

1 **Connectome architecture, gene expression and functional co-activation** 2 **shape the propagation of misfolded proteins in neurodegenerative disease**

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9 **ABSTRACT**

10 It is becoming increasingly clear that brain network organization shapes the course and expression
11 of neurodegenerative diseases. Parkinson's disease (PD) is marked by progressive spread of atrophy
12 from the midbrain to subcortical structures and eventually, to the cerebral cortex. Recent discoveries
13 suggest that the neurodegenerative process involves the misfolding of endogenous proteins (α -
14 synuclein) and prion-like spread of these pathogenic proteins via axonal projections. However, the
15 mechanisms that translate local "synucleinopathy" to large-scale network dysfunction and atrophy
16 remain unknown. Here we use an agent-based epidemic spreading model to integrate structural
17 connectivity, functional connectivity and gene expression, and to predict sequential volume loss
18 due to neurodegeneration. We demonstrate three key findings. First, the dynamic model replicates
19 the spatial distribution of empirical atrophy identified in an independent dataset of PD patients.
20 Second, the model implicates the substantia nigra as the disease epicenter, consistent with previous
21 literature. Third, we reveal a significant role for both connectome topology and spatial embedding
22 (geometry) in shaping the distribution of atrophy. Gene expression and functional co-activation
23 further amplify the course set by connectome architecture. Altogether, these results support the

24 notion that the progression of neurodegenerative disease is a multifactorial process that depends
25 on both cell-to-cell spreading of misfolded proteins and local regional vulnerability. The model
26 proves powerful in modelling neurodegeneration and provides insights into developing preventative
27 procedures.

28 INTRODUCTION

29 Neurodegenerative diseases such as Alzheimer's Disease (AD), Parkinson's Disease (PD), and
30 Amyotrophic Lateral Sclerosis, are a major cause of psychosocial burden and mortality, and lack
31 specific therapy. Until recently, the mechanism of progressive neuronal death in these conditions
32 was unknown. However, converging lines of evidence from molecular, animal and human post-
33 mortem studies point to misfolded neurotoxic proteins that propagate through the central nervous
34 system via neuronal connections (Brundin and Melki 2017; Guo and Lee 2014; Polymenidou and
35 Cleveland 2012; Jucker and Walker 2013; Brettschneider et al. 2015; Walsh and Selkoe 2016).
36 These pathogenic misfolded disease-specific proteins function as corruptive templates that induce
37 their normal protein counterparts to adopt a similar conformational alteration, analogous to the self-
38 replication process of misfolded proteins in prion diseases. Examples include amyloid β -protein
39 ($A\beta$) and *tau* in AD and α -synuclein in PD. The misfolded proteins can deposit into insoluble
40 aggregates and progressively spread to interconnected neuronal populations through synaptic con-
41 nections. The model of a propagating proteinopathy remains controversial however (Surmeier et al.
42 2017), and direct evidence in humans remains mostly circumstantial (Kordower et al. 2008).

43 The prion hypothesis suggests that propagation dynamics in neurodegenerative diseases may be
44 modeled using methods derived from infectious disease epidemiology. Just as infectious diseases
45 spread via social networks, misfolded proteins propagate via the brain's connectome. There are
46 different approaches for modeling epidemic spread over a network. In simple compartmental
47 (equation-based) models, disease in any region is modeled as a concentration (e.g. of misfolded
48 protein) and propagation obeys the law of mass effect with first order kinetics (Raj et al. 2012;
49 Iturria-Medina et al. 2014). The epidemic is defined by a series of differential equations. Such
50 models are easily solved mathematically but have limited explanatory power. Another approach is

51 the agent-based model (Frias-Martinez et al. 2011), in which the infectious state of each individual
52 agent and its motility are simulated, and where simple local interactions can translate into complex
53 global behavior. They have the advantage of easily incorporating additional emergent properties of
54 a system as the epidemic spreads – for example a brain region may lose its ability to propagate the
55 disease once it is severely affected. They also easily incorporate differences among agents (e.g. in
56 susceptibility to infection or mobility), and are useful for testing interventions (e.g. vaccination).
57 Agent-based models tend to be computationally demanding and are limited in their ability to
58 model epidemics on large or complex networks. Metapopulation structured models are hybrids
59 in which disease dynamics within subpopulations follow a compartmental model, while disease
60 spread from region to region depends on network properties (Balcan et al. 2010). They are also
61 less computationally expensive and more tractable than pure agent-based models.

62 Here we propose a Susceptible-Infectious-Removed (S-I-R) metapopulation structured model
63 on a brain network to model the spreading of pathological proteins in neurodegenerative diseases
64 (FIG. 1). The agents are individual proteins. The population is split into S, the portion yet
65 to be infected (normal proteins); I, the portion capable of transmitting the infection (misfolded
66 proteins); and R, the portion no longer active in the spreading (metabolized and cleared proteins).
67 We took PD as an example to show how a S-I-R metapopulation structured model can track the
68 spreading of misfolded α -synuclein, the pathological fibrillar species of endogenous α -synuclein
69 suggested to be responsible for PD pathology. Although convincing evidence from animal (Luk
70 et al. 2012; Mougenot et al. 2012; Goedert et al. 2013; Masuda-Suzukake et al. 2013; Peelaerts
71 et al. 2015; Rey et al. 2016; Brundin and Kordower 2012) and neuroimaging studies (Zeighami
72 et al. 2015; Yau et al. 2018) supports the propagation of misfolded and neurotoxic α -synuclein,
73 other mechanisms may also drive PD pathology, including cell-autonomous factors, dependent
74 on gene expression, that modulate regional neuronal vulnerability (Surmeier et al. 2017). If
75 the pathology of neurodegenerative diseases is indeed driven by progressive accumulation and
76 propagation of disease-related proteins, such a model should recapitulate the spatial pattern of
77 regional neurodegeneration in patients thereby providing converging and independent evidence for

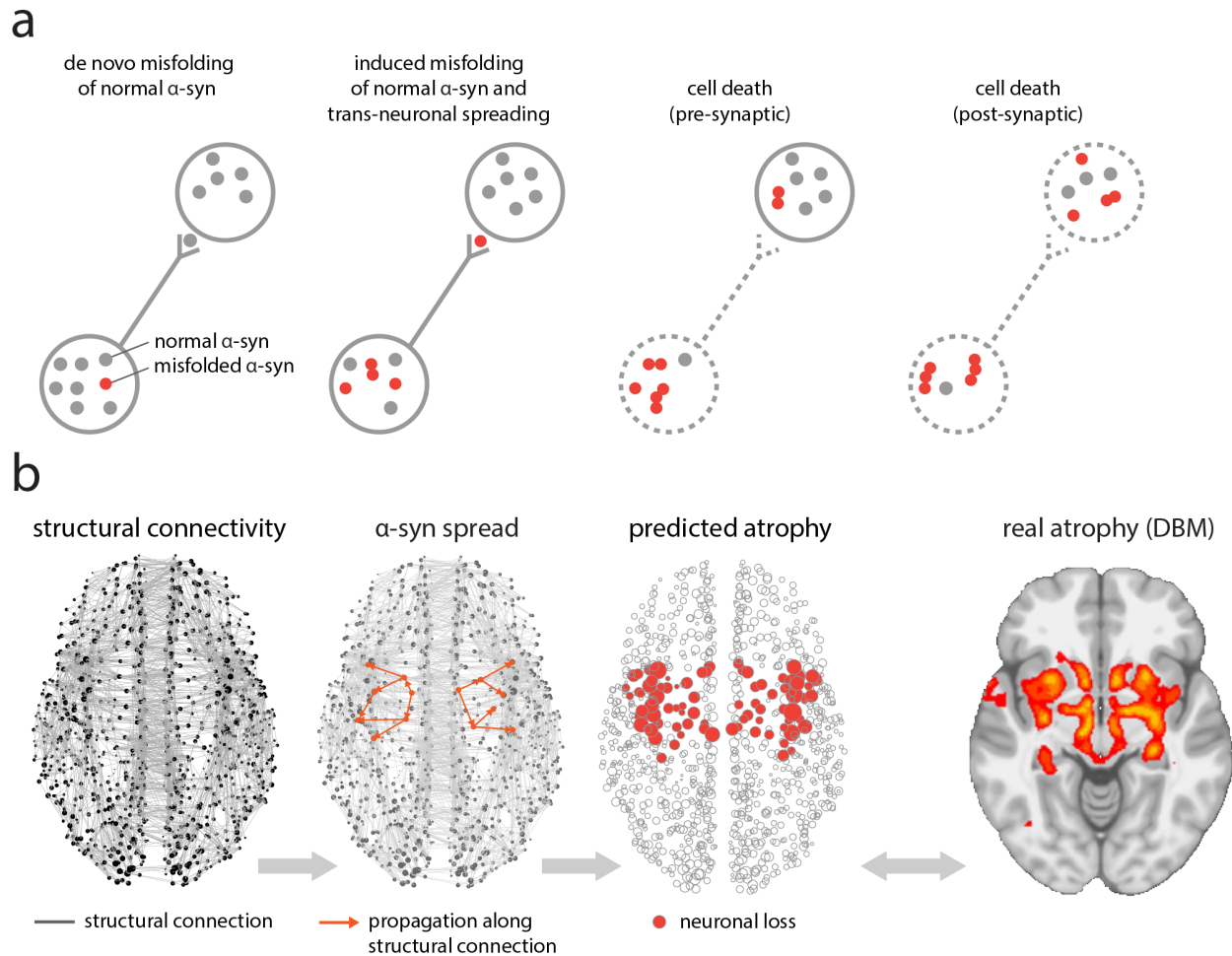


Fig. 1. Agent-based S-I-R model | (a) Misfolded α -synuclein (red) may diffuse through synaptic connections into adjacent neurons, causing misfolding of normal α -synuclein (gray). Accumulation of misfolded α -synuclein induces neuronal loss. (b) At the macroscopic level, misfolded α -synuclein propagates via structural connections, estimated from diffusion-weighted imaging. Simulated neuronal loss (atrophy) is compared against empirical atrophy, estimated from PD patients using deformation-based morphometry (DBM).

78 the pathogenic spread hypothesis. We also investigate whether selective vulnerability may influence
79 the spatial patterning of the disease.

80 Using brain imaging data from Parkinson's Progression Markers Initiative (PPMI) (Marek et al.
81 2011) and Human Connectome Project (HCP) (Van Essen et al. 2013), and gene expression profiles
82 from the Allen Human Brain Atlas (AHBA) (Hawrylycz et al. 2012), we constructed a S-I-R
83 metapopulation structured model to simulate the spreading of misfolded α -synuclein and regional
84 accrual of neuronal loss (atrophy). Measurements of empirical atrophy in PD patients were derived

85 from structural magnetic resonance imaging (MRI) scans in PPMI and healthy connectomes that
86 characterize the mobility pattern of the agents (α -synuclein) were constructed from HCP, while
87 local gene expression of *SNCA* and *GBA* that modulate synuclein formation and degradation were
88 derived from AHBA. Simulated regional atrophy derives from (1) the accumulation of misfolded α -
89 synuclein aggregates and (2) deafferentation due to neurodegeneration in interconnected neuronal
90 populations. The study is organized as follows: first, we determine whether the model replicates
91 empirically measured brain atrophy in PD; second, we identify the likely epicenter for disease
92 initiation; third, we assess whether the disease spread is driven by non-cell-autonomous factors
93 (structural connectivity) and cell-autonomous vulnerability (regional gene expression data); finally,
94 we assess the role of activity-dependent spread of α -synuclein by incorporating resting state
95 functional connectivity information into the model.

96 RESULTS

97 Model Construction

- 98 • *Structural connectivity.* Diffusion-weighted MRI data from N=1027 healthy participants
99 was used to construct the anatomical network for α -synuclein propagation (source: HCP,
100 2017 S1200 release; (Van Essen et al. 2013)). Adjacency matrices were reconstructed
101 using deterministic streamline tractography (Yeh et al. 2013). A group consensus structural
102 connectivity matrix was constructed by selecting the most commonly occurring edges
103 averaged across all subjects, resulting in a binary density of 35% (Mišić et al. 2015; Mišić
104 et al. 2018).
- 105 • *Functional connectivity.* Resting-state functional MRI (fMRI) data from N=496 healthy
106 participants (source: HCP, 2015 S500 release; (Van Essen et al. 2013)) was used to construct
107 the functional connectome. Individual functional connectivity matrices were calculated
108 using Pearson's correlation coefficient and then normalized using Fisher's z transform. A
109 group correlation matrix was then constructed by first averaging the z-score connectivity
110 matrices across subjects, and then converted back to correlation values using the inverse
111 transformation. Negative correlation values in the resultant group connectivity matrix were

- 112 set to zero.
- 113 • *Gene expression.* mRNA transcription (measured using in-situ hybridization) profiles of
114 *SNCA* and *GBA* were averaged across samples in the same brain parcel and across the six
115 subjects in the AHBA dataset. These gene expression profiles determine the local synthesis
116 and degradation of α -synuclein (see *Methods*).
 - 117 • *Atrophy.* An atrophy map was derived from T1-weighted MRI scans of 237 PD patients and
118 118 age-matched healthy controls (source: PPMI; (Marek et al. 2011)). For each participant
119 (patient or healthy control), the Deformation-based Morphometry (DBM) value in each
120 parcel was estimated to quantify the local volume change, on which an un-paired t-test was
121 conducted between the patients and healthy controls. The resulting t-statistics were taken
122 as the measure of regional atrophy (Zeighami et al. 2015).

123 The brain MRI template was parcellated according to an anatomical segmentation-based atlas,
124 featuring 68 bilateral cortical and 15 subcortical regions (Desikan et al. 2006; Cammoun et al. 2012;
125 Keuken et al. 2014). As only two of the six post-mortem AHBA brains have right hemispheric data
126 available, and diffusion tractography is prone to errors in detecting interhemispheric connections,
127 we simulated propagation using only the left hemisphere from the model, yielding 42 regions in
128 total.

129 *Synuclein propagation.* We posited that regional expression level of endogenous α -synuclein
130 already existing in the brain before disease onset may bias the trajectory of misfolded α -synuclein
131 propagation. Therefore, to estimate regional density of endogenous α -synuclein in healthy brain,
132 we set up a process that used generic information only to simulate the population growth of normal
133 α -synuclein agents. Normal agents in region i are synthesized in each unit area (1mm^3 voxel) per
134 unit time with probability α_i (the synthesis rate in region i). Meanwhile, any agent already existing
135 in region i can: (a) exit region i and move into the edges it connects to with probabilities proportional
136 to the corresponding connection strengths (densities of the fiber tracts); (b) remain in region i where
137 it may be metabolized with probability β_i (the clearance rate in region i). Likewise, the agents in
138 edge (i, j) can (a) exit edge (i, j) to enter region j with probability $1/l_{ij}$ where l_{ij} is the mean length of

139 the fiber tracts between region i and j , reflecting our intuition that agents in longer edges have lower
140 probability of exiting the edge; (b) remain in edge (i, j) with probability $1 - 1/l_{ij}$. The synthesis
141 rate α_i and clearance rate β_i in region i are the *SNCA* and *GBA* expression z-scores respectively
142 in region i converted to $[0, 1]$ using the standard normal cumulative distribution function. The
143 system has only one stable point which can be found numerically (see *Supplementary Information*),
144 suggesting that the growth of α -synuclein will deterministically converge to an equilibrium state
145 set by the connectome and the gene expression profiles. The regional density of normal agents
146 (number of agents per voxel) solved at the stable point was taken as the initial state of the misfolded
147 α -synuclein spreading process.

