in 2016.   173
Similarly, MPS and LPI also show a monotonic increase, parallel among the three   174
agglomerations, but again with higher values for Zurich. Such trends are overall   175
characteristic of coalescence stages and the higher values observed in Zurich are   176
consistent with its higher population density.   177
On the other hand, PD reveals more complex and idiosyncratic trends, which   178
suggest that new urban patches can basically emerge at any period. The Bern   179
agglomeration shows the highest PD values, which is consistent with its MPS and LPI   180
being the lowest among the three agglomerations and denotes a landscape configured by   181
numerous small urban patches. Despite the irregularity of PD, ED shows more   182
consistent tendencies of increase in Bern and Lausanne and decrease in Zurich. From   183

the perspective of the diffusion and coalescence hypothesis, Bern and Lausanne are   184
seemingly undergoing a diffusion stage, whereas the decrease of Zurich is more   185
characteristic of coalescence. The flat evolution of ED during the first period in Zurich   186
suggests a transition from diffusion to coalescence, which is also observed in Lausanne   187
during the last period. This postulate is also supported by the trend of AWMFD, which   188
in Zurich is almost identical to that of ED, and shows an unimodal pattern for   189
Lausanne, also characteristic of a transition from diffusion to coalescence. The decline   190
of the AWMFD observed during the last period in Bern also suggest that albeit tardier   191
than its counterparts, Bern might also be undergoing a shift towards coalescence. The   192
monotonic decrease of the LSI reveals that the landscape is becoming less edgy, which is   193
also characteristic of coalescence. Similarly, ENN shows an overall monotonic decrease   194
which suggests that distances between neighboring urban patches are decreasing.   195

The two metrics that operate at the landscape level, CONTAG and SHDI show   196
consistent monotonic trends which are almost identical for Bern and Lausanne. The   197
decrease of CONTAG indicates that urban and natural patches are becoming   198
increasingly disaggregated and interspersed, which is characteristic of diffusion and   199
contrasts with the hallmarks of coalescence exhibited by most of the other metrics. On   200
the other hand, the increase of SHDI denotes an increasing compositional diversity. The   201
fact that the values of CONTAG and SHDI are respectively lower and higher in Zurich   202
is mostly due to its higher proportion of urbanized landscape, which make the   203
proportional abundance of urban and natural pixels more even than in Bern or   204
Lausanne. Overall, given that only two classes (i.e., urban and natural) are considered   205
within this study, CONTAG and SHDI are almost perfectly correlated with PLAND   206
(see Code S1), because the relative abundance of each class is the main determinant of   207
the aggregation, interspersion and diversity of its patches [29].   208

Growth modes   209

The relative dominance of infilling, edge expansion and leapfrog development during the   210
period of study is displayed in Figure 4. As suggested by Li et al. [9], all three urban   211
growth modes act simultaneously. Edge-expansion is the most dominant growth mode   212
and maintains its importance throughout all agglomerations and time periods,   213
nevertheless, it tends to diminish over time. Such a decrease of edge-expansion is   214
compensated by an increasing influence of infilling. Leapfrog is by far the least dominant   215
growth mode, and its influence does not show any clear trend of increase or decrease.   216

As with landscape metrics, Bern and Lausanne show similar characteristics, namely   217
an unequivocal dominance of edge-expansion and a slight increase of the area-weighted   218
influence of infilling. On the other hand, leapfrog has very little influence in the   219
agglomeration of Zurich, while the prevalence of edge-expansion and infilling is equally   220
significant, especially in the latter periods. Like the time series of landscape metrics   221
suggest, the higher dominance of infilling observed in Zurich is characteristic of   222
coalescence. Similarly, the increasing influence of infilling in Bern and especially in   223
Lausanne are consistent with the transition from diffusion to coalescence that the   224
concave trends of ED and AWMFD seemingly indicate.   225

## Fractal aspects of urban patterns   226

The area-radius scaling and the patch size-frequency distribution of the three urban   227
agglomerations at each temporal snapshot are plotted in Figure 5 and Figure 6   228
respectively.   229


