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Thalamo-cortical interactions define functional dissociations across the macaque attention network

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ABSTRACT

Spatial attention is discontinuous, sampling behaviorally relevant locations in theta-rhythmic cycles (3–6 Hz). Underlying this rhythmic sampling are intrinsic theta oscillations in frontal and parietal cortices that provide a clocking mechanism for two alternating attentional states that are associated with either engagement at the presently attended location (and enhanced perceptual sensitivity) or disengagement (and diminished perceptual sensitivity). It has remained unclear, however, how these theta-dependent states are coordinated across the large-scale network that directs spatial attention. The pulvinar is a candidate for such coordination, having been previously shown to regulate cortical activity. We therefore examined pulvino-cortical interactions during theta-rhythmic sampling by simultaneously recording from FEF, LIP, and the pulvinar. Neural activity propagated from (i) pulvinar to cortex during periods of engagement and (ii) from cortex to pulvinar during periods of disengagement. A rhythmic reweighting of pulvino-cortical interactions thus defines functional dissociations in the macaque attention network.

INTRODUCTION

Spatial attention leads to enhanced sensory processing and improved behavioral outcomes (e.g., higher hit rates and faster reaction times)^{1,2}. Classic studies of spatial attention assumed that its neural and behavioral effects were continuous during attentional deployment. Recent studies, however, have instead demonstrated that spatial attention is discontinuous, sampling the visual environment in theta-rhythmic cycles (3–8 Hz)³⁻⁸. We recently linked rhythmic sampling to theta oscillations in frontal and parietal cortices^{4,5}. These theta rhythms organize neural activity into alternating attentional states associated with either enhanced or diminished perceptual sensitivity⁴. We have proposed that theta-rhythmic sampling thus reflects alternating periods of either (i) engagement at the presently attended location or (ii) relative disengagement, with periods of disengagement likely associated with an increased probability of attentional shifts⁴. In this way, theta-rhythmic sampling provides spatial attention with critical flexibility, offering windows of opportunity when it is easier to disengage from the presently attended location and move to another location. But how are these functionally defined attentional states coordinated across the large-scale network that directs spatial attention?

Research into the neural basis of spatial attention has largely focused on cortical contributions, particularly from frontal and parietal cortices^{9,10}. Microstimulation and inactivation studies have shown that these higher-order cortical regions generate modulatory signals that are fed back to sensory cortex¹¹⁻¹³, boosting sensory processing at behaviorally relevant locations². Recent research has challenged this cortico-centric view¹⁴. Several studies have shown that a subcortical structure, the pulvinar nucleus of the thalamus, regulates cortical activity during spatial attention^{15,16}. For example, pulvino-cortical interactions seem to facilitate

communication between visual cortices (i.e., V4 and TEO) by aligning the phase of alpha/low-beta activity (8–15 Hz).

The pulvinar is the largest nucleus in the primate thalamus, yet its functional significance has remained largely unknown^{17,18}. Lesion and inactivation studies have indicated that the pulvinar plays a critical role in mediating spatial attention. For example, lesions of the pulvinar can result in symptoms that are similar to hemineglect following lesions of parietal cortex^{19,20}. Behavioral impairments in human patients are particularly strong when distractor stimuli compete for attentional resources^{21,22}. Wilke, et al.²³, who used muscimol to inactivate the pulvinar, reported similar behavioral impairments in monkeys. That is, the animals demonstrated diminished exploration of the contralesional visual hemifield during inactivations, particularly when stimuli appeared in both hemifields.

The ventral pulvinar is ideally positioned to regulate interactions across the visual system based on its connectivity with cortex^{15,17}. Whereas ventral regions of the pulvinar are largely interconnected with visual cortex²⁴⁻²⁷, dorsal regions are largely interconnected with higher-order cortical regions, including the frontal eye fields (FEF) and the lateral intraparietal area (LIP)²⁸⁻³⁰. The dorsal pulvinar is therefore an ideal candidate for influencing cortical interactions in the attention network. Few studies, however, have measured neuronal responses in the dorsal pulvinar during spatial attention^{31,32}, and its functional role in the attention network has not yet been defined.

Here, we investigated whether pulvino-cortical interactions coordinate the theta-rhythmic attentional states that seemingly shape spatial attention. We therefore simultaneously recorded single-unit activity (SUA) and local field potentials (LFPs) from FEF³³, LIP³⁴, and the pulvinar¹⁷, while monkeys performed a spatial attention task that has previously been shown to promote theta-rhythmic sampling³. We specifically targeted the mediodorsal pulvinar (mdPul),

which receives overlapping projections from frontal and parietal cortices (Fig. S1)²⁸. The present results show that the source of functional connectivity between mdPul and higher-order cortices—which occurs in the alpha/low-beta band (10–20 Hz)—shifts with attentional state, with (i) mdPul being its source during the theta-dependent state associated with engagement (and enhanced perceptual sensitivity) (ii) and LIP being its source during the theta-dependent state associated with relative disengagement (and diminished perceptual sensitivity). We propose that theta-dependent changes in alpha/low-beta activity reflect a functional re-weighting across hubs of the attention network. This rhythmic re-weighting alternately favors brain regions and pathways that promote either attentional sampling or shifting.

RESULTS

We trained two male monkeys (*Macaca fascicularis*, 6–9 years old) to perform a covert spatial-cueing paradigm based on the Egly-Driver task^{4,35}, where a peripheral spatial cue indicated the most likely location of a subsequent, low-contrast visual target (78% cue validity; see Fiebelkorn, et al.⁴, Fig. 1). The animals maintained fixation throughout each trial and responded by releasing a lever. We focused on neural activity during the time period after the cue-evoked response (i.e., the visual-sensory response) and until target onset. During this cue-target delay, the animals were deploying spatial attention at the cued location and neural activity generally satisfied methodological assumptions of stationarity (see online Methods). For between-condition comparisons, we measured neural activity when receptive/response fields overlapped the cued location relative to when receptive/response fields overlapped the non-cued location positioned on a second object^{4,35} (see Fiebelkorn, et al.⁴ for previously reported behavioral evidence of attentional deployment at the cued location).

mdPul contributes to the maintenance of spatial attention at a cued location

Given that the present study is the first to investigate attention-related function in mdPul, we started by characterizing neuronal responses in mdPul and then comparing them with neuronal responses in FEF and LIP. Table S1 displays the number of neurons in each region of interest (ROI) that demonstrated task-related activity. Neurons in frontal and parietal cortices are typically classified based on their response profiles as visual (i.e., sensory-related responses), movement (i.e., saccade-related responses), and visual-movement (i.e., sensory and saccade-related responses) types (see online Methods and Fiebelkorn, et al. ⁴). We recorded from a total of 224 neurons in mdPul, with 52 neurons (23.2%) demonstrating significantly increased spiking activity after presentation of the cue (N = 20 visual-sensory neurons), the target (N = 13 movement neurons), or both the cue and the target (N = 19 visual-movement neurons). A small population of neurons demonstrated significantly decreased task-related activity (N = 9). In comparison to mdPul, 98/238 neurons (41.2%) in FEF and 98/259 neurons (37.8%) in LIP had significantly increased task-related activity. Although the overall percentage of task-responsive neurons was higher in both FEF and LIP, the distributions of visual, movement, and visual-movement neurons (among task-responsive neurons) were similar across the three ROIs.

Figure 1A shows normalized population spiking, time-locked to the cue and averaged across all neurons with a significantly increased visual-sensory response (i.e., visual and visual-movement neurons). Figure 1B shows normalized population spiking, time-locked to the target and averaged across all neurons with a significantly increased movement response (i.e., movement and visual-movement neurons). In both cases, the responses of mdPul neurons were more similar to LIP than to FEF. For example, spiking activity during the delay did not differ between mdPul and LIP (Wilcoxon rank-sum test, $p = 0.386$), but was significantly higher for FEF

neurons (FEF vs. mdPul, Wilcoxon rank-sum test, $p = 0.013$; FEF vs. LIP, Wilcoxon rank-sum test, $p = 0.0008$).

Previous studies on cortical hubs of the attention network have shown that only neurons with visual-sensory responses (i.e., visual and visual-movement neurons)—and not movement neurons—demonstrate significant spiking during the cue-target delay under conditions of spatial attention^{36,37}. Here, we demonstrate that mdPul neurons follow the same pattern, with only visual and visual-movement neurons having significant spiking during the cue-target delay (Fig. S2). We therefore only used neurons with visual-sensory responses (i.e. visual and visual-movement neurons) to determine whether delay spiking in mdPul was significantly higher when receptive fields overlapped the cued location relative to when receptive fields overlapped the non-cued location. For this comparison (i.e., cued vs. non-cued), we averaged spike rates across a 450-ms window, just prior to target presentation, revealing significantly higher delay spiking under conditions of spatial attention (Wilcoxon rank-sum test, $p = 0.011$). We previously performed the same analysis to demonstrate significantly higher, attention-related delay spiking in FEF and LIP⁴. The present findings therefore demonstrate that mdPul—like FEF and LIP—contributes to the maintenance of spatial attention at the cued location and appears to be an integral part of the attention network.

mdPul contributes to theta-rhythmic sampling during spatial attention

Recent evidence has demonstrated that spatial attention samples the visual environment in theta-rhythmic cycles³⁻⁸. We previously linked this theta-rhythmic sampling to the phase of theta oscillations in FEF and LIP⁴. Theta rhythms organized neural activity in these cortical hubs of the attention network into two alternating attentional states, associated with either (i) better visual-target detection at the cued location (i.e., during the “good” theta phase)

or (ii) worse visual-target detection at the cued location (i.e., during the “poor” theta phase). If mdPul serves as a subcortical hub of the attention network, then theta rhythms there might be similarly linked to behavioral performance. We therefore measured whether theta phase in mdPul influenced the likelihood of detecting a low-contrast visual target (see online Methods). We found a significant phase-detection relationship (permutation test, $p < 0.0009$), with a peak at 5 Hz (Fig. 2A), demonstrating that mdPul—like FEF and LIP—has a role in theta-rhythmic sampling during spatial attention. That is, theta-band activity in mdPul is also associated with alternating periods of either better or worse visual-target detection.

In FEF and LIP, we previously observed significant phase-detection relationships not only in the theta band but also at higher frequencies (i.e., in the alpha [9–15 Hz], beta [15–35 Hz], and gamma [> 35 Hz] bands), with different frequency bands characterizing the two rhythmically alternating attentional states⁴. For example, the theta-dependent state associated with better visual-target detection was characterized by increases in both (i) FEF-dominated beta activity and (ii) LIP-dominated gamma activity. Beta and gamma activity in FEF and LIP were therefore only predictive of behavioral performance during this “good” theta phase (see Fiebelkorn et al., 2018, Fig. 3E–F). In comparison, the theta-dependent attentional state associated with worse visual-target detection was characterized by an increase in alpha/low-beta activity in LIP. Alpha/low-beta activity in LIP was therefore only predictive of behavioral performance during the “poor” theta phase (see Fiebelkorn et al., 2018, Fig. 3F).

Based on these previous findings in FEF and LIP, we next examined whether higher-frequency activity in mdPul was linked to a specific attentional state. We re-calculated phase-detection relationships in mdPul (from 9–60 Hz) after first splitting trials into two bins: (i) a bin centered on the “good” theta phase (at 5 Hz) and (ii) a bin centered on the “poor” theta phase. Figure 2B displays the results, showing a significant link between alpha/low-beta phase (12–16

Hz) and visual-target detection (permutation test, $p < 0.001$). This phase-detection relationship specifically occurred during the “good” theta phase. Notably, this is opposite to the result that we previously reported in LIP (10–18 Hz; see Fiebelkorn et al., 2018, Fig. 3F)⁴, where alpha/low-beta phase was only predictive of visual-target detection during the “poor” theta phase. See Figure S3 for corresponding evidence of (i) PAC between theta phase and alpha/low-beta power (10–22 Hz) in mdPul and (ii) previously reported evidence of PAC between theta phase and alpha/low-beta power (9–16 Hz) in LIP⁴. These results demonstrate that increases in alpha/low-beta activity in mdPul and LIP are associated with opposite theta-dependent states, indicating a functional dissociation between these two hubs of the attention network. Alpha/low-beta activity in mdPul is predictive of behavioral performance during periods of engagement at an attended location, while alpha/low-beta activity in LIP is predictive of behavioral performance during periods of disengagement.

mdPul regulates low-frequency oscillatory activity in FEF and LIP

There has been previous evidence that the ventral pulvinar regulates alpha/low-beta activity in interconnected regions of visual cortex (i.e., V4 and TEO), possibly facilitating the exchange of information under conditions of spatial attention¹⁵. In the previous section, we demonstrated that alpha/low-beta activity in mdPul was predictive of behavioral performance (Fig. 2). Here, we asked whether alpha/low-beta activity from mdPul plays a role in regulating neural activity in FEF and LIP, thereby extending previous results¹⁴ from lower-order to higher-order cortex.

