# APPLES: Distance-based Phylogenetic Placement for Scalable and Assembly-free Sample Identification

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### Abstract

Placing a new species on an existing phylogeny has increasing relevance to several 1 applications. Placement can be used to update phylogenies in a scalable fashion and can help identify unknown query samples using (meta-)barcoding, skimming, or metagenomic 3 data. Maximum likelihood (ML) methods of phylogenetic placement exist, but these methods are not scalable to reference trees with many thousands of leaves, limiting their ability to enjoy benefits of dense taxon sampling in modern reference libraries. They also 6 rely on *assembled* sequences for the reference set and aligned sequences for the query. 7 Thus, ML methods cannot analyze datasets where the reference consists of unassembled reads, a scenario relevant to emerging applications of genome-skimming for sample 9 identification. We introduce APPLES, a distance-based method for phylogenetic 10 placement. Compared to ML, APPLES is an order of magnitude faster and more memory 11 efficient, and unlike ML, it is able to place on large backbone trees (tested for up to 12 200,000 leaves). We show that using dense references improves accuracy substantially so 13 that APPLES on dense trees is more accurate than ML on sparser trees, where it can run. 14 Finally, APPLES can accurately identify samples without assembled reference or aligned 15 queries using kmer-based distances, a scenario that ML cannot handle. APPLES is 16 available publically at github.com/balabanmetin/apples. 17

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<sup>18</sup> Key words: Phylogenetic placement, Distance-based methods, Genome-skimming.

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Phylogenetic placement is the problem of finding the optimal position for a new query species on an existing backbone (or, reference) tree. Placement, as opposed to a de novo reconstruction of the full phylogeny, has two advantages. In some applications (discussed below), placement is all that is needed, and in terms of accuracy, it is as good as, and perhaps even better than, de novo reconstruction. Moreover, placement can be more scalable than de novo reconstruction when dealing with very large trees.

Earlier research on placement was motivated by scalability. For example, placement 26 is used in greedy algorithms that start with an empty tree and add sequences sequentially 27 (e.g., Felsenstein, 1981; Desper and Gascuel, 2002). Each placement requires polynomial 28 (often linear) time with respect to the size of the backbone, and thus, these greedy 29 algorithms are scalable (often requiring quadratic time). Despite computational challenges 30 (Warnow, 2017), there has been much progress in the *de novo* reconstruction of ultra-large 31 trees (e.g., thousands to millions of sequences) using both maximum likelihood (ML) (e.g., 32 Price et al., 2010; Nguyen et al., 2015) and the distance-based (e.g., Lefort et al., 2015) 33 approaches. However, these large-scale reconstructions require significant resources. As new 34 sequences continually become available, placement can be used to update existing trees 35 without repeating previous computations on full dataset. 36

More recently, placement has found a new application in sample identification: given one or more *query* sequences of unknown origins, detect the identity of the (set of) organism(s) that could have generated that sequence. These identifications can be made easily using sequence matching tools such as BLAST (Altschul *et al.*, 1990) when the query either exactly matches or is very close to a sequence in the reference library. However, when the sequence is novel (i.e., has lowered similarity to known sequences in the reference), this *closest* match approach is not sufficiently accurate (Koski and Golding, 2001), leading some researchers to adopt a phylogenetic approach (Sunagawa *et al.*, 2013;

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Nguyen et al., 2014). Sample identification is essential to the study of mixed environmental 45 samples, especially of the microbiome, both using 16S profiling (e.g., Gill et al., 2006; 46 Krause et al., 2008) and metagenomics (e.g., von Mering et al., 2007). It is also relevant to 47 barcoding (Hebert et al., 2003) and meta-barcoding (Clarke et al., 2014; Bush et al., 2017) 48 and quantification of biodiversity (e.g., Findley et al., 2013). Driven by applications to 49 microbiome profiling, placement tools like pplacer (Matsen *et al.*, 2010) and EPA(-ng) 50 (Berger et al., 2011; Barbera et al., 2018) have been developed. Researchers have also 51 developed methods for aligning query sequence (e.g., Berger and Stamatakis, 2011; 52 Mirarab et al., 2012) and for downstream steps (e.g., Stark et al., 2010; Matsen and Evans, 53 2013). These publications have made a strong case that for sample identification, 54 placement is sufficient (i.e., de novo is not needed). Moreover, some studies (e.g., Janssen 55 et al., 2018) have shown that when dealing with fragmentary reads typically found in 56 microbiome samples, placement can be *more* accurate than *de novo* construction and can 57 lead to improved associations of microbiome with clinical information. 58

Existing phylogenetic placement methods have focused on the ML inference of the 59 best placement – a successful approach, which nevertheless, suffers from two shortcomings. 60 On the one hand, ML can only be applied when the reference species are *assembled* into 61 full-length sequences (e.g., an entire gene) and are *aligned*; however, in new applications 62 that we will describe, assembling (and hence aligning) the reference set is not possible. On 63 the other hand, ML, while somewhat scalable, is still computationally demanding, 64 especially in memory usage, and cannot place on backbone trees with many thousands of 65 leaves. As the density of reference substantially impacts the accuracy and resolution of 66 placement, this inability to use ultra-large trees as backbone also limits accuracy. This 67 limitation has motivated alternative methods using local sensitive hashing (Brown and 68 Truszkowski, 2013) and divide-and-conquer (Mirarab et al., 2012). 69

Assembly-free and alignment-free sample identification using genome-skimming
 (Dodsworth, 2015) can also benefit from phylogenetic placement. A genome-skim is a

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shut-gun sample of the genome sequenced at low coverage (e.g., 1X) – so low that 72 assembling the nuclear genome is not possible (though, mitochondrial or plastid genomes 73 can often be assembled). Genome-skimming promises to replace traditional marker-based 74 barcoding of biological samples (Coissac et al., 2016) but limiting analyses to organelle 75 genome can limit resolution. Sarmashghi et al. (2019) have recently shown that using 76 shared k-mers, the distance between two unassembled genome-skims with low coverage can 77 be accurately estimated. This approach, unlike assembling organelle genomes, uses data 78 from the entire nuclear genome and hence promises to provide a higher resolution (e.g., at 79 species or sub-species levels) while keeping the low sequencing cost. However, ML and 80 other methods that require assembled sequences cannot analyze genome-skims, where both 81 the reference and the query species are unassembled genome-wide bags of reads. 82

<sup>83</sup> Distance-based approaches to phylogenetics are well-studied, but no existing tool <sup>84</sup> can perform distance-based placement of a query sequence on a given backbone. The <sup>85</sup> distance-based approach promises to solve both shortcomings of ML methods.

<sup>86</sup> Distance-based methods are computationally efficient and do not require assemblies. They
<sup>87</sup> only need distances (however computed). Thus, they can take as input assembly-free
<sup>88</sup> estimates of genomic distance estimated from low coverage genome-skims using Skmer

<sup>89</sup> (Sarmashghi et al., 2019) or other alternatives (Haubold, 2014; Leimeister and

Morgenstern, 2014; Leimeister et al., 2017; Yi and Jin, 2013; Benoit et al., 2016; Fan et al.,

<sup>91</sup> 2015; Ondov *et al.*, 2016; Jain *et al.*, 2017). While alignment-based phylogenetics has been
<sup>92</sup> traditionally more accurate than alignment-free methods when both methods are possible,
<sup>93</sup> in these new scenarios, only alignment-free methods are applicable.

Here, we introduce a new method for distance-based phylogenetic placement called
APPLES (Accurate Phylogenetic Placement using LEast Squares). APPLES uses dynamic
programming to find the optimal distance-based placement of a sequence with running
time and memory usage that scale linearly with the size of the backbone tree. We test
APPLES in simulations and on real data, both for alignment-free and aligned scenarios.

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### MATERIALS AND METHODS

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### Problem Statement.

Notations. Let an unrooted tree T = (V, E) be a weighted connected acyclic undirected graph with leaves denoted by  $\mathcal{L} = \{1 \cdots n\}$ . We let  $T^*$  be the rooting of T on a leaf 1 obtained by directing all edges away from 1. For node  $u \in V$ , let p(u) denote its parent, c(u) denote its set of children, sib(u) denote its siblings, and g(u) denote the set of leaves at or below u (i.e., those that have u on their path to the root), all with respect to  $T^*$ . Also let l(u) denote the length of the edge (p(u), u).

Distances. The tree T defines an  $n \times n$  matrix where each entry  $d_{ij}(T)$  corresponds to the path length between leaves i and j. We further generalize this definition so that  $d_{uv}(T^*)$  indicates the length of the undirected path between any two nodes of  $T^*$  (when clear, we simply write  $d_{uv}$ ). Given some input data, we can compute a matrix of all pairwise sequence distances  $\Delta$ , where the entry  $\delta_{ij}$  indicates the dissimilarity between species i and j. When the sequence distance  $\delta_{ij}$  is computed using (the correct) phylogenetic model, it will be a noisy but statistically consistent estimate of the tree distance  $d_{ij}(T)$  (Felsenstein, 2003). Given these "phylogenetically corrected" distances (e.g.  $\frac{3}{4} \ln(1 - \frac{4}{3}h)$  is the corrected hamming distance h under the Jukes and Cantor (1969) model), we can define optimization problems to recover the tree that best fits the distances. A natural choice is minimizing the (weighted) least square difference between tree and sequence distances:

$$Q^*(T) = \sum_{i=1}^n \sum_{j=1}^n w_{ij} (\delta_{ij} - d_{ij}(T))^2 .$$
(1)

Here, weights (e.g.,  $w_{ij}$ ) are used to reduce the impact of large distances (expected to have high variance). A general weighting schema can be defined as  $w_{qi} = \delta_{qi}^{-k}$  for a *constant* value  $k \in \mathbb{N}$ . Standard choices of k include k = 0 for the ordinary least squares (OLS) method of Cavalli-Sforza and Edwards 1967, k = 1 due to Beyer *et al.* 1974 (BE), and k = 2 due to Fitch and Margoliash 1967 (FM).

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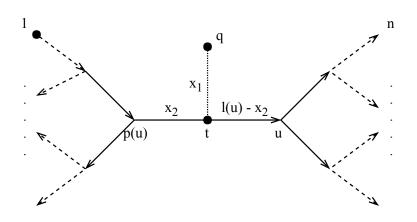


Fig. 1. Any placement of q can be characterized as a tree  $P(u, x_1, x_2)$ , shown here. The backbone tree  $T^*$  is an arborescence on leaves  $\mathcal{L} = \{1 \dots n\}$ , rooted at leaf 1. Query taxon q is added on the edge between u and p(u), creating a node t. All placements on this edge are characterized by  $x_1$ , the length of the pendant branch, and  $x_2$ , the distance between t and p(u).

Finding  $\arg \min_{T} Q^{*}(T)$  is NP-Complete (Day, 1987). However, decades of research has produced heuristics like neighbor-joining (Saitou and Nei, 1987), alternative formulations like (balanced) minimum evolution (Cavalli-Sforza and Edwards, 1967; Desper and Gascuel, 2002), and several effective tools for solving the problem heuristically (e.g., FastME by Lefort *et al.* 2015, DAMBE by Xia 2018, and Ninja by Wheeler 2009).