148 *Synuclein misfolding.* We next initiated the pathogenic spread by injecting misfolded α -
149 synuclein agents into the seed region, here chosen as the substantia nigra. The updating rules
150 of normal agents (above) were adapted to account for their susceptibility to infection from con-
151 tact with misfolded agents. Apart from the rules defined in the aforementioned growth process,
152 normal (susceptible) agents in region i that survive degradation can be infected with probability
153 γ_i thereby becoming misfolded (infected) agents (see *Methods*). In the absence of any molecular
154 evidence to the contrary, misfolded agents are updated with the same mobility (exiting/remaining
155 in regions/edges) and degradation (clearance rate) as normal agents. The new system seeded with
156 misfolded α -synuclein has two fixed points: (1) one represents the scenario in which misfolded
157 α -synuclein dies out, cleared by metabolic mechanisms before being able to transmit the infection to
158 the entire population; (2) the other represents a major outbreak of misfolded α -synuclein, spreading
159 to other regions via physical connections, causing further misfolding of endogenous α -synuclein
160 and widespread propagation (FIG. S1). In this model, neither the injection number of misfolded
161 α -synuclein agents nor the choice of seed region will affect the magnitude of misfolded α -synuclein
162 accumulation at the fixed point; rather, they determine whether the spreading process converges to
163 the epidemic scenario or dies out quickly. See TABLE. S1 for the full list of parameters and their
164 explanations.

165 Simulated neuronal loss replicates the spatial pattern of atrophy

166 We first investigated whether misfolded α -synuclein spreading on the healthy connectome can
167 replicate the spatial patterning of atrophy observed in PD patients. We simulated the propagation
168 of misfolded agents and the accrual of atrophy due to the toxic accumulation of the aggregates.
169 Two factors that may induce neuronal loss were accounted for: (1) the accumulation of misfolded
170 α -synuclein that will cause region-specific cell death directly; (2) atrophy due to deafferentation
171 secondary to cell death in connected regions. At each time point, we compared the relative
172 magnitude of simulated atrophy with the spatial pattern of empirical atrophy using Spearman's
173 rank correlation coefficient, yielding the model fit as a function of time t .

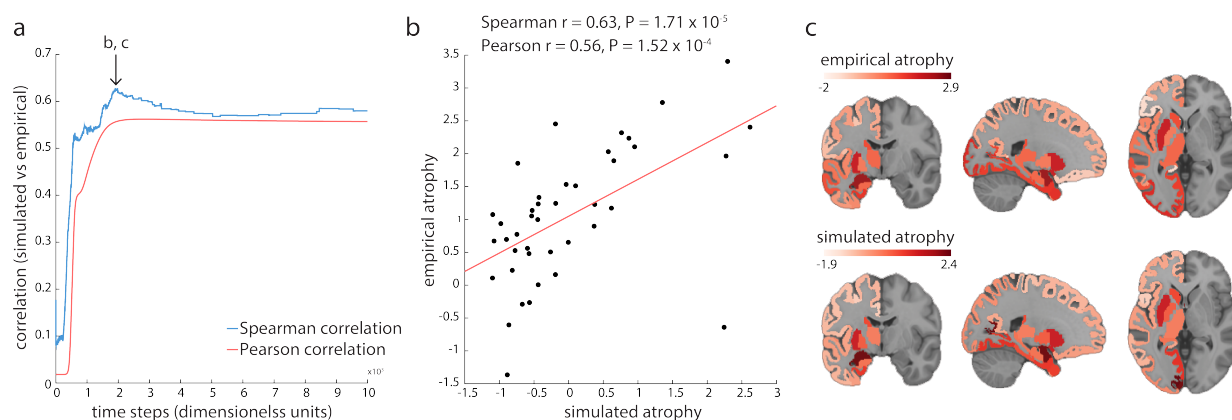


Fig. 2. Model fit | (a) Correlations between simulated atrophy and empirical atrophy derived from PD patient DBM maps up to $t = 10^4$. Correlations are shown as a function of simulation time. After reaching the peak value ($r = 0.63, r = 1.71 \times 10^{-5}$), the model fit slightly drops and finally stabilizes. In scanning along t to find the peak value, beginning timeframes were discarded to avoid picking up spurious correlation value as the peak (See *Supplementary Information*). See FIG. S2 for correlations up to $t = 10^5$. (b) Model fit at the peak of Spearman's correlation taken from panel a. Using Pearson's correlation coefficients yielded comparable results ($r = 0.56, p = 1.52 \times 10^{-4}$). Values shown in the axes are normalized. The outlier at the bottom right is the nucleus accumbens (for a possible explanation see *Discussion*). (c) Simulated atrophy and empirical atrophy plotted on the ICBM152 standard MNI template. The slices were chosen at $x=-22, y=-7, z=0$ (MNI coordinates).

174 As the misfolded agents propagate and accumulate in the system, the model fit increases up
175 to a maximum value ($r=0.63, p=1.71 \times 10^{-5}$, FIG. 2(a)) after which it drops slightly and stabilizes.
176 Note that we discarded early-spreading timeframes when scanning along t to find the maximum

177 correlation value (see *Supplementary Information*) to avoid picking up spurious model fit. We posit
178 that the slight decrease following the peak occurs because simulated atrophy becomes increasingly
179 widespread as the propagation of misfolded agents progresses, while the empirical atrophy was
180 derived from *de novo* PD patients at their first-visit in PPMI. FIG. 2(b) shows the linear relationship
181 between simulated and empirical atrophy across all nodes at peak fit, while FIG. 2(c) shows the
182 spatial correspondence between simulated and empirical atrophy. Model fit assessed by Pearson's
183 correlation coefficient produced comparable results ($r=0.56$, $p=1.52\times 10^{-4}$ at the peak, FIG. 2(a)(b)).
184 Interestingly, the model fit finally stabilizes with increasing t as the regional accumulation of
185 misfolded α -synuclein approximates the stable point (see FIG. S2 for model fit up to 10^5 time
186 steps), a finding that mirrors recent discoveries in animal models that α -synuclein eventually ceases
187 to propagate in later stages (Rey et al. 2018). We also note that misfolded α -synuclein arrival time
188 at each brain region follows the well-established Braak stages of PD (Braak et al. 2003; Braak et al.
189 2004) (FIG. S3).

190 We next investigated if the pattern of model fit as a function of t and its peak value were
191 consistent across variations in structural network densities. We selected varying subsets of the
192 most commonly occurring edges in the individual structural connectivity matrices, varying the
193 binary density of the group structural network matrix from 25% to 45%. We then simulated the
194 spreading processes on each network, derived the neuronal loss at each region and compared it with
195 the empirical atrophy pattern using Spearman's rank correlation coefficient. All the simulations
196 yielded comparable model fits with the peak correlation values consistently around 0.6 (FIG. 3,
197 blue curve), suggesting that the S-I-R metapopulation structured model is robust to variations in
198 network densities. Notably, we also assessed the Spearman's correlation between the regional
199 density of misfolded α -synuclein and the empirical atrophy pattern. Across the same set of
200 networks, simulated atrophy consistently provides better fits with the empirical atrophy than the
201 regional density of misfolded α -synuclein (FIG. 3, red curve), indicating that the cell death induced
202 by α -synuclein and deafferentation is a better measure to model regional atrophy accrual than the
203 mere accumulation of misfolded α -synuclein.

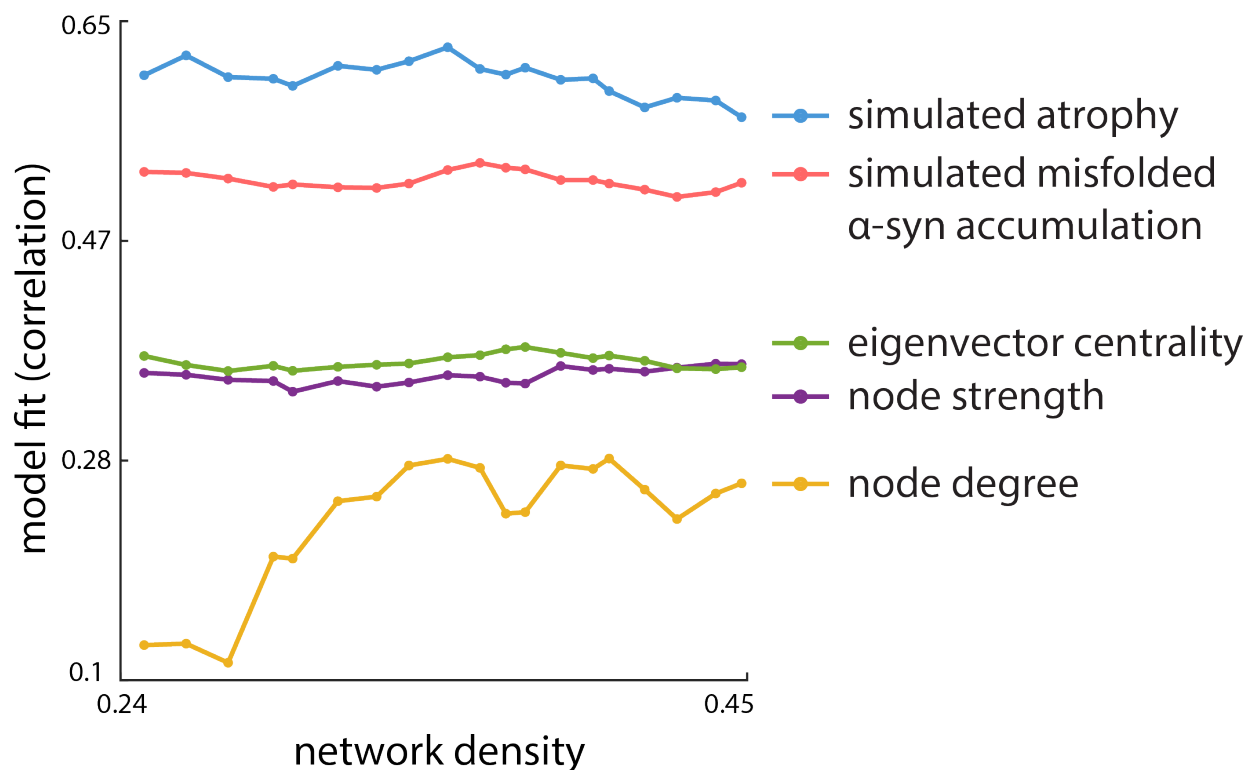


Fig. 3. The full dynamic model outperforms static network measures across multiple network densities | The full spread model has more predictive power than static topological metrics, including node degree (yellow), node strength (purple) and eigenvector centrality (green). Moreover, simulated atrophy (blue) yielded higher correlation with empirical atrophy than the density of misfolded α -synuclein (red, peak correlation along t at each density), suggesting that neuronal death induced by misfolded α -synuclein is a better measure to model atrophy in PD than the mere accumulation of misfolded α -synuclein. Model fit was assessed using Spearman's correlation coefficient. The overall pattern of results was consistent across multiple network densities. Using Pearson's correlation coefficient yielded similar results (FIG. S4).

204 Finally, we investigated whether the observed atrophy patterns could be directly reproduced from
205 simpler topological measures, without invoking metapopulation dynamics. We first tested whether
206 simple regional variation in *GBA* or *SNCA* expression are associated with regional variation in
207 atrophy. Neither *GBA* nor *SNCA* expression profiles bear a strong association with the spatial map of
208 empirical atrophy (*GBA*: Spearman's $r=-0.2402$, $p=0.1301$; Pearson's $r=-0.3109$, $p=0.0478$; *SNCA*:
209 Spearman's $r=-0.2385$, $p=0.1330$; Pearson's $r=-0.2824$, $p=0.0736$). Next, we tested whether simple
210 network metrics provide a comparable fit to the observed atrophy values. Structural connectivity
211 dictates the mobility pattern of the agents such that hub regions have a higher probability of

212 misfolded α -synuclein infiltration. We correlated the atrophy map with node-level network metrics
213 including node degree, node strength, and eigenvector centrality at each network density ranging
214 from 25% to 45%. Hubs, or nodes with greater degree connectivity or centrality, tend to be
215 more atrophied (FIG. 3, green, purple and yellow curves), echoing the findings that hubs are
216 often implicated in a host of brain disorders (Crossley et al. 2014). However, none of the metrics
217 performed better than simulated atrophy from the metapopulation model in matching the spatial
218 pattern of empirical atrophy. Altogether, these results suggest that the protein dynamics embodied
219 by the S-I-R metapopulation structured model provide predictive power above and beyond network
220 topology and gene expression.

221 **Identifying the disease epicenter**

222 We next investigate whether the model yielded a disease epicenter consistent with previous
223 literature. In the aforementioned process of normal α -synuclein growth, we solved the regional
224 density of normal agents at the stable point as a baseline estimation of endogenous α -synuclein
225 level in healthy brains. Recent findings from animal studies have suggested that α -synuclein
226 expression level correlates with neuronal vulnerability in PD (Rey et al. 2018; Luna et al. 2018);
227 likewise, in our model, higher regional abundance of normal α -synuclein agents indicates greater
228 likelihood of exposure to and growth of infectious agents, higher chance of disease transmission,
229 and consequently, greater vulnerability to the accumulation of misfolded α -synuclein.

230 We compared the regional density of normal α -synuclein agents with the empirical selective
231 vulnerability in patients to identify if highly vulnerable regions, such as substantia nigra, also
232 manifest abundance of α -synuclein. We find that, of the 42 left hemisphere regions, substantia nigra
233 has the highest normal α -synuclein level (FIG. 4, blue line). The elevated density of endogenous
234 α -synuclein renders substantia nigra susceptible to the encroaching of infectious misfolded α -
235 synuclein in the model, increasing both its vulnerability to misfolded protein and its chance of
236 acting as a disease epicenter. This corresponds with the clinical observations of Lewy body
237 inclusions and dopaminergic neuron loss identified in substantia nigra of PD patients as well as
238 its role in most of the presenting symptoms of the disease (Spillantini et al. 1998; Damier et al.

239 1999), supporting that substantia nigra is one of the most vulnerable regions to the epidemic attack
 240 of misfolded α -synuclein fibrils (Braak et al. 2004). Moreover, other basal ganglia regions have
 241 relatively high levels of normal α -synuclein at the equilibrium compared to cortical regions (caudate
 242 ranks among the highest 42.9% of all the regions; putamen, 31.0%; pallidum, 28.6%), consistent
 243 with their role in propagating the disease process to the cerebral cortex (Yau et al. 2018). These
 244 findings suggest that our model can indeed represent regional variations in selective vulnerability
 245 to the pathogenic attacks underlying PD progression by combining information from the healthy
 246 connectome and *SNCA* and *GBA* expressions.