We first examined spike-LFP phase coupling, which measures whether there is a consistent clustering of spikes around oscillatory phases in LFPs. Figure 3A–B demonstrates significant coupling between spikes in mdPul and the phase of alpha/low-beta activity in both

FEF (8–19 Hz) and LIP (15–20 Hz), specifically occurring under conditions of spatial attention (permutation test, $p < 0.0009$). When measuring spike-LFP phase coupling, spikes are typically viewed as reflecting regional outputs, while LFPs are viewed as reflecting a summation of regional inputs³⁸. The present results are therefore consistent with mdPul driving alpha/low-beta activity in cortical hubs of the attention network.

For mdPul-FEF synchronization, spike-LFP phase coupling was uni-directional, meaning spikes in FEF were not linked to oscillatory phase in mdPul (Fig. 3A). For mdPul-LIP synchronization, however, spike-LFP phase coupling was bi-directional, with attention-related coupling also occurring between spikes in LIP and the phase of low-frequency oscillatory activity in mdPul (Fig. 3B; permutation test, $p < 0.0009$). We later provide evidence that these bi-directional effects (i.e., LIP to mdPul and mdPul to LIP) are temporally dissociable (see Fig. 5).

We next examined whether alpha/low-beta activity (i.e., the frequency band most prominently linked to pulvino-cortical interactions) mediates cortico-cortical interactions in the attention network. Figure 3C shows spike-LFP phase coupling between FEF and LIP, combining all cue-responsive neurons (i.e., visual and visual-movement neurons). These results revealed no evidence of coupling between spikes in FEF and alpha/low-beta activity in LIP. In comparison, there was significant coupling between spikes in LIP and low-beta activity in FEF (permutation test, $p < 0.0009$), but that coupling occurred at a higher frequency than coupling between mdPul and either of the two cortical regions (Fig. 3C).

To further investigate whether alpha/low-beta activity shapes interactions between FEF and LIP, we also used a second, broader measure of spiking activity at the population level. That is, we measured between-region phase-amplitude coupling (PAC), specifically investigating links between alpha/low-beta phase and high-frequency band activity (HFB; 80–200 Hz). HFB is an established proxy for population spiking³⁹. Unlike our analysis of spike-LFP phase coupling (Fig.

3)—which examined the responses of single neurons identified as having task-related increases in spiking activity—the present analysis (i.e., with HFB) examined summed responses from the entire population of neurons near the recording electrode. Figure S4 displays the results, suggesting that cortico-cortical interactions between FEF and LIP indeed occur in windows defined by alpha/low-beta activity (see also Saalman, et al. ¹⁵).

To evaluate the directionality of functional connectivity in the attention network, we then calculated Granger causality, estimating the influences of alpha/low-beta activity in mdPul on FEF and LIP (relative to the influences of FEF and LIP on mdPul). Granger causal influences were generally stronger from mdPul to both cortical regions than vice versa (Fig. 4A; permutation test, $p < 0.001$). There was also an alpha/low-beta peak (at 14 Hz) in Granger causal influence from LIP to FEF. The magnitude of that peak, however, suggests that LIP had a weaker influence on FEF than did mdPul. Figure S5 displays conditional Granger causality, which was based on a subset of recording sessions when response fields were aligned across all three ROIs. Conditional Granger causality estimates the influence of one region (X) on another (Y), while accounting for the influence of a third region (Z). The general pattern of results did not change when considering all three ROIs simultaneously rather than in pairs (Fig. 4A). Granger causal influence therefore corroborates our previous interpretation of spike-LFP phase coupling. That is, mdPul regulates alpha/low-beta activity in cortical hubs of the attention network (Figs. 3, 4, S5).

Theta-dependent changes in pulvino-cortical interactions define functional dissociations

We have thus far shown that theta-band activity in mdPul—like in FEF and LIP ⁴—is associated with alternating periods of either enhanced or diminished perceptual sensitivity (i.e., theta-rhythmic sampling), with increased alpha/low-beta activity in mdPul specifically linked to

periods of enhanced perceptual sensitivity (Figs. 2, S3). We have also shown that mdPul regulates alpha/low-beta activity in cortical hubs of the attention network (Figs. 3, 4). We next examined whether pulvino-cortical interactions differed between (i) the theta-dependent attentional state associated with better visual-target detection (i.e., during the “good” theta phase) or (ii) the theta-dependent state associated with relatively worse visual-target detection (i.e., during the “poor” theta phase). We therefore re-calculated each of our between-region measures (i.e., spike-LFP phase coupling and Granger causality) after first binning trials based on theta phase, with one bin centered on the “good” theta phase and the other centered on the “poor” theta phase. The results consistently point to a functional dissociation between mdPul and LIP.

Figure 5A shows spike-LFP phase coupling between mdPul and LIP as a function of theta phase (at 5 Hz). Coupling between spikes and alpha/low-beta activity was generally dependent on theta phase (permutation test, $p < 0.001$), regardless of directionality (i.e., spikes in mdPul coupled to phase in LIP and vice versa). However, the present results demonstrate that spikes in mdPul were specifically coupled to alpha/low-beta activity (12–18 Hz) in LIP during the “good” theta phase, consistent with mdPul driving alpha/low-beta activity during periods of relatively better visual-target detection. Figure S6 provides evidence that spikes in mdPul were similarly coupled to alpha/low-beta activity in FEF during the “good” theta phase. In comparison, spikes in LIP were coupled to alpha/low-beta activity (14–24 Hz) in mdPul during the “poor” theta phase (Fig. 5A), suggesting that LIP drives alpha/low-beta activity during periods of relatively worse visual-target detection.

We previously demonstrated coupling between theta phase and alpha-low/beta power in both mdPul and LIP (Fig. S3). Because the reliability of phase estimates improves at higher power, changes in alpha/low-beta power as a function of theta phase (i.e., PAC) could create

spurious relationships between spike-LFP phase coupling (in the alpha/low-beta range) and theta phase. We therefore conducted a control analysis, equating both the number of trials and alpha/low-beta power across theta-phase bins (see online Methods). This stratification procedure did not change the results (Fig. 5B), confirming that the apparent directionality of connectivity between mdPul and LIP shifts with theta phase.

A similar pattern of results was revealed when we examined Granger causal influence as a function of theta phase (Fig. 4B). That is, the influence of mdPul on cortical hubs of the attention network was stronger during the “good” theta phase than during the “poor” theta phase. Figure S7 shows the same results after stratification by alpha/low-beta power. These data again suggest that mdPul specifically regulates cortical activity during the theta-dependent attentional state associated with better visual-target detection (or enhanced perceptual sensitivity).

The functional role of alpha/low-beta activity in LIP and mdPul

We previously demonstrated that the attentional state associated with better visual-target detection was characterized by an increase in LIP-dominated gamma activity⁴. A large body of evidence has linked such increases in cortical gamma to enhanced sensory processing⁴⁰. Here, we investigated whether gamma power in LIP was dependent on the phase of alpha/low-beta activity during either of the theta-dependent attentional states. That is, we examined whether the primary frequency band for pulvino-cortical interactions (i.e., alpha/low-beta) influenced a frequency band previously associated with attention-related effects in LIP (i.e., gamma).

Figure 6A–B shows significant PAC between alpha/low-beta phase (at 15–18 Hz) and gamma power in LIP (28–49 Hz), occurring exclusively during periods of disengagement at the

cued location (permutation test, $p < 0.001$). We previously reported that these periods of disengagement (i.e., the “poor” theta phase) were associated with lower overall gamma power in LIP (i.e., relative to periods of engagement at the cued location)⁴. Combined across the two studies, our findings suggest that alpha/low-beta activity disrupts gamma synchronization during periods of relatively worse visual-target detection (i.e., periods of disengagement), perhaps leading to lower overall gamma power during these periods (see Fiebelkorn, et al.⁴, Fig. 4).

We also measured significant PAC between alpha/low-beta phase and gamma power when receptive/response fields overlapped the non-cued location (Fig. 6A–B), occurring regardless of the theta-dependent attentional state (permutation test, $p < 0.001$). Alpha/low-beta activity in cortex has been repeatedly linked to the suppression of sensory processing⁴¹. The present results (at both the cued and the non-cued location) are therefore consistent with a gating by inhibition hypothesis, whereby alpha/low-beta activity in LIP provides pulsed inhibition of sensory processing⁴².

In comparison, we did not observe significant PAC between alpha/low-beta phase and gamma power in mdPul during either of the theta-dependent attentional states (Fig. 6C–D). These differences between mdPul and LIP in local PAC—as well as previously described links to opposite theta-dependent attentional states (Figs. 3, 5, S3)—suggest that alpha/low-beta activity has different functional roles in mdPul and LIP. Below we further discuss this apparent functional dissociation between mdPul-driven and LIP-driven alpha/low-beta activity (see the Discussion).

DISCUSSION

The present results are the first to functionally link mdPul with cortical hubs of the attention network. Locally, we demonstrated significantly increased spiking activity during the cue-target delay in mdPul (i.e., under conditions of spatial attention), which was similar in magnitude to that observed in LIP (Fig. 1). These electrophysiological results thus support previous findings from lesion and inactivation studies¹⁹⁻²³, indicating that mdPul plays a role in mediating spatial attention at behaviorally relevant locations. We further demonstrated increased coupling between mdPul and both FEF and LIP during spatial attention (Fig. 3), indicating that previously described anatomical connectivity between these cortical and subcortical structures²⁸⁻³⁰ serves to mediate attention-related processing. The present results thus firmly establish mdPul as a subcortical hub of the attention network. We next consider its functional role in this large-scale network.

Spatial attention samples the visual environment in theta-rhythmic cycles³⁻⁸. We previously demonstrated that these theta-rhythmic cycles are seemingly shaped by the phase of theta oscillations in frontal and parietal cortices^{4,5}. Here, we demonstrate that theta activity in mdPul is similarly associated with alternating periods of either enhanced or diminished perceptual sensitivity (Fig. 2). That is, theta oscillations organize neural activity in both cortical and subcortical hubs of the attention network into two rhythmically alternating attentional states. We propose that these attentional states alternately promote either (i) engagement at the presently attended location (and therefore enhanced perceptual sensitivity) or (ii) relative disengagement (and therefore diminished perceptual sensitivity), in anticipation of a potential attentional shift. Periods of engagement are associated with increased alpha/low-beta activity in mdPul, while periods of relative disengagement are associated with increased alpha/low-beta activity in LIP (Figs. 2, S3).

This state-dependent shifting of alpha/low-beta activity between mdPul and LIP is indicative of a functional dissociation. Although it is broadly assumed that there is functional specialization across hubs of the attention network^{43,44}, electrophysiological evidence has been sparse. Only a few studies have simultaneously recorded from multiple hubs of the attention network. Buschman and Miller⁴⁵, for example, reported that neural activity in FEF first signaled the target location during a serial search task (i.e., a task emphasizing goal-directed attention), while neural activity in LIP first signaled the target location during a pop-out task (i.e., a task emphasizing stimulus-driven attention). Their results thus indicated that FEF and LIP have task-specific functions, with (i) FEF leading LIP during goal-directed attention and (ii) LIP leading FEF during stimulus-driven attention. The present results instead provide evidence of functional specialization during unchanging task demands (i.e., during a task that promotes sustained attention at a cued location). We not only observed a rhythmic re-weighting of alpha/low-beta power between mdPul and LIP (Fig. S3), but spike-LFP phase coupling and Granger causality also revealed a rhythmic re-weighting of functional connectivity (Figs. 4, 5). That is, the directionality of alpha/low-beta activity shifted between theta-dependent attentional states, with (i) mdPul regulating cortical activity during periods of engagement at the attended location (i.e., during the “good” theta phase) and (ii) LIP regulating thalamic activity during periods of relative disengagement (i.e., during the “poor” theta phase). These proposed functional roles for mdPul (i.e., engagement) and LIP (i.e., disengagement) mirror those first suggested by Posner and Petersen⁴³, largely based on data from human lesion studies.

Interactions between higher-order cortical regions and mdPul occurred almost exclusively in the alpha/low-beta band, which is typically linked to functional inhibition⁴¹. Both parietal cortex and the thalamus have been proposed as primary alpha/low-beta generators^{15,46,47}. A recent study in human epilepsy patients investigated the source of alpha rhythms (7–13

Hz) during quiet wakefulness, recording from both posterior cortex and the pulvinar⁴⁶. Halgren, et al.⁴⁶ reported that alpha in higher-order cortical regions (i) propagates to visual-sensory cortices and (ii) leads alpha in the pulvinar. Their results thus support a cortical source of alpha rhythms. In comparison, Saalman, et al.¹⁵ reported that alpha (8–15 Hz) in the ventral pulvinar leads alpha in visual-sensory cortices, specifically under conditions of spatial attention. Their results thus support a thalamic source of alpha rhythms. The present findings, on the other hand, indicate that the source of alpha/low-beta activity dynamically shifts between mdPul (i.e., thalamus) and LIP (i.e., cortex). That is, the source of alpha/low-beta rhythms is state-dependent (Figs. 4, 5), potentially explaining the conflicting results of the previously described studies^{15,46}. We next consider whether the function of alpha/low-beta rhythms in the attention network is the same regardless of the source (i.e., mdPul vs. LIP) and the theta-dependent attentional state (i.e., engagement vs. disengagement).

