

1 **Research Article: A framework for disentangling ecological** 2 **mechanisms underlying the island species-area relationship**

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4 Jonathan M. Chase^{1,2,*}, Leana Gooriah¹, Felix May^{1,3}, Wade A. Ryberg⁴, Matthew S. Schuler⁵,
5 Dylan Craven^{6,1,7}, Tiffany M. Knight^{6,8,1}

6

7 ¹German Centre for Integrative Biodiversity Research (iDiv) Halle-Jena-Leipzig. Deutscher Platz
8 5e, Leipzig, 04103, Germany

9 ²Department of Computer Science, Martin Luther University, 06099, Halle, Germany

10 ³Leuphana University Lüneburg, Universitätsallee 1, D-21335 Lüneburg, Germany

11 ⁴Texas A&M Natural Resources Institute, College Station, Texas, USA

12 ⁵Department of Biological Sciences, Darrin Fresh Water Institute, Rensselaer Polytechnic
13 Institute, Troy, NY 12180, USA

14 ⁶Department of Community Ecology, Helmholtz Centre for Environmental Research - UFZ,
15 Halle (Saale), Germany

16 ⁷Biodiversity, Macroecology & Biogeography, Faculty of Forest Sciences and Forest Ecology,
17 University of Göttingen, Göttingen, Germany

18 ⁸Institute of Biology, Martin Luther University Halle-Wittenberg, Halle (Saale), Germany

19

20 *Corresponding author: jonathan.chase@idiv.de

21 URL: https://www.idiv.de/groups_and_people/employees/details/eshow/chase_jonathan.html

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28 *Individual-Based Rarefaction.*

29

30 **Abstract:**

31 The relationship between an island's size and the number of species on that island—the island
32 species-area relationship (ISAR)—is one of the most well-known patterns in biogeography, and
33 forms the basis for understanding biodiversity loss in response to habitat loss and fragmentation.
34 Nevertheless, there is contention about exactly how to estimate the ISAR, and the influence of
35 the three primary ecological mechanisms—random sampling, disproportionate effects, and
36 heterogeneity—that drive it. Key to this contention is that estimates of the ISAR are often
37 confounded by sampling and estimates of measures (i.e., island-level species richness) that are
38 not diagnostic of potential mechanisms. Here, we advocate a sampling-explicit approach for
39 disentangling the possible ecological mechanisms underlying the ISAR using parameters derived
40 from individual-based rarefaction curves estimated across spatial scales. If the parameters
41 derived from rarefaction curves at each spatial scale show no relationship with island area, we
42 cannot reject the hypothesis that ISARs result only from random sampling. However, if the
43 derived metrics change with island area, we can reject random sampling as the only operating
44 mechanism, and infer that effects beyond sampling (i.e., disproportionate effects and/or
45 heterogeneity) are also operating. Finally, if parameters indicative of within-island spatial
46 variation in species composition (i.e., β -diversity) increase with island area, we can conclude that
47 intra-island compositional heterogeneity plays a role in driving the ISAR. We illustrate this
48 approach using representative case studies, including oceanic islands, natural island-like patches,
49 and habitat fragments from formerly continuous habitat, illustrating several combinations of
50 underlying mechanisms. This approach will offer insight into the role of sampling and other
51 processes that underpin the ISAR, providing a more complete understanding of how, and some
52 indication of why, patterns of biodiversity respond to gradients in island area.

53

54 **Introduction:**

55 The relationship between the area sampled and the number of species in that area—the species-
56 area relationship—is one of the oldest laws in ecology (e.g., Arrhenius 1921, Lawton 1999,
57 Lomolino 2000, Drakare et al. 2006). There are many forms of SARs that represent rather
58 distinct patterns and processes (e.g., Scheiner 2003, Scheiner et al. 2011), but we here focus
59 specifically on one type, the Island Species-Area Relationship (hereafter ISAR). The ISAR
60 correlates how the numbers of species (species richness) varies with the size of islands or distinct
61 habitat patches (natural or fragmented due to human activities). Like other types of SARs, the
62 ISAR is usually positive (e.g., MacArthur and Wilson 1963, 1967, Connor and McCoy 1979,
63 Triantis et al. 2012). However, complexities such as island age, habitat heterogeneity and/or
64 isolation can complicate this simple expectation (Kreft et al. 2008, Borregard et al. 2016).

65 We refer to 'islands' in the ISAR as any insular system, including true islands, habitat patches
66 that are surrounded by distinctly different habitats (matrix) (e.g., lakes, edaphically delimited
67 habitats), and habitat fragments that have been insularized by human activities. In addition to
68 being an important biogeographic pattern in its own right, the ISAR and concepts closely related
69 to it play an important role in understanding how biodiversity changes when habitat is lost and/or

70 fragmented into smaller island-like habitats (e.g., Diamond 1975, Simberloff and Abele 1976,
71 Matthews et al. 2014, 2016, Fahrig 2017). As a result, understanding the patterns and the
72 processes underlying ISARs and their derivatives would seem to be an important endeavor in the
73 context of island biogeography and conservation.

74 Despite its conceptual importance, there remains a great deal of ambiguity regarding ISAR
75 patterns, as well as its underlying processes (e.g., Scheiner et al. 2011). When describing ISAR
76 patterns, authors report and analyze different aspects of species richness regressed against total
77 island size, including total numbers of species and the number of species found within a
78 constantly-sized sub-sampled area. Such different sampling designs have created confusion
79 when comparing slopes of ISARs; an increasing number of species measured in a fixed-area plot
80 with increasing island area means something quite different than an increasing number of species
81 on the entire island (see also Hill et al. 1994, Gilaldi et al. 2011, 2014). In terms of processes
82 underlying the ISAR, there is similar confusion. Multiple mechanisms, including passive
83 sampling, colonization/extinction (i.e., metacommunity) dynamics, and habitat heterogeneity, as
84 well as their interactions, have been invoked to explain ISARs. Unfortunately, the exact ways by
85 which these mechanisms operate, and how they can be disentangled from observational data,
86 remains in question.

87 Following others (e.g., Triantis et al. 2012, Mathews et al. 2014, 2016), we refer to the ISAR as
88 the relationship between the total species richness on a given island (or habitat patch) and the
89 size of that island. However, simply knowing the shape of the relationship between the size of
90 an island and the total species richness (hereafter S_{total}) on that island can tell us very little about
91 the possible mechanisms underlying the ISAR. In order to understand the mechanisms
92 underlying the ISAR, it is necessary to collect and analyze data at the level below the scale of the
93 entire island (see also Hill et al. 1994, Yaacobi et al. 2007, Stiles and Scheiner 2010, Gilaldi et
94 al. 2011, 2014). Specifically, we recommend collecting data from multiple standardized plots
95 where both the numbers and relative abundances of species are available, as well as
96 compositional differences of species among locations within an island. We recognize that this
97 requires extra data often not available for many biogeographical and macroecological studies of
98 island systems, but emphasize that the extra effort involved allows a much deeper understanding
99 of the possible processes underlying the ISAR patterns observed.

100 **Mechanisms Underlying the ISAR**

101 We overview three general classes of potential mechanisms underlying the ISAR—passive
102 sampling, disproportionate responses and heterogeneity—from least complex to most complex
103 (see also Connor and McCoy 1979, McGuinness 1984, Scheiner et al. 2011 for deeper
104 discussions of these mechanisms more generally for all types of SARs). Then we discuss how
105 they can be detected using a multi-scale, multi-metric approach. Importantly, there remains
106 much confusion in the literature regarding exactly which mechanisms can create the ISAR,
107 which patterns these mechanisms generate, and how to disentangle them. Thus, we begin with a
108 general overview of the general classes of mechanisms and discuss how they can be disentangled
109 with a more directed sampling approach.

110 In brief, *passive sampling* (sometimes called the ‘more individuals hypothesis’) emerges when
111 larger islands have more species than smaller islands via passive sampling of individuals (and
112 thus species) from a larger regional pool. *Disproportionate response* (sometimes called ‘area
113 per se’) include a large array of possible mechanisms that influence the likelihood that some
114 species are favored, and others disfavored, on islands of different sizes, such that they achieve
115 different relative abundances on different sized islands. *Heterogeneity* also leads to
116 disproportionate responses and altered relative abundances of species, but these emerge at larger
117 scales via clumping of species that can emerge because of habitat differences and/or dispersal
118 limitation. In the following sections, we discuss each of these mechanisms, and possible ways to
119 detect them from within-island surveys.