[3] https://www.openstreetmap.org/
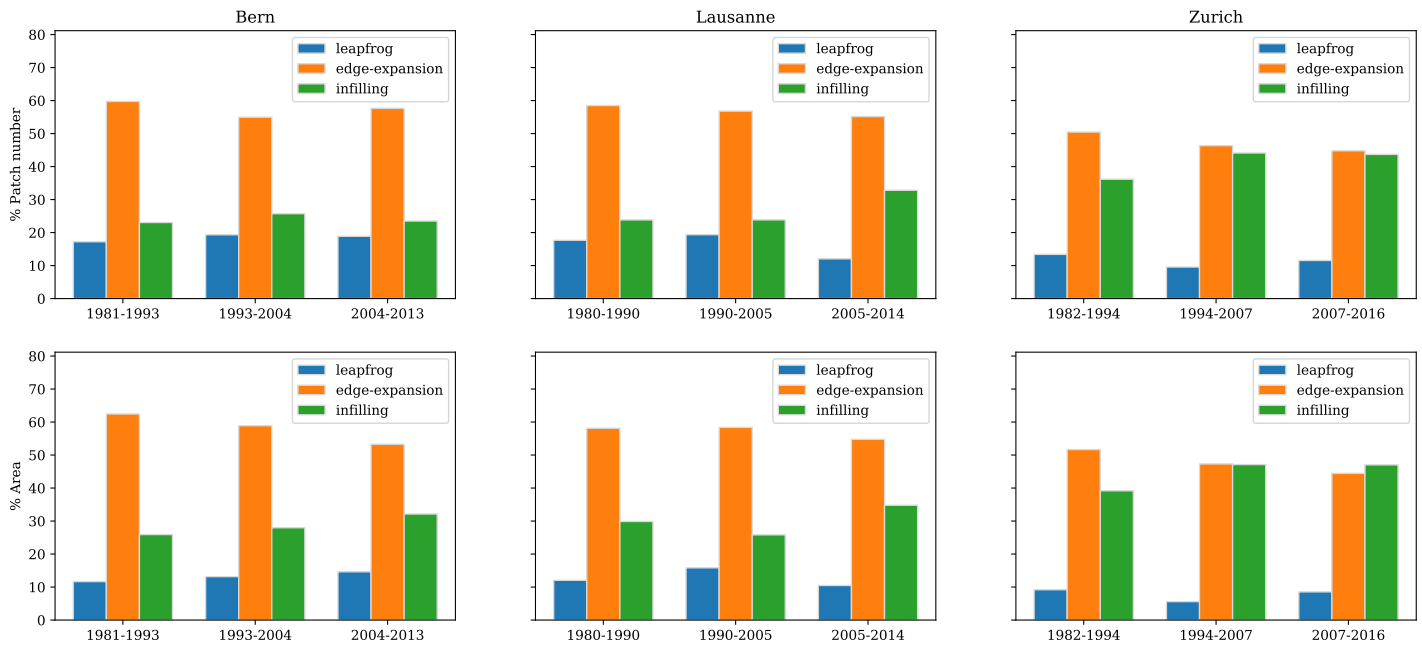
Figure 4. Changes in the relative dominance of infilling, edge expansion and leapfrog over the three time periods of each urban agglomeration in terms of number of new urban patches (upper row) and their respective area (lower row).
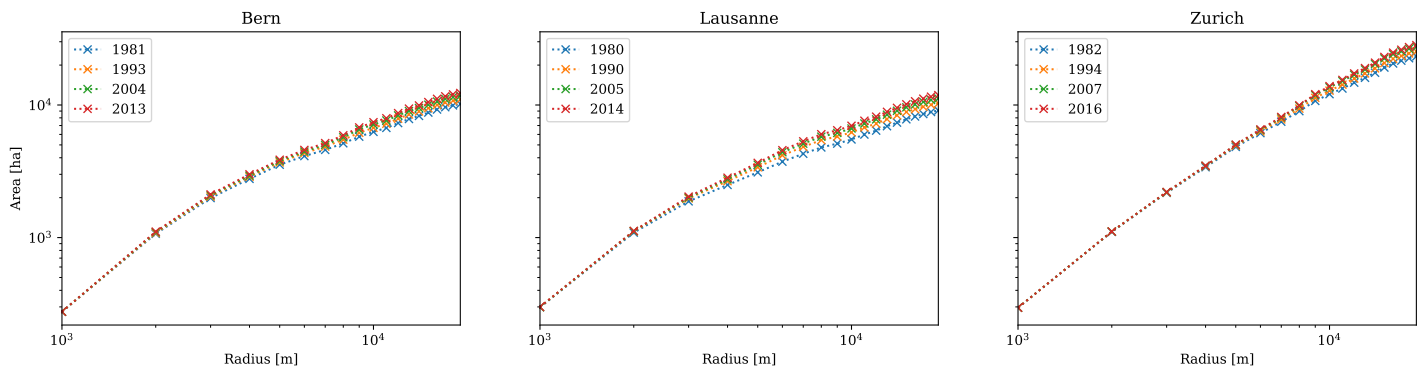
Figure 5. Area-radius scaling of the three urban agglomerations at each temporal snapshot. The relationship has been estimated by computing the total area occupied by urban land uses laying within a series of radius values (noted by the cross-shaped markers) from 1000 to 20000m, successively increasing by a step of 1000m. The reference center point has been manually retrieved from the OpenStreetMap[3]. See Code S3.