<sup>117</sup> Phylogenetic placement. We let  $P(u, x_1, x_2)$  be the tree obtained by adding a <sup>118</sup> query taxon q on an edge (p(u), u), creating three edges (t, q), (p(u), t), and (t, u), with <sup>119</sup> weights  $x_1, x_2$ , and  $l(u) - x_2$ , respectively (Fig. 1). When clear, we simply write P and <sup>120</sup> note that P induces T both in topology and branch length. We now define the problem.

<sup>121</sup> Least Squares Phylogenetic Placement (LSPP).

Input: A backbone tree T on  $\mathcal{L}$ , a query species q, and a vector  $\Delta_{q*}$  with elements  $\delta_{qi}$ giving sequence distances between q and every species  $i \in \mathcal{L}$ ;

**Output:** The placement tree P that adds q on T and minimizes

$$Q(P) = \sum_{i=1}^{n} w_{qi} (\delta_{qi} - d_{qi}(P))^2$$
(2)

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# Linear Time Solution for LSPP

The number of possible placements of q is 2n - 3. Therefore, LSPP can be solved by simply iterating over all the topologies, optimizing the score for that branch, and returning the placement with the minimum least square error. A naive algorithm can accomplish this in  $\Theta(n^2)$  running time by optimizing Eq. 2 for each of the 2n - 3 branches. However, using dynamic programming, the optimal solution can be found in linear time.

<sup>130</sup> THEOREM 1 The LSPP problem can be solved with  $\Theta(n)$  running time and memory.

The proof (given in Appendix A) follows easily from three lemmas that we next state. The algorithm starts with precomputing a fixed-size set of values for each nodes. For any node u and exponents  $a \in \mathbb{Z}$  and  $b \in \mathbb{N}^+$ , let  $S(a, b, u) = \sum_{i \in g(u)} \delta^a_{qi} d^b_{ui}$  and for b = 0, let  $S(a, 0, u) = S'(a, u) = \sum_{i \in g(u)} \delta^a_{qi}$ . Note that S'(0, u) = |g(u)|. Similarly, for  $u \in V \setminus \{1\}$ , let  $R(a, b, u) = \sum_{i \notin g(u)} \delta^a_{qi} d^b_{p(u)i}$  for b > 0 and let  $R(a, 0, u) = R'(a, u) = \sum_{i \notin g(u)} \delta^a_{qi}$ .

LEMMA 2 The set of all S(a, b, u) and R(a, b, u) values can be precomputed in  $\Theta(n)$  time with two tree traversals using the dynamic programming given by:

$$S(a, b, u) = \begin{cases} \delta^{a}_{qu} & u \in \mathcal{L} \setminus \{1\} \& b = 0 \\ 0 & u \in \mathcal{L} \setminus \{1\} \& b \neq 0 \\ \sum_{j=0}^{b} \sum_{v \in c(u)} l(v)^{j} {b \choose j} S(a, b - j, v) & u \notin \mathcal{L} \setminus \{1\} \end{cases}$$
(3)  
$$R(a, b, u) = \begin{cases} \delta^{a}_{q1} & u = 1' = c(1) \& b = 0 \\ 0 & u = 1' = c(1) \& b \neq 0 \\ \sum_{j=0}^{b} \left( l(p(u))^{j} {b \choose j} R(a, b - j, p(u)) + \sum_{v \in sib(u)} l(v)^{j} {b \choose j} S(a, b - j, v) \right) & u \notin \{1, 1'\} \end{cases}$$
(4)

LEMMA 3 Equation 2 can be rearranged (see Eq. S2 in Appendix A) such that computing Q(P) for a given  $P = P(u, x_1, x_2)$  requires a constant time computation using S(a, b, u)and R(a, b, u) values for  $-k \leq a \leq 2 - k$  and  $0 \leq b \leq 2$ .

Thus, after a linear time precomputation, we can compute the error for any given placement in constant time. It remains to show that for each node, the optimal placement on the branch above it (e.g.,  $x_1$  and  $x_2$ ) can be computed in constant time.

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LEMMA 4 For a fixed node  $u \in V \setminus \{1\}$ , if  $(\hat{x}_1, \hat{x}_2) = \arg\min_{x_1, x_2} Q(P(u, x_1, x_2))$ , then

$$\begin{bmatrix} R'(-k,u) + S'(-k,u) & R'(-k,u) - S'(-k,u) \\ R'(-k,u) - S'(-k,u) & R'(-k,u) + S'(-k,u) \end{bmatrix} \cdot \begin{bmatrix} \hat{x}_1 \\ \hat{x}_2 \end{bmatrix} = \begin{bmatrix} R'(1-k,u) + S'(1-k,u) - l(u)S'(-k,u) - R(-k,1,u) - S(-k,1,u) \\ R'(1-k,u) - S'(1-k,u) + l(u)S'(-k,u) - R(-k,1,u) + S(-k,1,u) \end{bmatrix}$$
(5)

and hence  $\hat{x}_1, \hat{x}_2$  can be computed in constant time.

<sup>146</sup> Non-negative branch lengths. The solution to Equation 5 does not necessarily <sup>147</sup> conform to constraints  $0 \le x_1$  and  $0 \le x_2 \le l(u)$ . However, the following lemma (proof in <sup>148</sup> Appendix A) allows us to easily impose the constraints by choosing optimal boundary <sup>149</sup> points when unrestricted solutions fall outside boundaries.

LEMMA 5 With respect to variables  $x_1$  and  $x_2$ ,  $Q(P(u, x_1, x_2))$  is a convex function.

<sup>151</sup> Minimum evolution An alternative to directly using MLSE (Eq. 1) is the <sup>152</sup> minimum evolution (ME) principle (Cavalli-Sforza and Edwards, 1967; Rzhetsky and Nei, <sup>153</sup> 1992). Our algorithm can also optimize the ME criterion: after computing  $x_1$  and  $x_2$  by <sup>154</sup> optimizing MLSE for each node u, we choose the placement with the minimum total <sup>155</sup> branch length. This is equivalent to using  $\arg \min_u x_1$ , since the value of  $x_2$  does not <sup>156</sup> contribute to total branch length. Other solution for ME placement exists (Desper and <sup>157</sup> Gascuel, 2002), a topic we return to in the Discussion section.

<sup>158</sup> Hybrid. We have observed cases where ME is correct more often than MLSE, but when it <sup>159</sup> is wrong, unlike MLSE, it has a relatively high error. This observation led us to design a <sup>160</sup> hybrid approach. After computing  $x_1$  and  $x_2$  for all branches, we first select the top  $log_2(n)$ <sup>161</sup> edges with minimum  $Q(P(u, x_1, x_2))$  values (this requires  $\Theta(n \log \log n)$  time). Among this <sup>162</sup> set of edges, we place the query on the edge satisfying the ME criteria.

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### Datasets

We benchmark accuracy and scalability of APPLES in two settings: sample
 identification using assembly-free genome-skims on real biological data and placement
 using aligned sequences on simulated data.

## Real genome-skim datasets for the assembly-free scenario

Columbicola genome-skims. We use a set of 61 genome-skims by Boyd et al. (2017), 168 including 45 known lice species (some represented multiple times) and 7 undescribed 169 species. We generate lower coverage skims of 0.1Gb or 0.5Gb by randomly subsampling the 170 reads from the sequence read archives (SRA) provided by the original publication (NCBI 171 BioProject PRJNA296666). We use BBTools (Bushnell, 2014) to filter subsampled reads 172 for adapters and contaminants and remove duplicated reads. Since this dataset is not 173 assembled, the coverage of the genome-skims is unknown; Skmer estimates the coverage to 174 be between 0.2X and 1X for 0.1Gb samples (and 5 times that coverage with 0.5Gb). 175

Anopheles and Drosophila datasets. We also use two insect datasets used by Sarmashghi et al. (2019): a dataset of 22 Anopheles and a dataset of 21 Drosophila genomes (Table S1), both obtained from InsectBase (Yin et al., 2016). For both datasets, genome-skims with 0.1Gb and 0.5Gb sequence were generated from the assemblies using the short-read simulator tool ART, with the read length l = 100 and default error profile. Since species have different genome sizes, with 0.1Gb data, our subsampled genome-skims range in coverage from 0.35X to 1X for Anopheles and from 0.4X to 0.8X for Drosophila.

<sup>183</sup> More recently, Miller *et al.* (2018) sequenced several Drosophila genomes, including <sup>184</sup> 12 species shared with the InsectBase dataset. Sarmashghi *et al.* (2019) subsampled the <sup>185</sup> SRAs from this second project to 0.1Gb or 0.5Gb and, after filtering contaminants, <sup>186</sup> obtained artificial genome-skims. We can use these genome-skims as query and the <sup>187</sup> genome-skims from the InsectBase dataset as the backbone. Since the reference and query

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come from two projects, the query genome-skim can have a non-zero distance to the same species in the reference set, providing a realistic test of sample identification applications.

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# Simulated datasets for the aligned sequence scenario

GTR. We use a 101-taxon dataset available from Mirarab and Warnow 2015. Sequences 191 were simulated under the General Time Reversible (GTR) plus the  $\Gamma$  model of site rate 192 heterogeneity using INDELible (Fletcher and Yang, 2009) on gene trees that were 193 simulated using SimPhy (Mallo et al., 2016) under the coalescent model evolving on 194 species trees generated under the Yule model. Note that the same model is used for 195 inference under ML placement methods (i.e., no model misspecification). We took all 20 196 replicates of this dataset with mutation rates between  $5 \times 10^{-8}$  and  $2 \times 10^{-7}$ , and for each 197 replicate, randomly selected five estimated gene trees among those with  $\leq 20\%$  RF distance 198 between estimated and true gene tree. Thus, we have a total of 100 backbone trees. 199

RNASim. Guo et al. 2009 designed a complex model of RNA evolution that does not 200 make usual i.i.d assumptions of sequence evolution. Instead, it uses models of energy of the 201 secondary structure to simulate RNA evolution by a mutation-selection population genetics 202 model. This model is based on an inhomogeneous stochastic process without a global 203 substitution matrix. The model complexity of RNASim allows us to test both ML and 204 APPLES under a substantially misspecified model. An RNASim dataset of 10<sup>6</sup> sequences is 205 available from Mirarab et al. 2015. We created several subsets of the full RNASim dataset. 206 i) Heterogeneous: We first randomly subsampled the full dataset to create 10 207 datasets of size  $10^4$ . Then, we chose the largest clade of size at most 250 from each 208 replicate; this gives us 10 backbone trees of mean size 249. 200

*ii*) Varied diameter: To evaluate the impact of the evolutionary diameter (i.e., the highest distance between any two leaves in the backbone), we also created datasets with low, medium, and high diameters. We sampled the largest five clades of size at most 250 from each of the 10 replicates used for the heterogeneous dataset. Among these 50 clades,

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we picked the bottom, middle, and top five clades in diameter, which had diameter in [0.3, 0.4] (mean: 0.36), [0.5, 0.52] (mean: 0.51), and [0.65, 1.07] (mean: 0.82), respectively. iii) Varied size: We randomly subsampled the tree of size 10<sup>6</sup> to create 5 replicates of datasets of size  $5 \times 10^2$ ,  $10^3$ ,  $5 \times 10^3$ ,  $10^4$ ,  $5 \times 10^4$ , and  $10^5$ , and 1 replicate (due to size) of size  $2 \times 10^5$ . For replicates that contain at least  $5 \times 10^3$  species, we removed sites that contain gaps in 95% or more of the sequences in the alignment.