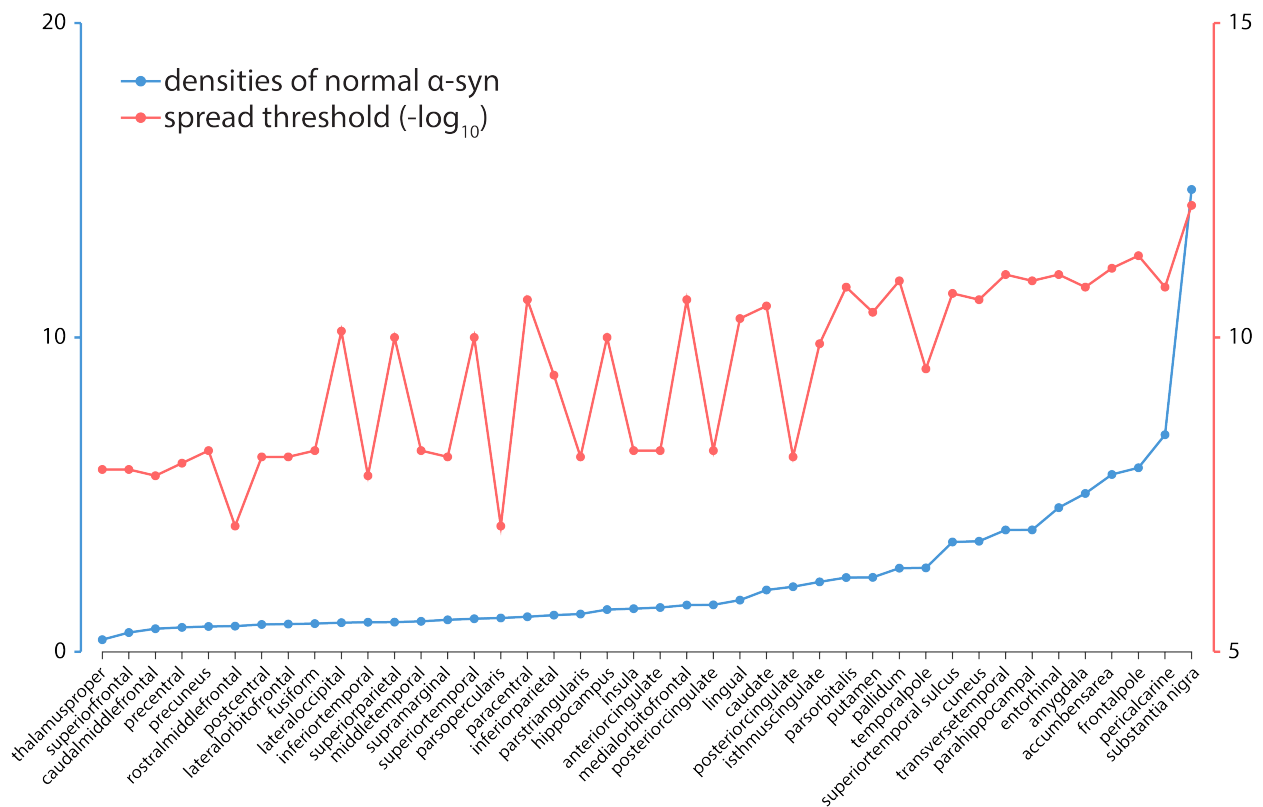


Fig. 4. Identifying the disease epicenter | Densities of normal α -synuclein (blue) at equilibrium (represented by the stable point) and spread threshold (red). Spread threshold was inverted by $-\log_{10}$, so higher values indicate lower thresholds. Spread thresholds reflect the susceptibility of a region to trigger an epidemic. Basal ganglia regions are rich in endogenous α -synuclein (caudate ranks among the top 42.9% regions; putamen, 31.0%; pallidum, 28.6%) and have relatively low spread threshold (caudate ranks among the lowest 35.7%; putamen, 38.1%; pallidum, 16.7%). Substantia nigra has the highest normal α -synuclein level and lowest spread threshold, making it the most probable epicenter of disease outbreak.

247 An alternative definition of disease epicenter is the seed node most likely to initiate a disease
248 outbreak. As explained in the previous section, the metapopulation model has two fixed points
249 representing disease extinction or major outbreak. Although the choice of seed region and injection
250 number of misfolded α -synuclein agents does not affect the magnitude of misfolded α -synuclein
251 accumulation, it can initially shift the properties of the two fixed points, determining which one
252 the system will converge to. We posited that the probability of triggering an outbreak indicates
253 the plausibility of acting as an epicenter. Therefore, we quantified the spread threshold for each
254 seed region, i.e., the minimally-required injection amount of misfolded α -synuclein to initiate an
255 outbreak. In traditional epidemic disease models that do not consider spatial structure or synthesis
256 of new susceptible hosts, *basic reproduction number* R_0 (the average number of susceptible agents
257 that could be affected by an infectious agent before it has been removed) marks the transition
258 between the regimes in which disease spreads or extinguishes (Newman 2010). However, in our
259 metapopulation structured high-order system in which new agents are constantly synthesized and
260 move across regions, the transition threshold can only be determined numerically.

261 Substantia nigra has the lowest spread threshold (FIG. 4, red line), suggesting that it is also the
262 most plausible seed region to initiate an epidemic spread. This is consistent with the notion that
263 substantia nigra acts as the epicenter for propagation to the supratentorial central nervous system
264 (Zeighami et al. 2015), and is generally one of the earliest regions to display neuronal loss in PD.
265 Interestingly, other basal ganglia regions also exhibited relatively low spread thresholds (caudate
266 ranks among the lowest 35.7% of all the regions; putamen, 38.1%; pallidum, 16.7%). Note however
267 that our model does not include regions caudal to the midbrain (see *Discussion*).

268 **Connectome architecture shapes disease spread**

269 We next asked whether model fit would be facilitated or degraded by disrupting the connectome's
270 topology or spatial embedding (geometry). To address this question, we implemented two types of
271 null models, in which (a) the topology of the connectome was randomized (rewired null); or (b) the
272 spatial positions of the regions were shuffled (spatial null). Rewired null networks were generated
273 by swapping pairs of edges while preserving the original degree sequence and density using the

274 Maslov-Sneppen algorithm (Maslov and Sneppen 2002) implemented in the Brain Connectivity
275 Toolbox (<https://sites.google.com/site/bctnet/>) (Rubinov and Sporns 2010). Spatial null networks
276 were generated by swapping the physical positions of the nodes while keeping their original
277 connection profiles (Roberts et al. 2016; Seguin et al. 2018). This null model retains the degree
278 sequence and connection profiles of every region, but randomizes spatial proximity. Networks at
279 binary density 25%, 30%, 35% and 40% were selected as representatives to construct the two types
280 of null networks, with 10,000 realizations each. We then implemented the dynamic model on each
281 network and compared model fits for the empirical and null networks.

282 The metapopulation model simulated on top of the empirical structural network yielded sig-
283 nificantly greater fit to empirical atrophy than models simulated on either type of null network.
284 This result was consistent across network densities (rewired null, FIG. 5(a): $p_{25\%} = 0.0014$,
285 $p_{30\%} < 0.001$, $p_{35\%} < 0.001$, $p_{40\%} = 0.0018$; spatial null, FIG. 5(b): $p_{25\%} < 0.001$, $p_{30\%} < 0.001$,
286 $p_{35\%} < 0.001$, $p_{40\%} < 0.001$) and suggests that the high correspondence between simulated and
empirical atrophy in PD is jointly driven by connectome topology and geometry.

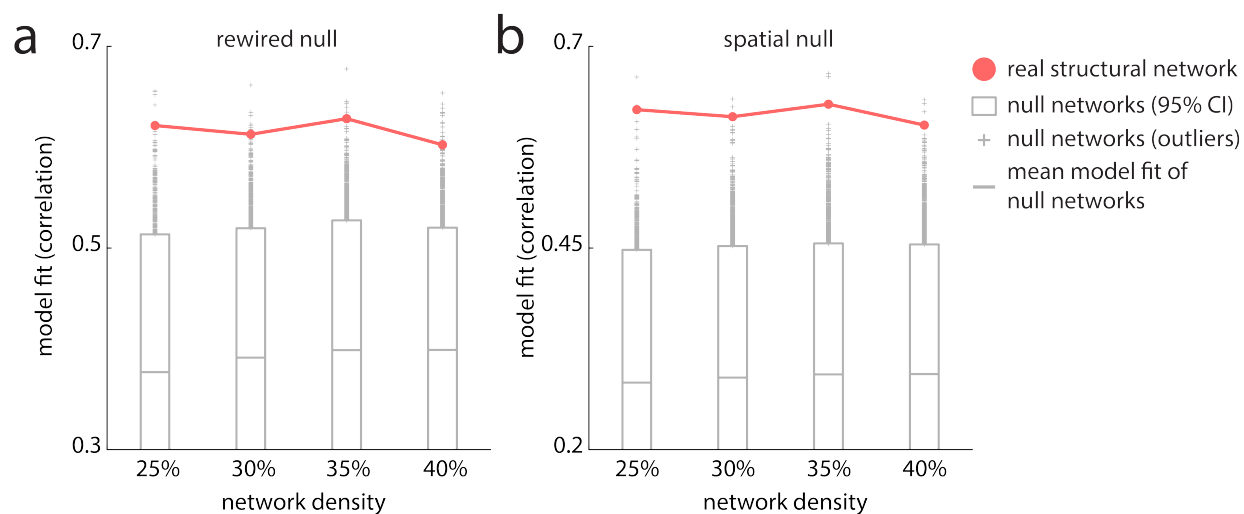


Fig. 5. Effects of network topology and geometry | Systematic disruption of (a) connectome topology (rewired null) or (b) spatial embedding (spatial null) significantly degrades model fit as measured by Spearman's correlation. Red = real structural network (empirical network); grey = null networks. Rewired null: $p_{25\%} = 0.0014$, $p_{30\%} < 0.001$, $p_{35\%} < 0.001$, $p_{40\%} = 0.0018$; spatial null: $p_{25\%} < 0.001$, $p_{30\%} < 0.001$, $p_{35\%} < 0.001$, $p_{40\%} < 0.001$.

287

288 **Gene expression shapes disease spread**

289 We next sought to directly assess the influence of local gene expression on spreading patterns
290 of neurodegeneration. Based on molecular evidence, the model uses regional expression of *GBA*
291 and *SNCA* as determinants of α -synuclein clearance and synthesis rate. Regional *GBA* and *SNCA*
292 expressions were shuffled 10,000 times respectively by re-assigning the expression scores in each
293 parcel (FIG. 6(a),(b) respectively). We then implemented the dynamic models with randomized
294 expression levels and compared differences in model fit when using the empirical gene expression
295 levels (FIG. 6, red) and permuted gene expression levels (FIG. 6, grey).

296 Shuffling the transcription profile of either gene significantly degrades model fit (FIG. 6(a), *GBA*:
297 $p_{25\%} = 0.0031$, $p_{30\%} < 0.001$, $p_{35\%} < 0.001$, $p_{40\%} = 0.0024$; FIG. 6(b), *SNCA*: $p_{25\%} = 0.0102$,
298 $p_{30\%} = 0.0201$, $p_{35\%} = 0.0084$, $p_{40\%} = 0.0334$) suggesting a significant role of *GBA* and *SNCA*
299 expression in driving the spatial patterning of atrophy. In other words, the regional expression of
300 the genes, as implemented in the dynamic model, serves to modulate the vulnerability of individual
301 nodes above and beyond their topological attributes by influencing α -synuclein synthesis, seeding
302 and clearance.

303 An alternative explanation for these results is that simply introducing regional heterogeneity in
304 gene expression levels improves model fit, for example because of differences in general transcrip-
305 tion levels between cortex and subcortex. To address this possibility, we further assessed model fit
306 in the cases where *GBA* and *SNCA* expression is made uniform across all brain regions. Instead of
307 using empirical gene expression, we set uniform synthesis/clearance rates across all regions using
308 the mean expression score, converted to a scalar value between [0, 1] using the standard normal
309 cumulative distribution function. We then computed the model fit (peak Spearman's correlation
310 value) for this "uniform" model. Critically, models using uniform transcription profiles under-
311 performed compared to those using empirical transcription profiles (FIG. 6, red = empirical, blue
312 = uniform); in other words, the incorporation of local differences in gene expression improves
313 model fit, suggesting that the atrophy pattern in PD is not solely explained by pathogenic spreading
314 *per se* but also depends on local vulnerability. Models implemented using uniform transcription

315 profiles of either gene exhibited above-chance model fit compared to shuffled transcription profiles
 316 (*GBA* uniform correlations: $r_{25\%} = 0.4479$, $r_{30\%} = 0.3869$, $r_{35\%} = 0.3672$, $r_{40\%} = 0.3481$; *SNCA*
 317 uniform correlations: $r_{25\%} = 0.5653$, $r_{30\%} = 0.5780$, $r_{35\%} = 0.5767$, $r_{40\%} = 0.5794$, blue line in
 318 FIG. 6). Altogether, these results demonstrate that regional expression of *GBA* and *SNCA* shapes
 319 the spatial patterning of atrophy in addition to connectome topology and spatial embedding.

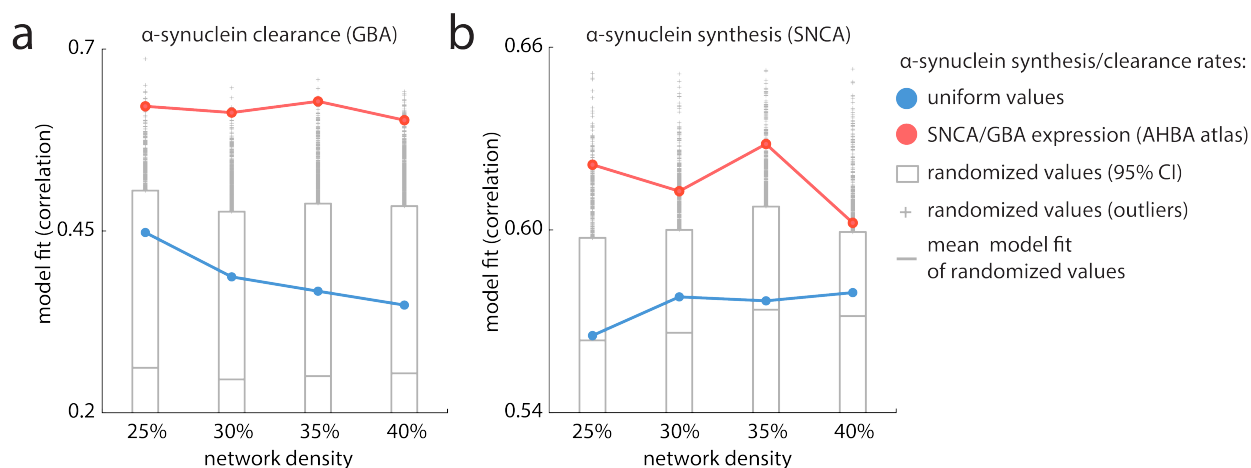


Fig. 6. Assessing the contribution of *GBA* and *SNCA* gene expression | To assess the influence of gene expression on atrophy, model fit using real expression values (red) is compared to null models in which node-wise expression profiles of *GBA* and *SNCA* (reflecting, respectively, α -synuclein clearance and synthesis) were shuffled. Both manipulations significantly reduce model fit regardless of network density (*GBA*: $p_{25\%} = 0.0031$, $p_{30\%} < 0.001$, $p_{35\%} < 0.001$, $p_{40\%} = 0.0024$; *SNCA*: $p_{25\%} = 0.0102$, $p_{30\%} = 0.0201$, $p_{35\%} = 0.0084$, $p_{40\%} = 0.0334$). Notably, uniform transcription profiles, in which all nodes have identical expression values (blue) yield above-chance model fit, but perform poorly compared to the model with real expression values (*GBA* uniform correlations: $r_{25\%} = 0.4479$, $r_{30\%} = 0.3869$, $r_{35\%} = 0.3672$, $r_{40\%} = 0.3481$; *SNCA* uniform correlations: $r_{25\%} = 0.5653$, $r_{30\%} = 0.5780$, $r_{35\%} = 0.5767$, $r_{40\%} = 0.5794$).