In line with the observed landscape metrics and growth modes, the urban agglomerations of Bern and Lausanne show similar scaling behavior, with a kink (located around the 3000m radial distance) separating the steeper inner urbanized zone and the outer zone with more non-urban land. The area-radius scaling of Zurich is characterized by a steeper slope with practically no appreciable kink, which denotes higher proportion of urban land uses at greater radial distances from the city center. At the same time, the curves become steeper through time in all agglomerations, which reflects how they fill the available space as urbanization unfolds. Overall, the area-radius scaling curves of Bern and Lausanne are consistent with the bifractal radial

city model [13,16]. However, the temporal evolution of their scaling curves suggests that   239
as they become more urbanized, the kink might attenuate, leading to the almost   240
straight line observed in Zurich. Such an hypothesis seems further supported by the   241
trends of the landscape metrics and growth modes reported above, which suggest that   242
the kink in the area-radius scaling curve might be characteristic of agglomerations   243
whose urban patches are still undergoing diffusion, whereas straight lines might   244
correspond to more consolidated agglomerations whose urban pathces are coalescing.   245
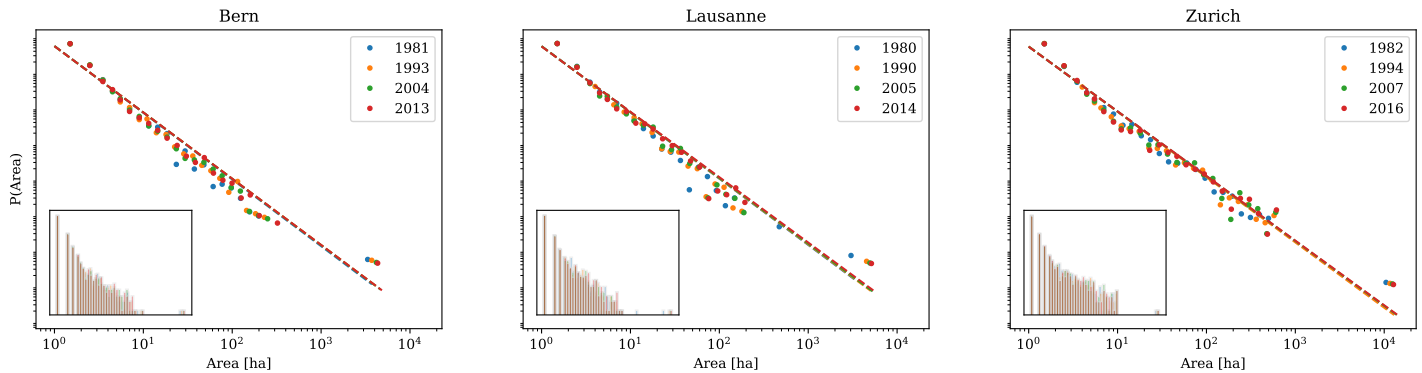
Figure 6. Size-frequency distribution of urban patches for the three urban agglomerations at each temporal snapshot. Each dot represents an observed patch, with the color code denoting the temporal snapshot to which the patch corresponds. The colored dashed lines represent the best maximum likelihood fit to a power-law distribution for all the patch sizes observed at their corresponding temporal snapshot. The insets display an histogram with logarithmic bins of the urban patch size distribution. The plots have been produced with the Python package powerlaw [33]. See Code S4.