Electrophysiological studies in both humans and monkeys have repeatedly demonstrated that increased alpha/low-beta activity is a signature of suppressed processing in sensory cortex^{41,42,48}. That is, these studies show increased alpha/low-beta power in cortical regions processing task-irrelevant information⁴¹. For example, Worden, et al.⁴⁹, who recorded electroencephalographic (EEG) data from humans during a spatial cueing task, reported increased alpha power (8–14 Hz) over occipital cortex contralateral to the to-be-ignored hemifield (i.e., over cortex processing a task-irrelevant location). In agreement with this interpretation, we have proposed that increased alpha/low-beta power in LIP during periods of disengagement (i.e., during the “poor” theta phase) is associated with the suppression of sensory processing⁴. That is, we proposed that periodic increases in alpha power disrupt neural activity associated with processing at the presently attended location (Fig. 6A–B). This rhythmic

re-weighting creates windows of opportunity when it is easier for an attentional shift to occur, if warranted by behavioral goals and the visual environment (e.g., stimulus salience).

While the suppressive role of alpha/low-beta activity in sensory cortex is well established, only a few studies have measured alpha/low-beta activity in the pulvinar^{15,16,46}. During periods of engagement at the attended location (i.e., during the “good” theta phase), we observed both (i) increased alpha/low-beta power in mdPul and (ii) increased pulvino-cortical influence, also occurring in alpha/low-beta (Figs. 4, 5). Saalmann, et al.¹⁵ provided evidence that pulvino-cortical coordination in alpha/low-beta facilitates communication between regions of visual cortex (i.e., V4 and TEO) during spatial attention. Those results similarly demonstrated (i) stronger pulvino-cortical spike-LFP phase coupling and (ii) stronger pulvino-cortical Granger causal influence. Our results therefore indicate that mdPul plays a similar role in the attention network, coordinating alpha/low-beta activity in FEF and LIP (Figs. 3, S4). Notably, this coordination specifically occurs during the attentional state associated with engagement at the attended location (i.e., during the “good” theta phase), when alpha/low-beta power is relatively low in LIP (Fig. S3).

It remains unclear whether the increase in alpha/low-beta power in mdPul during periods of engagement is associated with functional inhibition (i.e., the functional role typically attributed to alpha/low-beta in cortex). For example, this increase in alpha/low-beta power might be associated with a gating of indirect pathways (i.e., cortico-pulvino-cortical), emphasizing direct pathways (i.e., cortico-cortical) during periods of enhanced sensory processing (i.e., during the “good” theta phase). This hypothesis, however, conflicts with observed increases in pulvino-cortical influence during periods of engagement (Figs. 4, 5). We therefore propose that alpha/low-beta activity in mdPul is associated with a different function than alpha/low-beta activity in cortex. As further support for this proposal, Bollimunta, et al.⁵⁰

previously described two cortical alpha generators, with opposite relationships to behavioral performance. For early visual cortices (i.e., V2 and V4), the primary alpha pacemaker was localized in the infragranular layer, and higher alpha power was associated with worse behavioral performance. For inferior temporal (IT) cortex, the primary alpha pacemaker was instead localized in the supragranular layer, and higher alpha power was associated with better behavioral performance. These results thus provide evidence that alpha/low-beta activity can reflect different functions in different brain regions, as here proposed for mdPul and LIP.

Future studies will need to investigate the specific mechanisms through which increased alpha/low-beta activity in mdPul is associated with both (i) decreased alpha/low-beta activity in LIP and (ii) increased alpha/low-beta synchronization in FEF and LIP. That is, future studies should examine whether increased alpha/low-beta activity in mdPul plays a direct role in reducing alpha/low-beta power in LIP (and vice versa). Zhou, et al.¹⁶, for example, demonstrated that inactivating the ventral pulvinar increased the power of low-frequency oscillations in visual cortical regions, suggesting that normal pulvinar function (i.e., without inactivation) reduces low-frequency power. The pulvinar might therefore facilitate cortico-cortical communication by both synchronizing and reducing cortical alpha/low-beta activity.

The present findings demonstrate that theta-rhythmic sampling during spatial attention is characterized by changes in thalamo-cortical interactions. Theta-dependent shifts in alpha/low-beta activity reflect a functional re-weighting of the attention network, with (i) mdPul dominating alpha/low-beta activity during periods of engagement (and therefore enhanced perceptual sensitivity) and (ii) LIP dominating alpha/low-beta activity during periods of relative disengagement (and therefore diminished perceptual sensitivity). We propose that these state-dependent shifts in alpha/low-beta activity alternately favor brain regions and pathways associated with either (i) sampling at the presently attended location or (ii) shifting to another

location. Theta rhythms thus seem to coordinate different functions of the attention network by shaping its spatiotemporal structure. Low-frequency oscillations might play a similar role in other large-scale networks, temporally resolving functional conflicts that arise, for example, from competing sensory stimuli⁵¹ or from multiple items being held in working memory⁵².

REFERENCES

- 1 Posner, M. I. Orienting of attention. *The Quarterly journal of experimental psychology* **32**, 3-25 (1980).
- 2 Moran, J. & Desimone, R. Selective attention gates visual processing in the extrastriate cortex. *Science* **229**, 782-784 (1985).
- 3 Fiebelkorn, I. C., Saalmann, Y. B. & Kastner, S. Rhythmic sampling within and between objects despite sustained attention at a cued location. *Current biology : CB* **23**, 2553-2558, doi:10.1016/j.cub.2013.10.063 (2013).
- 4 Fiebelkorn, I. C., Pinsk, M. A. & Kastner, S. A dynamic interplay within the frontoparietal network underlies rhythmic spatial attention. *Neuron* **99**, 842-853 (2018).
- 5 Helfrich, R. F. *et al.* Neural mechanisms of sustained attention are rhythmic. *Neuron* **99**, 854-865 (2018).
- 6 Landau, A. N. & Fries, P. Attention samples stimuli rhythmically. *Current biology : CB* **22**, 1000-1004, doi:10.1016/j.cub.2012.03.054 (2012).
- 7 Busch, N. A. & VanRullen, R. Spontaneous EEG oscillations reveal periodic sampling of visual attention. *Proceedings of the National Academy of Sciences of the United States of America* **107**, 16048-16053, doi:10.1073/pnas.1004801107 (2010).
- 8 VanRullen, R., Carlson, T. & Cavanagh, P. The blinking spotlight of attention. *Proceedings of the National Academy of Sciences of the United States of America* **104**, 19204-19209, doi:10.1073/pnas.0707316104 (2007).
- 9 Corbetta, M. *et al.* A common network of functional areas for attention and eye movements. *Neuron* **21**, 761-773 (1998).
- 10 Kastner, S. & Ungerleider, L. G. Mechanisms of visual attention in the human cortex. *Annual review of neuroscience* **23**, 315-341, doi:10.1146/annurev.neuro.23.1.315 (2000).
- 11 Armstrong, K. M., Fitzgerald, J. K. & Moore, T. Changes in visual receptive fields with microstimulation of frontal cortex. *Neuron* **50**, 791-798, doi:10.1016/j.neuron.2006.05.010 (2006).
- 12 Moore, T. & Armstrong, K. M. Selective gating of visual signals by microstimulation of frontal cortex. *Nature* **421**, 370-373, doi:10.1038/nature01341 (2003).
- 13 Gregoriou, G. G., Rossi, A. F., Ungerleider, L. G. & Desimone, R. Lesions of prefrontal cortex reduce attentional modulation of neuronal responses and synchrony in V4. *Nature neuroscience* **17**, 1003-1011, doi:10.1038/nn.3742 (2014).
- 14 Halassa, M. M. & Kastner, S. Thalamic functions in distributed cognitive control. *Nature neuroscience* **20**, 1669-1679, doi:10.1038/s41593-017-0020-1 (2017).
- 15 Saalmann, Y. B., Pinsk, M. A., Wang, L., Li, X. & Kastner, S. The pulvinar regulates information transmission between cortical areas based on attention demands. *Science* **337**, 753-756, doi:10.1126/science.1223082 (2012).
- 16 Zhou, H., Schafer, R. J. & Desimone, R. Pulvinar-Cortex Interactions in Vision and Attention. *Neuron* **89**, 209-220, doi:10.1016/j.neuron.2015.11.034 (2016).
- 17 Saalmann, Y. B. & Kastner, S. Cognitive and perceptual functions of the visual thalamus. *Neuron* **71**, 209-223, doi:10.1016/j.neuron.2011.06.027 (2011).
- 18 Bridge, H., Leopold, D. A. & Bourne, J. A. Adaptive Pulvinar Circuitry Supports Visual Cognition. *Trends in cognitive sciences* **20**, 146-157, doi:10.1016/j.tics.2015.10.003 (2016).

- 19 Karnath, H. O., Himmelbach, M. & Rorden, C. The subcortical anatomy of human spatial neglect: putamen, caudate nucleus and pulvinar. *Brain : a journal of neurology* **125**, 350-360 (2002).
- 20 Petersen, S. E., Robinson, D. L. & Morris, J. D. Contributions of the pulvinar to visual spatial attention. *Neuropsychologia* **25**, 97-105 (1987).
- 21 Danziger, S., Ward, R., Owen, V. & Rafal, R. Contributions of the human pulvinar to linking vision and action. *Cognitive, affective & behavioral neuroscience* **4**, 89-99 (2004).
- 22 Snow, J. C., Allen, H. A., Rafal, R. D. & Humphreys, G. W. Impaired attentional selection following lesions to human pulvinar: evidence for homology between human and monkey. *Proceedings of the National Academy of Sciences of the United States of America* **106**, 4054-4059, doi:10.1073/pnas.0810086106 (2009).
- 23 Wilke, M., Turchi, J., Smith, K., Mishkin, M. & Leopold, D. A. Pulvinar inactivation disrupts selection of movement plans. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **30**, 8650-8659, doi:10.1523/JNEUROSCI.0953-10.2010 (2010).
- 24 Adams, M. M., Hof, P. R., Gattass, R., Webster, M. J. & Ungerleider, L. G. Visual cortical projections and chemoarchitecture of macaque monkey pulvinar. *The Journal of comparative neurology* **419**, 377-393 (2000).
- 25 Arcaro, M. J., Pinsk, M. A. & Kastner, S. The Anatomical and Functional Organization of the Human Visual Pulvinar. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **35**, 9848-9871, doi:10.1523/JNEUROSCI.1575-14.2015 (2015).
- 26 Gattass, R., Galkin, T. W., Desimone, R. & Ungerleider, L. G. Subcortical connections of area V4 in the macaque. *The Journal of comparative neurology* **522**, 1941-1965, doi:10.1002/cne.23513 (2014).
- 27 Weller, R. E., Steele, G. E. & Kaas, J. H. Pulvinar and other subcortical connections of dorsolateral visual cortex in monkeys. *The Journal of comparative neurology* **450**, 215-240, doi:10.1002/cne.10298 (2002).
- 28 Gutierrez, C., Cola, M. G., Seltzer, B. & Cusick, C. Neurochemical and connectional organization of the dorsal pulvinar complex in monkeys. *The Journal of comparative neurology* **419**, 61-86 (2000).
- 29 Romanski, L. M., Giguere, M., Bates, J. F. & Goldman-Rakic, P. S. Topographic organization of medial pulvinar connections with the prefrontal cortex in the rhesus monkey. *The Journal of comparative neurology* **379**, 313-332 (1997).
- 30 Selemon, L. D. & Goldman-Rakic, P. S. Common cortical and subcortical targets of the dorsolateral prefrontal and posterior parietal cortices in the rhesus monkey: evidence for a distributed neural network subserving spatially guided behavior. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **8**, 4049-4068 (1988).
- 31 Petersen, S. E., Robinson, D. L. & Keys, W. Pulvinar nuclei of the behaving rhesus monkey: visual responses and their modulation. *Journal of neurophysiology* **54**, 867-886, doi:10.1152/jn.1985.54.4.867 (1985).
- 32 Bender, D. B. & Youakim, M. Effect of attentive fixation in macaque thalamus and cortex. *Journal of neurophysiology* **85**, 219-234, doi:10.1152/jn.2001.85.1.219 (2001).
- 33 Squire, R. F., Noudoost, B., Schafer, R. J. & Moore, T. Prefrontal contributions to visual selective attention. *Annual review of neuroscience* **36**, 451-466, doi:10.1146/annurev-neuro-062111-150439 (2013).
- 34 Bisley, J. W. & Goldberg, M. E. Attention, intention, and priority in the parietal lobe. *Annual review of neuroscience* **33**, 1-21, doi:10.1146/annurev-neuro-060909-152823 (2010).