120 *Passive sampling*—The simplest mechanism of the ISAR is that islands passively sample
121 individuals from a larger ‘regional’ pool of individuals of different species. Larger islands
122 passively sample more individuals, and thus more species, from the regional pool. This is
123 essentially a ‘null’ hypothesis, but one that can be tested using standard methods, and which
124 provides important insights about the potential underlying processes leading the ISAR. The
125 influence of passive sampling on the ISAR was first described by Arrhenius (1921) in one of the
126 first quantitative explorations of the ISAR. It is important to emphasize that sampling effects are
127 sometimes thought of as an artifact of limited sampling for uncovering the true numbers of
128 species. This is not the case for this passive sampling null hypothesis. It is also implicit in
129 several early quantitative explorations of the ISAR where the regional pool consists of few
130 common and many rare species, and smaller islands passively sample fewer individuals, and thus
131 fewer species than larger islands (i.e., Preston 1960, May 1975).

132 Coleman (1981) developed an analytical formula for this process based on random placement of
133 individuals on islands and Coleman et al. (1982) applied it to data from samples of breeding
134 birds on islands in a reservoir to suggest that this passive sampling mechanism most likely
135 explained the ISAR in this system. This will create a positive ISAR with more rare species being
136 present on larger islands, but only in proportion to their abundance in the total pool (i.e., the
137 relative proportions of species does not change from small to large islands). Importantly, this
138 random placement method is nearly identical to individual-based rarefaction methods (e.g.,
139 Gotelli and Colwell 2001), which we use below to test the random sampling hypothesis.

140 Several authors have tested the passive sampling hypothesis by measuring the numbers of
141 species in a given fixed area on islands of different sizes and correlating that density with the
142 total area of the island (e.g., Hill et al. 1994, Kohn and Walsh 1994, Yaacobi et al. 2007, Gilaldi
143 et al. 2011, 2014). If the number of species in a fixed area sample does not vary as island size
144 varies, this is taken to imply that passive sampling is most likely the only mechanism acting.
145 However, if the number of species in a fixed area increases as island size increases, we would
146 instead conclude that there is some biological effect, beyond sampling, that allows more species
147 to persist in a given area on larger than smaller islands.

148 While fixed-area sampling can be useful for inferring whether ISAR patterns deviate from
149 patterns expected from pure sampling effects, this method is unfortunately not as powerful of a
150 ‘null hypothesis’ as has often been suggested. There are at least two common factors that can

151 lead to patterns that appear consistent with the passive sampling hypothesis that in fact emerge
152 from effects that are beyond sampling. First, when disproportionate effects are primarily
153 experienced by rare species, sampling at small spatial grains may miss this effect, especially
154 when averages of the numbers of species are taken from the smallest spatial scale. For example,
155 Karger et al. (2014) found that fern species richness in standardized plots did not increase with
156 island area when measured at small spatial grains (i.e., 400m²-2400m²), but that the slope
157 significantly increasing at the largest sampling grain (6400 m²). Second, it is possible that
158 species richness measured in standardized plots may not vary with island size, but that habitat
159 heterogeneity leads to different species present in different habitat types, creating the ISAR. For
160 example, Sfenthourakis and Panitsa (2012) found that plant species richness on Greek islands
161 measured at local (100m²) scales did not change with island area, but that there were high levels
162 of β -diversity on islands that were larger, likely due to increased heterogeneity. In both of these
163 studies, simply measuring standardized species richness in small plots across islands of different
164 spatial grains may have led to the faulty conclusion of random sampling effects.

165 ***Disproportionate effects***—When disproportionate effects underlie the ISAR, there are more
166 species on larger islands because species from the regional pool are differentially influenced by
167 island size (as opposed to the passive sampling hypothesis, where species are proportionately
168 influenced by island size). Disproportionate effects includes a number of different sub-
169 mechanisms whereby some species are favored, and others disfavored, by changes in island size.

170 Most such mechanisms predict that the numbers of species in a fixed sampling area should
171 increase with increasing island size (sometimes called ‘area per se’ mechanisms; Connor and
172 McCoy 1979). The mostly widely considered of these mechanisms is MacArthur and Wilson’s
173 (1963, 1967) theory of island biogeography. Here, the rates of colonization of species increases
174 with island size, and the rates of extinction decrease with island size, leading to the expectation
175 that more species should often be able to persist in a fixed area on larger islands. Several other
176 kinds of spatial models can also predict similar patterns whereby the coexistence of several
177 species is favored when the total area increases (e.g., Hanski et al. 2013), or when population-
178 level processes, such as Allee-effects or demographic stochasticity, are less likely on larger
179 relative to smaller islands (e.g., Hanski and Gyllenberg 1993, Orrock and Wattleing 2010).
180 Disproportionate effects can also emerge when changes in island size influences island-level
181 environmental conditions. For example, smaller islands are often more likely to experience
182 disturbances and/or have lower productivity (McGuinness 1984), and in the context of habitat
183 fragmentation, smaller island fragments often have edge effects whereby habitat-specialist
184 species are negatively impacted (Ewers and Didham 2006).

185 Although often less well appreciated, mechanisms similar to those described above can favor
186 multiple species in smaller, rather than larger habitats. For example, it is possible that more
187 widespread species can dominate larger habitats via high rates of dispersal and mass effects.
188 Likewise, especially in the context of habitat islands formed via habitat fragmentation,
189 disproportionate effects favoring species in smaller islands can include the disruption of
190 exclusion interspecific interactors (e.g., pathogens, predators or competitors), or more species
191 favored by edges and heterogeneity created in smaller habitats (Fahrig 2017). In such cases, we

192 might expect a weaker or even negative ISAR depending on whether random sampling effects
193 (which are always operating) outweigh the disproportionate effects

194 **Heterogeneity**—The last family of mechanisms that have been proposed to lead to the ISAR
195 involve heterogeneity in the composition of species within islands. These mechanisms are
196 centered on the supposition that larger islands can have more opportunity for species to
197 aggregate intraspecifically or clump (leading to heterogeneity in species composition) than
198 smaller islands. This can emerge from two distinct sub-mechanisms:

199 (i) *Habitat heterogeneity*. Habitat heterogeneity leads to dissimilarities in species composition
200 via the ‘species sorting’ process inherent to niche theory (e.g., Whittaker 1970, Tilman 1982,
201 Chase and Leibold 2003). As a mechanism for the ISAR, larger islands are often assumed to
202 have higher levels of habitat heterogeneity than smaller islands (e.g., Williams 1964, Hortal et al.
203 2009). For example, larger oceanic islands typically have multiple habitat types, including
204 mountains, valleys, rivers, etcetera, allowing for multiple types of species to specialize on these
205 habitats, whereas smaller islands only have a few habitat types. Likewise, in freshwater lakes,
206 which can be thought of as aquatic islands in a terrestrial ‘sea’, larger lakes typically have more
207 habitat heterogeneity (e.g., depth zonation) than smaller lakes.

208 (ii) *Compositional heterogeneity due to dispersal limitation*. Dispersal limitation can also lead to
209 compositional heterogeneity through a variety of spatial mechanisms, including ecological drift,
210 colonization and competition tradeoffs, and the like (e.g., Condit et al. 2002, Leibold and Chase
211 2017). If dispersal limitation is more likely on larger islands, we might expect greater within-
212 island spatial coexistence via dispersal limitation, higher compositional heterogeneity, and thus
213 greater total species richness on larger than on smaller islands.

214 Patterns of species compositional heterogeneity that emerge from these two distinct mechanisms
215 are difficult to distinguish without explicit information on the characteristics of habitat
216 heterogeneity itself, as well as how species respond to that heterogeneity. While we do not
217 explicitly consider it further here, the spatial versus environmental drivers of compositional
218 heterogeneity (β -diversity) can be more acutely disentangled if site-level environmental
219 conditions and spatial coordinates are known by using standard methods in metacommunity
220 ecology (e.g., Peres-Neto et al. 2006, Ovaskainen et al. 2017).