# Methods

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Alternative methods. For aligned data, we compare APPLES to two ML methods: 221 pplacer (Matsen et al., 2010) and EPA-ng (Barbera et al., 2018). Matsen et al. (2010) 222 found pplacer to be substantially faster than EPA (Berger and Stamatakis, 2011) while 223 their accuracy was similar. EPA-ng improves the scalability of EPA; thus, we compare to 224 EPA-ng in analyses that concerned scalability (e.g., RNASim-Varied Size). We run pplacer 225 and EPA-ng in their default mode using  $GTR+\Gamma$  model (the only option for pplacer). We 226 also compare with a simple method referred to as CLOSEST that places the query as the 227 sister to the species with the minimum distance to it. CLOSEST is meant to emulate the 228 use of BLAST (if it could be used). For the assembly-free setting, existing phylogenetic 229 placement methods cannot be used, and we compared only against CLOSEST. 230

Distance calculation and models. We modified FastME to compute distances only between query and backbone sequences, not among backbone sequences. This version, called FastME\* here, also ensures that when estimating model parameters, positions that have a gap in at least one of the two sequences are always ignored.

We compute phylogenetic distances under the parameter-free JC69 model, the six-parameter Tamura and Nei 1993 (TN93) model, and the 12-parameter general Markov model (Lockhart *et al.*, 1994). We compute distances independently for all pairs, and not simultaneously as suggested by Tamura *et al.* (2004). We also use the Gamma model of

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sites rate heterogeneity for JC69 and TN93 using the standard approach (Waddell and 239 Steel, 1997). Pairing Gamma with GTR is theoretically possible in the absence of noise; 240 however, the method can run into problems on real data (Waddell and Steel, 1997). Thus, 241 we do not include a GTR model directly. Instead, we use the log-det approach that can 242 handle the most general (12-parameter) Markov model (Lockhart *et al.*, 1994); however, 243 log-det cannot account for rate across sites heterogeneity (Waddell and Steel, 1997). The  $\alpha$ 244 parameter of the Gamma model cannot be computed from pairwise sequence comparisons 245 (Steel, 2009); instead, we use the  $\alpha$  computed from the backbone tree. We used the  $\alpha$ 246 parameter computed by RAxML (Stamatakis, 2014) run on the backbone alignment and 247 given the backbone tree. 248

In analyses on assembly-free datasets, we first compute genomic distances using Skmer (Sarmashghi *et al.*, 2019). We then correct these distances using the JC69 model, without the Gamma model of rate variation.

Backbone trees. For genome-skimming experiments, we estimated the backbone 252 tree using FastME<sup>\*</sup> from the JC69 distance matrix computed from genome-skims using 253 Skmer. For simulated datasets, we estimated the topology of the backbone tree by running 254 RAxML (Stamatakis, 2014) on the true alignment using GTRGAMMA model and used 255 this tree as the backbone for pplacer and EPA-ng. However, to handle large trees, we used 256 FastTree-2 (Price et al., 2010) to estimate the backbone tree for RNASim-varied size and 257 re-estimated branch lengths on the fixed topology using RAxML. For the backbone of 258 APPLES, we always used the same tree topology but re-estimated branch lengths using 259 FastTree-2 under the JC69 model. 260

APPLES parameters. We have chosen default parameter settings for APPLES and refer
 to this version as APPLES\*. By default, we use FM weighting, the MLSE selection
 criterion, enforcement of non-negative branch lengths, and JC69 distances. When not
 specified otherwise, these default parameters are used.

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### Evaluation Procedure

To evaluate the accuracy, we use a leave-one-out strategy. We remove each leaf ifrom the backbone tree T and place it back on this  $T \setminus i$  tree to obtain the placement tree P. However, on the RNAsim-varied size dataset, due to its large size, we only removed and added back 200 randomly chosen leaves per replicate.

Delta error. We measure the accuracy of the placement using delta error  $(\Delta e)$ : the number of branches of the true tree missing from P minus the number of branches of the true tree missing from  $T \setminus i$  (induced on the same leafset). Note that  $\Delta e \ge 0$  because adding i cannot decrease the number of missing branches in  $T \setminus i$ . Note that placing i to the same location as the backbone before leaving it out (e.g., T) can still have a non-zero delta error because the backbone tree is not the true tree. We refer to the placement of a leaf into its position in the backbone tree as the *de novo* placement.

On biological data, where the true tree is unknown, we use a reference tree (Fig. S1). For Drosophila and Anopheles, we use the tree available from the Open Tree Of Life (Hinchliff *et al.*, 2015) as the reference. For Columbicola, we use the ML concatenation tree published by Boyd *et al.* (2017) as the reference.

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### RESULTS

# Assembly-free Placement of Genome-skims

On our three biological genome-skim datasets, APPLES<sup>\*</sup> successfully places the queries on the optimal position in most cases (97%, 95%, and 71% for Columbicola, Anopheles, and Drosophila, respectively) and is never off from the optimal position by more than one branch. Other versions of APPLES are less accurate than APPLES<sup>\*</sup>; e.g., APPLES with ME can have up to five wrong branches (Table 1). On genome-skims, where assembly and alignment are not possible, existing placement tools cannot be used, and the only alternative is the CLOSEST method (emulating BLAST if assembly was possible).

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|                     | (a) | Colum      | bicola    | (b | ) Anop     | heles     | (c) Drosophila |            |           |  |
|---------------------|-----|------------|-----------|----|------------|-----------|----------------|------------|-----------|--|
|                     | %   | $\Delta e$ | $e_{max}$ | %  | $\Delta e$ | $e_{max}$ | %              | $\Delta e$ | $e_{max}$ |  |
| $\mathbf{APPLES}^*$ | 97  | 0.03       | 1         | 95 | 0.05       | 1         | 71             | 0.29       | 1         |  |
| APPLES-ME           | 84  | 0.28       | 5         | 95 | 0.05       | 1         | 67             | 0.42       | 2         |  |
| APPLES-HYBRID       | 87  | 0.16       | 2         | 95 | 0.05       | 1         | 67             | 0.33       | 1         |  |
| CLOSEST             | 54  | 1.15       | 7         | 91 | 0.09       | 1         | 57             | 0.62       | 3         |  |
| DE-NOVO             | 98  | 0.02       | 1         | 95 | 0.05       | 1         | 71             | 0.29       | 1         |  |

Table 1. Assembly-free placement of genome-skims. We show the percentage of placements into optimal position (those that do not increase  $\Delta e$ ), average delta error ( $\Delta e$ ), and maximum delta error ( $e_{max}$ ) for APPLES, assignment to the CLOSEST species, and the placement to the position in the backbone (DE-NOVO) over the 61 (a), 22 (b), and 21 (c) placements. Results are shown for genome skims with 0.1Gbp of reads. Delta error is the increase in the missing branches between the reference tree and the backbone tree after placing each query.

<sup>290</sup> CLOSEST finds the optimal placement only in 54% and 57% of times for Columbicola and <sup>291</sup> Drosophila; moreover, it can be off from the best placement by up to seven branches for <sup>292</sup> the Columbicola dataset. On the Anopheles dataset, where the reference tree is unresolved <sup>293</sup> (Fig. S1), all methods perform similarly.

APPLES<sup>\*</sup> is less accurate on the Drosophila dataset than other datasets. However, here, simply placing each query on its position in the backbone tree would lead to identical results (Table 1). Thus, placements by APPLES<sup>\*</sup> are as good as the *de novo* construction, meaning that errors of APPLES<sup>\*</sup> are entirely due to the differences between our backbone tree and the reference tree. Moreover, these errors are not due to low coverage; increasing the genome-skim size 5x (to 0.5Gb) does not decrease error (Table S4).

On Drosophila dataset, we next tested a more realistic sample identification scenario using the 12 genome-skims from the separate study (and thus, non-zero distance to the corresponding species in the backbone tree). As desired, APPLES\* places all of 12 queries from the second study as sister to the corresponding species in the reference dataset.

### Alignment-based Placement

We first compare the accuracy and scalability of APPLES<sup>\*</sup> to ML methods and then compare various settings of APPLES. For ML, we use pplacer (shown everywhere) and EPA-ng (shown only when we study scalability).

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|                     |    | Low        |           |    | Medium     |           |  |    | High       |           |  |    | Heterogeneous |           |  |  |
|---------------------|----|------------|-----------|----|------------|-----------|--|----|------------|-----------|--|----|---------------|-----------|--|--|
|                     | %  | $\Delta e$ | $e_{max}$ | %  | $\Delta e$ | $e_{max}$ |  | %  | $\Delta e$ | $e_{max}$ |  | %  | $\Delta e$    | $e_{max}$ |  |  |
| $\mathbf{APPLES}^*$ | 86 | 0.15       | 2         | 85 | 0.18       | 5         |  | 84 | 0.18       | 3         |  | 85 | 0.17          | 5         |  |  |
| CLOSEST             | 59 | 0.88       | 13        | 60 | 0.88       | 13        |  | 60 | 0.85       | 14        |  | 60 | 0.87          | 14        |  |  |
| pplacer             | 88 | 0.13       | 2         | 89 | 0.11       | 3         |  | 87 | 0.13       | 3         |  | 88 | 0.13          | 3         |  |  |

Table 2. The delta error for APPLES<sup>\*</sup>, CLOSEST match, and pplacer on the RNASim-varied diameter dataset (low, medium, or high) and the RNA-heterogeneous dataset. Measurements are shown over 1250 placements for each diameter size category, corresponding to 5 backbone trees and 250 placements per replicate.

### <sup>308</sup> Comparison to Maximum Likelihood (ML)

GTR dataset. On this dataset, where it faces no model misspecification, pplacer has high 309 accuracy. It finds the best placement in 84% of cases and is off by one edge in 15%310 (Fig. 2a); its mean delta error ( $\Delta e$ ) is only 0.17 edges. APPLES<sup>\*</sup> is also accurate, finding 311 the best placement in 78% of cases and resulting in the mean  $\Delta e = 0.28$  edges. Thus, even 312 though pplacer uses ML and faces no model misspecification and APPLES<sup>\*</sup> uses distances 313 based on a simpler model, the accuracy of the two methods is within 0.1 edges on average. 314 In contrast, CLOSEST has poor accuracy and is correct only 50% of the times, with the 315 mean  $\Delta e$  of 1.0 edge. 316

<sup>317</sup> Model misspecification. On the small RNASim data with subsampled clades of  $\approx 250$ <sup>318</sup> species), both APPLES<sup>\*</sup> and pplacer face model misspecification. Here, the accuracy of <sup>319</sup> APPLES<sup>\*</sup> is very close to ML using pplacer. On the heterogeneous subset (Fig. 2b and <sup>320</sup> Table 2), pplacer and APPLES<sup>\*</sup> find the best placement in 88% and 86% of cases and have <sup>321</sup> a mean delta error of 0.13 and 0.17 edges, respectively. Both methods are much more <sup>322</sup> accurate than CLOSEST, which has a delta error of 0.87 edges on average.