On the other hand, the size frequency distribution of urban patches can be   246
approximated by a power-law (see Code S4), i.e., a straight line in the log-log scale,   247
with its slope reflecting the scaling exponent α of (3). The slopes of the fitted curves   248
are very stable through time for the three urban agglomerations, although they display   249
a slight tendence to decrease over time (note the smaller slope of the fit curves of latter   250
years in Figure 6 and Code S4). Such a trend reflects how urban patches are becoming   251
larger, which is in consonance with the increase of MPS observed for all the urban   252
agglomerations. Nonetheless, the overall increase of MPS is counterbalanced by the   253
emergence of new urban patches of smaller size, which seemingly contribute not only to   254
keeping the size-frequency distribution of urban patches as a power-law, but also to   255
scaling exponents that remain very stable through time. This is relatively surprising,   256
especially considering that PD — the metric that reflects the number of urban patches   257
— and the dominance of leapfrog growth show the most irregular trends.   258

Discussion   259

Testing hypothesis of urbanization patterns   260

The examination of the spatiotemporal patterns of land use change of the three Swiss   261
urban agglomerations by means of landscape metrics, growth modes and fractal scaling   262
reveal novel connections between the frameworks, which offer complementary   263
perspectives. Firstly, the time series of landscape metrics generally support the diffusion   264
and coalescence hypothesis, with Zurich, the largest Swiss urban agglomeration,   265
exhibiting most characteristics of coalescence, whereas Bern and Lausanne are seemingly   266
undergoing a transition between diffusion and coalescence. Additionally, the trend of   267

SHDI, which is not explicitly considered in the diffusion and coalescence formulation of Dietzel et al. [4], suggests that the landscape is becoming increasingly diverse in land use. However, it must be noted that SHDI is not very informative when considering only urban and natural classes, since it will be strongly correlated with the proportion of landscape occupied by urban patches (PLAND). Secondly, the temporal changes in the relative dominance of infilling, edge-expansion and leapfrog are overall consistent with the characterization of urbanization as a "spiraling process that involves three growth modes of leapfrogging, edge-expanding and infilling [where] leapfrog and infilling tend to alternate in their relative dominance while edge-expansion is likely to remain its importance throughout much of the urbanization process" [9]. Such formulation does not necessarily contradict the diffusion and coalescence model of urban land use change. Instead, the diffusion and coalescence dichotomy might be viewed as a particular case where the way in which leapfrog and infilling alternate their dominance is not aleatory but rather characterized by a progressive decrease of the former and an increase of the latter. In any case, the importance of leapfrog growth in the present study does not necessarily decrease over time, instead it seems that infilling is becoming increasingly influent at the expense of edge-expansion. Lastly, the three urban agglomerations clearly conform to the reviewed fractal morphological hallmarks, namely the bifractal area-radius scaling and the power-law size-frequency distribution of urban patches. In coherence with the landscape metrics and growth modes, Bern and Lausanne show very similar traits. On the one hand, both urban agglomerations display a clear kink in the area-radius scaling, while the area-radius scaling in Zurich practically delineates a steeper straight line, suggesting that urbanization in Zurich fills the available space more intensely even at higher distances to the main center. On the other hand, the power-law decay as patch sizes increase is faster for Bern and Lausanne than for Zurich, which denotes that the latter urban agglomeration is dominated by larger urban patches.

