### Using set theory to reduce redundancy in pathway sets

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### 1 1. Abstract

### 2 1.01 Background

- 3 The consolidation of pathway databases, such as KEGG[1], Reactome[2] and
- 4 ConsensusPathDB[3], has generated widespread biological interest, however the
- 5 issue of pathway redundancy impedes the use of these consolidated datasets.
- 6 Attempts to reduce this redundancy have focused on visualizing pathway overlap
- 7 or merging pathways, but the resulting pathways may be of heterogeneous sizes
- 8 and cover multiple biological functions. Efforts have also been made to deal with
- 9 redundancy in pathway data by consolidating enriched pathways into a number of
- 10 clusters or concepts. We present an alternative approach, which generates
- 11 pathway subsets capable of covering all of genes presented within either pathway
- 12 databases or enrichment results, generating substantial reductions in redundancy.
- 13
- 14

### 15 1.02 **Results**

16 We propose a method that uses set cover to reduce pathway redundancy, without 17 merging pathways. The proposed approach considers three objectives: removal of 18 pathway redundancy, controlling pathway size and coverage of the gene set. By applying set cover to the ConsensusPathDB dataset we were able to produce a 19 20 reduced set of pathways, representing 100% of the genes in the original data set 21 with 74% less redundancy, or 95% of the genes with 88% less redundancy. We 22 also developed an algorithm to simplify enrichment data and applied it to a set of 23 enriched osteoarthritis pathways, revealing that within the top ten pathways, five 24 were redundant subsets of more enriched pathways. Applying set cover to the 25 enrichment results removed these redundant pathways allowing more informative pathways to take their place. 26

27

### 28 1.03 **Conclusion**

29 Our method provides an alternative approach for handling pathway redundancy, 30 while ensuring that the pathways are of homogeneous size and gene coverage is maximised. Pathways are not altered from their original form, allowing biological 31 32 knowledge regarding the data set to be directly applicable. We demonstrate the 33 ability of the algorithms to prioritise redundancy reduction, pathway size control 34 or gene set coverage. The application of set cover to pathway enrichment results 35 produces an optimised summary of the pathways that best represent the 36 differentially regulated gene set. 37

- 38 <u>Keywords</u>
- 39 Set cover, data redundancy, pathways, gene enrichment analysis
- 40

## 41 2. Background

42 Pathways are sets of genes corresponding to functionally related interacting 43 proteins. Pathway data is available from many databases dependent on biological 44 focus. The fragmented nature of pathways across multiple databases makes it 45 difficult to perform inclusive analysis of all known data. To address this issue, 46 many attempts have been made to consolidate pathway databases such as 47 ConsensusPathDB (CPDB) [4]. PathwavCommons [5]. The Human Pathwav 48 Database (HPD) [6], Pathway Interaction Database (PID) [7], and NCBI Biosystems [8]. Amalgamating multiple databases into a consistent searchable format 49 50 facilitates the use of these resources, however the arbitrary nature of pathway boundaries results in overlap and redundancy. This redundancy greatly increases 51 the quantity and complexity of pathway data, which has lead to the development of 52 53 a range of tools to assist in data simplification and interpretation [6, 7, 9–11]. Previous solutions presented to deal with redundancy include visualizing 54 redundancy between pathways to the user [6], merging pathways based on 55 56 similarity [10, 11] and even integrating full pathway sets into a non-redundant, 57 single unified pathway [12]. Reducing redundancy simplifies the pathway-related descriptive space, allowing multiple resources to be combined while limiting the 58 59 number of pathway attributes assigned to each gene. The advantages are apparent, with resources such as PathCards being integrated into the widely used 60 GeneCards[11]. 61

62

Redundancy Control in Pathway Databases (ReCiPa) [10] uses a pathway merging
algorithm to combine pathways with high levels of overlap. Users select a
maximum overlap threshold and pathway pairs displaying greater levels of
overlap are merged. Within that study redundancy was observed within five large
databases (KEGG, Biocarta, CGP, NCI-PID, and Reactome). They proceeded to
merge pathways from the Molecular Signatures Database (MSigDB), whose overlap