- 35 Egly, R., Driver, J. & Rafal, R. D. Shifting visual attention between objects and locations: evidence from normal and parietal lesion subjects. *Journal of experimental psychology. General* **123**, 161-177 (1994).
- 36 Gregoriou, G. G., Gotts, S. J. & Desimone, R. Cell-type-specific synchronization of neural activity in FEF with V4 during attention. *Neuron* **73**, 581-594, doi:10.1016/j.neuron.2011.12.019 (2012).
- 37 Thompson, K. G., Biscoe, K. L. & Sato, T. R. Neuronal basis of covert spatial attention in the frontal eye field. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **25**, 9479-9487, doi:10.1523/JNEUROSCI.0741-05.2005 (2005).
- 38 Pesaran, B. Neural correlations, decisions, and actions. *Current opinion in neurobiology* **20**, 166-171, doi:10.1016/j.conb.2010.03.003 (2010).
- 39 Ray, S. & Maunsell, J. H. Different origins of gamma rhythm and high-gamma activity in macaque visual cortex. *PLoS biology* **9**, e1000610, doi:10.1371/journal.pbio.1000610 (2011).
- 40 Fries, P. Neuronal gamma-band synchronization as a fundamental process in cortical computation. *Annual review of neuroscience* **32**, 209-224, doi:10.1146/annurev.neuro.051508.135603 (2009).
- 41 Foxe, J. J. & Snyder, A. C. The Role of Alpha-Band Brain Oscillations as a Sensory Suppression Mechanism during Selective Attention. *Frontiers in psychology* **2**, 154, doi:10.3389/fpsyg.2011.00154 (2011).
- 42 Jensen, O. & Mazaheri, A. Shaping functional architecture by oscillatory alpha activity: gating by inhibition. *Frontiers in human neuroscience* **4**, 186, doi:10.3389/fnhum.2010.00186 (2010).
- 43 Posner, M. I. & Petersen, S. E. The attention system of the human brain. *Annual review of neuroscience* **13**, 25-42, doi:10.1146/annurev.ne.13.030190.000325 (1990).
- 44 Corbetta, M. & Shulman, G. L. Control of goal-directed and stimulus-driven attention in the brain. *Nature reviews. Neuroscience* **3**, 201-215, doi:10.1038/nrn755 (2002).
- 45 Buschman, T. J. & Miller, E. K. Top-down versus bottom-up control of attention in the prefrontal and posterior parietal cortices. *Science* **315**, 1860-1862, doi:10.1126/science.1138071 (2007).
- 46 Halgren, M. *et al.* The Generation and Propagation of the Human Alpha Rhythm. *bioRxiv* (2017).
- 47 Vijayan, S. & Kopell, N. J. Thalamic model of awake alpha oscillations and implications for stimulus processing. *Proceedings of the National Academy of Sciences of the United States of America* **109**, 18553-18558, doi:10.1073/pnas.1215385109 (2012).
- 48 Haegens, S., Nacher, V., Luna, R., Romo, R. & Jensen, O. alpha-Oscillations in the monkey sensorimotor network influence discrimination performance by rhythmical inhibition of neuronal spiking. *Proceedings of the National Academy of Sciences of the United States of America* **108**, 19377-19382, doi:10.1073/pnas.1117190108 (2011).
- 49 Worden, M. S., Foxe, J. J., Wang, N. & Simpson, G. V. Anticipatory biasing of visuospatial attention indexed by retinotopically specific alpha-band electroencephalography increases over occipital cortex. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **20**, RC63 (2000).
- 50 Bollimunta, A., Chen, Y., Schroeder, C. E. & Ding, M. Neuronal mechanisms of cortical alpha oscillations in awake-behaving macaques. *The Journal of neuroscience : the official journal of the Society for Neuroscience* **28**, 9976-9988, doi:10.1523/JNEUROSCI.2699-08.2008 (2008).

- 51 Caruso, V. C. *et al.* Single neurons may encode simultaneous stimuli by switching between activity patterns. *Nature communications* **9**, 2715, doi:10.1038/s41467-018-05121-8 (2018).
- 52 Peters, B., Rahm, B., Kaiser, J. & Bledowski, C. Attention samples objects held in working memory at a theta rhythm. *bioRxiv* **369652**, doi:<https://doi.org/10.1101/369652> (2018).

FIGURES:

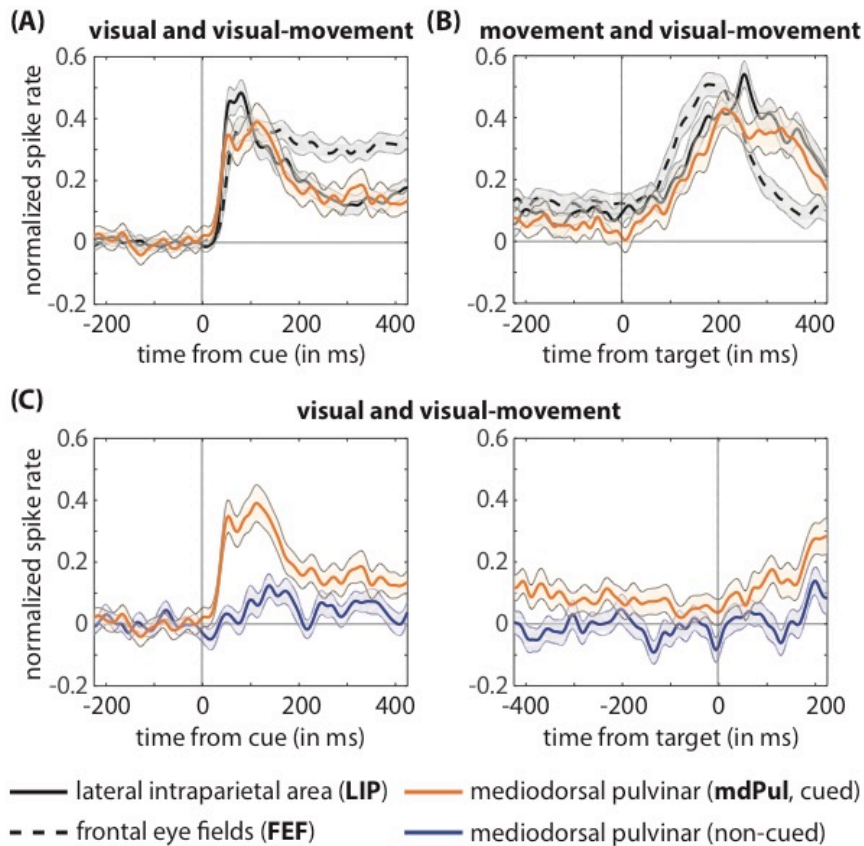


Figure 1. *mdPul* contributes to the maintenance of spatial attention at a cued location. **(A)** Normalized, cue-locked spike rates, averaged across the population of neurons with significantly increased visual-sensory responses (i.e., visual and visual-movement neurons) when receptive fields overlapped the cued location. **(B)** Normalized, target-locked spike rates, averaged across the population of neurons with significantly increased movement responses (i.e., movement and visual-movement neurons) when receptive fields overlapped the cued location. **(C)** Normalized spike rates in *mdPul*, time-locked to either the cue (left) or the target (right), both when receptive fields overlapped the cued location (orange) and when receptive fields overlapped the non-cued location (blue). These plots are averaged across all *mdPul* neurons with a significantly increased visual-sensory response (i.e., visual and visual-movement neurons). Shaded regions around the lines represent SEs.

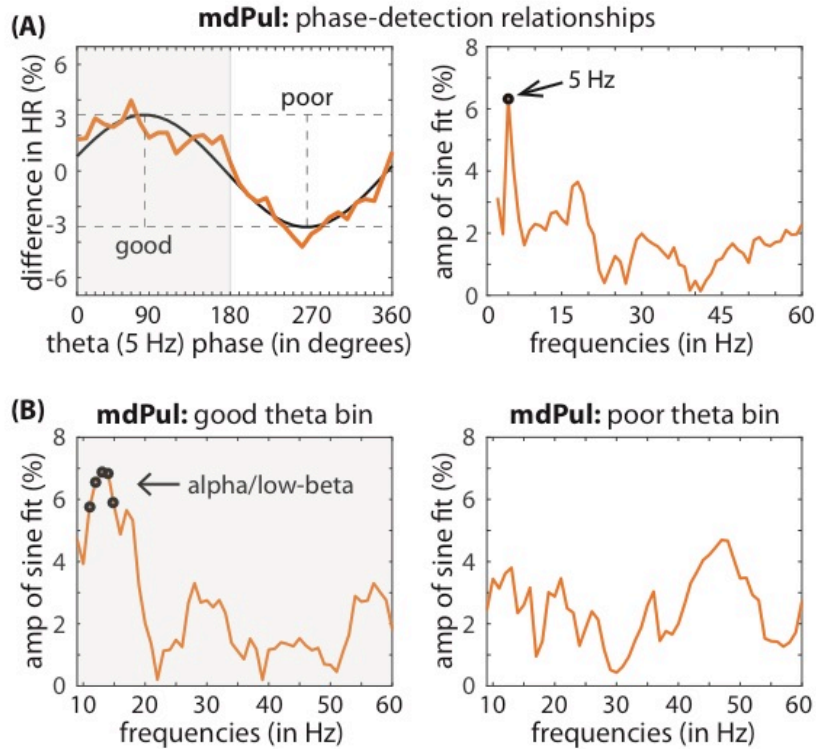


Figure 2. The phase of low-frequency oscillatory activity in mdPul is linked to the likelihood of detecting a low-contrast visual target. Hit rates (HRs) were calculated (across recording sessions, $N = 95$) as a function of oscillatory phase when response fields overlapped the cued location. **(A)** Phase-detection functions were then fit with one-cycle sine waves (left), with the amplitude of that sine wave representing the strength of the relationship between visual-target detection and oscillatory phase. These phase-detection relationships were calculated at different frequencies, from 3–60 Hz (right). Phase-detection relationships at higher frequencies (in FEF and LIP) were previously shown to be dependent on the phase of theta-band rhythms⁴. **(B)** Phase-detection relationships in mdPul were therefore re-calculated after first binning trials into two theta-phase bins: (i) one centered on the theta phase associated with better visual-target detection (i.e., the “good” bin), and (ii) one centered on the theta phase associated with worse visual-target detection (i.e., the “poor” bin). The black dots represent statistically significant results after corrections for multiple comparisons.

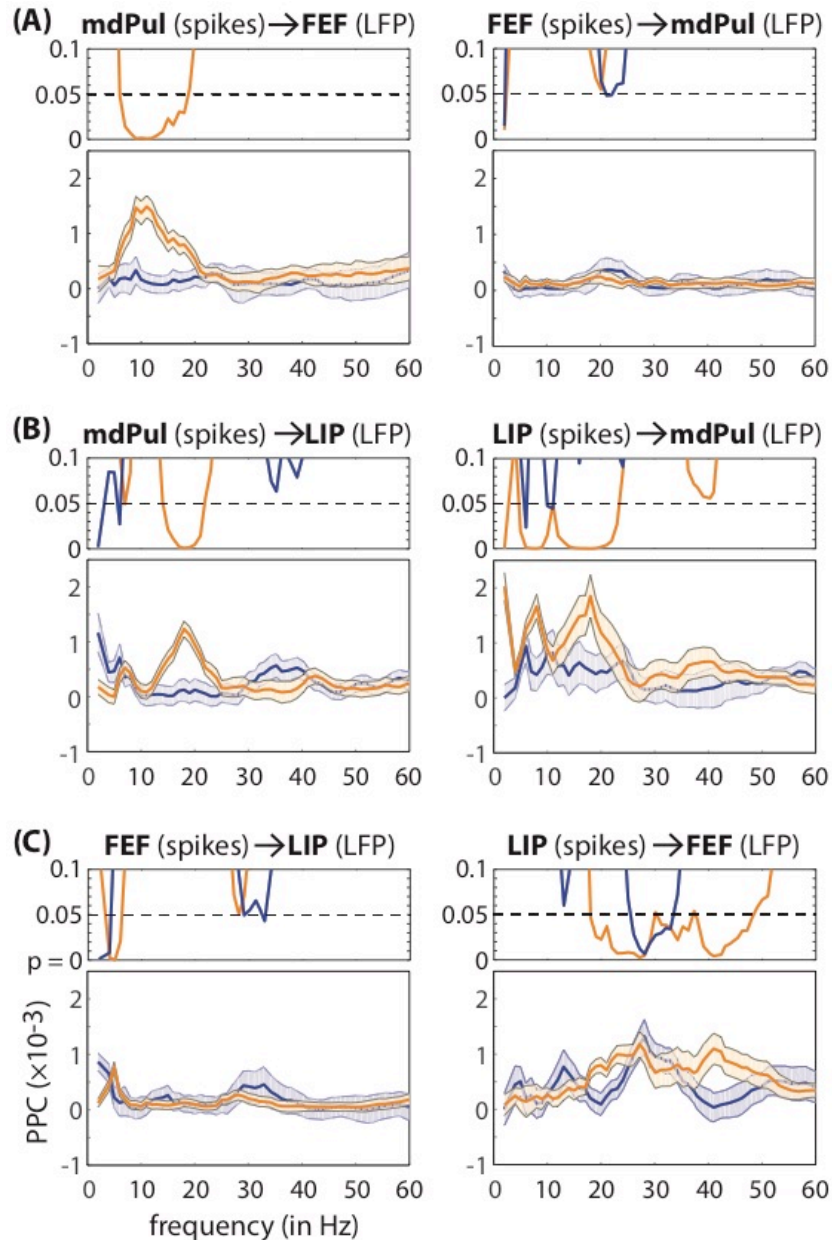


Figure 3. Spike-LFP phase coupling demonstrates increased functional connectivity between *mdPul* and cortical hubs of the attention network (i.e., *FEF* and *LIP*) during spatial attention. The top panel of each plot shows p-values, indicating whether spike-LFP phase coupling is statistically significant for each condition, cued (orange) or non-cued (blue). The bottom panel compares spike-LFP phase coupling between the two conditions (cued vs. non-cued). **(A)** Examines spike-LFP phase coupling between *mdPul* and *FEF*, **(B)** examines spike-LFP phase coupling between *mdPul* and *LIP*, and **(C)** examines spike-LFP phase coupling between *FEF* and *LIP*. These plots are based on data from all task-responsive neurons (see Table S1). Shaded regions around the lines represent SEs.