Impact of diameter. When we control the tree diameter, APPLES<sup>\*</sup> and pplacer remain very close in accuracy (Fig. 2c). The changes in error are small and not monotonic as the diameters change (Table 2). The accuracies of the two methods at low and high diameters are similar. The two methods are most divergent in the medium diameter case, where pplacer has its lowest error ( $\Delta e = 0.11$ ) and APPLES<sup>\*</sup> has its highest error ( $\Delta e = 0.18$ ).

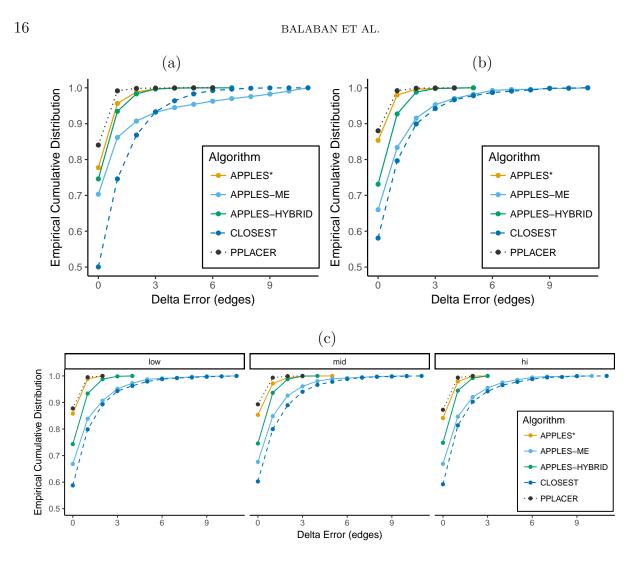


Fig. 2. Accuracy on simulated data. We show empirical cumulative distribution of the delta error, defined as the increase in the number of missing branches in the estimated tree compared to the true tree. We compare pplacer (dotted), CLOSEST match (dashed), and APPLES with FM weighting and JC69 distances and MLSE (APPLES\*), ME, or Hybrid optimization. (a) GTR dataset. (b) RNASim-Heterogeneous. (c) RNASim-varied diameter, shown in boxes: low, medium (mid), or high (hi). Distributions are over 10,000 (a), 2450 (b), and 3675 (c) points.

To summarize results on small RNASim dataset with model misspecification, although APPLES\* uses a parameter-free model, its accuracy is extremely close to ML using pplacer with the  $GTR+\Gamma$  model.

<sup>331</sup> Impact of taxon sampling. The real advantage of APPLES\* over pplacer becomes clear for

<sup>332</sup> placing on larger backbone trees (Fig. 3 and Table 3). For backbone sizes of 500 and 1000,

<sup>333</sup> pplacer continues to be slightly more accurate than APPLES<sup>\*</sup> (mean  $\Delta e$  of pplacer is

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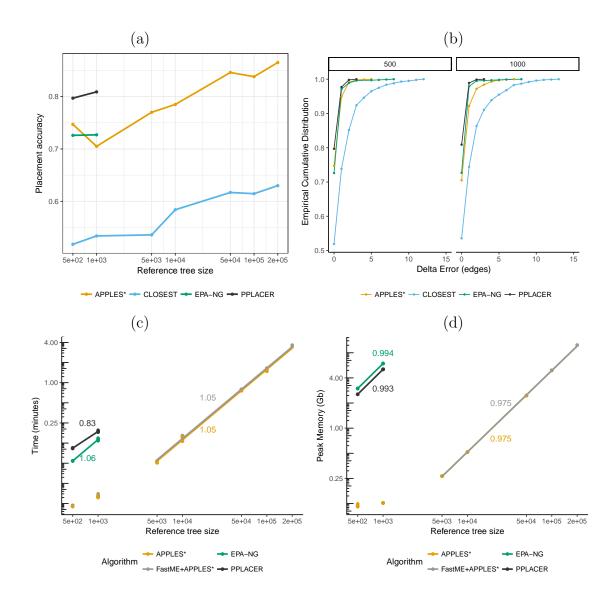


Fig. 3. **Results on RNASim-Varied size.** (a) Placement accuracy for various levels of taxon sampling, comparing pplacer, CLOSEST match, EPA-ng, and APPLES\* on RNASim dataset with backbone size ranging from 500 to 200,000. (b) The empirical cumulative distribution of the delta error on the same datasets, only shown for the backbone size 500 and 1000 where all methods can run. Distributions are over 1000 points. (c,d) Running time and peak memory usage of placement methods for a single placement. For APPLES\*, measurements are shown with and without the distance calculation step performed using FastME\*. On backbones of size 5000, pplacer managed to correctly run for only 551 out of 1000 placements, whereas EPA-ng managed to run for 200/1000 placements (Fig S2). Lines are fitted in the log-log scale; thus, the slope of the line (indicated on the figure) gives an empirical estimate of the polynomial degree of the asymptotic growth curve. All curves grow close to linearly (slopes  $\approx$ 1). APPLES lines are fitted to  $\geq$  5,000 points because the first two values correspond to extremely low memory (100Mb) and are irrelevant to asymptotic behavior. All calculations are on 8-core, 2.6GHz Intel Xeon CPUs (Sandy Bridge) with 64GB of memory.

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|                                | n = 500 |            | : | $n = 10^{3}$ |            | n    | $n = 5 \times 10^3$ |            |  | $n = 10^4$ |            |   | $n = 10^{5}$ |            |  | $n=2\times 10^5$ |            |  |
|--------------------------------|---------|------------|---|--------------|------------|------|---------------------|------------|--|------------|------------|---|--------------|------------|--|------------------|------------|--|
|                                | %       | $\Delta e$ | 0 | 70           | $\Delta e$ |      | %                   | $\Delta e$ |  | %          | $\Delta e$ |   | %            | $\Delta e$ |  | %                | $\Delta e$ |  |
| $\overline{\mathbf{APPLES}^*}$ | 75      | 0.32       | 7 | '1           | 0.43       |      | 77                  | 0.37       |  | 79         | 0.33       |   | 84           | 0.25       |  | 87               | 0.25       |  |
| CLOSEST                        | 52      | 1.16       | 5 | 3            | 1.18       |      | 54                  | 1.15       |  | 59         | 0.90       |   | 61           | 0.69       |  | 63               | 0.70       |  |
| EPA-ng                         | 73      | 0.33       | 7 | 3            | 0.31       | fail | (449)               | n.p        |  | n.p        | n.p        | r | ı.p          | n.p        |  | n.p              | n.p        |  |
| pplacer                        | 80      | 0.23       | 8 | 1            | 0.20       | fail | (800)               | n.p        |  | n.p        | n.p        | r | ı.p          | n.p        |  | n.p              | n.p        |  |

Table 3. Percentage of correct placements (shown as %) and the delta error ( $\Delta e$ ) on the RNASim datasets with various backbone size (n). % and  $\Delta e$  is over 1000 placements (except n = 200,000, which is over 200 placements). Running pplacer and EPA-ng was not possible (n.p) for trees with at least 10,000 leaves and failed in some cases (number of fails shown) for 5,000 leaves.

better than APPLES<sup>\*</sup> by 0.09 and 0.23 edges, respectively). However, with backbones of 334 5000 leaves, pplacer fails to run on 449/1000 cases, producing infinity likelihood (perhaps 335 due to numerical issues) and has 41 times higher error than APPLES<sup>\*</sup> on the rest (Fig. S2). 336 Since pplacer could not scale to 5,000 leaves, we also tested the recent method, 337 EPA-ng (Barbera et al., 2018). On datasets with up to 1000 leaves, EPA-ng was less 338 accurate than pplacer and close in accuracy to APPLES<sup>\*</sup> (Fig. 3ab). It also failed in 339 800/1000 replicates of the 5000-taxon backbone but had 4% less error than APPLES<sup>\*</sup> in 340 the minority of cases where it could run (Fig. S2). 341

For backbones trees with at least  $10^4$  leaves, pplacer and EPA-ng were not able to 342 run, and CLOSEST is not very accurate (finding the best placement in only 59% of cases). 343 However, APPLES<sup>\*</sup> continues to be accurate for all backbone sizes. As the backbone size 344 increases, the taxon sampling of the tree is improving (recall that these trees are all 345 random subsets of the same tree). With denser backbone trees, APPLES<sup>\*</sup> has increased 346 accuracy despite placing on larger trees (Fig. 3a, Table 3). For example, using a backbone 347 tree of  $2 \times 10^5$  leaves, APPLES<sup>\*</sup> is able to find the best placement of query sequences in 348 87% of cases, which is better than the accuracy of either APPLES<sup>\*</sup> or ML tools on any 349 backbone size. Thus, an increased taxon sampling helps accuracy, but ML tools are limited 350 in the size of the tree they can handle. 351

Running time and memory. As the backbone size increases, the running times of all methods increase close to linearly with the size of the backbone tree (Fig. 3c). However,

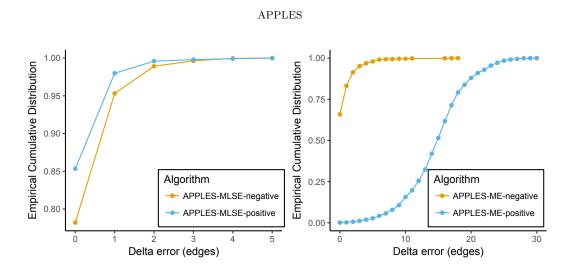


Fig. 4. The effect of imposing positivity constraint on error. We show the error of (a) APPLES-MLSE and (b) APPLES-ME run both with and without enforcement of non-negative branch lengths on RNASim heterogeneous dataset. Accuracy improves substantially for MLSE whereas it reduces drastically for ME.