221 Finally, as with disproportionate effects above, opposite patterns are also possible. While we
222 typically assume that heterogeneity increases with island area, leading to the positive ISAR, this
223 need not be true. For example, smaller islands have higher perimeter:area ratios (i.e., edge
224 effects), and thus can have higher levels of heterogeneity than larger islands by some measures.

225 **Disentangling ISAR Mechanisms with Observational Data**

226 As a result of the often impracticality of field experiments on the ISAR at realistic scales (but see
227 Simberloff 1976), considerable attention has been paid towards developing sampling and
228 analytical methodology that can allow a deeper understanding of potential ISAR mechanisms
229 from observational data. However, these approaches have appeared piecemeal in the literature,
230 are incomplete, and have not yet been synthesized into a single analytical framework.

231 Furthermore, two or more of these mechanisms can act in concert and are non-exclusive (e.g.,
232 Chisholm et al. 2016). For example, the influence of passive sampling is likely always occurring
233 in the background even when disproportionate effects and/or heterogeneity also influence ISAR
234 patterns. Thus, even if we reject passive sampling as the sole mechanism leading to the ISAR
235 via deviations from the null expectation, we cannot say that passive sampling does not at least
236 partially influence the observed patterns. The same is true for any null modelling approach.
237 Likewise, it is possible that disproportionate responses of species via alterations to spatial or
238 local conditions can act in concert with changes in habitat heterogeneity. In this case, however,
239 we can more completely falsify these processes by comparing patterns both within communities
240 (α -diversity) and among communities (β -diversity), as we will discuss in more detail below.

241 Here, we overview a generalized approach for disentangling the possible mechanisms underlying
242 the ISAR. Our approach is based on recent work that uses an individual-based rarefaction
243 framework (e.g., Gotelli and Colwell 2001) to calculate several measures of biodiversity at
244 multiple spatial scales (e.g., Chase et al. 2018, McGlenn et al. 2018). And then to relate these
245 measures to variation in island size. In a sense, then, we propose the use of within-island species
246 richness relationships (Type II or Type III curves from Scheiner 2003, Scheiner et al. 2011) to
247 evaluate the mechanisms underlying among-island ISAR relationships (Type IV curves from
248 Scheiner 2003, Scheiner et al. 2011).

249 Figure 1a overviews the sampling design necessary on an island in order to calculate the
250 parameters necessary to disentangle ISAR mechanisms. Specifically, in addition to estimating
251 the total numbers of species on an island (S_{total}), we advocate sampling multiple standardized
252 plots within a given island (ideally stratified across the island and any potential habitat
253 heterogeneity) so that a number of parameters can be derived and compared with island size.
254 These parameters are described in Table 1 and can be visualized as components along individual-
255 based rarefaction curves as in Figure 1b.

256 From the combination of all sampled plots within an island, one can generate a γ -rarefaction
257 curve and several diversity parameters that can be derived from that information. We refer to the
258 rarefied number of species expected from n randomly sampled individuals from the γ -rarefaction
259 curve as ${}^{\gamma}S_n$. Because the γ -rarefaction curve is generated by combining all sample plots on a
260 given island and randomly choosing individuals, any spatial heterogeneity in species associations
261 is broken. In addition to ${}^{\gamma}S_n$, which weights common and rare species equally, we can also derive
262 a measure which weights common species more heavily than rare species. Specifically,
263 Hurlbert's (1971) Probability of Interspecific Encounter (PIE) is a measure of evenness in the
264 community and is equivalent to the slope of the rarefaction curve at its base, as illustrated by the
265 gray arrows in Figure 1b (e.g., Gotelli and Graves 1996, Olszewski 2004). We use the bias-
266 corrected version, $PIE = \left(\frac{N}{N-1}\right) * \left(1 - \sum_{i=1}^S p_i^2\right)$, where N is the total number of individuals in
267 the entire community, S is the total number of species in the community, and p_i is the proportion
268 of each species i . For analyses, we convert PIE to an effective number of species (the number of
269 species that would be observed if all of the species in a sample were equally abundant) (Jost
270 2006), which we call $S_{PIE} (=1/(1-PIE))$. PIE is the same as 1-Simpson's diversity index, and
271 when converted to an effective number of species, is part of the Hill continuum of diversity

272 numbers that places more weight on common species (whereas richness places equal weight on
273 common and rare species) (e.g., Hill 1973, Jost 2006). When S_{PIE} is calculated from the γ -
274 rarefaction curve, we refer to the effective number of species as ${}^{\gamma}S_{PIE}$. Note that only PIE, not
275 S_{PIE} , is illustrated in Figure 1b, because the forms of S_{PIE} are not readily illustrated in the
276 individual-based rarefactions construct.

277 To discern whether any of the ISAR patterns emerge from within-island heterogeneity in species
278 composition, we need to derive estimates of β -diversity. To do so, we can generate an α -
279 rarefaction curve and estimate diversity parameters similar to those above, but at the local
280 (within plot) scale. From this, we can compare the parameters from the γ -rarefaction curve
281 which eliminates any plot-to-plot variation due to heterogeneity in species composition by
282 randomizing across the plots, to the α -rarefaction curve calculated from individual plots (or a
283 spatially defined subset of plots) which contains local information only (dashed line in Figure
284 1b). The degree to which the γ -rarefaction curve (which eliminates spatial heterogeneity) differs
285 from the α -rarefaction curve (which keeps spatial heterogeneity) tells us how much local
286 variation there is in species composition across sites, providing an index of β -diversity resulting
287 from species aggregations (see Olszewski 2004, Chase et al. 2018, McGlenn et al. 2018). If the
288 γ -and α -rarefaction curves are on top of each other, then we can conclude that there is no
289 heterogeneity in the region. Alternatively, if the α -rarefaction curve is far below the γ -
290 rarefaction curve, this implies that intraspecific aggregation has created compositional
291 heterogeneity in the community. Two β -diversity parameters are informative in this context: β_{S_n}
292 ($={}^{\gamma}S_n/{}^{\alpha}S_n$) which indicates the influence of aggregation of all species, and $\beta_{S_{PIE}}$ ($={}^{\gamma}S_{PIE}/{}^{\alpha}S_{PIE}$),
293 which indicates aggregations primarily by more common species (i.e., the effective number of
294 unique communities; Tuomisto 2010).

295 In what follows, we discuss how this analytical methodology can be used to disentangle ISAR
296 relationships where explicit sampling information from within and among islands is available.
297 At the outset, it is important to note that in most of what follows, we focus exclusively on island
298 systems where the primarily independent variable influencing species diversity is island size,
299 with minimal variation in other diversity drivers. We focus on this because our goal is to
300 elucidate and disentangle the ISAR, which describes a bivariate relationship between island size
301 and species richness, and for which there remains much confusion and little synthesis.
302 Nevertheless, as with all diversity studies, focusing on a single independent driver is a limiting
303 case. In many island systems, islands vary in size as well as other drivers (e.g., productivity,
304 isolation). Nevertheless, it is quite straightforward to extend the approach that we advocate
305 below to include these complexities and still disentangle the influence of island size in the
306 context of the ISAR. In such cases, one could simply use these other potential drivers as
307 covariates with island size in an analysis focusing on the response variables we overview in
308 Table 1 and Figure 1, using the same framework as described below. Or one could add more
309 complexity by including these independent variables in a hierarchical model or structural
310 equation model with the same response variables, which we discuss in more detail in the
311 conclusions below (see e.g., Blowes et al. 2017, Chase et al. 2018 for similar analyses in a
312 different context).