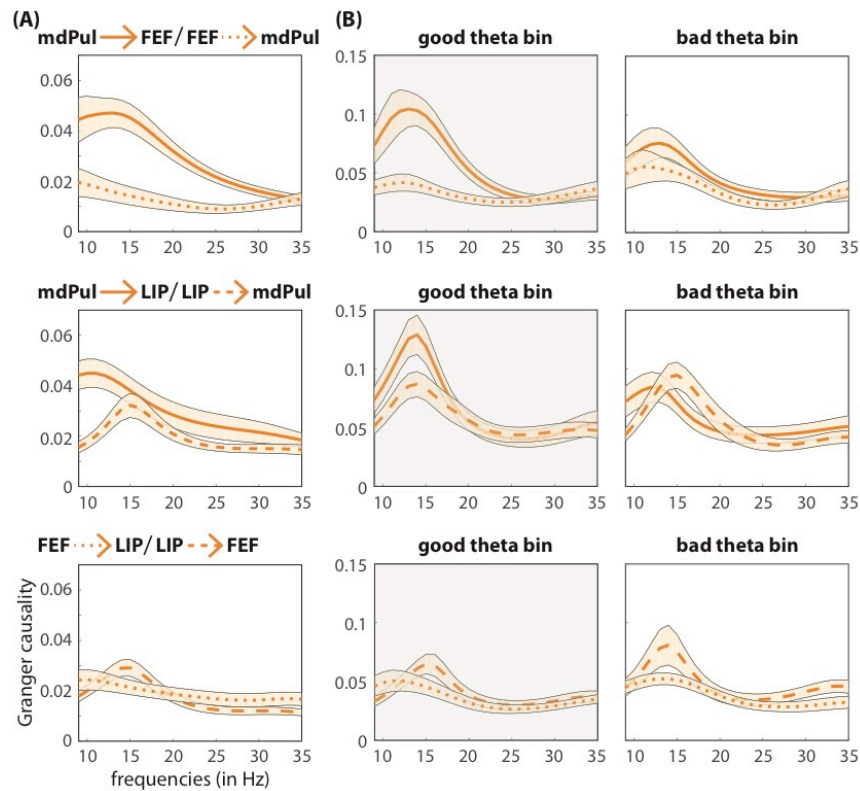


Figure 4. Granger causal influence indicates that mdPul regulates alpha/low-beta activity in cortical hubs of the attention network (i.e., FEF and LIP). **(A)** For each pair of ROIs, Granger causal influence (model order = 8) was based on all recording sessions with overlapping response fields (mdPul vs. FEF, N = 51; mdPul vs. LIP, N = 57; FEF vs. LIP, N = 67). Figure S4 instead shows conditional Granger causality for a subset of sessions when all 3 ROIs had overlapping response fields (N = 31). **(B)** Shows Granger causal influence after binning based on theta phase (“good” vs. “poor”). mdPul specifically regulates cortical activity during periods of relatively better visual-target detection (i.e., during the “good” theta phase). Shaded regions around the lines represent SEs.

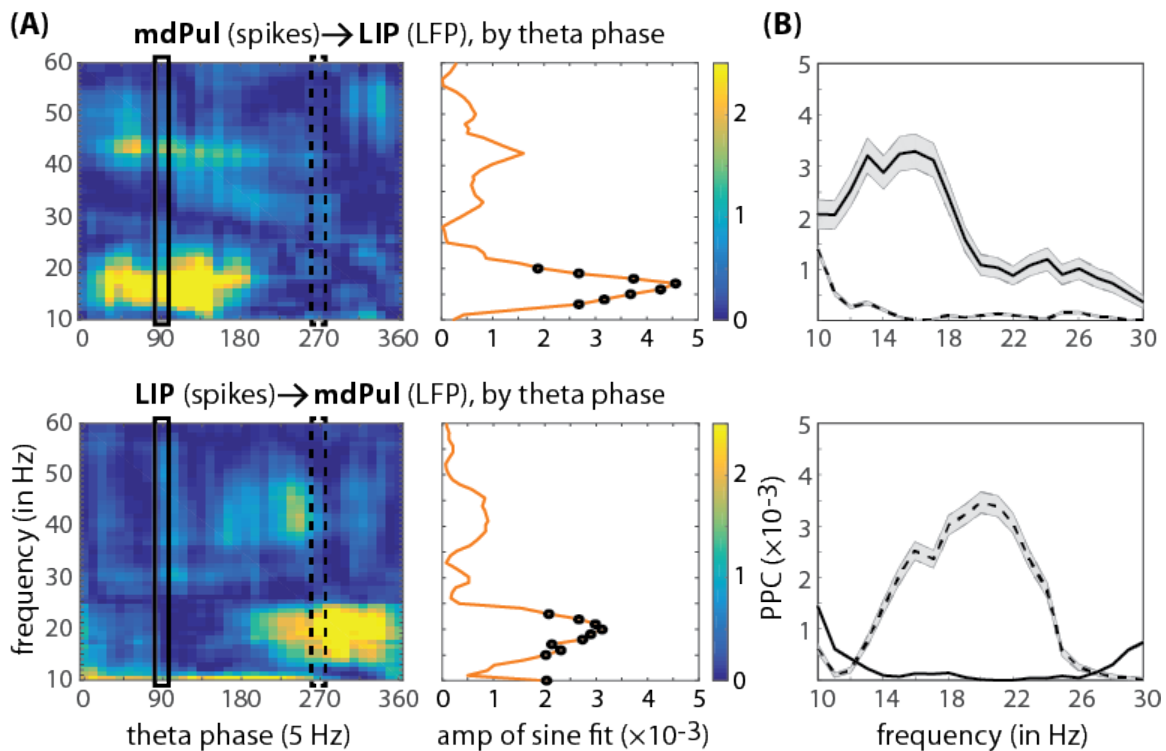


Figure 5. Spike-LFP phase coupling between mdPul and LIP as a function of theta phase. **(A)** Spike-LFP phase coupling (from 9–60 Hz) was calculated in overlapping theta-phase bins (on left), using step sizes of 10 degrees. The resulting functions were then fit with one-cycle sine waves. The amplitude of these sine waves provided a measure of how strongly spike-LFP phase coupling was modulated by the phase of theta rhythms (on right, see Fig. 2A for depiction of a similar approach). The black dots represent statistically significant results after corrections for multiple comparisons. **(B)** To control for potentially spurious results from theta-dependent changes in alpha/low-beta power (i.e., PAC; see Fig. S3), a stratification procedure was used to equate trials numbers and alpha/low-beta power between two theta-phase bins, centered on either 90 or 270 degrees (outlined in plots on far left). Because this stratification process involves downsampling trials and therefore different results on each run, it was re-run 1500 times. The above plots **(B)** represent the means and standard deviations (shaded regions around the lines) of those power-equating iterations.

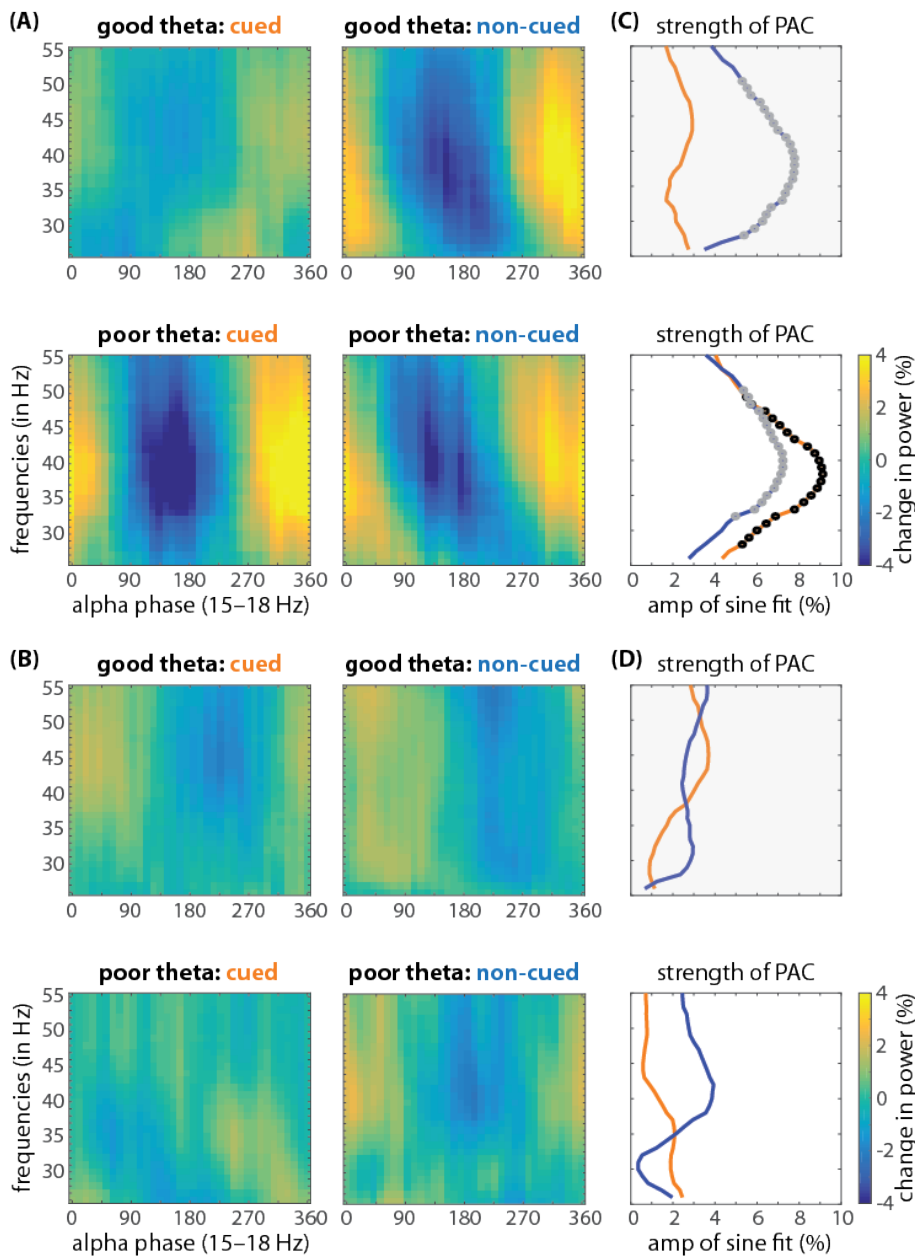


Figure 6. PAC in LIP between alpha/low-beta phase and gamma power is state-dependent when response fields overlap the cued location (i.e., under conditions of spatial attention). We measured phase amplitude coupling after first binning trials based on theta phase, with one bin centered on the “good” theta phase (i.e., the phase associated with better visual-target detection) and the other centered on the “bad” theta phase (i.e., the phase associated with worse visual-target detection). **(A, B)** Shows power as a function of alpha/low-beta phase by theta-phase bin (good vs. poor) and by attention condition (cued [orange] vs. non-cued [blue]), for both **(A)** LIP (N = 96) and **(B)** mdPul (N = 95). **(C, D)** The strength of PAC was measured by using the fast Fourier transform to extract the amplitude of a one-cycle, sinusoidal component (see Fig. 2A for an illustration of this approach), for both **(C)** LIP and **(D)** mdPul. The black (cued location) and gray (uncued location) dots represent statistically significant results after corrections for multiple comparisons.

METHODS

Subjects

The study used two male *Macaca fascicularis* monkeys (6–9 years old). The Princeton University Animal Care and Use Committee approved all procedures, which conformed to the National Institutes of Health guidelines for the humane care and use of laboratory animals.

Data from the two animals were qualitatively similar, so we combined them for all analyses. See Fiebelkorn, et al. ¹ for a supplemental figure illustrating common behavioral and electrophysiological effects between the two animals. Both monkeys demonstrated significantly better visual-target detection at the cued location, significantly increased spiking activity during the cue-target delay, significant theta-band rhythmicity in their behavioral data, and statistically significant phase-amplitude coupling.