320 Structural and functional connectivity interact to drive disease spread

321 Finally, we tested whether neuronal activity or pre- and post-synaptic co-activation may facilitate
 322 α -synuclein propagation. Past neuroimaging studies have shown that cortical thinning in PD is
 323 predicted in part by functional connectivity to affected subcortical regions, and that regions that
 324 exhibit stronger functional connectivity with the substantia nigra tend to exhibit greater atrophy
 325 (Zeighami et al. 2015; Yau et al. 2018). Secretion of α -synuclein by neurons has been shown to
 326 be activity dependent (Paillusson et al. 2013). Spread of α -synuclein through multiple anatomical

327 pathways may be biased by synchronous activity between the pre- and post-synaptic cells, such that
328 the agents are more likely to move towards regions with higher functional connectivity to a seed
329 region.

330 To address this question, we integrated resting-state fMRI functional connectivity into the model.
331 We introduce a term $e^{k \times fc_{(i,j)}}$ to rescale the probability of moving from region i to region j previously
332 defined by the connection strength of edge (i, j) while keeping the sum of the probabilities equal to 1
333 to preserve the multinomial distribution (see *Methods*). As k is increased, the influence of functional
334 connectivity is greater: stronger co-activation patterns play a more influential role in modulating
335 the motion of the agents on structural connections. For structural edges with relatively small
336 corresponding functional connectivity values, larger k may decrease those edges' contributions to
337 favour propagation through edges with greater functional connectivity. All negative-valued and
338 non-significant functional connections were set to zero.

339 We varied k from 0 (no influence of functional connectivity) to 5 and derived the corresponding
340 peak values of model fit using the same four structural connectome densities as before (FIG. 7).
341 Model fit was improved by progressively increasing the importance of functional connectivity, but
342 only up to a point ($k_{25\%} = 1$, $k_{30\%} = 2.5$, $k_{35\%} = 2.5$, $k_{40\%} = 2.5$). Beyond this point, the influence
343 of functional connectivity dominates the agents' mobility pattern resulting in diminished model
344 fit. The results were consistent across network densities. These results provide evidence for the
345 notion that while α -synuclein propagation and resultant brain atrophy patterns occur via anatomical
346 connections, they may also be biased by neuronal activity.

347 An alternative explanation is that inclusion of functional connectivity simply leads to over-
348 fitting the model. To test this possibility, we investigated if the same improvement in model fit
349 could be observed if α -synuclein spread is biased by randomized functional connectivity patterns.
350 We generated "null" functional connectivity matrices by randomly re-assigning the parcellated
351 rs-fMRI time series into the 42 left hemisphere regions. The results are shown in FIG. S6. We note
352 two important results. First, atrophy patterns based on real functional connectivity consistently
353 yield significantly higher model fit than atrophy patterns based on null functional connectivity.

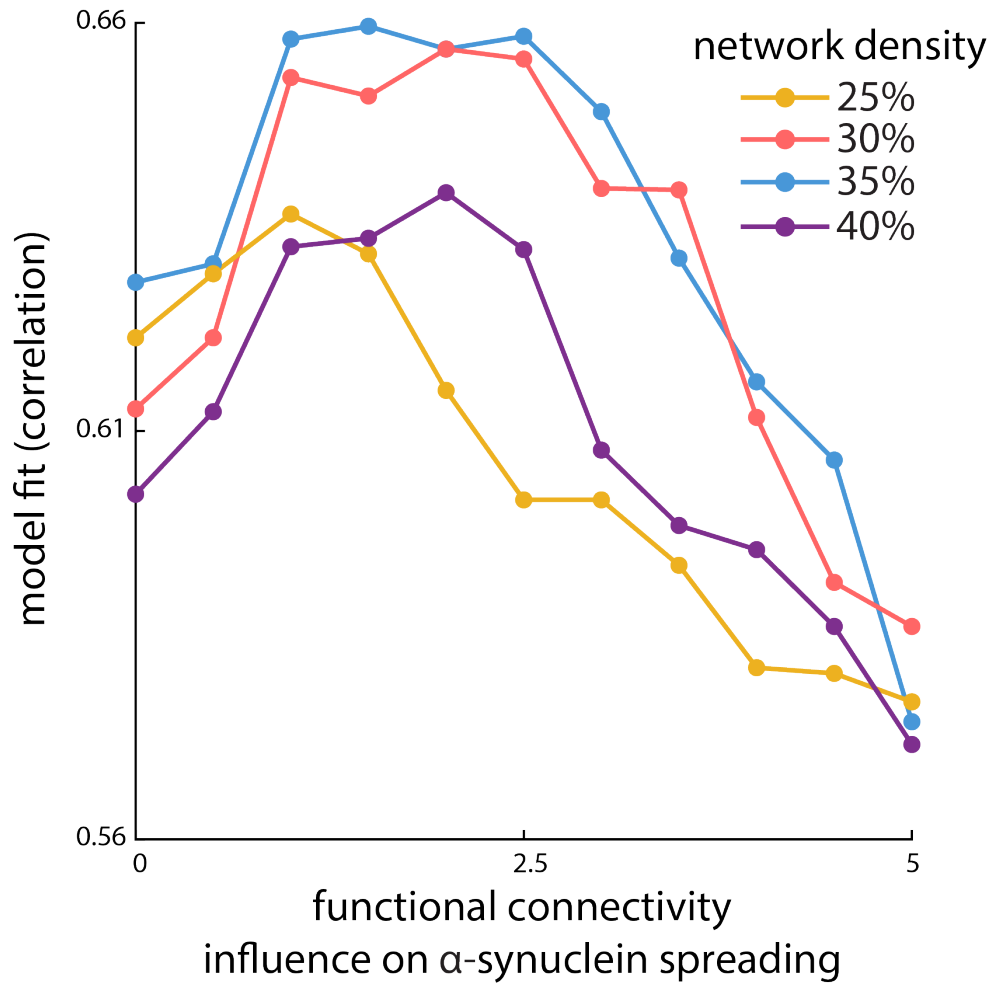


Fig. 7. Incorporating functional connectivity improves model fit | Resting-state fMRI functional connectivity was incorporated in the model by tuning the probability of α -synuclein propagation along structural connections. As the influence of functional connectivity is increased, α -synuclein spreading is biased towards structural connections that exhibit high functional connectivity. Model fit is shown for a range of structural connection densities. A balanced effect of functional connectivity and structural connectivity improves model performance, while excessive influence of functional connectivity degrades model fit. The same beneficial effect is not observed when randomized, “null” functional connectivity patterns are used (FIG. S6).

354 Second, model fits based on null functional connectivity do not have the same peaked shape as
355 observed when using real functional connectivity. This further support the conclusion that atrophy
356 patterns observed in PD patients depend on both the structural and functional architecture of the
357 brain.

358 DISCUSSION

359 We developed a metapopulation structured model of neurodegenerative disease consisting of
360 normal and misfolded proteins. Taking PD as an example, we integrated multimodal neuroimaging
361 and gene expression data to simulate the propagation of misfolded α -synuclein on the healthy
362 connectome. The metapopulation S-I-R model incorporates pathogenic spread (dominated by
363 the connectome) and selective vulnerability (modulated here by gene expression) under the same
364 computational framework. The dynamic model replicated the spatial pattern of measured brain
365 atrophy in PD patients and had greater predictive power than any of the constituent features (i.e.
366 network metrics or gene expression) on their own. Our results demonstrate that connectome
367 topology and geometry, local gene expression, and functional co-activation jointly shape disease
368 progression, as systematic disruption of each of these elements significantly degraded model
369 performance. This model yields insights into the mechanism of PD, providing support for the
370 propagating proteinopathy theory, and can be readily adapted to other neurodegenerative diseases.

371 Network-based epidemic models can be classified into two main categories: (1) compartmental
372 models, in which nodes of the graph adopt different states (e.g. concentration of disease), and
373 the infection propagates via diffusion; and (2) agent-based models, in which agents (in this case,
374 proteins) adopt different states (S-I-R) and interact with each other according to simple rules
375 (Newman 2010). The metapopulation S-I-R model used here is a hybrid, using a compartmental
376 model within (brain) subregions, but allowing agents to travel along the connectome (Balcan et al.
377 2010). This allows it to map the interaction between network architecture and regional susceptibility
378 and transmissibility. Solving our metapopulation S-I-R model numerically yielded two fixed (or
379 stable) points of the process after seeding of the infection: rapid extinction or epidemic spread. If
380 the system is attracted to extinction, misfolded proteins will eventually be removed from the system.
381 If the system is attracted to the fixed point that represents an outbreak, misfolded proteins will still
382 not accumulate boundlessly, but will finally achieve a stable concentration and co-exist with normal
383 proteins. These results are consistent with recent experimental evidence in rodents where injection
384 of misfolded α -synuclein fibrils either died out at specific injection sites (extinction), or grew but

385 ceased to propagate at a certain stage (Rey et al. 2018), suggesting the existence of an equilibrium.
386 These different outcomes (extinction vs outbreak) might perhaps represent normal aging versus
387 progressive neurodegeneration, or mild versus malignant PD (Fereshtehnejad et al. 2017).

388 *A priori* there are several topological properties of brain networks that favour disease spread.
389 Brains are canonical examples of small-world networks (Watts and Strogatz 1998), where path
390 lengths between any two nodes are relatively short, a feature that facilitates disease outbreaks
391 (Moore and Newman 2000). Brain networks display prominent community structure: the tendency
392 to cluster into highly interconnected communities or modules (Hilgetag and Kaiser 2004; Sporns
393 and Betzel 2016). Perhaps counter-intuitively, community structure may also potentiate global
394 disease spread by enhancing local, intra-community infection (Nematzadeh et al. 2014). Finally,
395 the presence of high degree nodes (hubs) that are highly interconnected with each other (van den
396 Heuvel et al. 2012) favours disease propagation. Hubs and are expected to have faster arrival
397 times, and greater accumulation of infected agents, making them especially vulnerable to attack.
398 Indeed, hubs manifest greater structural abnormalities in a host of neurodegenerative diseases
399 (Crossley et al. 2014). We showed that disruptions of the network's architecture reduce model fit,
400 providing evidence that the emergent dynamics of synucleinopathy depend on network connectivity
401 (topology) and geometry (spatial embedding).

402 While we did find that network metrics predict brain atrophy, the full dynamic agent-based
403 model provided a better fit to the empirical data (FIG. 3). Spatial proximity among regions
404 and local differences in synthesis/clearance (see below) both impose constraints on the spreading
405 process, amplifying or damping the rate of infection. As a result, atrophy patterns are shaped by,
406 but ultimately transcend, the underlying connection patterns. The present model correctly predicts
407 that the regions most vulnerable to atrophy are not simply those that participate in the greatest
408 number of connections or those that are a few steps away from other infected regions. A similar
409 phenomenon was recently described in schizophrenia: vulnerability of prefrontal "hub" regions to
410 grey matter atrophy may be a function of both connectivity and spatial location (Gollo et al. 2018).

411 More generally, the metapopulation model also allowed us to test two competing theories of

412 PD pathogenesis: protein propagation versus regional vulnerability (Brundin and Melki 2017;
413 Surmeier et al. 2017). Protein propagation, or the “pathogenic spread” hypothesis, is suggested to
414 be primarily driven by non-cell-autonomous factors such as network connectivity. Our model inte-
415 grates gene expression into a node’s properties, enabling us to operationalize additional molecular
416 cell-autonomous factors on hubs, which cannot be solely explained by network structure. Thus the
417 dynamics arise from an interplay between regional vulnerability and network-wide propagation.

418 Regional vulnerability may also depend on local cell-autonomous factors such as gene expres-
419 sion (Jackson 2014). Here we chose to model regional vulnerability by incorporating estimated
420 local α -synuclein concentration, known to facilitate seeding (Volpicelli-Daley et al. 2011) and
421 increase neuronal vulnerability in animal models (Luna et al. 2018). We used regional expression
422 of *GBA* and *SNCA* as estimates of α -synuclein clearance and synthesis rates to derive the concen-
423 tration of endogenous α -synuclein. We showed that incorporating this information into the model
424 improved the correlation with empirical atrophy in PD patients; moreover, spatial permutation of
425 gene expression degraded the fit. Thus, our findings support a key role for both propagation and
426 local vulnerability in shaping PD progression.

427 Our results provide converging evidence for the involvement of *GBA* and *SNCA* in PD pathology
428 previously indicated in animal and cellular studies (Alcalay et al. 2015). Mutations in *GBA* are
429 the most common genetic risk factor for PD (Aharon-Peretz et al. 2004; Sidransky and Lopez
430 2012); mutations and multiplications of *SNCA* have been implicated in driving the severity of the
431 pathology (Singleton et al. 2003; Chartier-Harlin et al. 2004; Ibanez et al. 2004). It is worth noting
432 that simple spatial correlation measures alone failed to uncover the effects of *GBA* or *SNCA* regional
433 expression on the empirical atrophy pattern; the gene expression effects only emerged from the
434 full agent-based propagating model, which therefore provides a new way to identify gene-disease
435 associations in the central nervous system. New genes can easily be incorporated to adapt the
436 model to other neurodegenerative diseases.

437 The benefit of augmenting network structure with protein spreading dynamics is exemplified
438 by the identification of the substantia nigra as the likeliest disease epicenter. Mirroring the *Repro-*

439 *duction number* R_0 (Newman 2010), which marks the transition between disease extinction and
440 outbreak in conventional epidemic models, we estimated spread threshold for our metapopulation
441 S-I-R model. This represents the minimum number of infectious agents that need to be introduced
442 in any area that will lead to a major outbreak. In our model, the substantia nigra has the lowest
443 spread threshold, identifying it as a likely disease epicenter. This is consistent with the Braak
444 hypothesis, where the substantia nigra is one of the earliest affected sites in the central nervous
445 system. Note that we could not include structures in the pons and medulla, thought to be affected
446 even earlier in PD (Braak et al. 2003; Braak et al. 2004), due to difficulty in imaging either brain
447 atrophy or white matter tracts in the brainstem.

448 It is also known that α -synuclein is secreted in an activity dependent manner (Paillusson et al.
449 2013). We therefore tested the influence of rs-fMRI derived measures of functional connectivity on
450 protein mobility. As a measure of synchronous neuronal activity in pre- and post-synaptic regions,
451 functional connectivity will bias the proteins into regions showing greater co-activation. Once again
452 we found that this addition significantly improved the model fit. Thus, functional co-activation also
453 shapes the pattern of disease propagation, explaining why atrophy patterns in neurodegenerative
454 diseases tend to resemble intrinsic functional networks (Seeley et al. 2009; Zeighami et al. 2015).