313

314

315 **Table 1. Parameters used to disentangle island species area relationship patterns**

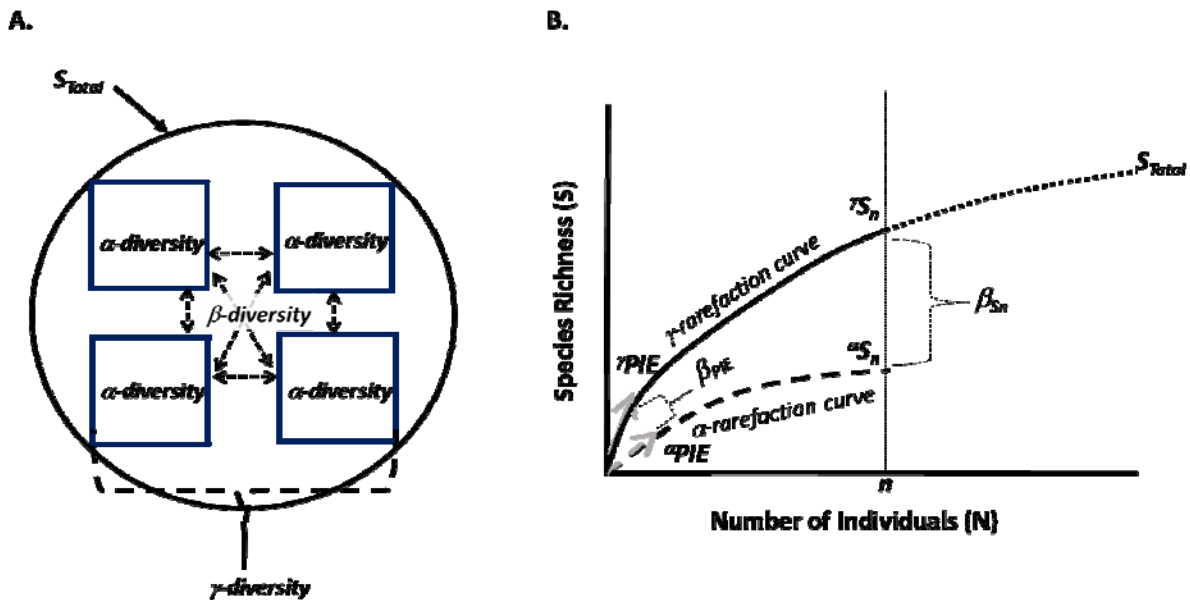
Parameter	Description
<i>Island-level patterns</i>	
S_{total}	Total number of species on an entire island. Estimated independently or with extrapolations from samples.
N	Number of individuals of all species found in a given sampling plot (usually expected to scale linearly with effort)
<i>γ-level patterns (derived by combining all sample plots on an island)</i>	
${}^{\gamma}S_n$	Number of species expected from n randomly sampled individuals from the γ -rarefaction curve
${}^{\gamma}S_{PIE}$	Effective number of species given the probability of interspecific encounter (PIE) from the γ -rarefaction curve
<i>α-level patterns (derived from a single sampling plot or subset of plots on an island)</i>	
${}^{\alpha}S_n$	Number of species expected from n randomly sampled individuals from the α -rarefaction curve
${}^{\alpha}S_{PIE}$	Effective number of species given the probability of interspecific encounter (PIE) from the α -rarefaction curve
<i>β-level patterns (derived from comparing γ to α-level patterns)</i>	
β_{S_n}	Ratio of numbers of species expected for a given n from γ -rarefaction curve to those expected for a given n from α -rarefaction (a measure of compositional heterogeneity) (${}^{\gamma}S_n/{}^{\alpha}S_n$)
$\beta_{S_{PIE}}$	Ratio of numbers of effective number of species for a given PIE from γ -rarefaction curve to the effective number of species for a given PIE from α -rarefaction (a measure of compositional heterogeneity emphasizing common species) (${}^{\gamma}S_{PIE}/{}^{\alpha}S_{PIE}$).

316

317

318 **Figure 1.**

319



320

321 *Figure 1.* A. Overview of a sampling scheme appropriate for applying the analytical approach
 322 outlined in this paper. The circle represents a hypothetical island, and each of the four squares
 323 represents individual sampling plots from which α -diversity metrics can be derived. The
 324 addition of all of the individuals sampled in all of the plots allows the calculation of γ -diversity
 325 metrics, while the differences among the α -diversity plots is β -diversity. S_{total} represents the
 326 total number of species on the island, including those that were not observed in any of the
 327 sampled plots. B. Illustration of how these diversity indices can be visualized graphically from
 328 individual-based rarefaction curves that plot species richness (S) against the numbers of
 329 individuals (N) across scales. The γ -rarefaction curve (solid line) is derived by combining all
 330 individuals from all plots measured on a given island and randomizing individuals to generate
 331 the curve. From this curve, the dashed line allows us to visualize the total number of species on
 332 the island including those that were not sampled in any plot (S_{total}). We can also visualize: (i) the
 333 numbers of species expected from a given n , γS_n (where the vertical dashed line at n intersects
 334 the solid curve) (ii) the probability of interspecific encounter (PIE), which represents the slope at
 335 the base of the rarefaction curve, γPIE (solid grey arrow). The α -rarefaction curve (dashed line)
 336 is derived by randomizing individuals from a single plot, and similar parameters can be derived
 337 — αS_n (vertical dashed line intersects the dashed curve) and αPIE (dashed grey arrow). The ratio
 338 between the γ - and α -rarefaction curves provides estimates of β -diversity that indicate the degree
 339 of intraspecific aggregation on the island. Note, in text, we advocate converting PIE values into
 340 effective numbers of species (S_{PIE}), but only illustrate PIE in the figure, as it is not
 341 straightforward to illustrate S_{PIE} on these axes.

342

343 ***Question 1: What is the shape of the overall ISAR?***

344 ***Parameter analyzed: Total number of species on an island (S_{total})***

345 S_{total} is the most straightforward ISAR variable one can measure. The ideal way to estimate S_{total}
346 is from independent information, such as exhaustive searching or checklists of species known to
347 occur on a given island. However, because this information is often unavailable, S_{total} can be
348 estimated via techniques for predicting the number of species in a given extent (e.g., Colwell and
349 Coddington 1994, Harte et al. 2009, Chao and Jost 2012, Chao and Chiu 2014, Azaele et al.
350 2015). None of these approaches are perfect, and we are agnostic as to which approach is best
351 for estimating S_{total} when complete species lists are not available. However, in our case studies
352 below, we use the Chao (1984) non-parametric estimator to extrapolate the total number of
353 species on a given island because it can be mathematically and conceptually linked to the
354 rarefaction curves that we use (Colwell et al. 2012). However, this can only be viewed as a
355 minimum expected S_{total} , and will likely underestimate the true S_{total} .

356 While S_{total} is the fundamental parameter of interest to calculate an ISAR, it alone provides little
357 information as to the nature of its potential underlying mechanisms. This is because S_{total} is
358 influenced by a number of underlying parameters, including the density of individuals, the
359 relative abundances of species, and the intraspecific aggregation or spatial heterogeneity
360 exhibited by species. Thus, to disentangle the factors underlying variation in S_{total} , we need to
361 look deeper into these underlying components, which we can do using the parameters
362 overviewed in Table 1 and Figure 1b (see also Chase et al. 2018, McGlenn et al. 2018).

363 ***Question 2: Does the ISAR result differ from what is expected from random sampling?***

364 ***Parameter Analyzed: Number of species expected from the γ -rarefaction curve (${}^{\gamma}S_n$)***

365 If patterns of the ISAR were generated simply by the random sampling hypothesis, we would
366 expect that γ -rarefaction curves of small and large islands would fall right on top of each other
367 (whereas the curve would go farther along the x-axis for the larger island, because more total N
368 are present on larger islands) (Figure 2a). If the γ -rarefaction curves between smaller and larger
369 islands differ, which we can quantify by comparing ${}^{\gamma}S_n$ among islands (Figure 2b), then we can
370 conclude that something other than random sampling influences the ISAR. This is essentially
371 the same procedure as that described by the random placement approach (Coleman 1981,
372 Coleman et al. 1982).

373
374 If ${}^{\gamma}S_n$ increases with increasing island area, this means that more species can persist for a given
375 sampling effort on larger than smaller islands. We can go one step further in describing this
376 pattern by examining how island size influences the relative commonness and rarity of species.
377 If island area influences the γ -rarefaction curve via an overall decrease in evenness of both
378 common and (as shown in Figure 2b), we would expect that both ${}^{\gamma}S_n$ and ${}^{\gamma}S_{PIE}$ would change.
379 However, if only relatively rarer species are disproportionately influenced by island area (not
380 shown in figure), we would expect that ${}^{\gamma}S_n$ would increase with increasing island area, but there
381 should be little to no effect on ${}^{\gamma}S_{PIE}$. Importantly, the slope of the ${}^{\gamma}S_n$ with island size very much

382 depend on exactly which n is used in the calculations, with steeper slopes observed at higher n .
383 This is similar to what was observed by Karger et al. (2014) on islands in Southeast Asia.