Behavioral Task

We trained the monkeys to perform a variant of the Egly-Driver task ², using Presentation software to control stimuli, monitor responses, and trigger reward delivery. See Fiebelkorn, et al. ¹ for an illustration of the task. An auditory “go” tone indicated the beginning of each trial. The monkeys initiated the trial sequence by depressing and holding down a lever. At trial onset, a fixation square (0.5°) appeared at the center of the monitor (eye-monitor distance = 57 cm). After a variable delay of 500–1200 ms, two-bar shaped objects (22° x 4.4°) appeared. These bars were presented either to the left and right of central fixation (vertically oriented) or above and below central fixation (horizontally oriented), with equal probability. The closest edge of each bar was 6.6° from central fixation. After a second variable delay of 500–1200 ms, a spatial cue briefly appeared (100 ms), surrounding the end of one of the bar-shaped objects. This cue indicated where a subsequent visual target was most likely to occur (with 78%

cue validity). After a third variable delay (i.e., the cue-target delay) of 300–1600 ms, a low-contrast (2.5–4%) target briefly appeared (100 ms) at the end of one of the bar-shaped objects. The closest corner of the target ($4.4^\circ \times 4.4^\circ$) was 9.4° from central fixation. If the target was not presented at the cued location, it could instead appear at one of the two equidistant, uncued locations (12% of all trials), split evenly between the uncued location on the same object as the cued location (i.e., the same-object location) and the uncued location on the second object (i.e., the different-object location). For the present manuscript, all of our analyses are focused on either the cued location (i.e., the attended condition) or the different-object location (i.e., our baseline condition). The monkeys released the lever when they detected a target, receiving a juice reward for correct responses (150 to 650 ms after the target). On 10% of trials, no visual target occurred following the spatial cue (i.e., catch trials). The monkeys instead released the lever when the screen cleared, 1600 ms after the cue. We monitored eye position using an infrared eye tracker (either an Eye-trac 6 at 240 Hz (Applied Science Laboratories Inc., Bedford MA) or an EyeLink 1000 Plus at 1000 Hz (SR Research Ltd., Ottawa CAN), and trials were aborted if eye position deviated by more than one degree from central fixation (i.e., if the monkey broke fixation). Visual stimuli appeared on a 21-inch CRT monitor set at a refresh rate of 100 Hz, and we verified stimulus timing using a customized photodiode system.

Electrophysiology

All surgical procedures were performed under general anesthesia with isoflurane (induction 2–5%, maintenance 0.5–2.5%) and under strictly aseptic conditions. We used titanium skull screws and bone cement to affix head implants and two customized plastic recording chambers (one frontal and one parietal) to the animals. After recordings in the left hemisphere, the chambers were moved to the right hemisphere for additional recordings.

Craniotomies (4.5 mm diameter) provided access to our regions of interest (ROIs). We fitted each craniotomy with a conical plastic-guide tube filled with bone wax³. These wax-filled guide tubes held glass-coated platinum-iridium electrodes (impedance: 5 M Ω) in place between recording sessions. Each recording session spanned a few hours, with up to seven sessions per week.

During recordings, we stabilized the animal's head using four thin rods that slid into hollows in the side of the implants. We independently lowered electrodes with microdrives (NAN Instruments Ltd., Nazaret Illit ISR) coupled to an adapter system that allowed different approach angles for each ROI. Electrode signals (40,000 Hz sample rate for spikes; 1,000 Hz sample rate for LFPs) were amplified and filtered (150–8,000 Hz for spikes; 0.7–300 Hz for LFPs) using a Plexon preamplifier (Plexon Inc., Dallas TX) with a high input impedance headstage and Multichannel Acquisition Processor (MAP) controlled by RASPUTIN software.

Prior to experimental recordings, we simultaneously recorded neural signals from three skull screws, one in each chamber and one placed over the opposite hemisphere (i.e., outside the chambers). We alternated across control recording sessions, using each skull screw as the reference electrode. After verifying the absence of visual and attention-related responses, we selected the skull screw placed over the opposite hemisphere as the reference electrode for all experimental recording sessions.

During recordings, we sorted spikes online to isolate neurons, then we re-sorted spikes for offline analyses using Plexon Offline Sorter software. The Egly-Driver task has four target locations, one in each quadrant. We used a quadrant-mapping task (i.e., large Gabor stimuli flashed in each quadrant), the spatial cue, and the target to determine the quadrant where individual neurons and LFPs had their strongest responses.

Here, we present data from 95 recording sessions in the mediodorsal pulvinar (mdPul; monkey L, N = 55, monkey R, N = 40). We also simultaneously recorded from FEF and LIP. There were 51 recording sessions when mdPul and FEF had their strongest responses to stimuli in the same visual quadrant, 58 recording sessions when mdPul and LIP had their strongest responses in the same visual quadrant, and 67 recording sessions when FEF and LIP had their strongest responses to stimuli within the same visual quadrant (i.e., aligned RFs and/or multi-unit RFs). We used these recording sessions for between-region analyses. There were 31 recording sessions when all three ROIs had their strongest responses to stimuli within the same visual quadrant. We used these recording sessions to confirm that our between-region analyses of Granger causality were still valid when accounting for the influence of the third region (i.e., conditional Granger causality). Across all recording sessions, we isolated 52 neurons in mdPul, 98 neurons in FEF, and 98 neurons in LIP that had significantly increased spike rates in response to the cue, the target, or both the cue and the target.

Acquisition of MR Images for Electrode Positioning

The animals were sedated with ketamine (1-10mg/kg i.m.) and xylazine (1-2 mg/kg i.m.), and provided with atropine (0.04 mg/kg i.m.). Sedation was maintained with tiletamine/zolazepam (1-5mg/kg i.m.). We then placed the animals in an MR-compatible stereotaxic frame (1530M; David Kopf Instruments, Tujunga CA) and monitored vital signs with wireless ECG and respiration sensors (Siemens AG, Berlin DEU), and a fiber optic temperature probe (FOTS100; Biopac Systems Inc, Goleta CA). Body temperature was maintained with blankets and a warm water re-circulating pump (TP600; Stryker Corp, Kalamazoo MI).

We collected structural MRI data for the whole brain on a Siemens 3T MAGNETOM Skyra using a Siemens 11-cm loop coil placed above the head. A high-quality structural image

was created for each animal by averaging 6-8 3-dimensional (3D) T1-weighted (T1w) volumes acquired in a single scan session (3D Magnetization-Prepared Rapid-Acquisition Gradient Echo (MPRAGE) sequence, voxel size: 0.5mm, slice orientation: sagittal, slice thickness: 0.5mm, field of view (FoV): 128x128mm, FoV phase: 100%, repetition time (TR): 2700ms, echo time (TE): 2.78ms, inversion time (TI): 861ms, base resolution: 256x256, acquisition time (TA): 11 min 31 sec). T2-weighted (T2w) volumes were acquired with a 3D turbo spin echo with variable flip-angle echo trains (3D T2-SPACE) sequence (voxel size: 0.5mm, slice orientation: sagittal, slice thickness: 0.5mm, FoV: 128x128mm, FoV phase: 79.7%, TR: 3390ms, TE: 386ms, base resolution: 256x256, TA: 17min 51sec. We used these T2w volumes both to select coordinates for chamber placements and to position electrodes for recordings. Platinum-iridium electrodes create a clearly identifiable, susceptibility-induced signal void along the length of the electrodes in structural MRI images. This “shadow” has a width of approximately one voxel (0.5 mm^3 on either side of the electrode), allowing us to visualize electrode placement (Fig. S1).

Prior to recordings, we positioned electrodes just dorsal to our ROIs. The electrodes were then held *in situ* by customized guide tubes and lowered into cortex over the course of typically one week of recordings. We then acquired additional structural MRI data prior to replacing the electrodes. We used the before and after images, as well as daily microdrive measurements, to reconstruct electrode tracks.

To further localize electrode penetrations, we aligned the D99 digital template atlas to each individual animal’s high quality T1w MRI volume, using a combination of FSL and AFNI software tools⁴⁻⁶. The D99 atlas is based on and aligned to MRI and histological data from the Saleem and Logothetis⁷ atlas, and allows identification of labeled areas within the native 3D MRI volume of an individual animal. Briefly, we first extracted the brains from the T1w MRI volumes using the FSL brain extraction tool (BET)⁸. We then implemented the pipeline provided

by Reveley, et al. ⁶ to align the atlas to each monkey's MRI volume. This pipeline included a sequence of affine and nonlinear registration steps to first align the individual animal's MRI volume to the atlas, then inverting the transformations to warp the atlas to the animal's original native space. Once aligned, we overlaid the warped atlas' anatomical subdivisions upon the individual monkey's high quality T1w MRI volume, co-registered the T2w MRI volumes that contained electrode penetrations, and visualized penetration locations with respect to the warped atlas on the animal's anatomy. For all recordings presented here, the electrodes were positioned in atlas-defined mdPul (labeled as medial pulvinar in the Saleem and Logothetis ⁷ atlas), FEF, and LIP. Figure S1 shows all of the mdPul penetrations. Fiebelkorn, et al. ¹ includes representative penetrations into FEF and LIP.

Spike Rate

For all analyses, we used a combination of customized MATLAB (MATLAB R2016a, The Mathworks Inc., Natick MA) functions and the Fieldtrip toolbox (<http://www.ru.nl/neuroimaging/fieldtrip>) ⁹. To estimate changes in spike rate over time, time-locked to either the cue or the target, we convolved spikes from each trial with a Gaussian filter ($\sigma = 10$ ms) and averaged the resulting functions. For each neuron, we determined whether there was a statistically significant increase in spike rate in response to the cue or the target (i.e., within 250 ms after cue or target presentation) by using a non-parametric randomization procedure. We randomly selected one response value from the pre-cue period (-350–0 ms) of each trial, averaging those values across trials. We repeated this procedure 5000 times to generate a reference distribution (for the baseline spike rate). The p-value for a non-parametric test is the proportion of values in the reference distribution that exceeds the test statistic (i.e., the observed value from collected data). For all statistical comparisons, unless otherwise

specified, we adopted an alpha criterion of 0.05, and used the Holm's sequential Bonferroni correction to control for multiple comparisons.

To create population PSTHs, we normalized the spike rate for each neuron by its maximum response during trials, and then grand-averaged the normalized rates across neurons. To test whether between-condition comparisons (i.e., cued vs. uncued) were statistically significant (i.e., to establish significant attention effects), we used a Wilcoxon rank-sum test, after averaging the response in a 500-ms window preceding the target (Fig. 1).

Phase-Detection Relationships

For this analysis, our goal was to test whether oscillatory phase in mdPul was linked to behavioral performance during spatial attention. We adapted an approach previously applied to EEG data¹⁰. We first convolved complex Morlet wavelets with the LFP signal just prior to target presentation. We then took the angle of the complex output, deriving pre-target phase estimates, aligned such that the temporal extent of the wavelet did not overlap with the target response.

We next sorted trials by their pre-target phase and calculated the HR within a 180° phase window (e.g., 0–180°). We then shifted this phase window by 5° and recalculated the HR (e.g., 5–185°, then 10–190°, etc.), repeating this procedure until we generated phase-detection relationship functions, spanning all phases, for each frequency (Fig. 2A). These functions provided the frequency-specific relationship between oscillatory phase and behavioral performance. Hypothesizing the same signature shape as phase-power relationships (i.e., with a peak in performance separated from a trough by approximately 180°) we reduced these phase-detection functions to a single value for each frequency (Fig. 2A). Specifically, we applied FFTs and kept the second component, which represented the amplitude of an oscillation with a single

cycle, matching the hypothesized shape.

To test for statistical significance, we (i) shuffled the observed pre-target phase measurements (1500 times) relative to the observed behavioral data (breaking the relationship between phase and behavioral performance) and (ii) repeated the analysis steps. We then compared the resulting reference distributions (at each frequency) to the magnitude of observed phase-detection relationships (accounting for multiple comparisons).

The present results revealed a significant phase-detection relationship in the theta band. We next examined whether phase-detection relationships at higher frequencies might be dependent on the phase of theta-band activity (at 5 Hz). We previously reported such a dependency between theta phase in FEF and LIP and phase-detection relationships at higher frequencies¹. We first binned trials into two (180°) theta-phase bins centered on the peaks and troughs of the phase-detection relationship (at 5 Hz) observed during the previous analysis (Fig. 2A). We then re-calculated the phase-detection relationships from 9–60 Hz, separately for each theta-phase bin (Fig. 2B), using the same procedure described above.

For this theta-dependent analysis, we tested statistical significance by (i) shuffling the observed pre-target phase estimates (1500 times), separately within each theta-phase bin, relative to the observed behavioral data (breaking the relationship between phase and behavioral performance) and (ii) repeated our analysis steps. We then compared the resulting bin-specific reference distributions (at each higher frequency) to the magnitude of observed bin-specific phase-detection relationships (accounting for multiple comparisons). This approach determined whether there were statistically significant phase-detection relationships (from 9–60 Hz) within each theta-phase bin.