APPLES is on average 15 times faster than pplacer and 12 times faster than EPA-ng on 354 backbone trees with 5000 leaves in cases where those methods could run. Similarly, the 355 memory of all methods increases linearly with the backbone size, but APPLES requires 356 dramatically less memory (Fig. 3d). For example, for placing on a backbone with 5000 357 leaves, pplacer requires 25GB of memory, EPA-ng requires 30GB whereas APPLES 358 requires only 0.25GB. APPLES easily scales to a backbone of  $2 \times 10^5$  sequences, running in 359 only 4 minutes and using 8GB of memory per query (including all precomputations in the 360 dynamic programming). These numbers also include the time and memory needed to 361 compute the distance between the query sequence and all the backbone sequences. 362

Comparing parameters of APPLES. We now compare different settings of 363 APPLES. Comparing five models of sequence evolution, we see similar patterns of accuracy 364 across all models despite their varying complexity, ranging from 0 to 12 parameters 365 (Fig. S3). Since the JC69 model is parameter-free and results in similar accuracy to others, 366 we have used it as the default. Next, we ask whether imposing the constraint to disallow 367 negative branch lengths improves the accuracy. The answer depends on the optimization 368 strategy. Forcing non-negative lengths marginally increases the accuracy for MLSE but 369 dramatically reduces the accuracy for ME (Fig. 4). Thus, we always impose non-negative 370

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constraints on MLSE but never for ME. Likewise, our Hybrid method includes the 371 constraint for the first MLSE step but not for the following ME step (Fig. S4). 372 The next parameter to choose is the weighting scheme. Among the three methods 373 available in APPLES, the best accuracy belongs to the FM scheme closely followed by the 374 BE (Fig. S5). The OLS scheme, which does not penalize long distances, performs 375 substantially worse than FM and BE. Thus, the most aggressive form of weighting (FM) 376 results in the best accuracy. Fixing the weighting scheme to FM and comparing the three 377 optimization strategies (MLSE, ME, and Hybrid), the MLSE approach has the best 378 accuracy (Fig. 2), finding the correct placement 84% of the time (mean error: 0.18), and 379 ME has the lowest accuracy, finding the best placement in only 67% of cases (mean error: 380 (0.70). The Hybrid approach is between the two (mean error: (0.34)) and fails to outperform 381 MLSE on this dataset. However, when we restrict the RNASim backbone trees to only 20 382 leaves, we observe that Hybrid can have the best accuracy (Fig. S6). 383

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### DISCUSSION

We introduced APPLES: a new method for adding query species onto large 385 backbone trees using both unassembled genome-skims and aligned data. The accuracy of 386 APPLES was very close to ML using pplacer in most settings where ML could run; the 387 accuracy advantages of ML were particularly small for the more realistic simulation, 388 RNASim, where both methods face model misspecification. As expected by the substantial 389 evidence from the literature (Hillis et al., 2003; Zwickl and Hillis, 2002), improved taxon 390 sampling increased the accuracy of placement. Thus, overall, the best accuracy on 391 RNASim dataset was obtained by APPLES<sup>\*</sup> run on the full reference dataset. This 302 observation motivates the use of scalable methods such as APPLES<sup>\*</sup> instead of ML 393 methods, which have to restrict their backbone to at most several thousand species. It is possible to follow up the APPLES<sup>\*</sup> placements with a round of ML placement on smaller 395 trees, but the small differences in accuracy of pplacer and APPLES<sup>\*</sup> on smaller trees did 396

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<sup>397</sup> not give us compelling reasons to try such hybrid approaches.

Phylogenetic insertion using the ME criterion has been previously studied for the 398 purpose of creating an algorithm for greedy minimum evolution (GME). Desper and 399 Gascuel 2002 have designed a method that given the tree T can update it to get a tree 400 with n+1 leaves in  $\Theta(n)$  after precomputation of a data-structure that gives the average 401 sequence distances between all adjacent clusters in T. The formulation by Desper and 402 Gascuel 2002 has a subtle but consequential difference from our ME placement. Their 403 algorithm does not compute branch lenghts for inserted sequence (e.g.,  $x_1$  and  $x_2$ ). It is 404 able to compute the optimal placement topology without knowing branch lengths of the 405 backbone tree. Instead, it relies on pairwise distances among backbone sequences ( $\Delta$ ), 406 which are precomputed and saved in the data-structure mentioned before. In the context 407 of the greedy algorithm for tree inference, in each iteration, the data structure can be 408 updated in  $\Theta(n)$ , which does not impact the overall running time of the algorithm. 409 However, if we were to start with a tree of n leaves, computing this structure from scratch 410 would still require  $\Theta(n^2)$ . Thus, computing the placement for a new query would need 411 quadratic time, unless if the  $\Theta(n^2)$  precomputation is allowed to be amortized over  $\Omega(n)$ 412 queries. Our formulation, in contrast, uses branch lengths of the backbone tree (which is 413 assumed fixed) and thus never uses pairwise distances among the backbone sequences. 414 Thus, using tree distances is what allows us to develop a linear time algorithm. 415

Our comparisons between versions of APPLES answered many questions but left 416 others to future work. For example, we observed no advantage in using models more 417 complex than  $JC69+\Gamma$  for distance calculation. However, these results may be due to our 418 estimation of model parameters (e.g., base compositions) for each pair of sequences. More 419 complex models may perform better if we instead estimate model parameters on the 420 backbone alignment/tree and reuse the parameters for queries (or simultaneously among 421 all queries and the reference sequences). Simultaneous estimation of distances has many 422 advantages over using independent distances for the *de novo* case (Tamura *et al.*, 2004; 423

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<sup>424</sup> Xia, 2009); these results gives us hope that using simultaneous distances inside APPLES
<sup>425</sup> can further improve its accuracy.

In the aligned case, we were unable to test other methods. LSHPlace is theoretically 426 fast, but we could not find an implementation of it. The distance-based insertion algorithm 427 of FastME (Desper and Gascuel, 2002) is available only as part of a larger greedy 428 algorithm but is not available as a stand-alone feature to place on a given tree. SEPP 429 (Mirarab et al., 2012) performs alignment and placement simultaneously (using alignment 430 scores to help the placement); however, in our experiments, our goal was only to test the 431 placement step and not the alignment. Thus, we used true alignments in all the simulation 432 tests and left an exploration of the impact of alignment error on different methods to 433 future work. On a related note, future work can incorporate APPLES inside SEPP to 434 perform alignment and placement in a unified pipeline. 435

In our assembly-free test, we used Skmer to get distances because alternative 436 alignment-free methods of estimating distance generally either require assemblies (e.g., 437 Haubold, 2014; Leimeister and Morgenstern, 2014; Leimeister et al., 2017) or higher 438 coverage than Skmer (e.g., Benoit et al., 2016; Yi and Jin, 2013; Ondov et al., 2016); 439 however, combining APPLES with other alignment-free methods can be attempted in 440 future (finding the best way of computing distances without assemblies was not our focus). 441 Moreover, the Skmer paper has described a trick that can be used to compute log-det 442 distances from genome-skims. Future studies should test whether using that trick and 443 using GTR instead of JC69 improves accuracy. 444

Branch lengths of our backbone trees were computed using the same distance model as the one used for computing the distance of the query to backbone species. Using consistent models for the query and for the backbone branch lengths is essential for obtaining good accuracy (see Fig. S7 for evidence). Thus, in addition to having a large backbone tree at hand, we need to ensure that branch lengths are computed using the right model. Fortunately, FastTree-2 can compute both topologies and branch lengths on

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large trees in a scalable fashion, without a need for quadratic time/memory computation
of distance matrices (Price *et al.*, 2010).

APPLES was an order of magnitude or more faster and less memory-hungry than 453 ML tools (pplacer and EPA-ng), but it has room for improvement. The python APPLES 454 code is not optimized and can be dramatically improved. For example, APPLES can save 455 precomputed values of Equations 3 and 4 for each backbone tree in a file, eliminating the 456 need to recompute them. Also, online processing of the backbone alignment can 457 dramatically reduce the memory usage for the distance calculation. Its current version uses 458 Dendropy (Sukumaran and Holder, 2010), which is not optimized for large trees; switching 459 to other platforms such as ETE (Huerta-Cepas *et al.*, 2010) can improve memory usage. 460 Future implementations of APPLES will improve speed and memory by applying such 461 optimizations. 462

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# APPENDIX

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| 654 | Appendix A. Proofs and derivations  |
|-----|---|
| 655 | Recall the following notations.   |
| 656 | • For any node $u$ and exponents $a \in \mathbb{Z}$ and $b \in \mathbb{N}^+$ , let                                      |
| 657 | $-S(a,b,u) = \sum_{i \in g(u)} \delta^a_{qi} d^b_{ui}$  |
| 658 | $- R(a, b, u) = \sum_{i \notin g(u)} \delta^a_{qi} d^b_{p(u)i} \text{ defined for } u \in V \setminus \{1\}$            |
| 659 | • For $b = 0$ , let $S(a, 0, u) = \sum_{i \in g(u)} \delta^a_{qi}$ and let $S'(a, u)$ be a shorthand for $S(a, 0, u)$ . |
| 660 | Similarly, let $R(a, 0, u) = R'(a, u) = \sum_{i \notin g(u)} \delta^a_{qi}$ .   |

# Proof of Lemma 2

*Proof.* Recall the dynamic programming recursions of Equations 3 and 4:

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$$S(a, b, u) = \sum_{j=0}^{b} \sum_{v \in c(u)} l(v)^{j} {b \choose j} S(a, b - j, v), \quad \text{for } u \notin \mathcal{L} \setminus \{1\}$$
$$R(a, b, u) = \sum_{j=0}^{b} \left( l(p(u))^{j} {b \choose j} R(a, b - j, p(u)) + \sum_{v \in sib(u)} l(v)^{j} {b \choose j} S(a, b - j, v) \right) \text{ for } u \notin \{1, 1'\}$$

Since u is not a leaf, for each leaf  $i \in g(u)$ , there exists a  $v \in c(u)$  such that the directed path from u to i passes through v. Therefore every leaf i can be grouped under its corresponding v.

$$S(a, b, u) = \sum_{i \in g(u)} \delta^{a}_{qi} d^{b}_{ui} = \sum_{v \in c(u)} \sum_{i \in g(v)} \delta^{a}_{qi} (l(v) + d_{vi})^{b} = \sum_{j=0}^{b} \sum_{v \in c(u)} \sum_{i \in g(v)} \delta^{a}_{qi} d^{b-j}_{vi} l(v)^{j} {b \choose j}$$
$$= \sum_{j=0}^{b} \sum_{v \in c(u)} l(v)^{j} {b \choose j} S(a, b - j, v)$$

Similarly, given the condition  $u \neq 1$ , for each leaf  $i \notin g(u)$ , either (1) there exists  $v \in sib(u)$  such that the directed path from p(u) to i passes through v, or (2) undirected path between i and p(u) passes through p(p(u)).

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$$\begin{aligned} R(a,b,u) &= \sum_{i \notin g(u)} \delta^a_{qi} d^b_{p(u)i} = \sum_{v \in sib(u)} \sum_{i \in g(v)} \delta^a_{qi} \left( l(v) + d_{vi} \right)^b + \sum_{i \notin g(p(u))} \delta^a_{qi} \left( l(p(u)) + d_{p(p(u))i} \right)^b \\ &= \sum_{j=0}^b \sum_{v \in sib(u)} \sum_{i \in g(v)} \delta^a_{qi} d^{b-j}_{vi} l(v)^j \binom{b}{j} + \sum_{j=0}^b \sum_{i \notin g(p(u))} \delta^a_{qi} d^{b-j}_{p(p(u))i} l(p(u))^j \binom{b}{j} \\ &= \sum_{j=0}^b \sum_{v \in sib(u)} l(v)^j \binom{b}{j} S(a, b - j, v) + \sum_{j=0}^b l(p(u))^j \binom{b}{j} R(a, b - j, p(u)) \end{aligned}$$

Boundary conditions follow from definitions. For  $u \notin \mathcal{L} \setminus \{1\}$ , since  $d_{ii} = 0$ , we have S(a, b, u) = 0 and it's trivial to see  $S'(a, u) = \delta^a_{qu}$ . For R(, ,) recursions, the boundary case happens at the unique child of the root, which we denote as 1'. Based on the definition, since the only  $i \notin g(1')$  is 1, and  $d^b_{p(1')1} = 0$ , we trivially have R(a, b, 1') = 0. For b = 0,  $R'(a, 1') = \delta^a_{q1}$ .