455 We took advantage of several useful features of metapopulation models to provide an un-
456 derstanding of factors involved in disease propagation. Others have applied more traditional
457 compartmental models to Alzheimer's Disease (Raj et al. 2012; Iturria-Medina et al. 2014) and to
458 neurodegeneration more generally (Weickenmeier et al. 2018); however the agent-based model used
459 here affords us the possibility of testing different mechanisms of disease, likelihood of outbreak,
460 effect of emergent properties (such as the effect of regional neuronal death on subsequent disease
461 propagation) and, eventually, therapeutic interventions. Notably, metapopulation models share the
462 assumption with agent-based models that the individuals act independently according to specific
463 rules. The metapopulation models are generalized agent-based models and are more tractable and
464 computationally efficient. They can be easily tailored to accommodate an agent-based setting by
465 introducing more fine-grained rules. For example, the transmission rate $\gamma_i = 1 - e^{M \ln(1-\gamma_i^0)}$ can be

466 extrapolated as $\gamma_i = 1 - e^{\sum_{k=1}^M \ln(1-\gamma_{i,k}^0)}$ to model individually differentiated transmission rates $\gamma_{i,k}^0$ in
467 region i .

468 Because the metapopulation or agent-based S-I-R models have proven useful in understanding
469 chain reaction-like infection transmission, we supposed that they would be a good candidate for
470 modelling prion-like mechanisms of neurodegeneration. These models may also be applied to other
471 neurodegenerative diseases, and perhaps eventually to developmental or non-progressive diseases
472 where transneuronal transmissibility may be implicated (e.g. autism, schizophrenia, epilepsy).

473 Although the S-I-R metapopulation structured model provided a good fit to observed neurode-
474 generation, there are several caveats and limitations in the present study. First, regional variations
475 in vulnerability to the toxicity of misfolded α -synuclein apart from the effects of α -synuclein con-
476 centration were not accounted for. Moreover, neuronal loss is homogeneously modelled as a simple
477 linear combination of cell death due to native α -synuclein accumulation and deafferentation, which
478 may not reflect reality. It is possible that regions respond differently to the toxicity of α -synuclein
479 aggregates, and this can easily be incorporated into the model by introducing new factors, such
480 as genes that control resilience to energetic stress for example (Michel et al. 2016). Moreover,
481 cell death may slow the propagation of misfolded α -synuclein and accrual of atrophy, especially
482 in more affected regions. Although we did not take this effect into account here, it can easily be
483 incorporated into the model using agent-based rules.

484 Second, the white matter network may not represent the exact physical routes of spread. It is
485 possible that α -synuclein spread occurs only between specific cell types, or in one direction, while,
486 in our model, the agents spread bi-directionally along the fiber tracts. The outlier region (accumbens,
487 FIG. 2(b)) that remarkably impedes model fit serves as an example. Nucleus accumbens is one of
488 the least atrophied regions in the dataset used here, whereas it exhibits high atrophy in the model.
489 One possible reason for this disagreement is that we did not include the different subsections of
490 the substantia nigra and their projections in the structural connectome used for the model. While
491 we seeded the entire substantia nigra, it is known that the medial portion, which projects to the
492 accumbens (Zhang et al. 2017), is less affected in PD than the lateral substantia nigra, which

493 projects to dorsal striatum (Braak et al. 2003; Braak et al. 2004).

494 Finally, we focused on only two genes in modelling synucleinopathy, while many other genes
495 such as *LRKK2* and *MAPT*, and proteins such as dopamine or *tau*, may also influence or interact
496 with synucleinopathy propagation. Using a small subset of genes avoids high model complexity
497 and allowed modelling the proteinopathy in a parameter-free setting. However, the parameter-free
498 setting introduces another caveat: the model converts gene expression scores and fiber density into
499 probabilities without scaling their relative magnitude, while the actual rate of synthesis/clearance
500 and protein spreading may not be at the same scale. In the future this can be solved by introducing
501 scaling parameters into the model, training the model on individual connectome and genetic data
502 to find the optimal solutions, and including multiple timepoints from patient data.

503 One of the future directions is to customize the model with individual anatomical, functional,
504 genetic or clinical data to increase its ability to predict disease trajectory and to identify factors
505 that promote resistance to disease spread. Moreover, this model can hopefully help test new
506 preventative procedures. Introducing medications may change the parameters of the dynamical
507 system; for example, increasing *GBA* activity to elevate the clearance rate would make the stable
508 point for extinction more robust to small perturbations (e.g., the invasion of misfolded α -synuclein
509 fibrils).

510 **METHODS**

511 **Human brain parcellation**

512 We used a brain parcellation generated by atlas-based segmentation (Cammoun et al. 2012).
513 68 cortical parcels were defined using curvature-based information (Desikan et al. 2006), which is
514 available in FreeSurfer (<http://surfer.nmr.mgh.harvard.edu>). Subcortical parcels, including thalamus,
515 caudate, putamen, pallidum, accumbens, amygdala, and hippocampus, were extracted using
516 the same software from a whole brain segmentation (Fischl et al. 2002). Finally, substantia nigra was
517 added to the atlas using the location provided in the ATAG atlas (<https://www.nitrc.org/projects/atag>)
518 (Keuken et al. 2014). Only the left hemisphere was used in this model, resulting in a total of 42
519 regions for the subsequent analysis. We used only the left hemisphere to simulate the propagation

520 model because it is difficult to accurately determine interhemispheric connections using tractogra-
521 phy (Jbabdi and Johansen-Berg 2011). Moreover, regional gene expression was mostly available
522 only for the left hemisphere (see *Regional gene expression*).

523 **PPMI patient data and image processing**

524 PPMI is an open-access comprehensive observational clinical study (Marek et al. 2011), lon-
525 gitudinally collecting multimodal imaging data, biological samples and clinical and behavioural
526 assessments in a cohort of PD patients. 3T high-resolution T1-weighted MRI scans of 355 subjects
527 (237 PD patients, 118 age-matched healthy controls) were obtained from the initial visit of PPMI
528 to assess group-level regional atrophy using Deformation-Based Morphometry (DBM) (Zeighami
529 et al. 2015), a method to detect local changes in tissue density.

After denoising (Coupé et al. 2008), inhomogeneity correction (Sled et al. 1998), and lin-
ear intensity scaling, individual MRI images are registered non-linearly to the MNI152-2009c
template (Collins and Evans 1997), yielding the corresponding transformation fields to be in-
verted into deformation maps in MNI space. Instead of directly using the displacement value
 $U(x) = (u_1(x), u_2(x), u_3(x))$ of voxel x at coordinates (x_1, x_2, x_3) , we calculate the derivative of the
displacement in each direction and take the determinant of the jacobian matrix J minus 1, namely,
 $|J| - 1$, as the value of deformation at x , which reflects local volume change.

$$J = \frac{\partial U}{\partial x} = \begin{pmatrix} \frac{\partial u_1}{\partial x_1} & \frac{\partial u_1}{\partial x_2} & \frac{\partial u_1}{\partial x_3} \\ \frac{\partial u_2}{\partial x_1} & \frac{\partial u_2}{\partial x_2} & \frac{\partial u_2}{\partial x_3} \\ \frac{\partial u_3}{\partial x_1} & \frac{\partial u_3}{\partial x_2} & \frac{\partial u_3}{\partial x_3} \end{pmatrix} \quad (1)$$

530 These values constitute a 3D deformation map for each subject, on which an un-paired t test is
531 conducted to derive the statistical difference (t-score) between the PD patients and the healthy
532 controls at each voxel as a measure of local atrophy.

533 **Regional gene expression**

534 Regional gene expression levels were derived from the six post-mortem brains included in the
535 Allen Human Brain Atlas (AHBA) (Hawrylycz et al. 2012), a multimodal atlas of the anatomy and

536 microarray-based gene expression of the human brain. Individuals who donated their brains had
537 no history of psychiatric or neurological disorders. Since four of the brains have data from the left
538 hemisphere only, we only modeled the left hemisphere in our study, selecting a total of 3021 samples
539 of *GBA* (probe ID: 1025373, 1025374), *SNCA* (probe ID: 1020182, 1010655) in left hemisphere
540 regions. Cortical samples were volumetrically mapped to the 34 cortical regions of our parcellation
541 according to their corrected MNI coordinates (<https://github.com/chrisfilo/alleninf>) (Gorgolewski
542 et al. 2014), also including samples that are within 1mm of the nearest gray matter coordinates
543 assigned to any region. Subcortical samples were assigned to one of the 8 subcortical regions as
544 specified by the structure names provided in the AHBA, due to imperfect registration of the post-
545 mortem brains onto MNI space. For each probe, all samples that fell in the same anatomical region
546 were averaged and then normalized across all 42 left hemisphere regions, generating transcription
547 maps of each individual probe. These probe maps were next averaged according to the gene
548 classification and normalized again across the regions, yielding the spatial expression profiles for
549 *SNCA* and *GBA* respectively, represented as 42×1 vectors (FIG. S7).

550 **Diffusion weighted image processing and structural connectivity**

551 A total of 1027 subjects' preprocessed diffusion MRI data with the corresponding T1 images
552 was obtained from the Human Connectome Project (2017 Q4, 1200-subject release) to construct
553 an average macroscopic structural connectivity map of the healthy brain. With a multishell scheme
554 of b values 1000, 2000, 3000 s/mm^2 and the number of diffusion sampling directions 90, 90,
555 90, the diffusion data were reconstructed in individual T1 spaces using generalized q-sampling
556 imaging (GQI) (Yeh et al. 2010) with a diffusion sampling length ratio of 1.0, outputting at each
557 voxel quantitative anisotropy (QA) and the Spin distribution function (SDF), a measurement of the
558 density of diffusing water at different orientations (Yeh and Tseng 2011).

559 Deterministic fiber tracking was conducted in native space using DSI studio (www.dsi-studio.lab
560 solver.org) (Yeh et al. 2013). The 42 left hemisphere regions in standard space were mapped non-
561 linearly onto the individual T1 images using the FNIRT algorithm (<https://fsl.fmrib.ox.ac.uk/>)
562 (Jenkinson et al. 2012) with a warp resolution of 8mm, 8mm, 8mm. The 34 cortical regions

563 were dilated toward the grey-white matter interface by 1mm. The QA threshold was set to
564 $0.6 \times$ Otsu's threshold, which maximizes the variance between background and foreground pixels.
565 To compensate for volume-size introduced biases, deterministic tractography was performed for
566 each region (taken as the seed region) separately. With an angular cutoff of 55, step size of
567 0.5mm, minimum length of 20mm, and maximum length of 400mm, 100,000 streamlines were
568 reconstructed for each seed region. Connection strength between the seed region and the target
569 region was set to be the density of streamlines (streamline counts) normalized by the volume
570 size (voxel counts) of the target region and the mean length of the streamlines. The goal of this
571 normalization is to correct for the bias toward large regions and long fibers inherent in the fiber
572 tracking algorithms. The procedure was repeated for each region (as the tractography seed region),
573 resulting in 42 connection profiles (42 1×42 vectors). Each connection profile consists of the
574 connection strengths between the seed region and all other brain regions with self-connection
575 setting to zero. These connection profiles were finally concatenated to generate a 42×42 structural
576 connectivity matrix per subject. Varying numbers of most commonly occurring edges were selected
577 and averaged across the individual structural connectivity matrices to construct the group structural
578 connectivity matrix with binary density ranging from 25% to 45%. These group-level matrices
579 were finally symmetrized to represent (un-directed) brain networks. Likewise, we also constructed a
580 group-level length matrix in which elements denote mean lengths of the corresponding streamlines,
581 which were used to model the mobility pattern of agents in the edges.

582 **S-I-R metapopulation structured model**

583 The S-I-R metapopulation structured model includes five modules:

- 584 • (a) production of normal α -synuclein
- 585 • (b) clearance of normal and misfolded α -synuclein
- 586 • (c) misfolding of normal α -synuclein (infection transmission)
- 587 • (d) propagation of normal and misfolded α -synuclein
- 588 • (e) accrual of neuronal death (atrophy).

589 It assumes that α -synuclein molecules are independent agents with mobility patterns and lifespans
590 characterized by the connectome's architecture, neuronal activity, and regional gene expression.
591 The normal α -synuclein agents, synthesized continuously under the modulation of regional *SNCA*
592 expressions, are susceptible to the misfolding process when they come in contact with a misfolded
593 agent. Once infected, they adopt the misfolded form and join the infectious population. Both
594 normal and infected agents may spread via fiber tracts towards connected regions. The degradation
595 rate of both agents is modulated by *GBA* expression, which codes for the lysosomal enzyme
596 glucocerebrosidase (Sidransky and Lopez 2012).

597 **Production of normal α -synuclein.** In each voxel of region i , a new normal agent may
598 get synthesized per unit time with probability α_i , i.e., the synthesis rate in region i . α_i is chosen
599 as $\Phi_{0,1}(SNCA_{expression_i})$ where $\Phi_{0,1}(\cdot)$ is the standard normal cumulative distribution function,
600 hence a higher expression score entails a higher α -synuclein synthesis rate. The increment of
601 normal agents in region i is $\alpha_i S_i \Delta t$ after a total time Δt , where S_i is the size (voxel count) of region
602 i . Δt was set to 0.01.

603 **Clearance of normal and misfolded α -synuclein.** Agents in region i , either normal or
604 misfolded, may get cleared per unit time with probability β_i , the clearance rate in region i . Likewise,
605 β_i is set to $\Phi_{0,1}(GBA_{expression_i})$. Considering that the probability that an agent is still active after
606 a total time Δt is given by $\lim_{\delta\tau \rightarrow 0} (1 - \beta\delta\tau)^{\Delta t/\delta\tau} = e^{-\beta\Delta t}$, the cleared proportion within time step
607 Δt is $1 - e^{-\beta\Delta t}$.

608 **Misfolding of normal α -synuclein (infection transmission).** The normal agents that survive
609 clearance may become infected with probability $\gamma_i = 1 - e^{M_i \ln(1-\gamma_i^0)}$ in region i , where M_i is
610 the population of misfolded agents and γ_i^0 is the baseline transmission rate which measures the
611 likelihood that a single misfolded agent can transmit the infection to other susceptible agents. γ_i
612 denotes the probability of getting infected by at least one of the M_i misfolded agents in region i per
613 unit time. The baseline transmission rate γ_i^0 in region i is set to the reciprocal of region size, $1/S_i$.
614 Analogous to the clearance module, the probability that a normal agent is uninfected after a total
615 time Δt is given by $\lim_{\delta\tau \rightarrow 0} (1 - \gamma_i^0 \delta\tau)^{M_i \Delta t/\delta\tau} = e^{-\gamma_i^0 M_i \Delta t}$, thus the proportion of normal agents that

616 undergo misfolding within Δt is $1 - e^{-\gamma_i^0 M_i \Delta t}$.

Therefore, in determining the baseline regional density of normal α -synuclein, we increment the population of normal agents N_i with:

$$\Delta N_i = \alpha_i S_i \Delta t - (1 - e^{-\beta_i \Delta t}) N_i \quad (2)$$

After the system reaches the stable point (error tolerance $\epsilon < 10^{-7}$), we initiate the pathogenic spread and update the population of normal (N) and misfolded (M) agents with:

$$\Delta N_i = \alpha_i S_i \Delta t - (1 - e^{-\beta_i \Delta t}) N_i - (e^{-\beta_i \Delta t})(1 - e^{-\gamma_i^0 M_i \Delta t}) N_i \quad (3)$$

$$\Delta M_i = (e^{-\beta_i \Delta t})(1 - e^{-\gamma_i^0 M_i \Delta t}) N_i - (1 - e^{-\beta_i \Delta t}) M_i \quad (4)$$

617 The system has two fixed points, whose final positions will not be affected by the initial conditions
 618 of (N_i, M_i) , including the choice of seed region and seeded misfolded agents (see *Supplementary*
 619 *Information*). Note that normal and misfolded agents are equivalent to susceptible and infected
 620 agents.