384
385 It is important to note that the hypotheses of increasing nS_n and/or ${}^nS_{PIE}$ with increasing island
386 area, as illustrated in Figure 2b are not the only possibilities. Estimates of diversity from
387 samples, such as nS_n and/or ${}^nS_{PIE}$, could certainly decrease with increasing island size. For
388 example, on islands that result from habitat fragmentation and/or those that are surrounded by a
389 relatively hospitable matrix, there are several mechanisms (e.g., habitat spillover) that can lead to
390 higher levels of diversity (both in S_{total} as well as from samples [nS_n and/or ${}^nS_{PIE}$]) in smaller
391 relative to larger islands (e.g., Ewers and Doham 2006, Fahrig 2017).

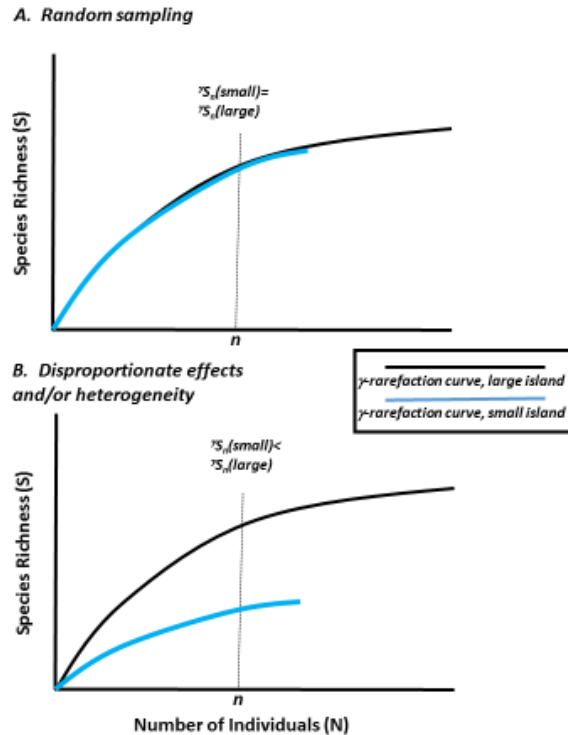
392
393 Even if the numbers of species (and evenness) for a given sampling effort (nS_n and/or ${}^nS_{PIE}$)
394 declines, this can be outweighed by the random sampling effect, leading to an overall increasing
395 ISAR even with decreasing components of diversity with increasing area. This emphasizes the
396 fact that ISAR mechanisms are not mutually exclusive. That is, random sampling effects are
397 likely always operating (as evidenced by the increase in species richness with increasing N along
398 the rarefaction curve), even when disproportionate effects and/or heterogeneity also influence the
399 ISAR pattern. As such, we can use rarefaction curves to examine whether random sampling is
400 the only mechanism operating, as it would be if there is no influence of island size on nS_n , and as
401 a result, conclude that differential effects and/or heterogeneity are not operating. However, we
402 cannot conversely say that random sampling is not operating if there is a relationship between nS_n
403 and island size. This is because random sampling effects are always operating anytime there are
404 fewer species on a given island than the total numbers of species in the regional species pool.

405
406 Finally, our discussion above implicitly assumed that island size changes the total number of
407 individuals on an island via passive sampling, but not the density of individuals in a given
408 sampled area. However, there are also reasons that island size can influence individual density.
409 For example, if larger islands are more favorable for some reason, the total numbers of
410 individuals would increase both because island size increases, as well as because the density in a
411 given sampled area increases. Alternatively, smaller islands could contain more individuals for a
412 given area (higher density) if there is high spillover from the matrix into smaller islands, or if
413 larger islands have less favorable habitats. In such cases, comparisons of nS_n are still necessary
414 to test the null hypothesis of whether the ISAR results from random sampling or not. However,
415 when N varies with island size, it will also be useful to compare estimates of S at the scale of the
416 sample rather than the number of individuals (i.e., sampled-based estimates sensu Gotelli and
417 Colwell 2001, McGlenn et al. 2018) to determine how changes in N influence the ISAR.

418

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422

423 Figure 2. A. Hypothetical case where a large island has more species than a smaller island in
424 total, but this entirely because of random sampling (the larger island has more total individuals).
425 Note that the rarefaction curves for each island fall on top of each other, and the parameters
426 derived from it, including ${}^{\gamma}S_n$ and ${}^{\gamma}S_{PIE}$ (not shown) are the same between larger and smaller
427 islands. B. Hypothetical case where a large island has more species than a smaller island, and
428 this results because both a sampling effect (the larger island has more N , and goes farther down
429 the x-axis) as well as a disproportionate effect whereby ${}^{\gamma}S_n$ is lower on the smaller than the larger
430 island. ${}^{\gamma}S_{PIE}$ in this case (not illustrated) is also smaller on the smaller island (because it has a
431 shallower slope), but this need not be the case if only rarer species are affected.

432
433

434
435

436 **Question 3: Does the ISAR result from disproportionate effects or from heterogeneity**
437 **Parameter analyzed: β -diversity as the difference between the γ -rarefaction curve and α -**
438 **rarefaction curve.**

439

440 If there is a relationship between ${}^{\gamma}S_n$ and/or ${}^{\gamma}S_{PIE}$ and island area, we can conclude that there is
441 something other than random sampling influencing the ISAR. With only the parameters from
442 the γ -rarefaction curve, however, we cannot yet discern whether this is due to disproportionate
443 effects that are equally distributed across the island, or whether these effects emerge because of
444 heterogeneity in species composition across the island (i.e., different species and relative

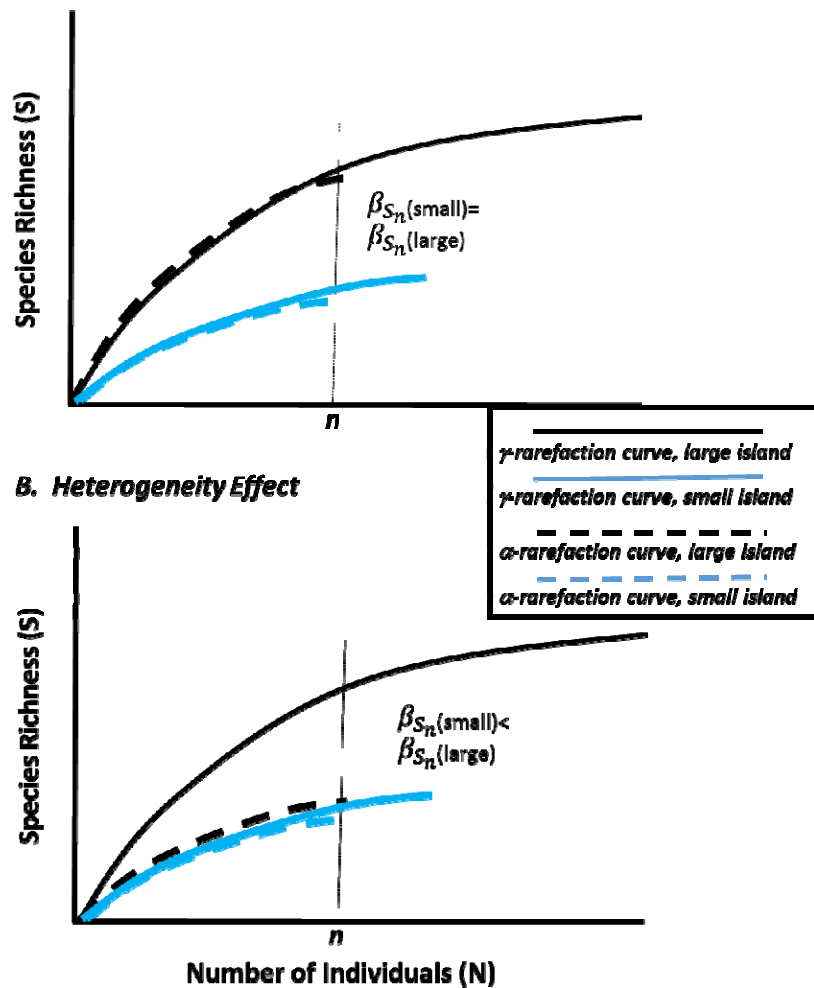
445 abundances in different parts of the island). To disentangle disproportionate effects from
446 heterogeneity, we must look more closely into the variation in species abundances and
447 composition within an island—that is, within-island β -diversity.