A post-order traversal on  $T^*$  can compute S(a, b, u), and a subsequent pre-order traversal can compute R(a, b, u), both in constant time and using constant memory per node. Recall that a and b are both no more than k, which is a constant. Thus, time and memory complexity of this dynamic programming is  $\Theta(bn)$ , which translates to  $\Theta(n)$  in least squares setting, where  $b \leq 2$ .

# Proof of Lemma 3.

Recall  $w_{qi} = \delta_{qi}^{-k}$  and that Equation 2:

$$Q(P) = \sum_{i=1}^{n} w_{qi} (\delta_{qi} - d_{qi}(P))^2 = \sum_{i=1}^{n} \delta_{qi}^{-k} (\delta_{qi} - d_{qi}(P))^2$$

<sup>676</sup> *Proof.* Equation 2 can be re-written as:

$$Q(P) = \sum_{i \in g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{ui}(P) - x_1 + x_2 - l(u) \right)^2 + \sum_{i \notin g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{p(u)i}(P) - x_1 - x_2 \right)^2$$
(S1)

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By simple rearrangement of the terms, we can rewrite Equation S1 as follows.

$$Q(P(u, x_1, x_2)) = R'(2 - k, u) + S'(2 - k, u) + R(-k, 2, u) + S(-k, 2, u) + 2(x_1 + x_2)(R(-k, 1, u) - R'(1 - k, u)) + 2(x_1 + l(u) - x_2)(S(-k, 1, u) - S'(1 - k, u)) + (x_1 + x_2)^2 R(-k, 1, u) + 2(x_1 + l(u) - x_2)^2 S(-k, 1, u) - 2R(1 - k, 1, u) - 2S(1 - k, 1, u)$$
(S2)

Note that computing  $Q(P(u, x_1, x_2))$  requires only S(, u) and R(, u) values and l(u). Thus, computing Q(P) requires only computing S(a, b, u) and R(a, b, u) values for

Find, computing 
$$Q(P)$$
 requires only computing  $S(a, b, u)$  and  $R(a, b, u)$  values for  
 $-k \leq a \leq 2 - k$  and  $0 \leq b \leq 2$ .

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Proof of Lemma 4.

**Recall** definitions

$$S(a, b, u) = \sum_{i \in g(u)} \delta^{a}_{qi} d^{b}_{ui} \quad (\text{for } b > 0) \qquad \text{and} \qquad S'(a, u) = S(a, 0, u) = \sum_{i \in g(u)} \delta^{a}_{qi} d^{b}_{qi}$$
$$R(a, b, u) = \sum_{i \notin g(u)} \delta^{a}_{qi} d^{b}_{p(u)i} \quad (\text{for } b > 0) \qquad \text{and} \qquad R'(a, u) = R(a, 0, u) = \sum_{i \notin g(u)} \delta^{a}_{qi} d^{b}_{qi}$$

and recall Eq. S1:

$$Q(P) = \sum_{i \in g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{ui}(P) - x_1 + x_2 - l(u) \right)^2 + \sum_{i \notin g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{p(u)i}(P) - x_1 - x_2 \right)^2.$$

<sup>683</sup> *Proof.* We take the derivative of Eq. S1 with respect to  $x_1$  and set it equal to zero:

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$$\begin{aligned} \frac{\partial Q(P)}{\partial x_1} &= -2\sum_{i\in g(u)} \delta_{qi}^{-k} \left(\delta_{qi} - d_{ui}(P) - x_1 + x_2 - l(u)\right) - 2\sum_{i\notin g(u)} \delta_{qi}^{-k} \left(\delta_{qi} - d_{p(u)i}(P) - x_1 - x_2\right) = 0\\ \implies \left(\sum_{i\in g(u)} \delta_{qi}^{-k} + \sum_{i\notin g(u)} \delta_{qi}^{-k}\right) x_1 + \left(-\sum_{i\in g(u)} \delta_{qi}^{-k} + \sum_{i\notin g(u)} \delta_{qi}^{-k}\right) x_2\\ &- \sum_{i\in g(u)} \delta_{qi}^{1-k} - \sum_{i\notin g(u)} \delta_{qi}^{1-k} + \sum_{i\in g(u)} \delta_{qi}^{-k} d_{ui}(P) + \sum_{i\notin g(u)} \delta_{qi}^{-k} d_{p(u)i}(P) + l(u) \sum_{i\in g(u)} \delta_{qi}^{-k} = 0\\ \implies \left(S'(-k,u) + R'(-k,u)\right) x_1 + \left(-S'(-k,u) + R'(-k,u)\right) x_2 = \\ S'(1-k,u) + R'(1-k,u) - S(-k,1,u) - R(-k,1,u) - l(u)S'(-k,u)\end{aligned}$$

Similarly,

$$\begin{aligned} \frac{\partial Q(P)}{\partial x_2} &= 2\sum_{i \in g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{ui}(P) - x_1 + x_2 - l(u) \right) - 2\sum_{i \notin g(u)} \delta_{qi}^{-k} \left( \delta_{qi} - d_{p(u)i}(P) - x_1 - x_2 \right) = 0 \\ \implies \left( -\sum_{i \in g(u)} \delta_{qi}^{-k} + \sum_{i \notin g(u)} \delta_{qi}^{-k} \right) x_1 + \left( \sum_{i \in g(u)} \delta_{qi}^{-k} + \sum_{i \notin g(u)} \delta_{qi}^{-k} \right) x_2 \\ &+ \sum_{i \in g(u)} \delta_{qi}^{1-k} - \sum_{i \notin g(u)} \delta_{qi}^{1-k} - \sum_{i \in g(u)} \delta_{qi}^{-k} d_{ui}(P) + \sum_{i \notin g(u)} \delta_{qi}^{-k} d_{p(u)i}(P) - l(u) \sum_{i \in g(u)} \delta_{qi}^{-k} = 0 \\ \implies \left( -S'(-k, u) + R'(-k, u) \right) x_1 + \left( +S'(-k, u) + R'(-k, u) \right) x_2 = \\ &- S'(1-k, u) + R'(1-k, u) + S(-k, 1, u) - R(-k, 1, u) + l(u)S'(-k, u) \end{aligned}$$

These two linear equations have a unique solution for the pair  $x_1, x_2$  if and only if the following matrix has the full rank:

$$H = \begin{bmatrix} R'(-k,u) + S'(-k,u) & R'(-k,u) - S'(-k,u) \\ R'(-k,u) - S'(-k,u) & R'(-k,u) + S'(-k,u) \end{bmatrix}.$$

Determinant of H is  $\det(H) = 4R'(-k, u)S'(-k, u)$ . Assuming that  $\delta_{qi} > 0$  for all  $i \in \mathcal{L}$ , both R'(-k, u) > 0 and S'(-k, u) > 0 hold. Therefore, H has the full rank. However,  $\delta_{qi} = 0$  for  $q \neq i$  can be encountered on real data, especially for low divergence times, low evolutionary rates, or short sequences. In this case, APPLES is designed to place q on the pendant edge of i with  $x_1 = 0$  and  $x_2 = l(i)$ . In case there are multiple leaves i that satisfy  $\delta_{qi} = 0$  for  $q \neq i$ , we pick one of them arbitrarily.

### REFERENCES

## Proof of Theorem 1

*Proof.* First, using two traversals of the tree, we compute all the S(a, b, u) and R(a, b, u)693 values by Lemma 2. To find the optimal placement edge, we first optimize  $Q(P(u, x_1, x_2))$ 694 for all  $u \in V \setminus \{1\}$ . By Lemma 4, this task requires only constant time after the 695 precomputions. Then, for each node, we compute  $Q(P(u, x_1, x_2))$  in constant time for the 696 optimal  $u, x_1, x_2$  by Lemma 3. Thus, each node is processed in linear time and the whole 697 optimization requires linear time. Note that the system of equations (shown in Lemma 4) 698 will not have a solution iff  $\delta_{qi} \leq 0$  for some *i*; if there is  $\delta_{qi} = 0$ , we make *q* sister to *i*, 699 breaking ties arbitrarily. 700

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# Proof of Lemma 5

Proof. Eigenvalues of the Hessian matrix of  $Q(P(u, x_1, x_2))$  are 2R'(-k, u) and 2S'(-k, u), which are both non-negative since  $\delta_{qi} \ge 0$  for  $i \in \mathcal{L}$ . Thus, the Hessian matrix is positive semidefinite and therefore  $P(u, x_1, x_2)$  is a convex function of  $x_1$  and  $x_2$ .

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## APPENDIX B. SUPPLEMENTARY FIGURES

### REFERENCES

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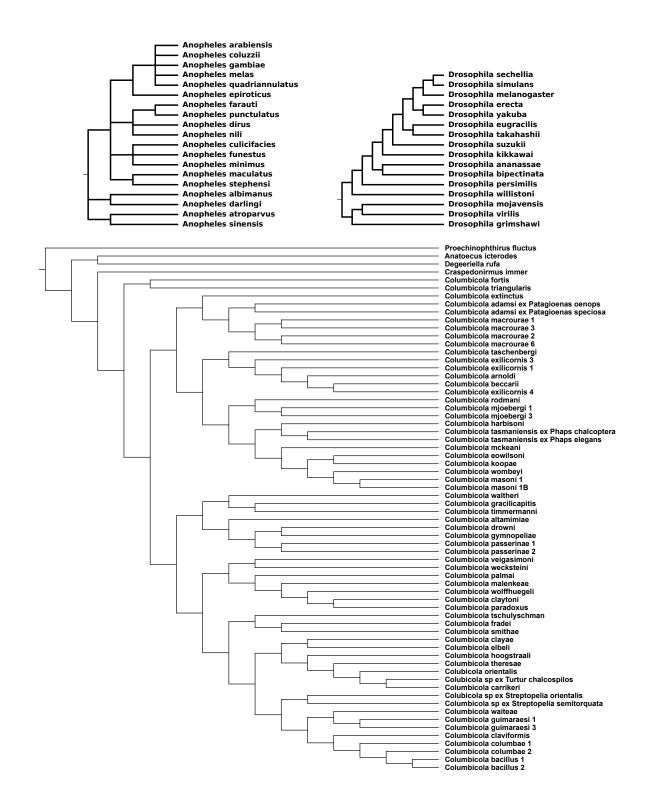


Fig. S1. The reference biological trees obtained from Open Tree of Life (Drosophila and Anopheles) and from Boyd *et al.* (2017) (Columbicola).