Propagation of normal and misfolded α -synuclein. Agents in region i may remain in region i or enter the edges according to a multinomial distribution per unit time with probabilities:

$$P_{\text{region } i \rightarrow \text{region } i} = \rho_i \quad (5)$$

$$P_{\text{region } i \rightarrow \text{edge } (i,j)} = (1 - \rho_i) \frac{w_{ij}}{\sum_j w_{ij}} \quad (6)$$

where w_{ij} is the connection strength of edge (i, j) (fiber tracts density between region i and j). The probability of remaining in the current region i , ρ_i , was set to 0.5 for all i (see FIG. S8(a) for other choices of ρ_i ; we note that the model fit is robust to variations in ρ_i). Analogously, the agents in

edge (i, j) may exit the edge or remain in the same edge per unit time with binary probabilities:

$$P_{\text{edge } (i,j) \rightarrow \text{region } j} = \frac{1}{l_{ij}} \quad (7)$$

$$P_{\text{edge } (i,j) \rightarrow \text{edge } (i,j)} = 1 - \frac{1}{l_{ij}} \quad (8)$$

where l_{ij} is the length of edge (i, j) (the mean length of the fiber tracts between region i and region j). We use $N_{(i,j)}$, $M_{(i,j)}$ to denote the normal/misfolded population in edge (i, j) . After a total time Δt , the increments of N_i , M_i in region i are:

$$\Delta N_i = \sum_j \frac{1}{l_{ji}} N_{(j,i)} \Delta t - (1 - \rho_i) N_i \Delta t \quad (9)$$

$$\Delta M_i = \sum_j \frac{1}{l_{ji}} M_{(j,i)} \Delta t - (1 - \rho_i) M_i \Delta t \quad (10)$$

Likewise,

$$\Delta N_{(i,j)} = (1 - \rho_i) \frac{w_{ij}}{\sum_j w_{ij}} N_i \Delta t - \frac{1}{l_{ij}} N_{(i,j)} \Delta t \quad (11)$$

$$\Delta M_{(i,j)} = (1 - \rho_i) \frac{w_{ij}}{\sum_j w_{ij}} M_i \Delta t - \frac{1}{l_{ij}} M_{(i,j)} \Delta t \quad (12)$$

621 We adopt an asynchronous implementation in which the propagation of normal and misfolded agents
 622 is operated before the synthesis, clearance and infection at each Δt . We have also tried other imple-
 623 mentations, including propagation after synthesis/clearance/infection at each Δt and synchronous
 624 implementation, and found the differences are negligible, suggesting that our results are independent
 625 of the modules' update order. The simulator is available at https://github.com/yingqiuz/SIR_simulator.

Accrual of neuronal death (atrophy). We model neuronal death as the result of two processes: direct toxicity from accumulation of native misfolded α -synuclein and deafferentation (reduction in neuronal inputs) from neuronal death in neighbouring (connected) regions. The atrophy accrual

at t within Δt in region i is given by the sum of the two processes:

$$\Delta L_i(t) = k_1(1 - e^{-r_i(t)\Delta t}) + k_2 \sum_j \frac{w_{ji}}{\sum_j w_{ji}} (1 - e^{-r_j(t-1)\Delta t}) \quad (13)$$

626 where $r_i(t)$ is the proportion of misfolded agents in region i at time t , and $1 - e^{-r_i(t)\Delta t}$ quantifies the
627 increment of atrophy caused by accumulation of native misfolded α -synuclein aggregates within Δt
628 at time t . The second term $1 - e^{-r_j(t-1)\Delta t}$, weighted by $w_{ji}/\sum_j w_{ji}$ and summed up across j , accounts
629 for the increment of atrophy induced by deafferentation from its neighbouring regions within Δt
630 at $t - 1$. k_1, k_2 are the weights of the two terms with $k_1 + k_2 = 1$. We set $k_1 = k_2 = 0.5$ such
631 that native α -synuclein accumulation and the deafferentation have equal importance in modelling
632 the total atrophy growth (see FIG. S8(b) for other choices of k_1, k_2 ; we note that the model fit is
633 consistent across k_1/k_2 ranging from 0.1 to 10).

634 **Integration of functional connectivity**

635 We used resting-state functional MRI (rs-fMRI) scans from the Human Connectome Project
636 (2015, S500 release) to construct the functional connectivity maps. Both left-right (LR) and right-
637 left (RL) phase encoding direction data were used. Based on the minimally preprocessed rs-fMRI
638 data, further processing steps were performed, including: 1) nuisance signal regression (including
639 white matter, cerebrospinal fluid, global signal, and six motion parameters); 2) bandpass temporal
640 filtering (0.01 Hz f 0.08 Hz); 3) spatial smoothing using a 4mm FWHM Gaussian kernel. After
641 quality control, 496 subjects were finally included.

642 We then extracted the mean time course in each of the 42 regions and computed the pairwise
643 Pearson's correlation coefficients to derive individual functional connectivity matrices. Normalized
644 by Fisher's z transform, the functional connectivity matrices were averaged across subjects and
645 converted back to correlations using inverse Fisher transform to generate the group functional
646 connectivity matrix. All negative correlations in the resultant functional connectivity matrix were
647 set to zero, having no influence on the agents' mobility pattern.

Integration of functional connectivity into the model should bias mobility of the agents towards

region pairs showing greater co-activation patterns. Agents thus have a higher chance of entering the edges that connect regions having stronger synchronous neuronal activity. More specifically, the weights w_{ij} (connection strength of structural connectivity) in equation (6) were scaled by $e^{k \times fc_{(i,j)}}$, where $fc_{(i,j)}$ is the functional connectivity between region i and region j . Therefore the probability that agents move from region i to edge (i, j) per unit time is determined by

$$P_{\text{region } i \rightarrow \text{edge } (i,j)} = (1 - \rho_i) \frac{e^{k \times fc_{(i,j)}} w_{ij}}{\sum_j e^{k \times fc_{(i,j)}} w_{ij}} \quad (14)$$

648 Note that increasing k makes the influence of functional connectivity more differentiated across
649 the edges: the stronger functional connectivity values will be enhanced while the weaker ones may
650 be suppressed.

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663 AUTHOR CONTRIBUTIONS

664 YQZ, BM, AD conceived the work; YQZ, YZhang, YY, YZeighami, KL, BM, AD aided in
665 analysis and interpretation of data; YQZ wrote new software; YQZ, YY, BM, AD drafted the work.

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859

SUPPLEMENTARY INFORMATION

860

Parameter List

notation	name	expression or value	explanation
Δt	time step	$\Delta t = 0.01$	time increment in the simulations
i	region index	N/A	used to index regions
(i, j)	edge label	N/A	used to index edges
N_i	normal population in region i	N/A	total number of normal agents in region i
M_i	misfolded population in region i	N/A	total number of misfolded agents in region i
$N_{(i,j)}$	normal population in edge (i, j)	N/A	total number of normal agents in edge (i, j)
$M_{(i,j)}$	misfolded population in edge (i, j)	N/A	total number of misfolded agents in edge (i, j)
α_i	synthesis rate in region i	$\alpha_i = \Phi_{0,1}(SNCAexpression_i)$	the probability that a new normal agent gets synthesized in each voxel of region i per unit time
β_i	clearance rate in region i	$\alpha_i = \Phi_{0,1}(GBAexpression_i)$	the probability that an existing agent (either normal or misfolded) in region i gets cleared per unit time
S_i	region size	N/A	voxel counts of region i
γ_i^0	baseline transmission rate	$\gamma_i^0 = 1/S_i$	the probability for a single misfolded agent to transmit the disease to other agents per unit time
γ_i	transmission probability	$1 - e^{M_i \ln(1-\gamma_i^0)}$	the probability that normal agents get infected (by at least one of the misfolded agents) per unit time
w_{ij}	connection strength of edge (i, j)	normalized fiber tracts density between region i and j	determining the probability of choosing edge (i, j) when exiting region i per unit time
l_{ij}	edge length of edge (i, j)	mean length of fiber tracts between region i and j	determining the probability of exiting edge (i, j) per unit time
ρ_i	the probability of remaining in region i	$\rho_i = 0.5$ for all i	Agents in region i have equal probability of remaining in region i or exiting region i per unit time
fc_{ij}	functional connectivity of edge (i, j)	N/A	biasing agents toward regions showing greater co-activation pattern
k	weight of functional connectivity	N/A	controlling the influence of functional connectivity in driving disease spread

k_1	weight of atrophy accrual due to native misfolded agents' accumulation	$k_1 + k_2 = 1$	controlling the contribution of native misfolded agents' accumulation to total atrophy growth
k_2	weight of atrophy accrual due to deafferentation	$k_1 + k_2 = 1$	controlling the contribution of deafferentation to total atrophy growth.
$r_i(t)$	the ratio of misfolded agents in region i	$r_i(t) = M_i(t)/(N_i(t) + M_i(t))$	measuring the burden of misfolded agents in region i at t . $1 - e^{-r_i(t)\Delta t}$ is the increment of neuronal death at t in region i

TABLE S1. Parameter List | Note that only k , ρ_i , k_1 , k_2 are free parameters: k was scanned from 0 to 5 to study the effect of functional connectivity on disease spread (FIG. 7); $\rho_i = 0.5$ for all the regions so that agents have equal chance of staying in the same region or moving out; $k_1 = k_2 = 0.5$ so that the two factors ((i) native misfolded α -synuclein accumulation; (ii) deafferentation from connected regions) contributed equally to the total atrophy growth. We also note that model fit is robust across multiple choices of ρ_i , k_1 , k_2 (FIG. S8).

861 Analysis of the fixed points

862 Although there is no analytical solution for α -synuclein concentration, phase plane analysis is
863 helpful in finding fixed points of the system. Considering that the rates of incoming and outgoing
864 agents in the edges are equal when the system is at the stable point, and that no clearance, synthesis,
865 or misfolding occurs in the edges, the effects of the propagation module are negligible in the analysis
866 of the system's fixed points. Therefore, we sought to use the "overall" or "total" synthesis rate (α),
867 normal agent clearance rate (β_1), misfolded agent clearance rate (β_2), and transmission rate (γ) to
868 approximately analyze the entire system using a series of differential equations (equation (S1)-(S3),
869 see below). Likewise, we use N , M to represent the total population of normal and misfolded agents
870 in the entire brain. β_1, β_2, γ depend on the actual N_i, M_i and thus are not static values (to see this,
871 for example, the total cleared normal agents per unit time is $\sum_i \beta_i N_i$, so the "overall" clearance rate
872 $\beta_1 = \sum_i \beta_i N_i / N$ depends on real-time N_i ; it is not the "real" clearance rate but an approximation of
873 the total rate of clearance); the total synthesis rate $\alpha = \sum_i \alpha_i S_i$, where α_i is the empirical synthesis
874 rate in region i in the formal model and S_i is region size. Note that the actual spreading dynamics
875 cannot be fully described by the following differential equations (S1)-(S3). However, they are
876 helpful in analyzing the possible states of disease propagation.

- **Growth of Normal α -synuclein.** The system of normal α -synuclein growth approximates like:

$$\frac{dN}{dt} = \alpha - \beta_1 N \quad (\text{S1})$$

877 with $\alpha \gg 1, 0 < \beta_1 < 1$, obviously $N = \alpha/\beta_1$ is a stable point (which is the baseline density
878 of endogenous α -synuclein, FIG. 4, blue line).

- **Spread of misfolded α -syn.** The system with misfolded agents injected behaves like:

$$\frac{dN}{dt} = \alpha - \beta_1 N - (1 - \beta_1)[1 - (1 - \gamma)^M]N \quad (\text{S2})$$

$$\frac{dM}{dt} = (1 - \beta_1)[1 - (1 - \gamma)^M]N - \beta_2 M \quad (\text{S3})$$

The nullclines of N, M are

$$M = \frac{\ln\left(\frac{N-\alpha}{N(1-\beta_1)}\right)}{\ln(1-\gamma)} \quad (\text{S4})$$

$$N = \frac{\beta_2 M}{(1-\beta_1)(1-(1-\gamma)^M)} \quad (\text{S5})$$

Note (S5) is not defined at $M = 0$. To study the number of fixed points and their positions, we need to find out the number of intersections of the two nullclines (S4) and (S5), and where they intersect. Adding (S2) and (S3), it is easy to see $(N, M) = (\alpha/\beta_1, 0)$ is one fixed point. It is easy to find that M decreases monotonously with N in (S4) and passes $(\alpha/\beta_1, 0)$. Therefore, the monotony and position of line (S5) relative to line (S4) becomes crucial. To find the monotony of (S5), we take its first order derivative

$$N' = \frac{\beta_2(1-\beta_1)[(1-(1-\gamma)^M) + M(1-\gamma)^M \ln(1-\gamma)]}{[(1-\beta_1)(1-(1-\gamma)^M)]^2} \quad (\text{S6})$$

Obviously, when $M = 0$, the first order derivative is 0. We then take the second derivative

$$N'' = C(\ln(1-\gamma))^2(1-\gamma)^M M \quad (\text{S7})$$

879 where C is a positive constant. When $M > 0$, (S7) is positive thus the first order derivative
 880 (S5) increases monotonously with M , and when $M < 0$, (S5) decreases monotonously
 881 with M . Therefore, (S6) is positive hence in (S5), N increases monotonously with M ,
 882 namely, there can be up to one intersection (denoted by (N^*, M^*) in the following) of the
 883 two nullclines apart from $(N, M) = (\alpha/\beta_1, 0)$. It determines that the system can have up
 884 to two fixed points, one is $(\alpha/\beta_1, 0)$, and the other is (N^*, M^*) which has no closed-form
 885 expression.

886 It is also important to find out the position of (N^*, M^*) , because $M^* < 0$ is not
 887 realistic in the actual disease spread. Under this condition, an outbreak can never take
 888 place. Take the limit of (S5) $\lim_{M \rightarrow 0} N = \beta_2/(\beta_1 - 1) \ln(1 - \gamma)$, we can see the intercept

889 of (S5) on the N axis is $\beta_2/(\beta_1 - 1)\ln(1 - \gamma)$. When (i) $\beta_2 = (\beta_1 - 1)\ln(1 - \gamma)\alpha/\beta_1$,
 890 $N^* = \alpha/\beta_1$, i.e., (N^*, M^*) “merges” with $(\alpha/\beta_1, 0)$; (ii) when $\beta_2 > (\beta_1 - 1)\ln(1 - \gamma)\alpha/\beta_1 = 0$,
 891 $N^* > \alpha/\beta_1, M^* < 0$ which is not realistic; (iii) when $\beta_2 < (\beta_1 - 1)\ln(1 - \gamma)\alpha/\beta_1 = 0$,
 892 $N^* < \alpha/\beta_1, M^* > 0$. Our results (with full spread in the end) are based on (iii).