448 If β_{S_n} has no relationship with island size, then we can reject the heterogeneity hypothesis
449 (Figure 3a; note, in the figure, we have illustrated that β_{S_n} is 1, indicating there is no
450 heterogeneity due to aggregation; however, this hypothesis would also be true if $\beta_{S_n} > 1$, but does
451 not significantly vary with island size). However, if β_{S_n} increases with island size, then we
452 conclude that heterogeneity plays at least some role in the generation of the ISAR. If the ISAR
453 is primarily driven by heterogeneity, we would expect there to be no relationship between ${}^{\alpha}S_n$
454 and island size, but a strong relationship with ${}^{\gamma}S_n$, giving us a significant β_{S_n} relationship with
455 island size (Figure 3b). Such a pattern was observed by Sfenthourakis and Panitsa (2012) for
456 plants on Greek islands in the Aegean Sea. In Figure 3b, we have illustrated a case where
457 heterogeneity influences rare as well as common species, indicating an effect on both β_{S_n} and
458 $\beta_{S_{PIE}}$ (not shown, but implied because the slope at the base of the curve [i.e., PIE] is influenced).
459 However, it is also possible that heterogeneity can influence just the rarer, but not more common
460 species, wherein we would expect an effect on β_{S_n} , but not $\beta_{S_{PIE}}$ (not shown in Figure).

461 It is quite possible that both disproportionate effects and heterogeneity occur simultaneously and
462 in the same direction, in which case, we would expect a significant relationship between ${}^{\alpha}S_n$ and
463 island size (indicating disproportionate effects) and stronger relationship between ${}^{\gamma}S_n$ island size,
464 giving a significant relationship between island size and β_{S_n} (not shown in Figure). On the other
465 hand, disproportionate effects and heterogeneity mechanisms can act in opposition to one
466 another. For example, the area-heterogeneity trade-off hypothesis assumes that as heterogeneity
467 increases, the amount of area of each habitat type declines when total area is held constant
468 (Kadmon and Allouche 2007, Allouche et al. 2012). Although perhaps not a common scenario
469 (e.g., Hortal et al. 2009), if the types of habitats increase with island area, while the total amount
470 of each habitat type declines, we might expect ${}^{\alpha}S_n$ and/or ${}^{\alpha}S_{PIE}$ to decline, while ${}^{\gamma}S_n$ and/or ${}^{\gamma}S_{PIE}$
471 can increase, remain unchanged or decrease, depending on the degree to which the heterogeneity
472 effect is overcome by disproportionate effects (not shown).

473 Finally, if there is a significant relationship between β_{S_n} and/or $\beta_{S_{PIE}}$ with island area, we can
474 conclude that compositional heterogeneity likely underlies the ISAR, but we cannot infer
475 whether this is due to habitat heterogeneity or dispersal limitation. To disentangle the relative
476 importance of these mechanisms, it would be necessary to have additional information; for
477 example, on the environmental conditions from different locations from within an island, and
478 how species compositional heterogeneity was related to those conditions (see e.g., Leibold and
479 Chase 2017 for an overview of approaches aimed at disentangling these).

A. No Heterogeneity Effect



480

481

482 Figure 3. A. A hypothetical case where there is no heterogeneity in species composition within
 483 islands (the α - and γ -rarefaction curves completely overlap), such that $\beta_{S_n} = 1$. And this does not
 484 vary with island size. Note, that it is also possible that $\beta_{S_n} > 1$, but we would conclude
 485 no heterogeneity effect underlying the ISAR if this is not influenced by island size. B. A case where
 486 there is heterogeneity in species composition in the larger island (the α - and γ -rarefaction curves
 487 differ), but not the smaller. And thus, there is a positive relationship between compositional
 488 heterogeneity (β_{S_n} and/or β_{S_n}) island size. In this case, note that the α - rarefaction curves
 489 between the larger and smaller island overlap, and the island-effect is just observed at the γ -level,
 490 indicating the ISAR results solely from heterogeneity. This need not be the case, however, and
 491 other complexities can arise (see text).

492

493 **Caveat:** Our approach, like all rarefaction-based analyses, assumes that sampling strategies can
 494 clearly identify and enumerate individuals of each species. Unfortunately, enumeration of
 495 individuals is much more difficult or impossible in certain kinds of communities (e.g.,
 496 herbaceous plants, corals). Nevertheless, there are some ‘workaround’ solutions that can be used
 497 to apply the rarefaction techniques we have advocated to data where numbers of individuals are
 498 not available, but other measures of relative abundance are (e.g., percent cover or occupancy).
 499 For example, one can convert percentages of a species to individuals via a multiplier. In such a
 500 case, the meaning of PIE, S_n and aggregation measures change slightly, but can be calculated.
 501 Alternatively, one can collect presence-absence data on species in many quadrats within a
 502 locality. The presence of a species in a quadrat can be taken as a proportion and given the often
 503 strong correlation between abundance and occupancy (e.g., Gaston et al. 2000, Borregaard and
 504 Rahbek 2010), converted to an estimate of percent cover and converted as above. Again, while
 505 the interpretation of the parameters measured above cannot be taken literally, they provide a
 506 useful way to compare multiple diversity measures (at multiple scales) so that the framework we
 507 advocate can be applied.

508 **Case studies:**

509 Next, we illustrate how to use our analytical framework to test the ecological mechanisms
 510 underlying the ISAR with examples from three datasets representing different taxa and island
 511 settings. (1) Lizards sampled from several islands in the Andaman and Nicobar archipelago in
 512 the Indian Ocean (data from Surendran and Vasudevan 2015a,b); (2) Grasshoppers (Orthoptera)
 513 from Ozark glades, which are rocky outcrop prairies that represent island-like patches in a
 514 forested ‘sea’ (data from Ryberg and Chase 2007, Ryberg 2009); (3) plants from island-like
 515 habitat fragments of desert/Mediterranean scrub within an agriculture matrix (data from Giladi et
 516 al. 2011). For each case study, we present a brief overview of the system, results, and an
 517 interpretation of the results. We only used data from islands where multiple plots were censused;
 518 γ -measures included all of these plots, while α -measures were taken as the average among plots.
 519 Results are presented in Table 1 and Figure 4.

520 All analyses were performed in R version 3.5.0 (R Core Team (2018)). For each system, we did
 521 not have independent estimates of S_{total} , and so we used extrapolation using iNEXT (Hsieh et al.
 522 2018). We also used iNEXT to calculate rarefied richness values (S_n). S_{PIE} was calculated using
 523 Vegan (Oksanen et al. 2017). Plots were generated using ggplot2 (Wickham 2016). Code and
 524 data for these analyses are available at https://github.com/Leana-Gooriah/ISAR_analysis