#### REFERENCES

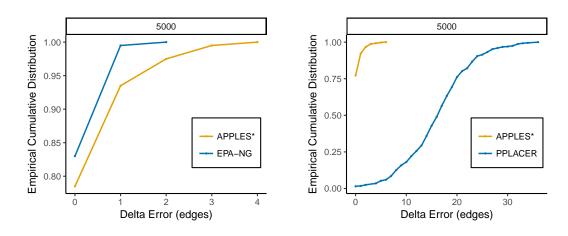


Fig. S2. **APPLES versus ML tools on 5,000 backbone trees**. The empirical cumulative distribution of the delta error is shown. We compare pplacer, EPA-ng, and APPLES\* on RNASim-varied backbone dataset with 5000 leaves. Distributions is over 551 cases where pplacer could run for the panel on the right and 200 points where EPA-NG could run for the panel on the left.

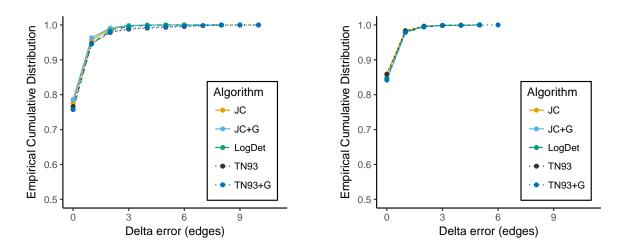


Fig. S3. **Comparing various models of DNA evolution**. For the GTR (a) and RNASim-heterogeneous (b) datasets, we show the delta error (edges) of APPLES\* run with five distance matrices calculated based on different models of DNA evolution. All model parameters are estimated per pair of sequences. The five models have similar accuracy.

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#### REFERENCES

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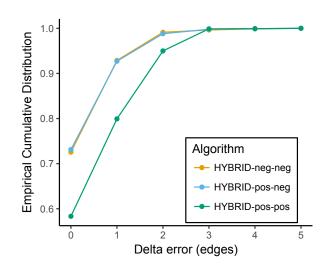


Fig. S4. The effect of imposing positivity constraint on accuracy on Hybrid. The HYBRID approach does not benefit from imposing positivity constraint on its second (ME) stage.

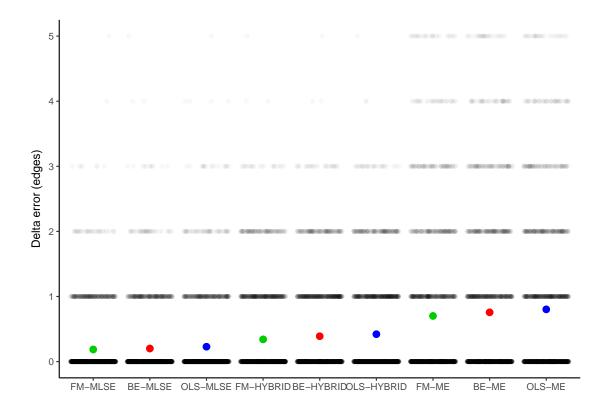


Fig. S5. **Comparing APPLES versions**. For the RNASim dataset (without controlling for the diameter), we show the delta error (edges) of APPLES run with three options for weighting: FM (green), BE (red), and OLS (blue), and three options for selection strategy (MLSE, ME, and Hybrid). For each method, the mean (colored circle) and standard errors (lines; too small to see) are shown over 2500 data points, each shown as dots. Some of the methods occasionally have error above 5 branches, but for better resolution, we cap the y-axis at 5.

REFERENCES

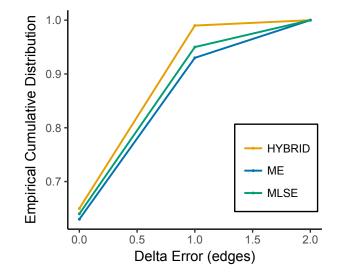


Fig. S6. **APPLES-HYBRID** has higher accuracy on sparse **RNAsim** dataset On the RNAsim dataset, we chose 20 sequences randomly from the larger RNAsim-heterogeneous dataset; here, APPLES-HYBRID has higher accuracy than APPLES\* (MLSE).

### REFERENCES



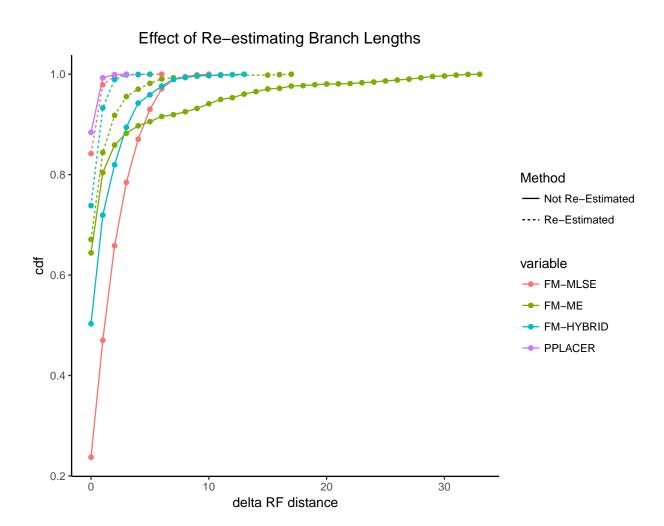


Fig. S7. The effect of reestimating branch lengths of the backbone tree on accuracy. We show the accuracy of pplacer and APPLES-FM with its three optimization criteria. APPLES is run both with (dotted) and without (solid) re-estimating branch lengths in the backbone tree using the same model (here, TN93+ $\Gamma$ ) used for computing distances of query sequences to backbone sequences. FastME\* is used to re-estimate branch lengths. Accuracy improves dramatically by recomputing backbone branch lengths using the same model. The case labeled "Not re-estimated" uses branch lengths produced using RAxML under the GTR+ $\Gamma$  model.

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### REFERENCES

## APPENDIX C. SUPPLEMENTARY TABLES

Table S1. GenBank accession numbers and URLs for the dataset of 22 Anopheles genomes

| Species                   | GenBank assembly accession | URL  |  |  |  |
|---------------------------|----------------------------|--|--|--|--|
| Anopheles albimanus       | GCA_000349125.1            | http://www.insect-genome.com/data/genome_download/Anopheles_albimanus/Anopheles_albimanus_genomic.fasta.gz   |  |  |  |
| Anopheles arabiensis      | GCA_000349185.1            | http://www.insect-genome.com/data/genome_download/Anopheles_arabiensis/Anopheles_arabiensis_genomic.fasta.gz |  |  |  |
| Anopheles atroparvus      | GCA_000473505.1            | http://www.insect-genome.com/data/genome_download/Anopheles_atroparvus/Anopheles_atroparvus_genomic.fasta.gz |  |  |  |
| Anopheles christyi        | GCA_000349165.1            | http://www.insect-genome.com/data/genome_download/Anopheles_christyi/Anopheles_christyi_genomic.fasta.gz     |  |  |  |
| Anopheles coluzzii        | -                          | http://www.insect-genome.com/data/genome_download/Anopheles_coluzzii/Anopheles_coluzzii_genomic.fasta.gz     |  |  |  |
| Anopheles culicifacies    | GCA_000473375.1            | http://www.insect-genome.com/data/genome_download/Anopheles_culicifacies/Anopheles_culicifacies_genomic.     |  |  |  |
|                           |                            | fasta.gz   |  |  |  |
| Anopheles darlingi        | GCA_000211455.3            | http://www.insect-genome.com/data/genome_download/Anopheles_darlingi/Anopheles_darlingi_genomic.fasta.gz     |  |  |  |
| Anopheles dirus           | GCA_000349145.1            | http://www.insect-genome.com/data/genome_download/Anopheles_dirus/Anopheles_dirus_genomic.fasta.gz           |  |  |  |
| Anopheles epiroticus      | GCA_000349105.1            | http://www.insect-genome.com/data/genome_download/Anopheles_epiroticus/Anopheles_epiroticus_genomic.fasta.gz |  |  |  |
| Anopheles farauti         | GCA_000956265.1            | http://www.insect-genome.com/data/genome_download/Anopheles_farauti/Anopheles_farauti_genomic.fasta.gz       |  |  |  |
| Anopheles funestus        | GCA_000349085.1            | http://www.insect-genome.com/data/genome_download/Anopheles_funestus/Anopheles_funestus_genomic.fasta.gz     |  |  |  |
| Anopheles gambiae         | GCA_000150785.1            | http://www.insect-genome.com/data/genome_download/Anopheles_gambiae/Anopheles_gambiae_genomic.fasta.gz       |  |  |  |
| Anopheles koliensis       | GCA_000956275.1            | http://www.insect-genome.com/data/genome_download/Anopheles_koliensis/Anopheles_koliensis_genomic.fasta.gz   |  |  |  |
| Anopheles maculatus       | GCA_000473185.1            | http://www.insect-genome.com/data/genome_download/Anopheles_maculatus/Anopheles_maculatus_genomic.fasta.gz   |  |  |  |
| Anopheles melas           | GCA_000473525.2            | http://www.insect-genome.com/data/genome_download/Anopheles_melas/Anopheles_melas_genomic.fasta.gz           |  |  |  |
| Anopheles merus           | GCA_000473845.2            | http://www.insect-genome.com/data/genome_download/Anopheles_merus/Anopheles_merus_genomic.fasta.gz           |  |  |  |
| Anopheles minimus         | GCA_000349025.1            | http://www.insect-genome.com/data/genome_download/Anopheles_minimus/Anopheles_minimus_genomic.fasta.gz       |  |  |  |
| Anopheles nili            | GCA_000439205.1            | http://www.insect-genome.com/data/genome_download/Anopheles_nili/Anopheles_nili_genomic.fasta.gz             |  |  |  |
| Anopheles punctulatus     | GCA_000956255.1            | http://www.insect-genome.com/data/genome_download/Anopheles_punctulatus/Anopheles_punctulatus_genomic.fasta. |  |  |  |
|                           |                            | gz   |  |  |  |
| Anopheles quadriannulatus | GCA_000349065.1            | -<br>http://www.insect-genome.com/data/genome_download/Anopheles_quadriannulatus/Anopheles_quadriannulatus_  |  |  |  |
|                           |                            | genomic.fasta.gz   |  |  |  |
| Anopheles sinensis        | GCA_000441895.2            | http://www.insect-genome.com/data/genome_download/Anopheles_sinensis/Anopheles_sinensis_genomic.fasta.gz     |  |  |  |
| Anopheles stephensis      | GCA_000300775.2            | http://www.insect-genome.com/data/genome_download/Anopheles_stephensi/Anopheles_stephensi_genomic.fasta.gz   |  |  |  |