Altogether, the only metric that does not conform to the diffusion and coalescence dichotomy is CONTAG, which should increase as patches coalesce, yet monotonic decreases are observed for the three urban agglomerations. Such behavior suggests that urban and natural patches are becoming increasingly disaggregated and interspersed, which might result from a combination of three factors. The first, which has already been noted above, is that the value of CONTAG strongly depends on the proportion of landscape occupied by each land use, especially when comprising only two classes like in the present study. Secondly, increases in MPS are proportionally less important than its corresponding decreases in ED and AWMFD, which is consistent with a central property of fractal objects, namely that their border is over-proportionally lengthened with respect to their area. Finally, the small yet persistent action of leapfrog growth and the irregular trend of PD are evidence that new urban patches do emerge at all periods. This suggests that fragmentation of natural patches occurs despite the apparent trend of coalescence exhibited by the other metrics. Furthermore, the continuous fragmentation of natural patches not only contributes to the decrease of CONTAG, but is also key to keeping the size-frequency relation of urban patches as a power-law with very stable scaling exponents. Given that many related studies report continuous fragmentation of natural land at the urban fringe, it is likely the size-frequency distribution of urban patches in their regions of study shows similar power-law scaling behaviors.

Examining the continuous fragmentation

As urbanization unfolds, urban patches are expected to grow, which suggests that eventually urban patches coalesce and thus the small ones disappear. Yet this contrasts with the continuous fragmentation of natural patches and the persistence of the power-law scaling of the urban patches observed in the present study. As a matter of fact, the complexity sciences offer a number of high-level models that intend to explain

the emergence and persistence of fractal structures and power-law distributions, such as Zipf's principle of minimal effort [34], or the concept of self-organized criticality [35]. Nevertheless, convincingly linking the observed urban patterns to models that account for socioeconomic, cultural and political drivers of urbanization remains a challenge [18, 36]. 319 320 321 322 323

The continuous fragmentation and persistence of the power-law scaling reported above might result from multiple factors. On the one hand, several key topological properties of urban street networks, such as the number of intersections per street or street length, also exhibit power law distributions [37], reflecting a scale-free hierarchical organization with a few major arterial roads and a large number of small streets. Since the organization of these networks exerts a central influence in the flows of people, goods and information that underpin the spatial development of cities and regions [38, 39], the fact that the size of urban patches also follows a power law certainly appears as more than a mere coincidence. Furthermore, the spatial evolution of urban street networks have also been characterized by two elementary processes, namely exploration, which expands the network towards previously non-urbanized areas, and densification, where new segments bridge gaps between existing streets [40]. The way in which exploration is observed to be more active in earlier stages and is followed by a phase of densification is seemingly analogous to the diffusion and coalescence hypothesis as well as to the increasing dominance of infilling. Overall, the foregoing findings urge deeper exploration of the connection between the evolution of transportation networks and land use patterns. 324 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340

Another factor that calls for consideration is the decentralized organization of the Swiss spatial planning system. The urban agglomerations examined in this study are configured by multiple municipalities which might adopt distinct approaches to spatial planning. During the last decades, most of the large Swiss municipalities have adopted land management measures that incentivize the densification [41], yet the above evidence shows that the majority of population growth and land conversion has occured in small and mid-sized municipalities that are located further away from the agglomeration core. It is therefore very likely that such municipalities have designated new building zones, especially for residential purposes, which contribute to the leapfrogging of urban patches surrounded by natural land, and ensure a continuous feed of small urban patches that keep their size-frequency distribution stable. The lack of coordination between of planning authorities is widely regarded as one of the main causes of urban sprawl [42, 43], and the revision of the Swiss Federal Act on regional planning of 2013 intends to overcome such shortcoming and define a national growth management strategy based on infill redevelopment and densification. 341 342 343 344 345 346 347 348 349 350 351 352 353 354 355