- 69 exceeded 75%, reducing pathway redundancy.
- 70

71 Pathcards described a multistep procedure to reduce pathway redundancy, also 72 through pathway merging [11]. Two thresholds were calculated and sequential 73 merging steps were used to minimize overlap, while preventing the generated 74 super-pathways from becoming too large to be informative. By merging pathways 75 into super-pathways, Pathcards suggested many new molecular interactions. They 76 demonstrated that many of these newly generated interactions are supported by 77 high numbers of literature co-mentions and high experimental interactions scores 78 according to STRING. However, while the generation of potential interactions can 79 be highly beneficial, if the aim is to utilize previously validated data, merging 80 pathways introduces a source of uncertainly into the dataset. 81

A major application of pathway data sets is pathway enrichment analysis. Both

83 Pathcards and ReCiPa explored the capability of their reduced pathway dataset to

84 improve enrichment results. Enrichment analysis of 830 differential expression sets was performed using the super-pathways generated within Pathcards. The 85 enrichment results from super-pathways tended to be more significant than the 86 87 enrichment scores of their constituent pathways. Similarly within the ReCiPa study 88 enrichment analysis was performed using genes differentially expressed in 89 obesity. After merging, the top 20 most significantly enriched pathways showed 90 less overlap and greater significance towards the disease, compared to the original 91 dataset. 92

- 93 Pathway Distiller implemented an alternative approach by removing redundancy
- 94 from enriched pathway sets following enrichment analysis [9]. Pathways may be
- 95 consolidated into pathway concepts based on gene expression profiles, gene
- 96 membership, protein-protein interaction data or shared Gene Ontology (GO)
- 97 terms. Each method provides varying, complementary views of the data, with
- 98 different pathway concepts generated. Consolidating enrichment output into a
- 99 reduced number of pathway concepts increases data manageability and
- 100 readability, by organizing redundant pathways into their major groups.
- 101

102 All of the approaches discussed to this point have used merging and consolidation 103 to address redundancy. Alexa et al. (2006) demonstrated that redundancy in GO 104 enrichment results could be reduced by selecting a subset of representative terms 105 [13]. Pathway enrichment analysis and GO enrichment analysis are similar techniques in which sets of differentially expressed genes are compared to gene 106 107 sets associated with pathways or GO terms. Alexa et al. (2006) introduced two 108 algorithms, *elim* and *weight*, which use the Gene Ontology topology to select a 109 representative subset of highly enriched GO terms [13]. The enrichment set cover algorithm presented in this paper shares some conceptual similarity with this 110 111 approach however, the implementation is different since there is no organized

- 112 topological hierarchy for combined pathway datasets and the rules governing the
- 113 Gene Ontology, such as the true path rule [14], do not apply.
- 114

115 Within this paper we show that set cover can be used to reducing redundancy by selecting subsets of representative pathways. We describe a set of algorithms for 116 117 reducing redundancy in pathway datasets, as well as a separate algorithm for 118 reducing redundancy from pathway enrichment results. The proportional set 119 cover algorithm and hitting set cover algorithm aim to identify a minimum subset 120 of pathways required to cover the genes in highly redundant, consolidated pathway databases. The generated set covers are not designed to depict the full 121 122 range of possible pathway boundaries and their accompanying cellular functions. 123 but rather they provide a simplified set of pathways to represent the actions of genes within the dataset. Since the pathways are not merged database and 124 125 biological information remains directly applicable and functional specificity is not lost through pathway size expansion. The proposed method also removes the risk 126 127 of biologically distinct pathways being merged. The algorithm's ability to remove 128 overlap is not limited by thresholds, conferring an advantage compared to 129 approaches such as Pathcards and ReCiPa in which redundancy between pathway pairs can only be removed if the overlap exceeds the threshold. Set cover