525 Table 2: Linear regression coefficients and fits for each response in each case study.

526 Coefficients are only given when the slope was significantly different from zero.

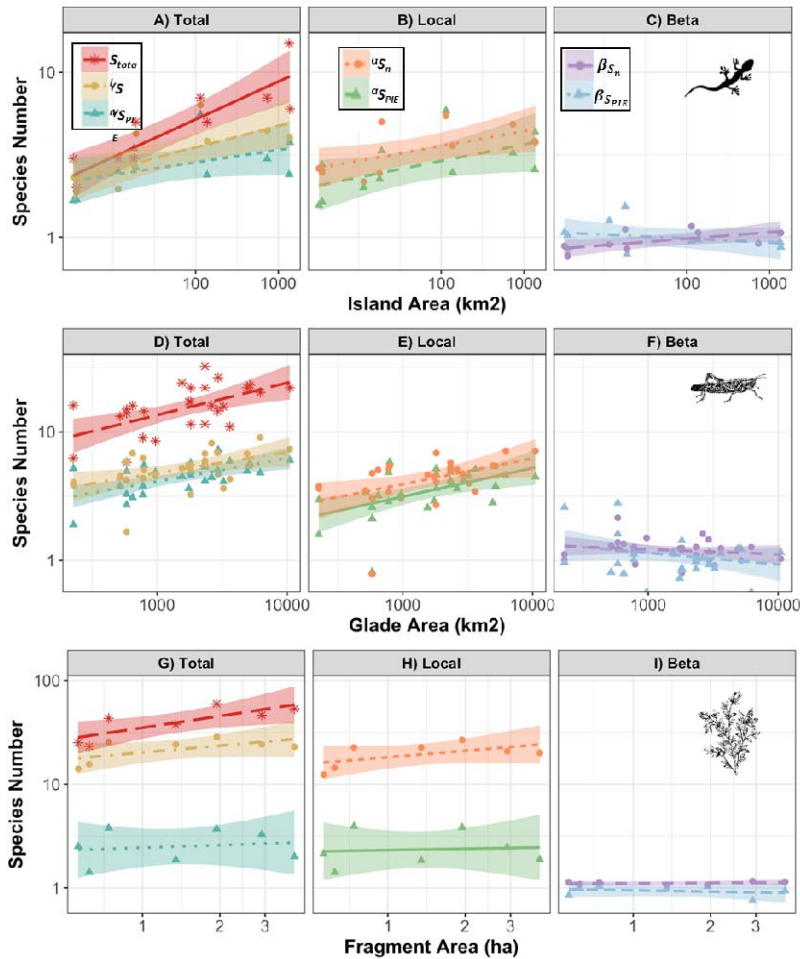
System	Response	Intercept	Slope	R ²	p-value
Lizards on Oceanic Islands	S_{total}	0.59	0.23	0.76	<0.0001
	γS_n	0.69	0.15	0.51	0.008
	γS_{PIE}	-	-	-	0.1
	αS_n	0.86	0.09	0.36	0.003
	αS_{PIE}	0.61	0.10	0.28	0.05

	β_{S_n}	-0.20	0.04	0.34	0.03
	$\beta_{S_{PIE}}$	-	-	-	0.37
Grasshoppers in Ozark Glades	S_{Total}	0.87	0.25	0.30	0.0001
	γS_n	0.45	0.16	0.19	0.01
	γS_{PIE}	0.18	0.18	0.35	0.0005
	αS_n	-0.02	0.2	0.18	0.013
	αS_{PIE}	-0.39	0.22	0.25	0.004
	β_{S_n}	-	-	-	0.54
	$\beta_{S_{PIE}}$	-	-	-	0.33
Plants in fragmented scrubland	S_{total}	3.61	0.24	0.37	0.03
	γS_n	-	-	-	0.13
	γS_{PIE}	-	-	-	0.71
	αS_n	-	-	-	0.17
	αS_{PIE}	-	-	-	0.85
	β_{S_n}	-	-	-	0.57
	$\beta_{S_{PIE}}$	-	-	-	0.56

527

528

529 **Figure 4.**



530

531 **Figure 4.** Log-log plots from the three case studies provided above. Each row represents results
 532 from a different case study; top row is for the lizards on the Andaman Islands; middle row is for
 533 the grasshoppers in Ozark glades; bottom row is for plants in Israeli fragments. Panels A,D,G
 534 represent parameters derived from the regional scale, including S_{total} (the number of species
 535 estimated on the total island), S_n (the number of species expected for a minimum N measured
 536 across plots), and S_{PIE} (the effective number of species given PIE across plots) (see text for
 537 explanation). Panels B, E, H represent parameters derived from the local scale, including αS_n
 538 (the number of species expected for a minimum n measured in a single plot) and αS_{PIE} (the
 539 effective number of species given PIE within a plot). Panels C, F, I represent parameters derived
 540 from comparing the local and regional scale (=β-diversity), including β_{S_n} (the difference which
 541 represents heterogeneity in rare and common species), and $\beta_{S_{PIE}}$ (the difference which represents
 542 heterogeneity in common species). Coefficients and significance values are given in Table 1.
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544

545 **Lizards on Oceanic Islands**—The Andaman and Nicobar islands are a relatively pristine island
546 archipelago in the Indian Ocean. A variety of taxa on these islands have been the subject of
547 island biogeography studies, including ISAR studies (e.g., Davidar et al. 2001, 2002). Here, we
548 used data from Surendran and Vasudevan (2015a,b) who intensively sampled lizards in 100 m²
549 quadrats from 11 islands that varied from 3.3 to 1375 km² in area. We only used data from
550 islands where two or more quadrats were censused.

551 As expected, we found a strong increase in our estimate of S_{total} as island size increased. We also
552 found that γS_n increases significantly with island area, allowing us to reject the null hypothesis
553 that the ISAR is driven by random sampling effects. However, the relationship between γS_{PIE}
554 and island area was not significant (Table 2, Figure 4a). A slightly different pattern emerged at
555 the local scale (Figure 3b), with individual quadrats on larger islands having more species (αS_n)
556 that were less uneven in species composition (αS_{PIE}) than on smaller islands. Because there were
557 significant relationships between island size and both the γ -scale and α -scale measures, we can
558 conclude that disproportionate effects played at least some role in driving the ISAR on these
559 islands. Without additional information, we cannot say for certain exactly which spatial
560 mechanisms are operating to allow more even communities, and more species co-occurring in
561 local quadrats on larger compared to smaller islands. However, because βS_n also increased with
562 island size, this indicates that there was at least some influence of heterogeneity on the ISAR.
563 This heterogeneity effect was only observed among the rarer species, but not the more common
564 species, because there was no concomitant relationship between βS_{PIE} and island size. From
565 other studies in these islands, we know that habitat heterogeneity does generally increase with
566 island size (Davidar et al. 2001, 2002), and so suspect this relationship influenced heterogeneity
567 in lizard composition from quadrat to quadrat more on larger relative to smaller islands.

568 **Grasshoppers in Ozark Glades**—Ozark glades are patchy island-like habitats within
569 Midwestern forested ecosystems that contain xeric adapted herbaceous plant communities
570 together with associated fauna (Ware 2002). Grasshoppers are diverse and abundant herbivores
571 that are known to respond to local and spatial processes in these patchy ecosystems (e.g., Östman
572 et al. 2007, Ryberg and Chase 2007). Here, we use data collected by Ryberg (2009) from area-
573 standardized sweep sample transects (each sample represented 50 sweeps taken from a transect
574 covering approximately 50 m²) taken from within glades without predatory lizards which varied
575 from 0.02 to 1.05 ha (ranging from four transects on the smallest glade to 32 on the largest).

576 As with the lizards above, we find that S_{total} increases with island size, as does γS_n . Furthermore,
577 in this case, γS_{PIE} also increased with island size (Table 2, Figure 4d). A similar pattern is
578 reflected at the local scale (Figure 4e). Thus, again, we can reject the null hypothesis that the
579 ISAR emerges from random sampling, and instead we see a clear signal for disproportionate
580 effects influencing both the number of species and their relative abundances. We suspect that
581 one reason for this was because we only used glades that were relatively isolated from one
582 another, and these grasshoppers do not readily disperse through the matrix. And thus, local
583 processes likely outweighed any regional-level sampling effects. Unlike the lizards, however,
584 we found no effect of glade size on β -diversity of grasshoppers between sweep samples within a
585 glade (Figure 4F), suggesting that the ISAR did not likely result from increased levels of

586 heterogeneity in larger glades, but rather from spatial processes associated with disproportionate
587 effects. This is despite the fact that we know that heterogeneity in microhabitat types does
588 increase with increasing glade size (Ryberg 2009). We suspect that the fact that these
589 grasshoppers are rather mobile within glades was a reason that heterogeneity in species
590 composition did not emerge among glades that varied in size. Unfortunately, however, without
591 further information, we cannot say exactly what sorts of mechanisms allowed more species of
592 grasshoppers to persist in larger glades than expected from random sampling.