Spike-LFP Phase Coupling

We measured the between-region clustering of spike times relative to oscillatory phase in LFPs (e.g., spikes time in FEF relative to oscillatory phase in LIP), from 3–60 Hz. Spike-LFP phase coupling, relative to LFP-LFP phase coupling, avoids spurious coupling attributable to a common reference. For each spike time that fell within a window from -500 to -125 ms prior to target presentation, we calculated corresponding phase estimates from the LFPs (centered on the spike time). To measure spike-LFP phase coupling, we used the pairwise phase consistency (PPC), which is not biased by differences in spike counts or trial numbers¹¹. Stronger clustering of spike times relative to frequency-specific oscillatory phase leads to higher PPC values. For between-region analyses, increased spike-LFP phase coupling (as measured with PPC) is thought to be associated with increased network connectivity. Spikes are typically interpreted as reflecting an output signal, while LFPs are typically interpreted as reflecting an input signal¹².

To test for statistically significant differences in spike-LFP phase coupling when receptive/response fields were centered on either the cued or the uncued location, we (i) shuffled (1500 times) trials between conditions (cued vs. uncued), and then (ii) recalculated the difference in PPC between the randomized conditions. We then compared the resulting reference distributions with the observed difference in PPC values.

We also measured spike-LFP phase coupling (from 9–60 Hz) as a function of theta phase (at 5 Hz). Here, we iteratively calculated spike-LFP phase coupling in overlapping, 180° phase windows (e.g., 0–180°), shifting the phase window in 5° steps (e.g., 5–185°, then 10–190°...). To measure the strength of any link between theta phase and spike-LFP phase coupling at higher frequencies, we hypothesized a signature shape, with a peak in theta-dependent spike-LFP phase coupling separated from a trough by approximately 180°. That is, we assumed that there would be a theta phase with particularly strong spike-LFP phase coupling (at higher frequencies), and 180° away from that phase, a theta phase with particularly weak spike-LFP phase coupling

(at higher frequencies). Based on this assumption, we reduced theta-dependent, spike-LFP phase coupling functions to a single value for each frequency by applying FFTs and keeping the second component¹⁰. This second component represents the amplitude of an oscillation with a single cycle, matching our hypothesized shape (see Fig. 2A).

Because the reliability of phase estimates improves at higher power, changes in power as a function of theta phase (i.e., phase-amplitude coupling) could create spurious relationships between spike-LFP phase coupling and theta phase. We therefore conducted a control analysis that equated higher-frequency power between theta-phase bins, comparing theta-phase bins centered at 90° and 270°. We used the `ft_stratify` function from the FieldTrip toolbox (Donders Institute for Brain, Cognition, and Behaviour), which also equates sample sizes. Stratification involves subsampling the original dataset to equate power, meaning that the results vary somewhat on each run. We therefore ran 1500 iterations of the stratification procedure. Figure 5B displays the mean and standard deviation of these power-equating iterations, confirming the theta-dependent results shown in Figure 5A.

Granger Causality

We used frequency-specific Granger causality to measure the influence of each ROI on the others, when response fields overlapped the cued location. We first downsampled the data to 250 Hz, subtracted the mean, and then divided by the standard deviation. For MVAR modeling, with the BSMART toolbox for MATLAB¹³, we used a model order of 8, which generally corresponded to the first Akaike information criterion value. For paired estimates (e.g., mdPul vs. LIP), we averaged across all recording sessions when each of two ROIs had overlapping response fields. We also calculated conditional Granger causality for a subset of recording sessions when all three ROIs had overlapping response fields (N = 31). Conditional Granger

causality measures the influence of one brain area (Y) on another (X), after taking into account additional areas (Z). The general pattern of results for Granger causal influence between ROIs (Fig. 4) remained the same when instead applying conditional Granger causality (Fig. S5).

We also examined Granger causal influence as a function of theta phase. We first used a two-cycle wavelet to measure the phase of theta-band activity just prior to target presentation. The wavelet was centered at -250 ms. We then sorted trials into two theta-phase bins (see Fig. 2A), one centered on the theta phase associated with enhanced perceptual sensitivity (i.e., the “good” theta phase) and the other centered on the theta phase associated with diminished perceptual sensitivity (i.e., the poor theta phase). For each theta-phase bin, we measured Granger causal influence using an epoch also centered at -250 ms (prior to target presentation), but only overlapping a time period equivalent to half of a theta cycle.

To establish statistical significance, we used a non-parametric randomization approach, shuffling the trial data and re-calculating Granger causality (1500 times). We then compared the compiled reference distribution of differences between, for example, mdPul to LIP and LIP to mdPul Granger causal influence to the observed values (controlling for multiple comparisons).

Cross-Frequency Phase-Amplitude Coupling (PAC)

We first examined PAC between FEF and LIP, focusing exclusively on the relationship between oscillatory phase in one region and high-frequency band (HFB) activity (from 80–200 Hz) in the other. HFB is an established proxy for population spiking¹⁴. We convolved complex Morlet wavelets with the LFP signal prior to target presentation (from -750 to -200 ms, in 10-ms steps), using the results to (i) derive phase estimates from 9 to 35 Hz (in 1-Hz steps) and (ii) to extract HFB activity. To get HFB, we first calculated power in 10-Hz steps (i.e., 80, 90, 100...). We then baseline corrected these power estimates by means of a z-score, relative to the pre-cue

baseline, before averaging across HFB frequencies (from 80–200 Hz). Note that this approach accounts for the $1/f$ signal drop off in HFB at increasing frequencies.

We next sorted frequency-specific phase estimates (From 9–35 Hz) and calculated average HFB power within 180° phase windows (e.g., $0-180^\circ$), shifting the phase window in 5° steps (e.g., $5-185^\circ$, then $10-190^\circ$, etc.). To aid in visual comparisons across frequencies, we normalized these phase-power relationships by subtracting and dividing by the average power across all phases (separately for each frequency). Multiplying by 100 revealed the percent modulation in HFB power as a function of oscillatory phase. The steps to this point (i.e., binning power estimates by phase) are similar to other approaches to measuring PAC^{15,16}. Here, we hypothesized that PAC should have a signature shape, with a peak in PAC separated from a trough by approximately 180° . We therefore reduced phase-power functions to a single value for each phase-providing frequency by applying the fast Fourier transform (FFT) to each function (i.e., at each frequency, from 3–60 Hz) and keeping the second component. This second component represents a one-cycle sine wave, matching the hypothesized shape of our phase-power functions. The amplitude of this one-cycle, sinusoidal component—determined both by how closely the function approximated a one-cycle sine wave and by the effect size—was used to measure the strength of PAC^{1,10}. We used the same procedure to measure within-region PAC for mdPul (Fig. S3), specifically examining the link between theta phase (at 5 Hz) and higher-frequency power (from 9–60 Hz). We previously reported within-region PAC (from 9–60 Hz) for FEF and LIP¹¹. We also used this procedure to examine PAC between alpha/low-beta phase and gamma power, separately for the “good” and “poor” theta-phase bins (Fig. 6).

To test for statistical significance, we (i) shuffled our observed pre-target phase estimates (1500 times) relative to observed power (breaking the relationship between phase

and power) and (ii) repeated our analysis steps. We then compared the magnitude of resulting reference distributions to the observed PAC (accounting for multiple comparisons).

REFERENCES

- 1 Fiebelkorn, I. C., Pinsk, M. A. & Kastner, S. A dynamic interplay within the frontoparietal network underlies rhythmic spatial attention. *Neuron* **99**, 842-853 (2018).
- 2 Egly, R., Driver, J. & Rafal, R. D. Shifting visual attention between objects and locations: evidence from normal and parietal lesion subjects. *Journal of experimental psychology. General* **123**, 161-177 (1994).
- 3 Pigarev, I. N., Saalman, Y. B. & Vidyasagar, T. R. A minimally invasive and reversible system for chronic recordings from multiple brain sites in macaque monkeys. *Journal of neuroscience methods* **181**, 151-158, doi:10.1016/j.jneumeth.2009.04.024 (2009).
- 4 Cox, R. W. AFNI: software for analysis and visualization of functional magnetic resonance neuroimages. *Computers and biomedical research, an international journal* **29**, 162-173 (1996).
- 5 Jenkinson, M., Beckmann, C. F., Behrens, T. E., Woolrich, M. W. & Smith, S. M. Fsl. *NeuroImage* **62**, 782-790, doi:10.1016/j.neuroimage.2011.09.015 (2012).
- 6 Reveley, C. *et al.* Three-Dimensional Digital Template Atlas of the Macaque Brain. *Cerebral cortex* **27**, 4463-4477, doi:10.1093/cercor/bhw248 (2017).
- 7 Saleem, K. S. & Logothetis, N. *A combined MRI and histology atlas of the rhesus monkey brain in stereotaxic coordinates.* (Academic, 2007).
- 8 Smith, S. M. Fast robust automated brain extraction. *Human brain mapping* **17**, 143-155, doi:10.1002/hbm.10062 (2002).
- 9 Oostenveld, R., Fries, P., Maris, E. & Schoffelen, J. M. FieldTrip: Open source software for advanced analysis of MEG, EEG, and invasive electrophysiological data. *Computational intelligence and neuroscience* **2011**, 156869, doi:10.1155/2011/156869 (2011).
- 10 Fiebelkorn, I. C. *et al.* Cortical cross-frequency coupling predicts perceptual outcomes. *NeuroImage* **69**, 126-137, doi:10.1016/j.neuroimage.2012.11.021 (2013).
- 11 Vinck, M., van Wingerden, M., Womelsdorf, T., Fries, P. & Pennartz, C. M. The pairwise phase consistency: a bias-free measure of rhythmic neuronal synchronization. *NeuroImage* **51**, 112-122, doi:10.1016/j.neuroimage.2010.01.073 (2010).
- 12 Pesaran, B. Neural correlations, decisions, and actions. *Current opinion in neurobiology* **20**, 166-171, doi:10.1016/j.conb.2010.03.003 (2010).
- 13 Cui, J., Xu, L., Bressler, S. L., Ding, M. & Liang, H. BSMART: a Matlab/C toolbox for analysis of multichannel neural time series. *Neural networks : the official journal of the International Neural Network Society* **21**, 1094-1104, doi:10.1016/j.neunet.2008.05.007 (2008).
- 14 Ray, S. & Maunsell, J. H. Different origins of gamma rhythm and high-gamma activity in macaque visual cortex. *PLoS biology* **9**, e1000610, doi:10.1371/journal.pbio.1000610 (2011).
- 15 Canolty, R. T. *et al.* High gamma power is phase-locked to theta oscillations in human neocortex. *Science* **313**, 1626-1628, doi:10.1126/science.1128115 (2006).

- 16 Tort, A. B., Komorowski, R., Eichenbaum, H. & Kopell, N. Measuring phase-amplitude coupling between neuronal oscillations of different frequencies. *Journal of neurophysiology* **104**, 1195-1210, doi:10.1152/jn.00106.2010 (2010).

SUPPLEMENTAL MATERIALS

ROI	all	visual	visual- movement	movement
mdPul	224	20	19	13
FEF	238	36	45	17
LIP	259	39	41	18

Table S1. *Numbers of neurons in each ROI with significantly increased task-related responses. Neurons were classified as visual (i.e., only visual-sensory activity), visual-movement (i.e., both visual-sensory and saccade-related activity), and movement (i.e., only saccade-related activity) types.*

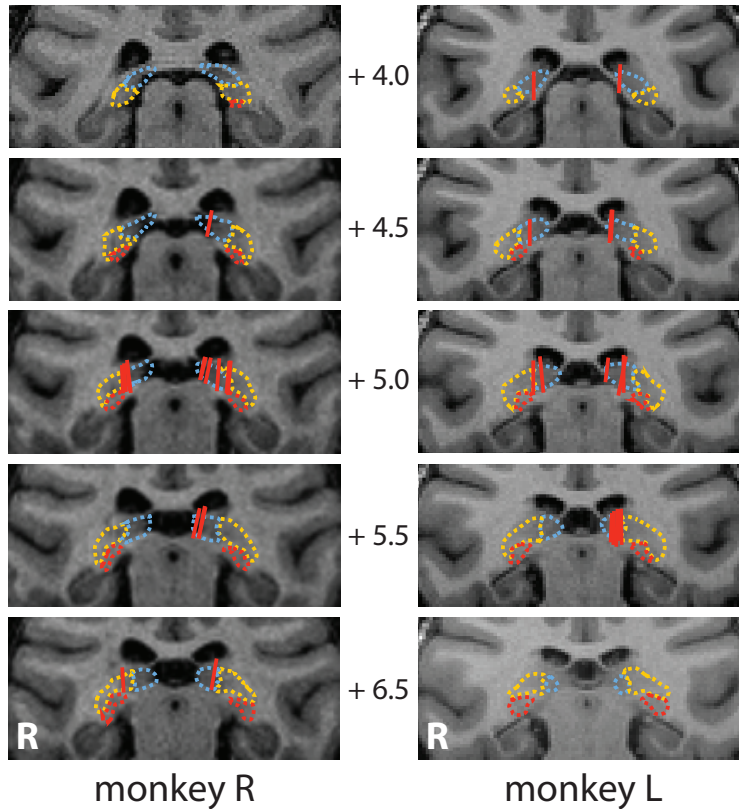


Figure S1. Penetrations targeting the atlas-defined mediodorsal pulvinar (*mdPul*). We previously published representative penetrations for FEF and LIP⁴. Here, a red line depicts each penetration. The numbers positioned between images from each of the animals represent anterior-posterior distances from the interaural line (*mm*). Atlas-defined pulvinar subdivisions: dashed blue = medial pulvinar; dashed yellow = lateral pulvinar; dashed red = inferior pulvinar. The white R = right hemisphere.