- algorithms also consider redundancy between multiple pathways, rather than justcomparing pathway pairs.
- 133

134 We also developed the enrichment set cover algorithm for handling pathway enrichment data and applied it to a set of enriched osteoarthritis pathways [15]. In 135 136 contrast to the approaches used by ReCiPa and Pathcards, the enrichment set cover algorithm is designed to be used following enrichment analysis, which 137 138 should be performed using the full pathway dataset. Redundancy is then removed 139 from the enriched pathway set by selecting the pathway with the lowest p-value to 140 cover each differentially regulated gene. Enriched pathways are not merged or 141 altered and the number of enriched pathways required to cover the dataset is 142 reduced. The resulting pathways set can therefore be used as an optimized 143 summary output, conveniently showing the most important pathways for 144 describing the differentially regulated gene set. By increasing the number of 145 differentially regulated genes covered by the most highly enriched pathways. researchers examining the top 10 or 20 pathways are provided with a more 146 inclusive portraval of the gene set. 147 148

## 149 3. Approach

- We downloaded pathway data from ConsensusPathDB (CPDB), an opensource
  online collection of pathways, that incorporates 32 sources including KEGG,
  Wikipathways, PDB, Reactome. CPDB makes these resources available as a single
  download, which we acquired on 24/09/2015 containing 4,011 pathways. We
- applied the set cover algorithm to the CPDB data set, analyzing it's effectiveness at:
   reducing pathway overlap; reducing pathway size variability; and preserving the
- 156 maximum number of genes in the data set. We found that standard set cover
- 157 caused unacceptable increases in pathway size, therefore we modified the
- algorithm and assessed the modified algorithms capability to meet the previous
- 159 three objectives.
- 160

Set cover is a well-defined algorithm in computer science for handling overlapping sets of sets. For example, set cover is used by CLASS, a bioinformatics program that maps RNA sequence data to transcripts [16]. Set cover has also been used to predict protein-protein interactions based on binding domains [17], to reduce the complexity of SNP sets [18] and to minimize the number of probes needed to

166 analyze DNA [19].

167

168 Set cover algorithms deal with elements and sets, which relate to genes and

- 169 pathways respectively. All the unique genes in the data set are collectively referred
- 170 to as the universe. The aim is to produce a reduced selection of sets (pathways),
- 171 which collectively cover all the elements (genes) in the universe (dataset). This

subset of the original data is called the cover set [20]. Each time a pathway is
added to the cover set the genes in the pathway become covered (Figure 1). Direct
application of set cover lead to extremely large, functionally non-specific pathways
dominating the cover set, therefore we implemented the proportional set cover
and hitting set cover algorithms to better control pathway size, while reducing
redundancy and covering the dataset.
When dealing with enrichment analysis data the aim is to reduce redundancy

between pathways, while preserving the order of enrichment significance denoted
by the p-values. We designed an algorithm that would select the set of pathways

- 182 with the lowest p-values capable of covering all the genes in the dataset. This
- 183 ensures that the filtered results return the most enriched pathways available for
- 184 each gene.
- 185

### 186 4. Methods

### 187 4.01 **Overlap score**

To measure overlap across different algorithms we measured the mean number of
pathways that each gene appears in. Within the raw data genes appeared in a
mean of 12.4 pathways. We refer to this metric as the overlap score.

### 191 4.02 **Set cover**

We applied the set cover algorithm to the data set, which generates a subset of
pathways called a cover set, in which all the genes in the data set are represented
or "covered". Set cover begins by first assigning values to each pathway (*v<sub>i</sub>*). The
set cover values correspond to the number of uncovered genes each pathway
contains (Equation 1).