593 **Plants in fragmented scrubland**—Xeric scrub habitat in Israel was once quite extensive, but
594 has been severely fragmented such that remnant habitats can be thought of as islands within a sea
595 of agriculture (mostly wheat fields). These fragments have been the subject of intensive research
596 on a number of organisms, including plants and several groups of animals (e.g., Yaacobi et al.
597 2007, Giladi et al. 2011, 2014, Gavish et al. 2012). Here, we used data from the Dvir region
598 from the study by Giladi et al. (2011) on plants identified and enumerated in two or three 225 m²
599 quadrats within seven fragments varying from 0.56 to 3.90 ha.

600 Again, we found that S_{total} increased with fragment area, indicating a positive ISAR relationship.
601 However, in this case, there were no significant relationships with ${}^{\gamma}S_n$ or ${}^{\gamma}S_{\text{PIE}}$ (Table 2, Figure
602 4g), any of the metrics from the α -rarefaction curve (Figure 4h), nor any of the β -scale metrics
603 (Figure 4i). In this case, then, we are not able to reject the null hypothesis and instead conclude
604 that the ISAR in these fragmented habitats is most consistent with the idea of random sampling.
605 Even though we used different (and in our opinion, more robust) analytical tools, our results are
606 qualitatively similar to those derived by the authors of the original study (Giladi et al. 2011). In
607 this case, these results would indicate one of two general possibilities. First, it could be that
608 these plants disperse well enough across the matrix that habitat size does not strongly influence
609 local population dynamics. Second, it could be that local population dynamics do not depend on
610 the numbers of individuals and types of species in local neighborhoods, at least during the time
611 scale in which habitat fragmentation has taken place.

612 **Discussion and Conclusions**

613 The island species-area relationship (ISAR)—depicting how the numbers of species increase
614 with the size of the island or habitat patch—is one of the most well-known patterns in
615 biogeography. Understanding the ISAR and the processes leading to it is not only important for
616 basic ecological knowledge, but is also of critical importance for biodiversity conservation in the
617 context of habitat loss and fragmentation. Despite this, the study of the ISAR continues to be
618 difficult to synthesize, primarily because of the confusion about the confounding influence of
619 sampling effects and spatial scale on the ISAR. For example, previous syntheses of the ISAR in
620 natural and fragmentation contexts have focused on estimates of species richness at the entire
621 island scale (e.g., Triantis et al. 2012, Matthews et al. 2016). Other syntheses, however, have
622 confounded species richness measurements from multiple scales and contexts, making
623 comparisons within and among studies difficult (e.g., Drakare et al. 2006, Smith et al. 2005,
624 Fahrig 2017). As we have shown here, it is important to understand and report how species
625 richness was sampled in order to interpret ISAR results. This is particularly true in the realm of
626 conservation biology, where the influence of habitat loss and fragmentation on biodiversity is a

627 critically important, but also controversial topic. In fact, a great deal of the controversy (e.g.,
628 Haddad et al. 2015, 2017, Hanski 2015, Fahrig 2013, 2017, Fletcher et al. 2018) is likely
629 attributable to different investigators using different sampling procedures, different analyses, and
630 different spatial scales for their comparisons, and thus comparing apples to oranges.

631 We are not alone in this call for a more careful consideration of sampling when measuring and
632 interpreting ISARs (Hill et al. 1994, Schroeder et al. 2004, Yaacobi et al. 2007, Giladi et al.
633 2011, 2014, Sfenthourakis and Panitsa 2012, Karger et al. 2014). However, our approach, using
634 metrics derived from γ - and α -rarefaction curves, provides an important advance over previous
635 approaches by allowing one to more explicitly examine the influence of sampling and scale on
636 the outcome. As our case studies illustrate, we can use this approach to explicitly disentangle the
637 main hypotheses suspected to underlie the ISAR (random sampling, disproportionate effects and
638 heterogeneity). For example, the case study on fragmentation in Israeli scrub habitats indicated
639 that random sampling was primarily responsible for the ISAR. Interestingly, this result is similar
640 to that found by Coleman et al. (1982) in their original use of this approach to another
641 fragmented system; birds on islands within a flooded reservoir. Such results might be expected
642 if species can readily use the matrix between habitat islands, or can easily disperse among
643 habitats. Alternatively, in both the lizard and grasshopper systems, species are less likely to use
644 the matrix and dispersal is likely lower, influencing the observation that disproportionate effects
645 and heterogeneity influence the ISAR. Nevertheless, these are just a few case studies we
646 analyzed where appropriate data were available. A more complete exploration of the generality
647 of the patterns and potential mechanisms leading to the ISAR will require more thorough
648 analyses of natural islands and patchy landscapes, as well as habitat islands that are created by
649 habitat loss and fragmentation. Such analyses will allow us to achieve a more general synthesis
650 of the patterns and possible processes creating ISARs in natural and fragmented island
651 landscapes, but will also require more data (i.e., spatially explicit data of total and relative
652 abundances of species as well as spatially explicit environmental data) than is typically analyzed
653 in such studies.

654 There are clearly some extensions that can be made to the simple approach that we have
655 overviewed. For example, when measuring ISARs in the real world, there are often many other
656 mechanisms that can influence diversity patterns in addition to island size. For example, another
657 important variable that influences diversity on islands is the isolation (distance) of those islands
658 from others (e.g., MacArthur and Wilson's 1967, Kreft et al. 2008). Habitat area can also
659 influence trophic structure (e.g., larger islands may be more likely to have top predators), which
660 in turn will feedback to influence the shapes of the rarefaction curves and patterns of diversity
661 (e.g., Östman et al. 2007, Gravel et al. 2011). Likewise, in volcanic archipelagos, larger islands
662 tend also to be younger and may have not had as much time for diversification as smaller/older
663 islands, and this confounding factor can also greatly influence the shape of the ISAR (e.g.,
664 Whittaker et al. 2008, Gillespie and Baldwin 2010). In addition, islands can vary in a number of
665 other environmental and biological features, all of which can interact with island area.
666 Fortunately, the metrics for which we have advocated which explicitly incorporate sampling
667 theory and scale (see also Chase et al. 2018) can be analyzed in more complex models than the
668 simple regressions that we have presented above. For example, hierarchical models can be

669 applied to each of these metrics, analyzing the influence of island area along with a number of
670 potential independent variables (see e.g., Blowes et al. 2017 for such analyses addressing a
671 different set of questions). Likewise, structural equation models comparing patterns of ISARs
672 along with several other covariables (e.g., Stiles and Scheiner 2010) can be applied to these
673 metrics to disentangle area effects from other potential drivers.

674 Finally, despite its advantages, it is important to note that our approach is purely observational.
675 As such, although it can provide deeper insights into the likely mechanisms that influence the
676 ISAR than previous observational approaches, it cannot definitively discern process from these
677 patterns. To more definitively test the primary ISAR mechanisms described here, we would
678 need to go a step or two further. This could include, for example, observational studies that take
679 advantage of variation, such as islands that varied semi-orthogonally in both area and
680 heterogeneity (Nilsson et al. 1988, Ricklefs and Lovette 1999, Kallimanis et al. 2008, Hannus
681 and Von Numers 2008, Stiles and Scheiner 2010), but also disentangling patterns of species
682 richness in a more scale-explicit way as we have outlined here. Or it could include manipulative
683 experiments that directly alter island size and/or heterogeneity (e.g., Simberloff 1976, Douglas
684 and Lake 1994, Matias et al. 2010), or disrupt the processes occurring within islands (e.g.,
685 altering patterns of within-island dispersal and/or extinction).

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697 **Author Contributions:**

698 JMC and TMK developed the initial conceptualization of the framework presented here, with
699 significant input from WAR, MAS, FM, DC and LG at different stages. WAR provided the data
700 for the grasshopper case study; FM provided the data for the fragmentation case study. LG wrote
701 the code, with help from DC and FM, and did the analyses. JMC wrote the first draft of the
702 manuscript, and all authors contributed significantly to revisions.

703 **Data and Code Accessibility:**

704 The code to run the analyses described here, as well as the data for the case studies, are freely
705 available on https://github.com/Leana-Gooriah/ISAR_analysis.

706

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