893 To study why different choice of seed region and injected α -synuclein may lead to
 894 different states (extinction or outbreak), we also investigated on what conditions the fixed
 895 points are stable. This can be studied by taking the jacobian matrix of the system linearized
 896 around the fixed points:

$$J = \begin{pmatrix} -\beta_1 - (1 - \beta_1)[1 - (1 - \gamma)^M] & (1 - \beta_1)(1 - \gamma)^M \ln(1 - \gamma)N \\ (1 - \beta_1)[1 - (1 - \gamma)^M] & -\beta_2 - (1 - \beta_1)(1 - \gamma)^M \ln(1 - \gamma)N \end{pmatrix} \quad (S8)$$

897 At $(\alpha/\beta_1, 0)$, $J|_{(\alpha/\beta_1, 0)} = \begin{pmatrix} -\beta_1 & (1 - \beta_1)\ln(1 - \gamma)\frac{\alpha}{\beta_1} \\ 0 & -\beta_2 - (1 - \beta_1)\ln(1 - \gamma)\frac{\alpha}{\beta_1} \end{pmatrix}$ has eigenvalues $-\beta_1$ and $-\beta_2 -$
 898 $(1 - \beta_1)\ln(1 - \gamma)\alpha/\beta_1$. When $\beta_2 > (\beta_1 - 1)\ln(1 - \gamma)\alpha/\beta_1$, both eigenvalues are negative
 899 hence $(\alpha/\beta_1, 0)$ is stable (disease extinction). The injection of misfolded agents introduces
 900 a small perturbation to the system at $(\alpha/\beta_1, 0)$. As the choice of seed region and injection
 901 amount affect the approximations of β_1, β_2, γ in equation (S2)(S3) that are used to analyze
 902 the system, the disease will either die out or fully spread. It is more difficult to initiate the
 903 disease spread in seed regions with relatively large β_1, β_2 and small γ (i.e., more resistant
 904 to disease spread), as it is more likely to satisfy the condition $\beta_2 > (\beta_1 - 1)\ln(1 - \gamma)\alpha/\beta_1$
 905 initially. As mentioned before, β_1, β_2, γ are not static and depend on the real-time N_i, M_i s;
 906 at the other fixed point (N^*, M^*) , the parameter set is not the same as the one near $(\alpha/\beta_1, 0)$.
 907 Therefore it is also possible, in theory, that certain choices of parameters may lead to an
 908 outbreak followed by gradual extinction.

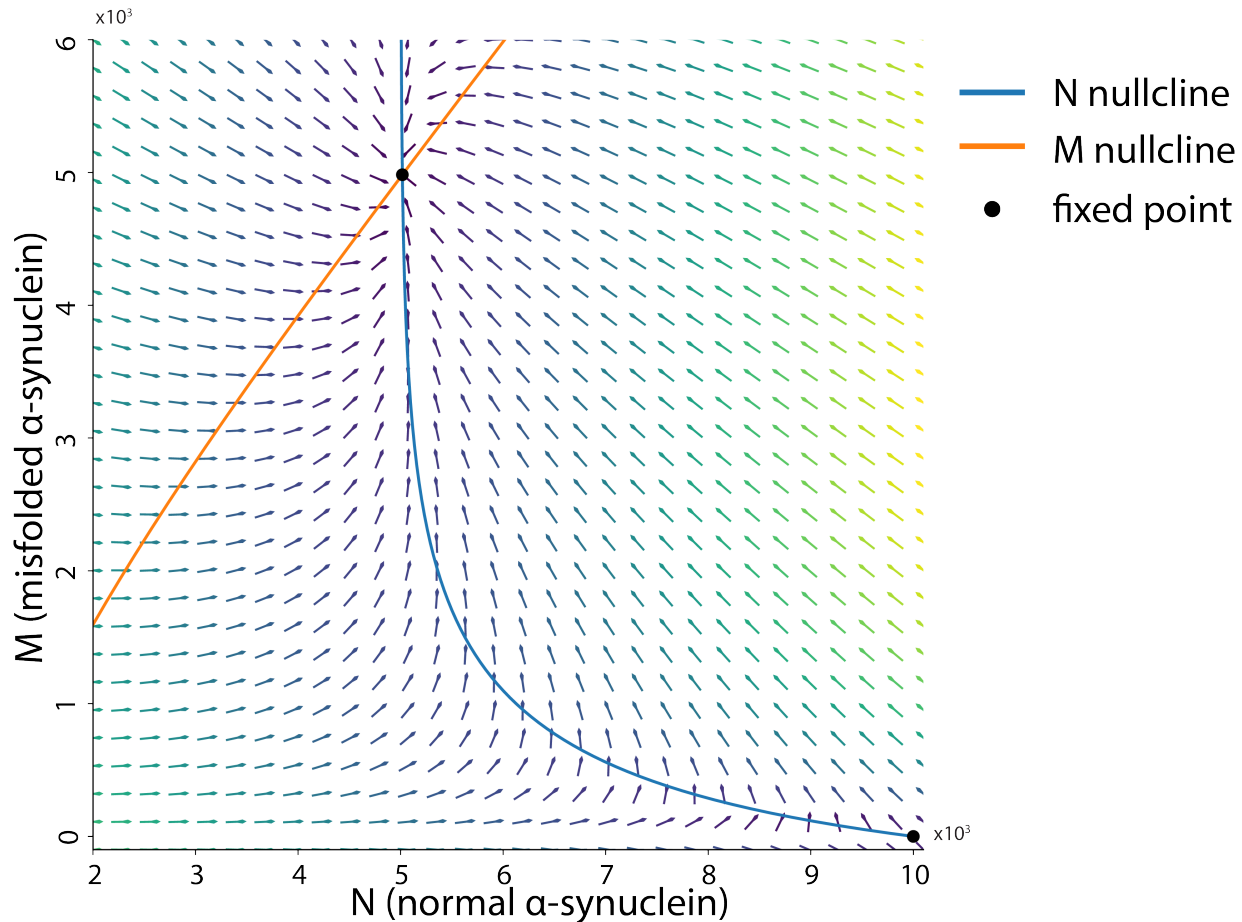


Fig. S1. An illustration of the phase plane at $\alpha = 5000, \beta_1 = 0.5, \beta_2 = 0.5, \gamma = 0.001$. | M decreases with N (N nullcline, blue, equation (S4)) and N increases with M (M nullcline, orange, equation (S5)), therefore apart from $(N = 10000, M = 0)$ there is only one another intersection $(N = 5017.15, M = 4982.85)$ of the two lines, indicating that the system has two fixed points only. The vector field (arrows) denotes the direction of the gradient at each position (i.e., the system at that point will move along the direction of the corresponding arrow).

909

Model fit in large t

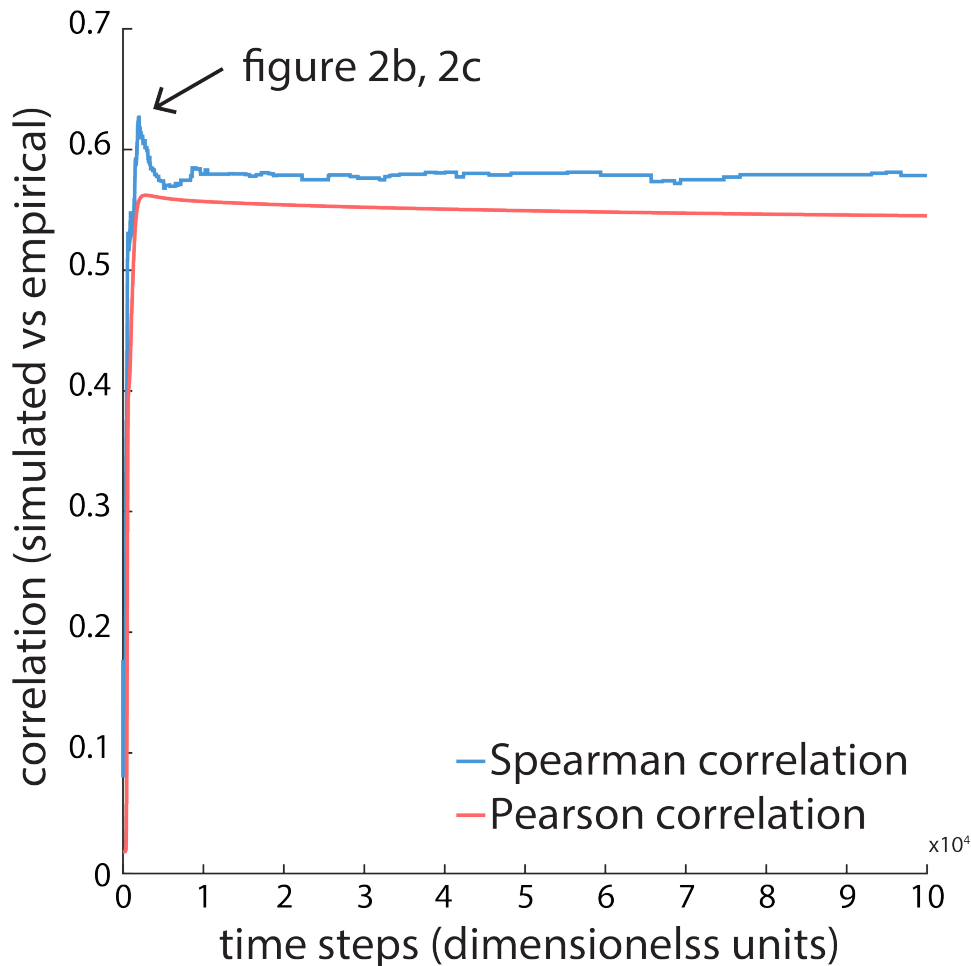


Fig. S2. Model fit up to $t = 10^5$ | Correlations between simulated atrophy and empirical atrophy derived from PD patient DBM maps. Correlations are shown as a function of simulation time. At large t , the model fit stabilizes as the system approaches the stable point.

910

Arrival time of misfolded α -synuclein compared to the Braak model

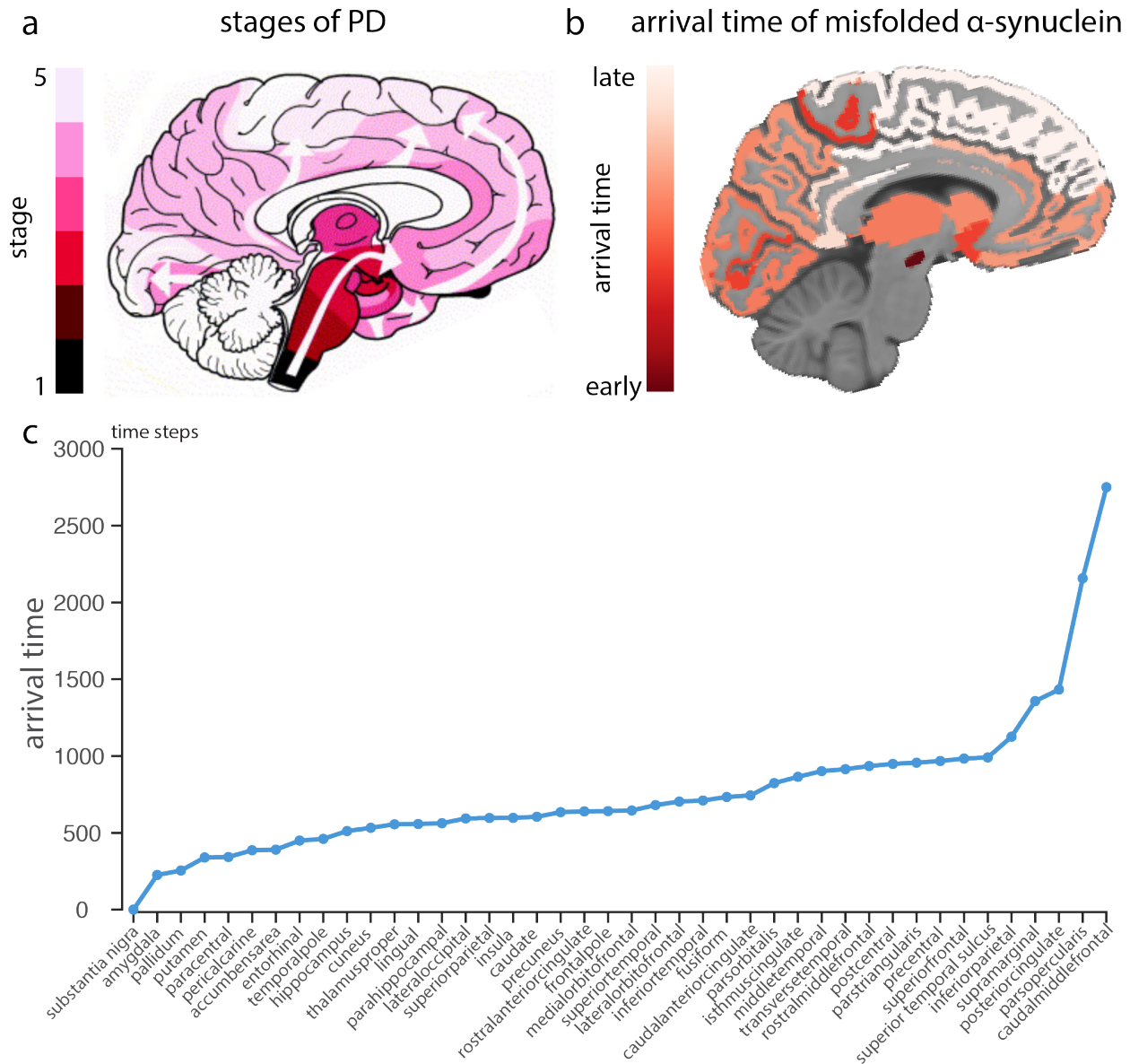


Fig. S3. Comparison between stages of PD and arrival time of misfolded α -synuclein in the model. (a) The stages of PD progression proposed by Braak. (b) Regional arrival time of misfolded α -synuclein is defined as the time steps required for misfolded α -synuclein amount to exceed 1 (after seeding at the substantia nigra with one misfolded agent). This roughly follows the Braak staging hypothesis. (c) Line chart of regional arrival time of misfolded α -synuclein.

911 **Spearman's correlation vs Pearson's Correlation**

912 . We adopted Spearman's correlation to assess model fit instead of Pearson's correlation. Al-
913 though assessing model fit using Spearman's correlation takes into account only relative magnitudes
914 of simulated neuronal loss and inevitably discards the information of data points' values, thus can
915 be sensitive to small changes that alter the rank order of regional neuronal loss, it is better capable
916 of capturing the similarity of the rank orders between two variables. It is preferred in our present
917 study as it measures the resemblance between the simulated atrophy and empirical atrophy as to
918 which region(s) display more atrophy compared to other regions. Moreover, the simulated neuronal
919 loss does not exhibit a normal distribution pattern, making the Pearson's correlation less suitable
920 in our study. However, to ensure the robustness of model fit, we also derived Pearson's correlations
921 across the same set of network densities, which all yield comparable results (FIG. S4). Also note
922 that, considering that the low spatial resolution of structural MRI scans of PD patients may cause
923 inaccuracy in assessing the atrophy in substantia nigra, it was excluded in the correlations.