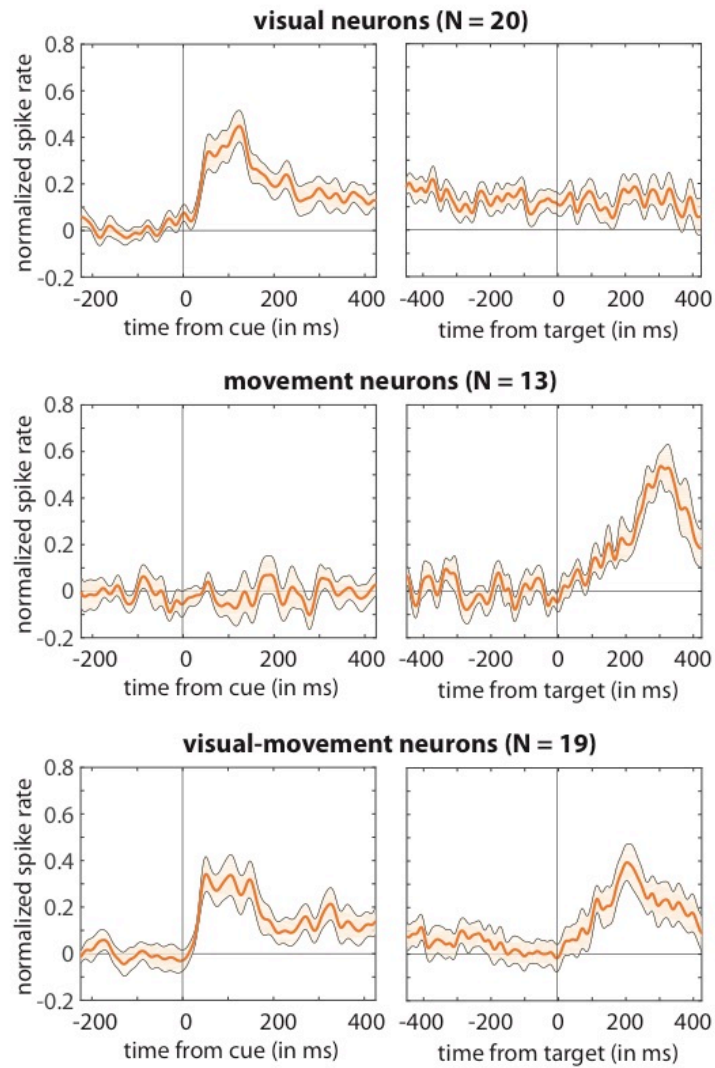


Figure S2. Normalized population spike rates in mdPul by cell type. Significant spiking during the cue-target delay was observed in visual and visual-movement neurons, but not in movement neurons.

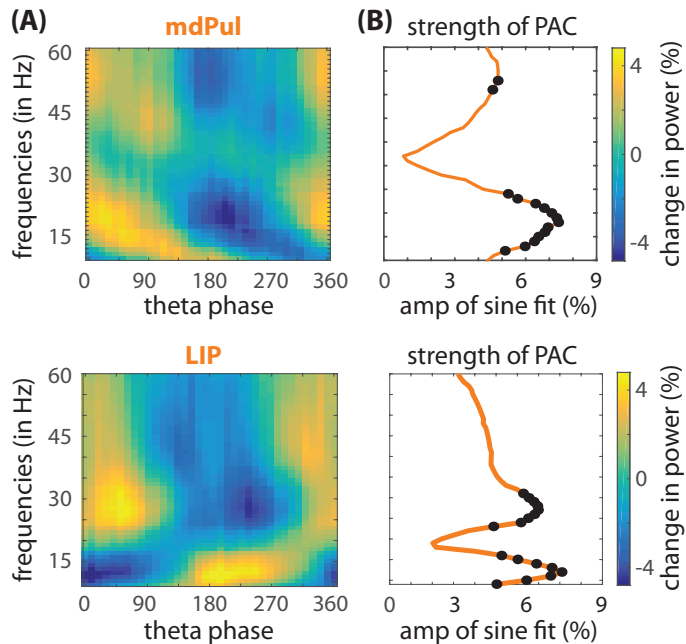


Figure S3. Phase-amplitude coupling (PAC) between theta phase and oscillatory power (from 9–60 Hz) in MdPul and LIP during spatial attention. **(A)** For mdPul, higher alpha/low-beta power occurred during the theta phase associated with relatively better visual-target detection (i.e., the “good” theta phase). For LIP, higher alpha/low-beta power occurred during the theta phase associated with relatively worse visual-target detection (i.e., the “poor” theta phase)⁴. **(B)** Oscillatory power as a function of theta phase was fit with one-cycle sine waves, with the amplitude of those fitted sine waves measuring the strength of PAC (see Fig. 2A for a depiction of a similar approach). The black dots represent statistically significant PAC after corrections for multiple comparisons.

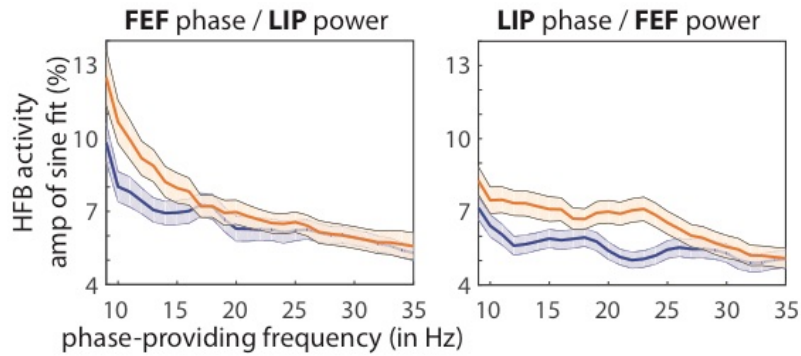


Figure S4. Phase-amplitude coupling (PAC) between alpha/low-beta phase in FEF (or LIP) and high-frequency band (HFB) power in LIP (or FEF) increases during spatial attention. HFB power, a proxy for population spiking, was binned by oscillatory phase (at frequencies from 9–35 Hz). PAC was measured by fitting one-cycle sine waves to the resulting HFB by phase functions (see Fig. 2A for depiction of a similar approach)⁴. The amplitudes of the fitted sine waves was used to estimate the strength of PAC at each phase-providing frequency. The above plots compare PAC when receptive/response fields overlapped either the cued (orange) or the non-cued (blue) location. These results demonstrate that alpha/low-beta activity is functionally relevant in FEF and LIP, organizing between-region interactions under conditions of spatial attention. Shaded regions around the lines represent SEs.

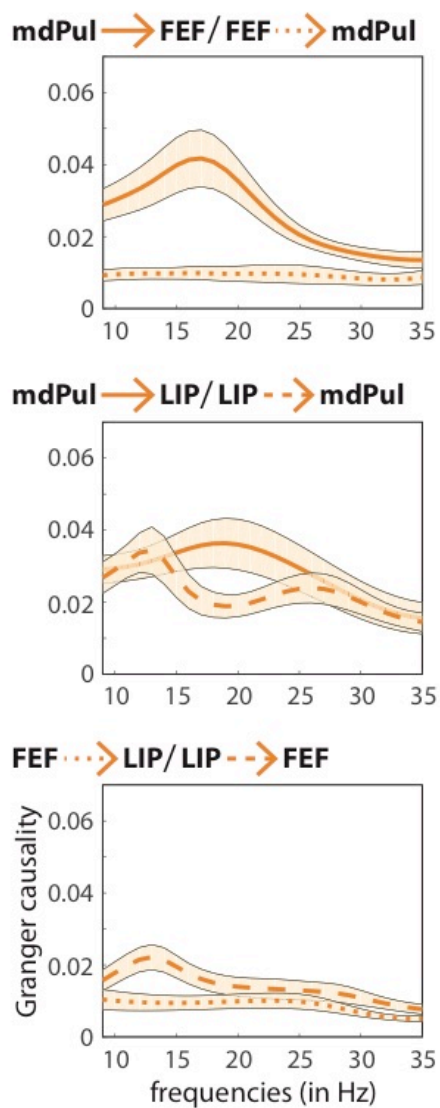


Figure S5. Conditional Granger causality for a subset of recording sessions ($N = 31$) when all 3 ROIs had overlapping response fields. These results are similar to those reported in Figure 5.

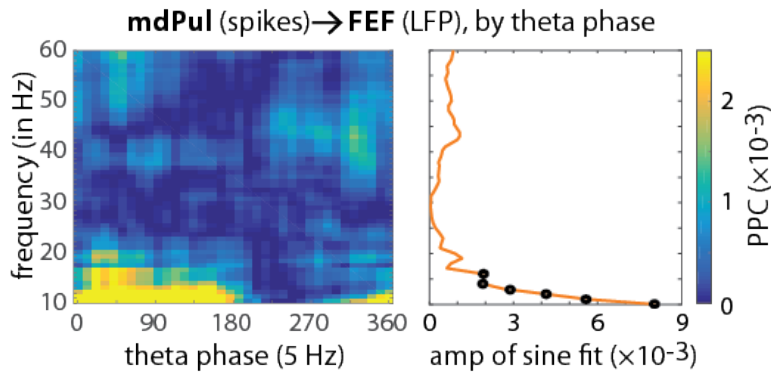


Figure S6. Spikes in mdPul also seem to be specifically coupled to alpha/low-beta activity in FEF during the “good” theta phase. Spike-LFP phase coupling (from 9–60 Hz) was calculated in overlapping theta-phase bins (on left), using step sizes of 10 degrees. The resulting functions were then fit with one-cycle sine waves. The amplitude of these sine waves provided a measure of how strongly spike-LFP phase coupling was modulated by the phase of theta rhythms (on right, see Fig. 2A for depiction of a similar approach). The black dots represent statistically significant results after corrections for multiple comparisons. See Fig. 4B for additional evidence.

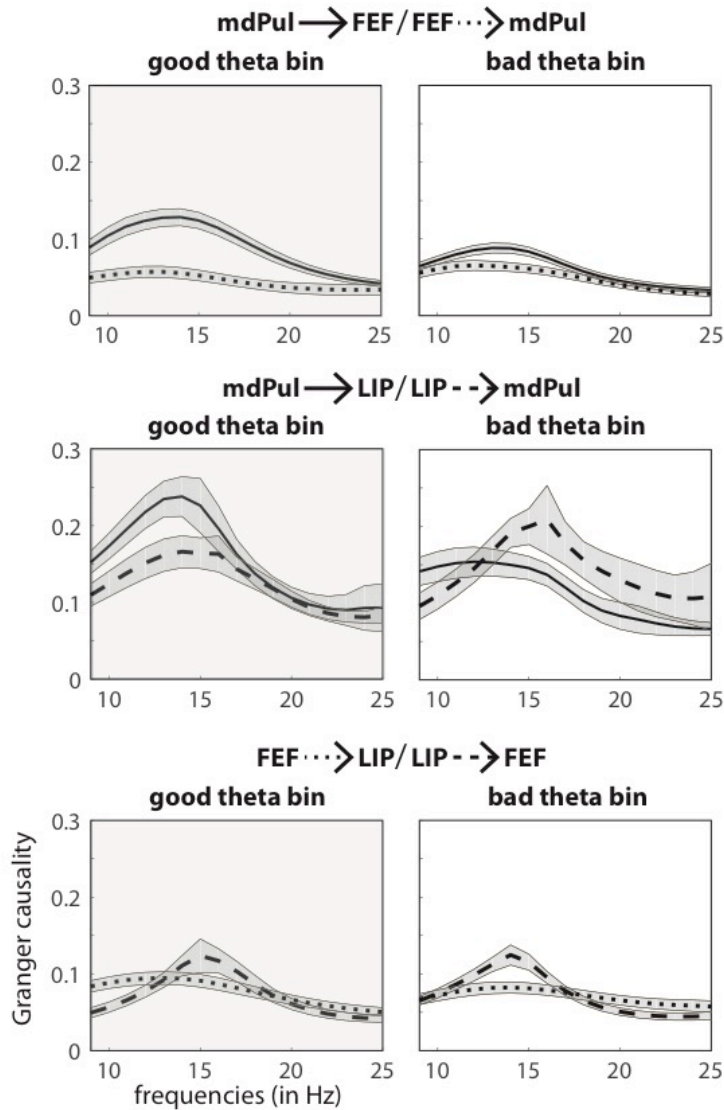


Figure S7. Granger causal influence indicates that mdPul regulates alpha/low-beta activity in cortical hubs of the attention network (i.e., FEF and LIP). Shows Granger causal influence after binning based on theta phase (“good” vs. “poor”). Here, we first used a stratification procedure to equate alpha/low-beta power, both across ROIs and across theta-phase bins. These findings confirm the results presented in Figure 4, demonstrating that mdPul specifically regulates cortical activity during periods of relatively better visual-target detection (i.e., during the “good” theta phase). Shaded regions around the lines represent SEs.