Planning implications 356

The fragmentation of natural habitats, as observed in the three Swiss urban agglomerations of this study, has been extensively linked to negative impacts on biodiversity and key ecosystem functions [44]. Nevertheless, growth management policies that misappreciate the residential preferences for low-density environments might inadvertently encourage households to relocate further away from the agglomeration centers, resulting in longer commute times and an overall increase of sprawl at the regional scale [45, 46]. On the other hand, the interspersion of patches of natural land within urban agglomerations provide valuable ecosystem services to its residents, such as the reduction of air pollution, alleviation of maximum temperatures, absorption of storm water, noise reduction, carbon sequestration, improvement of aesthetic and cultural values as well as the preservation of ecological habitats and biodiversity [47, 48]. In Switzerland, the lowest supply of such ecosystem services is found in the cantons with highest population density, hence policies encouraging 357 358 359 360 361 362 363 364 365 366 367 368 369

densification should consider the role of natural patches to ensure a sustainable supply   370
of ecosystem services [49]. To that end, recent planning approaches based on fractal   371
geometry [50] might be exploited in order to satisfy the residential demand for green   372
environments while explicitly considering planning objectives such as protecting natural   373
habitats and improving accessibility to urban and natural amenities [19].   374

Conclusion   375

The present study combines three different approaches to study the spatiotemporal   376
patterns of land use change associated to urbanization of three of the main Swiss urban   377
agglomerations over four periods of study from 1980 to 2016. The results are quite   378
consistent with the diffusion and coalescence model of urbanization, and suggest that   379
Zurich is already immersed in the coalescence phase, whereas Bern and Lausanne seem   380
to be at the transition between diffusion and coalescence. However, despite the   381
characteristics of coalescence exhibited by most metrics, continuous leapfrogging of   382
urban patches occurs in the three agglomerations, which fragments natural land and   383
maintains the structural complexity of the landscapes over the four periods of study.   384
Overall, the analysis of this paper shows how landscape metrics, urban growth modes   385
and fractal scaling can be combined to obtain insights into the spatiotemporal patterns   386
of urbanization that would be hard to obtain with any of the approaches individually.   387
The way in which complex fractal structures are sustained despite important changes in   388
the landscape is reminiscent of the dynamic behaviors encountered in a wide range of   389
complex self-organizing systems, and in the context of this study, is probably related to   390
the distinct planning policies adopted by the various municipalities that configure each   391
urban agglomeration, as well as to residential preferences for low density environments.   392
With the current Federal planning precepts aiming at the concentration growth within   393
the existing urban agglomerations, local planning authorities should devote special   394
attention to the valuable ecosystem services that the persisting patches of natural land   395
can provide to urban dwellers.   396

Supporting Information   397

Code S1   398

Computation of the time series of landscape metrics and exploration of their   399
correlations over all the urban agglomerations and the whole period of study, as Jupyter   400
Notebook (IPYNB). `https://github.com/martibosch/swiss-urbanization/blob/`   401
`master/notebooks/metrics_time_series.ipynb`   402

Code S2   403

Exploration of the sensitivity of the time series of landscape metrics to the spatial   404
extent of the urban agglomerations, as Jupyter Notebook (IPYNB).   405
`https://github.com/martibosch/swiss-urbanization/blob/master/notebooks/`   406
`sensitivity_extent.ipynb`   407

Code S3   408

Exploration of the area-radius scaling of each urban agglomerations over the whole   409
period of study, as Jupyter Notebook (IPYNB). `https://github.com/martibosch/`   410
`swiss-urbanization/blob/master/notebooks/area_radius_scaling.ipynb`   411

Code S4 412

Exploration of the size-frequency distribution of urban patches of each urban 413
agglomeration over the whole period of study, as Jupyter Notebook (IPYNB). 414
`https://github.com/martibosch/swiss-urbanization/blob/master/notebooks/` 415
`size_frequency_distribution.ipynb` 416

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