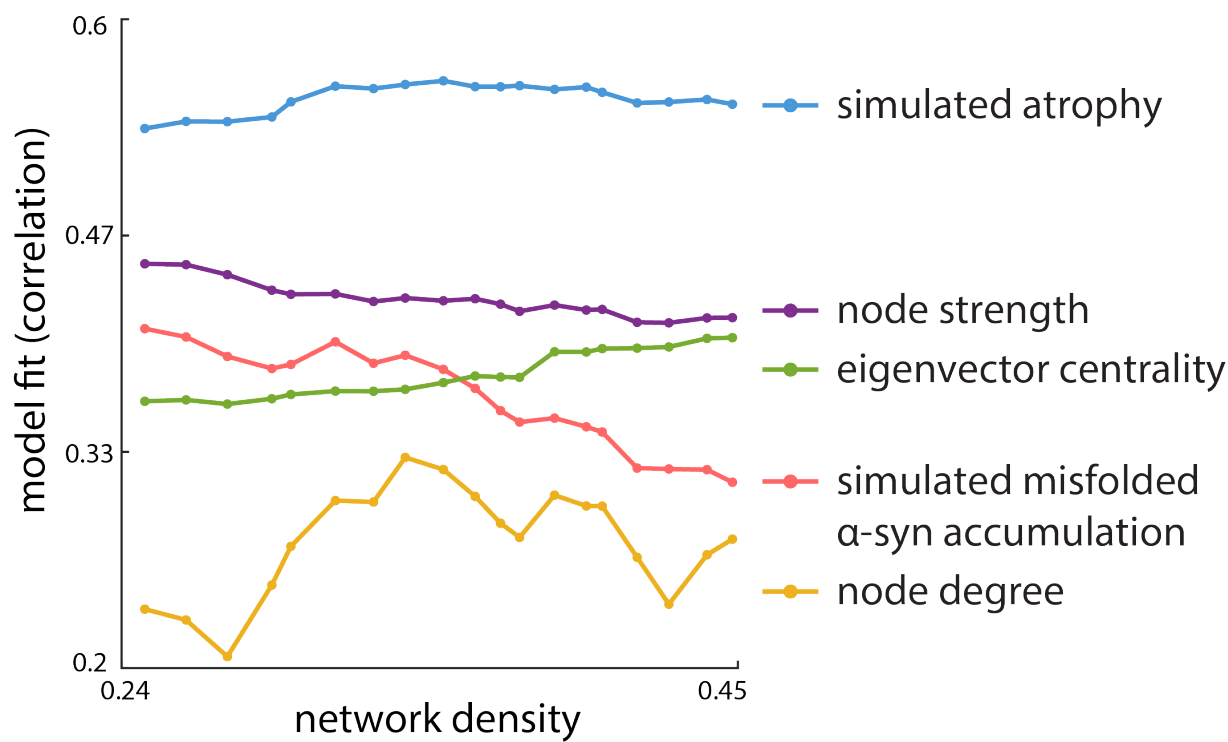


Fig. S4. Model fit based on Pearson's correlation coefficient yielded comparable results across network density from 25% to 45% | The model integrated with gene expression levels has more predictive power than the density of misfolded α -synuclein (red) and the static network metrics, including node degree (yellow), node strength (green), or eigenvector (purple) centrality.

924 **Cutoff of the early-spreading timeframes**

925 . The sensitivity of Spearman's correlation to rank orders may be problematic in the early
926 spreading period, as the measure takes in ranking information only so that even small increments
927 that alter ranking order of the original neuronal loss may cause substantial changes to model fit.
928 Therefore, to avoid picking up spurious peak correlation value (model fit) in the early timeframes
929 after seeding, we discarded the timeframes where change of misfolded α -synuclein densities exceeds
930 1% within $\Delta t = 0.01$ in at least one region, resulting in a cutoff point at around 1000 time steps
931 depending on the network density.

932 We also adopted a less rigorous cutoff point, removing only the first 100 timeframes. The
933 difference in results is negligible (FIG. S5).

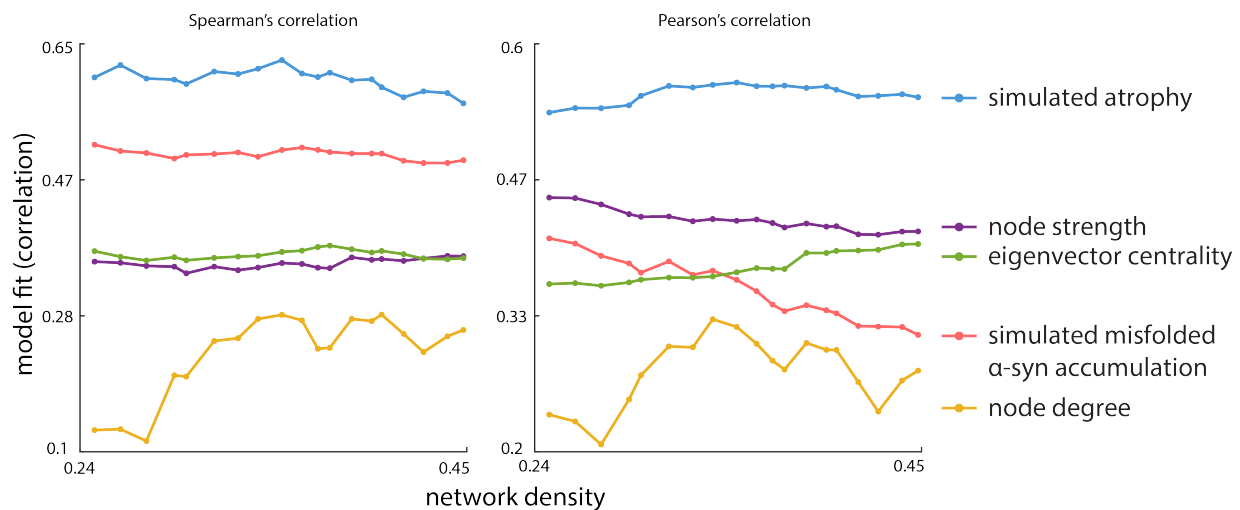


Fig. S5. The model fit across network density 25% to 45% after removing the first 100 timeframes in finding the peak correlation values. Left: Spearman's correlation. Right: Pearson's correlation.

934 **Permutation test of functional connectivity**

935 As the influence of functional connectivity increases, the variances of model fit based on null
936 functional connectivity matrices increase while the means consistently drop across four network
937 densities without displaying a curved pattern, indicating that only real functional connectivity
938 significantly facilitates model fit at smaller k (FIG. S6). At larger k , simulations based on real
939 functional connectivity may yield model fit lower than the mean of null models, indicating that the
940 harmful role of functional connectivity when it begins to erode structural connectivity structure
941 may make the model perform worse than chance. The variance of null model fits increases as k
942 goes up, increasing the occurrence of high model fit values.

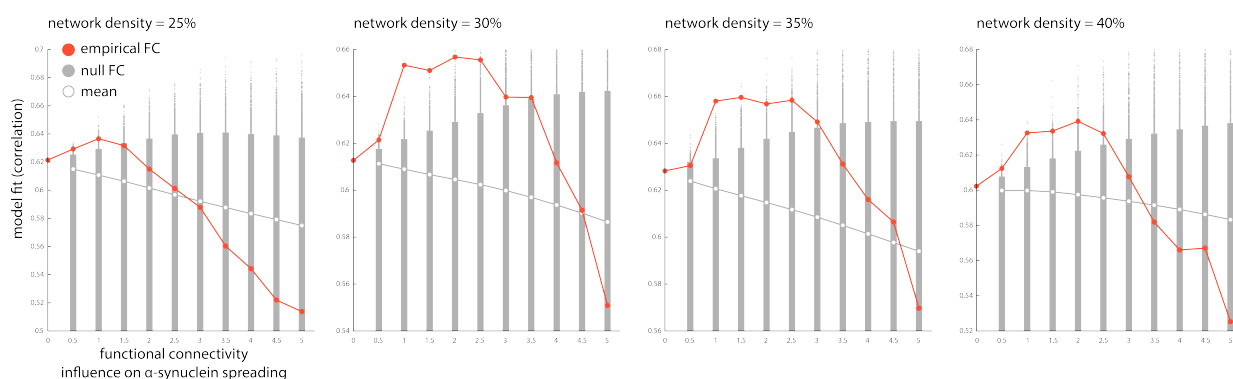


Fig. S6. Permutation tests for functional connectivity (FC). Increasing k (the influence of FC) first facilitates then degrades model fit. The red line indicates model fit using true FC values. At each k , rs-fMRI time series were re-assigned to construct null FC matrices, which degrades model fit monotonously as k increases. At smaller k , simulations based on real FC yield significantly higher model fit than the null settings as indicated by the 95% confidence interval (gray bar), while at larger k , real FC ceases to have advantage over null FC matrices in facilitating model fit and can even become significantly more harmful than the nulls.

943 **Gene expression**

944 There are three probes for *GBA* (probe id: 1025372, 1025373, 1025374) and two probes for
 945 *SNCA* (probe id: 1020182, 1010655) (FIG. S7). *GBA* probe 1025374 was excluded in the analysis as
 946 it deviates too much from probe 1025372 (Pearson correlation=0.30) and probe 1025373 (Pearson
 947 correlation=0.24) while the correlation between the latter two probes is 0.79. Compared to *GBA*
 948 expression, *SNCA* is more homogenous especially in cortical regions.

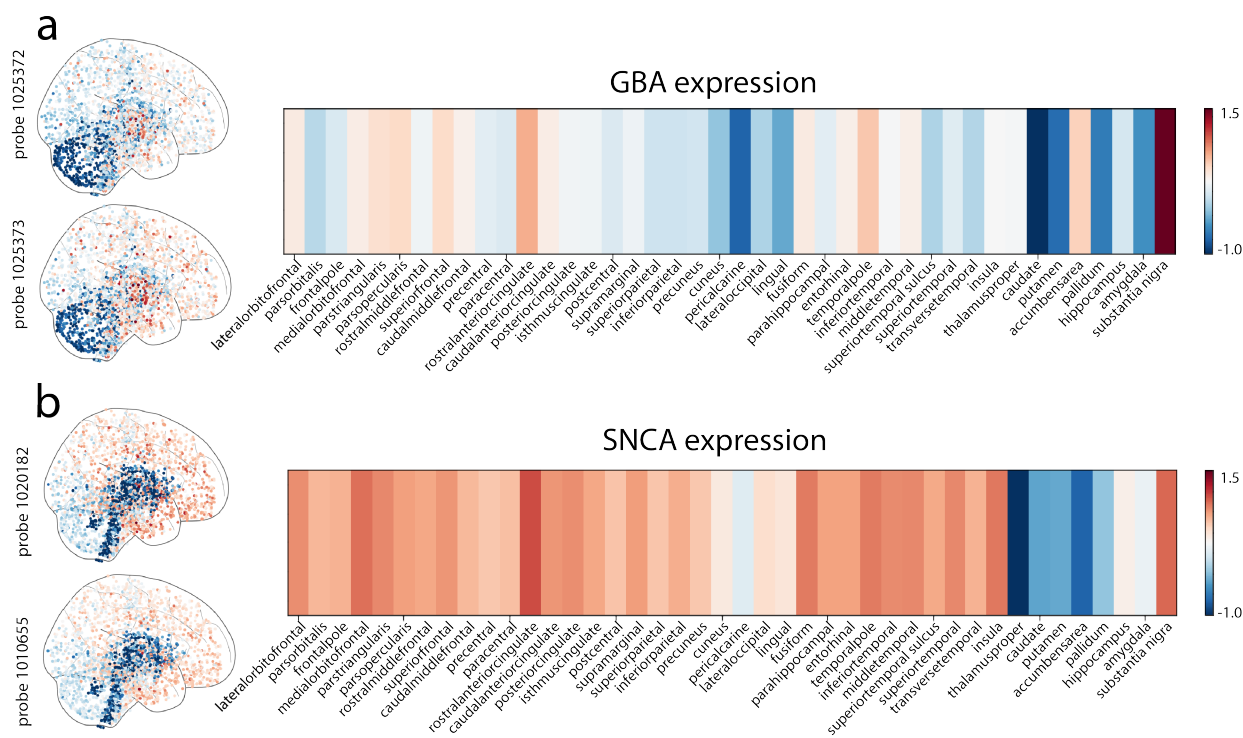


Fig. S7. (a) Regional *GBA* expression. Probe 1025372, 1025373 were included to generate the group transcription profile. (b) Regional *SNCA* expression. Probe 1020182, 1010655 were included to generate the group transcription profile.

949

The effect of free parameters on model fit

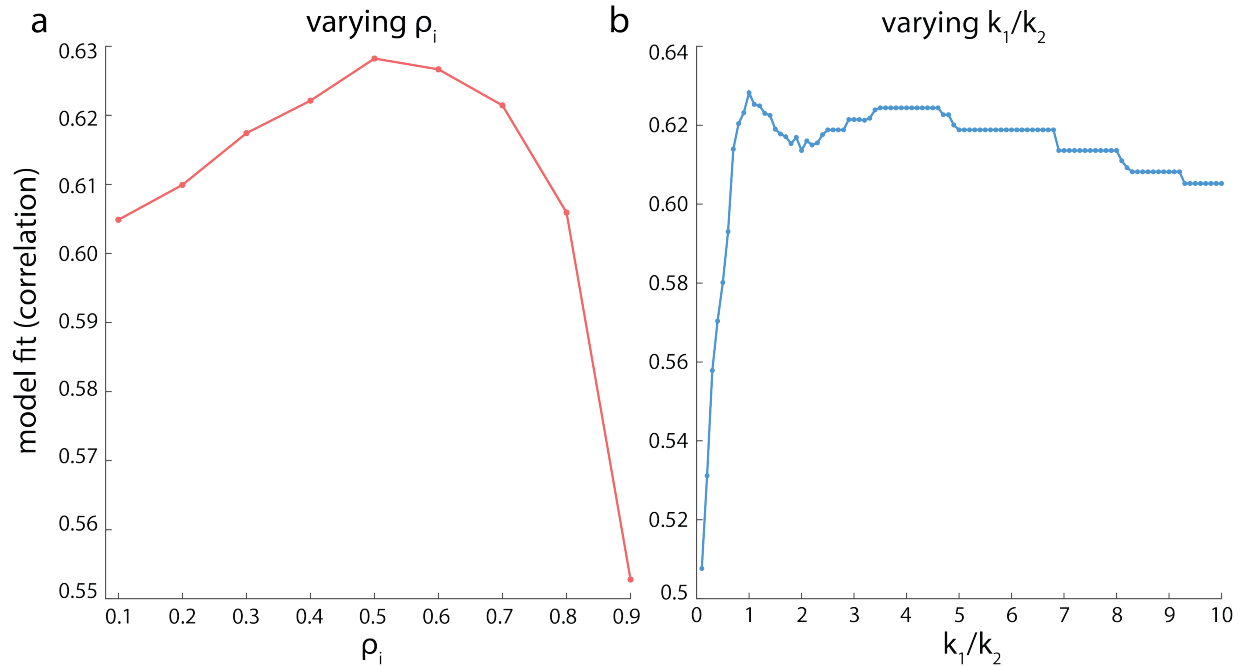


Fig. S8. Testing free parameters ρ_i, k_1, k_2 | Model fit (Spearman's correlation) is robust to variations in ρ_i, k_1, k_2 (results shown at network density 0.35). (a) ρ_i controls the probability of remaining in region i while $(1-\rho_i)$ is the probability of exiting region i per unit time. The main results are based on $\rho_i = 0.5$. However, the model fit is consistently above 0.55 across ρ_i ranging from 0.1 to 0.9. (b) For the atrophy in region i , k_1 controls the contribution of α -synuclein accumulation inside region i , while k_2 controls the contribution of deafferentation induced by atrophy in connected regions. $k_1 + k_2 = 1$. The model fit is consistently over 0.5 across k_1/k_2 ranging from 0.1 to 10. These results suggest that the predicative power of the model is robust to variations in free parameters ρ_i or k_1/k_2 .