197

$$v_i = |s_i \cap R|$$

198 199 where  $(s_i)$  is the pathway's gene set and **R** is the set of all uncovered genes. 200 201 At the beginning of the algorithm all the genes in the dataset are uncovered so the 202 algorithm selects the largest pathway. The genes from the selected pathway are 203 then covered, so it is unnecessary to cover them again using additional pathways. 204 The algorithm then recalculates how many uncovered genes each pathway 205 contains and continues to add the pathway with the maximum value to the set 206 cover until all genes in the data set are covered. 207 208 209 Algorithm 1 Set cover (in separate file)

- where **R** is the set of uncovered genes, **U** is all the genes in the dataset, **C** is the
- covered genes, *SC* is the set cover result, *GC* is the gene coverage (see Section 4.03)
- 212 and  $s_i$  is a pathway.
- 213
- 214 Application of the set cover algorithm was effective in reducing overlap between
- 215 the pathways; however, it selected very large pathways with reduced
- 216 informativeness (maximum size 2320, standard deviation 160, almost double the
- standard deviation on the original dataset 86.9). We therefore explored methods
- that avoid preferential selection of large pathways.
- 219

### 220 4.03 Gene Set Coverage

As the set cover algorithm approaches completion and the final sets are added to the cover set, increases in data coverage are gained at the expense of redundancy reduction. This is because the final sets required to cover the few remaining genes tend to have the most overlap with other pathways already in the set cover. In addition, fewer pathways are available to cover the final few genes, restricting options to control pathway size. To allow a user-defined compromise between the gene coverage, pathway redundancy and pathway size we introduce the Gene

- Coverage (*GC*) parameter. Setting *GC* below 100% allows the algorithm to finish
  before the final elements have been covered. We experimented setting *GC* to 90,
- 230 95, 99 and 100% of the number of genes in the data set.
- 231

### 232 4.04 **Proportional set cover**

When reducing pathway redundancy there are three competing aims: reducing
redundancy; controlling pathway size; and covering the entire gene set. The
proportional set cover algorithm was generated to focus on controlling pathway
size.

237

To control the size of the pathways we altered the scoring mechanism to rank
pathways based on the proportion of uncovered genes they contained, rather than

- the absolute number (Equation 2). This works because larger pathways are morelikely to have a proportion of their genes covered when other pathways are
- selected. Additionally this mechanism directly penalizes overlap, which the
- 243 standard algorithm does not. At the beginning of the proportional set cover
- algorithm none of the genes are covered so the proportion of uncovered genes in
- every pathway is 1. This would result in the starting pathway being selected at
- random. To ensure that pathway size variability is controlled as strictly as
- 247 possible, we implemented the second part of Equation 2, which ensures that
- 248 pathways of mean pathway size are preferentially selected when multiple
- 249 pathways with the same proportion of uncovered genes are available.
- 250

$$v_i = \frac{|s_i \cap R|}{|s_i|} + \frac{1}{abs(|s_i| - \overline{|s_i|}) * k}$$

251

- 252 where  $s_i$  is the pathway's gene set,  $\overline{|s_i|}$  is the mean pathway length, **R** is the
- 253 uncovered genes set and *k* is a large constant to limit the influence of the second
- term (taken equal to 10,000).
- 255

### 256 4.05 Hitting set cover

The set-covering problem can be reformulated into the equivalent set-hitting 257 problem. In this formulation genes and pathways are visualized as bi-partite graph 258 259 in which the pathways are connected to the genes that they contain. In this 260 depiction it is clear that some genes are only linked to a single pathway, which 261 must be selected if the gene is to be covered. The importance of pathways can 262 therefore be considered as a factor of how infrequent their genes are. The hitting 263 set cover is therefore designed to reduce redundancy as much as possible without 264 directly selecting for pathway size.