Table S2. GenBank accession numbers and URLs for the dataset of 21 Drosophila genomes

| Species                 | GenBank assembly accession | URL  |  |  |  |
|-------------------------|----------------------------|--|--|--|--|
| Drosophila ananassae    | GCA_000005115.1            | http://www.insect-genome.com/data/genome_download/Drosophila_ananassae/Drosophila_ananassae_genomic.fasta.gz   |  |  |  |
| Drosophila biarmipes    | GCA_000233415.2            | http://www.insect-genome.com/data/genome_download/Drosophila_biarmipes/Drosophila_biarmipes_genomic.fasta.gz   |  |  |  |
| Drosophila bipectinata  | GCA_000236285.2            | http://www.insect-genome.com/data/genome_download/Drosophila_bipectinata/Drosophila_bipectinata_genomic.fasta. |  |  |  |
|                         |                            | gz   |  |  |  |
| Drosophila elegans      | GCA_000224195.2            | http://www.insect-genome.com/data/genome_download/Drosophila_elegans/Drosophila_elegans_genomic.fasta.gz       |  |  |  |
| Drosophila erecta       | GCA_000005135.1            | http://www.insect-genome.com/data/genome_download/Drosophila_erecta/Drosophila_erecta_genomic.fasta.gz         |  |  |  |
| Drosophila eugracilis   | GCA_000236325.2            | http://www.insect-genome.com/data/genome_download/Drosophila_eugracilis/Drosophila_eugracilis_genomic.fasta.gz |  |  |  |
| Drosophila ficusphila   | GCA_000220665.2            | http://www.insect-genome.com/data/genome_download/Drosophila_ficusphila/Drosophila_ficusphila_genomic.fasta.gz |  |  |  |
| Drosophila grimshawi    | GCA_000005155.1            | http://www.insect-genome.com/data/genome_download/Drosophila_grimshawi/Drosophila_grimshawi_genomic.fasta.gz   |  |  |  |
| Drosophila kikkawai     | GCA_000224215.2            | http://www.insect-genome.com/data/genome_download/Drosophila_kikkawai/Drosophila_kikkawai_genomic.fasta.gz     |  |  |  |
| Drosophila melanogaster | GCA_000778455.1            | http://www.insect-genome.com/data/genome_download/Drosophila_melanogaster/Drosophila_melanogaster_genomic.     |  |  |  |
|                         |                            | fasta.gz   |  |  |  |
| Drosophila miranda      | GCA_000269505.2            | http://www.insect-genome.com/data/genome_download/Drosophila_miranda/Drosophila_miranda_genomic.fasta.gz       |  |  |  |
| Drosophila mojavensis   | GCA_000005175.1            | http://www.insect-genome.com/data/genome_download/Drosophila_mojavensis/Drosophila_mojavensis_genomic.fasta.gz |  |  |  |
| Drosophila persimilis   | GCA_000005195.1            | http://www.insect-genome.com/data/genome_download/Drosophila_persimilis/Drosophila_persimilis_genomic.fasta.gz |  |  |  |
| Drosophila rhopaloa     | GCA_000236305.2            | http://www.insect-genome.com/data/genome_download/Drosophila_rhopaloa/Drosophila_rhopaloa_genomic.fasta.gz     |  |  |  |
| Drosophila sechellia    | GCA_000005215.1            | http://www.insect-genome.com/data/genome_download/Drosophila_sechellia/Drosophila_sechellia_genomic.fasta.gz   |  |  |  |
| Drosophila simulans     | GCA_000259055.1            | http://www.insect-genome.com/data/genome_download/Drosophila_simulans/Drosophila_simulans_genomic.fasta.gz     |  |  |  |
| Drosophila suzukii      | GCA_000472105.1            | http://www.insect-genome.com/data/genome_download/Drosophila_suzukii/Drosophila_suzukii_genomic.fasta.gz       |  |  |  |
| Drosophila takahashii   | GCA_000224235.2            | http://www.insect-genome.com/data/genome_download/Drosophila_takahashii/Drosophila_takahashii_genomic.fasta.gz |  |  |  |
| Drosophila virilis      | GCA_000005245.1            | http://www.insect-genome.com/data/genome_download/Drosophila_virilis/Drosophila_virilis_genomic.fasta.gz       |  |  |  |
| Drosophila willistoni   | GCA_000005925.1            | http://www.insect-genome.com/data/genome_download/Drosophila_willistoni/Drosophila_willistoni_genomic.fasta.gz |  |  |  |
| Drosophila yakuba       | GCA_000005975.1            | http://www.insect-genome.com/data/genome_download/Drosophila_yakuba/Drosophila_yakuba_genomic.fasta.gz         |  |  |  |

Table S3. GenBank accession numbers of microbial species used in contamination removal.

| Species                    | GenBank assembly accession |  |
|----------------------------|----------------------------|--|
| Pasteurella langaaensis    | GCA_003096995.1            |  |
| Providencia stuartii       | GCA_001558855.2            |  |
| Serratia marcescens        | GCA_000783915.2            |  |
| Shiqella flexneri          | GCA_000006925.2            |  |
| Commensalibacter intestini | GCA_002153535.1            |  |
| Acetobacter malorum        | GCA_002153605.1            |  |
| Acetobacter pomorum        | GCA_002456135.1            |  |
| Lactobacillus plantarum    | GCA_000203855.3            |  |
| Lactobacillus brevis       | GCA_003184305.1            |  |
| Enterococcus faecalis      | GCA_002208945.2            |  |
| Vagococcus teuberi         | GCA_001870205.1            |  |
| Wolbachia                  | GCA_000022285.1            |  |

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|                       | 0.1G |            |           | $0.5\mathrm{G}$ |            |           |
|-----------------------|------|------------|-----------|-----------------|------------|-----------|
|                       | %    | $\Delta e$ | $e_{max}$ | %               | $\Delta e$ | $e_{max}$ |
| (a) Columbicola       |      |            |           |                 |            |           |
| $\mathbf{APPLES}^*$   | 97   | 0.03       | 1         | 92              | 0.08       | 1         |
| APPLES-ME             | 84   | 0.28       | 5         | 87              | 0.21       | 5         |
| <b>PPLES-HYBRID</b>   | 87   | 0.16       | 2         | 87              | 0.16       | 2         |
| CLOSEST               | 54   | 1.15       | 7         | 58              | 0.91       | 8         |
| DE-NOVO               | 98   | 0.02       | 1         | 92              | 0.08       | 1         |
| (b) <b>Anopheles</b>  |      |            |           |                 |            |           |
| $\mathbf{APPLES}^*$   | 95   | 0.05       | 1         | 95              | 0.05       | 1         |
| APPLES-ME             | 95   | 0.05       | 1         | 95              | 0.05       | 1         |
| PPLES-HYBRID          | 95   | 0.05       | 1         | 95              | 0.05       | 1         |
| CLOSEST               | 91   | 0.09       | 1         | 95              | 0.05       | 1         |
| DE-NOVO               | 95   | 0.05       | 1         | 95              | 0.05       | 1         |
| (c) <b>Drosophila</b> |      |            |           |                 |            |           |
| APPLES*               | 71   | 0.29       | 1         | 71              | 0.33       | 2         |
| APPLES-ME             | 67   | 0.42       | 2         | 67              | 0.48       | 2         |
| PPLES-HYBRID          | 67   | 0.33       | 1         | 67              | 0.38       | 2         |
| CLOSEST               | 57   | 0.62       | 3         | 57              | 0.57       | 2         |
| DE-NOVO               | 71   | 0.29       | 1         | 71              | 0.33       | 2         |

Table S4. Assembly-free placement of genome-skims. We show the percentage of correct placements (those that do not increase  $\Delta e$ ), average delta error ( $\Delta e$ ), and maximum delta error ( $e_{max}$ ) for APPLES, assignment to the CLOSEST species, and the placement to the position in the backbone (DE-NOVO) over the 61 (a), 22 (b), and 21 (c) placements. Results are shown for skims with 0.1 and 0.5Gbp of reads. Delta error is the increase in the number missing branches between the reference tree and the backbone tree after placing each query.

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|-----|--|
| 707 | Appendix D. Commands   |
| 708 | Sampling Clades  |
| 709 | For sampling clades of size at most 250 from a tree "tree.nwk", we used the                    |
| 710 | TreeCluster package, available at https://github.com/niemasd/TreeCluster.                      |
|     | #!/bin/bash  |
|     | python TreeCluster/TreeCluster.py -i 250 -o clusters.txt -t tree.nwk                           |
|     | -m count_max_clade   |
|     |  |
| 711 | Backbone tree estimation   |
| 712 | When multiple sequence alignment is available, we used the following RAxML                     |
| 713 | command to compute backbone tree for all datasets except RNAsim varied size dataset.           |
| 714 | We used RAxML version 7.2.6  |
|     | #!/bin/bash  |
|     | raxmlHPC-PTHREADS -m GTRGAMMA -p 88 -n REF -s aln_dna.phy -T 6                                 |
| 715 | For RNAsim varied size dataset, we used FastTreeMP version 2.1.10 for estimating               |
| 716 | backbone topology. We run FastTreeMP with the following command:                               |
|     | #!/bin/bash  |
|     |  |
|     | FastTreeMP -nosupport -gtr -gamma -nt -log tree.log < aln_dna.fa > tree.nwk                    |
| 717 | For alignment free datasets such as Drosophila dataset, we computed backbone tree              |
| 718 | using FastME* (based on FastME version 2.1.6.1) which is available at                          |
| 719 | $\verb+https://github.com/balabanmetin/FastME-personal-copy.\ FastME* \ is \ run \ with \ the$ |
| 720 | following command:   |

# #!/bin/bash

fastme -i dist.mat -o tree.nwk -T 1

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Note that we performed Jukes-Cantor correction on the distance matrix "dist.mat"
 before running FastME\*.

723

## Backbone tree branch length re-estimation

When multiple sequence alignment is available, we used FastME\* to recompute backbone tree branch lengths for all datasets except RNAsim varied size dataset. We run

 $_{^{726}}$  FastME\* with the following command:

## #!/bin/bash

fastme -dJ -i aln\_dna.phy -u RAxML\_result.REF -o tree\_me.nwk

<sup>727</sup> For RNAsim varied size dataset, we used RAxML version 7.2.6 for re-estimating

<sup>728</sup> ML based branch lengths and used that tree for performing placements using pplacer.

<sup>729</sup> RAxML is run with the following command:

## #!/bin/bash

## raxmlHPC-PTHREADS -f e -t tree.nwk -m GTRGAMMA -s aln\_dna.phy -n REF -p 1984 -T 8

For the same dataset, we used FastTree again for re-estimating Minimum Evolution

<sup>731</sup> based branch lengths and used that tree for performing placements using APPLES.

<sup>732</sup> FastTree is run with the following command:

## #!/bin/bash

FastTreeMP -nosupport -nt -nome -noml -log tree.log
-intree tree.nwk < aln\_dna.fa > tree\_me.nwk

## Performing placement

We performed phylogenetic placement of a query using pplacer with the following commands:

### #!/bin/bash

733

nw\_prune RAxML\_result.REF query > backbone.nwk

47

48

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pplacer -m GTR -s RAxML\_info.REF -t backbone.nwk -o query.jplace aln\_dna.fa