265

266 We calculated the frequency of each gene in the data set (*F*), then assigned the

267 gene's value gv(j) as 1/F. We then assigned a value  $v_i$  to each pathway defined as

the sum of each uncovered gene's scores divided by the number of genes in the

- 269 pathway (Equation 3).
- 270

$$gv(j) = 1 / F(j)$$
$$v_i = \frac{\sum_{j \in s_i \cap R} gv(j)}{|s_i|}$$

271

- where gv(j) is the value of a gene, F(j) is the number of pathways a gene is in,  $j \in s_i \cap R$  means for each uncovered gene in the pathway and  $|s_i|$  is the length of the pathway.
- 275

### 276 4.06 Set cover for pathway enrichment analysis

277 Pathway analysis is a frequently used method; therefore a modified set cover 278 algorithm to address this situation could be highly useful. The universe represents 279 differentially expressed genes and the sets are enriched pathways generated 280 through enrichment analysis. Enrichment analysis results represent entirely different input data compared to the pathway datasets used in the previous 281 282 algorithms, as the enriched pathways already have scores (p-values). We wish to reduce redundancy (gene overlap) between enriched pathways and it is essential 283 284 that the pathways with the lowest possible p-values are selected. Equation 4 285 allows the pathways with the lowest p-values to be selected, unless all of their 286 genes are covered by other enriched pathways with even lower p-values.

287

$$s_i \cap \mathbf{R} = \theta \rightarrow b = 0,$$
  $s_i \cap \mathbf{R} \neq \theta \rightarrow b = 1$   
 $v_i = (1 - pvalue_i) * b$ 

288

289	where $s_i$ is the enriched pathway's gene set, $R$ is the uncovered gene set, $b$ is a
290	binomial operator, $pvalue_i$ is the pathway's p-value and $v_i$ is the pathway's set
291	cover value.

292	We generated the enriched data set by applying GOseq [21] to expression data
293	from the damaged cartilage in osteoarthritis patients and controls [15].

294

### 295 5. Results

We started with the large, extensively redundant CPDB data set and used set cover to reduce pathway overlap, while controlling pathway size and seeking to cover as much of the data set as possible. We describe the ability of the standard set cover algorithm and two modified algorithms, in conjunction with the *GC* parameter, to meet these objectives.

301

### 302 5.01 Pathway redundancy varies between different algorithms

303 The original pathway data set contained 11,196 genes and 3,305 pathways; the 304 starting overlap score (see methods) was 12.4. The standard set cover algorithm 305 reduced overall redundancy from 12.4 to 4.1, a 73% reduction (since a completely 306 discrete pathway set would have a score of 1). The overlap score for proportional set cover was 4.36, slightly higher than the standard set cover algorithm, but still 307 representing a 70% reduction in overlap from the original data. The hitting set 308 309 cover algorithm was designed to select pathways that contained rare genes within the data set, resulting in the greatest reduction in overlap (overlap score of 3.95 310 311 equivalent to a 74% reduction).

312

After application of the set cover algorithms the distribution of the remaining
overlap between pathways varied greatly. Figure 2 shows the Jaccard similarity

between pairs of pathways, in the outputs produced by each of the three

algorithms. The standard set cover algorithm produced the lowest maximum

317 overlap (Jaccard similarity = 0.68) between the pathway pairs. However, compared

to the original data, a higher proportion of pathway pairs in the set cover output

319 showed Jaccard similarities between 10-30%. Proportional set cover had the

- 320 greatest maximum Jaccard similarity at 0.93, out of the set cover algorithms. The
- 321 hitting set cover algorithm produced a maximum Jaccard similarity between two
- 322 pathways of 0.82, despite having the lowest overlap score.

323

### 324 Gene Coverage can be lowered to reduce redundancy

For each of the algorithms it is possible to use the GC parameter to prioritize 325 reductions in redundancy over gene coverage by stopping any algorithm before all 326 of the genes in the dataset have been covered. Figure 3 shows improved ability of 327 the set cover algorithms to reduce pathway overlap for different values of GC. If 328 329 99% of the genes are required then the hitting set algorithm achieves the lowest overlap score of 3.24, equivalent to an 80% reduction in overlap. Redundancy can 330 331 be further reduced if only 95% of the genes are covered, with the proportional and 332 hitting set algorithms producing an overlap score of 2.41, equivalent to a 88% reduction in redundancy. Both the proportional set cover and the hitting set cover 333 334 are more effective at reducing redundancy than the standard set cover if GC is set 335 to less than 100%.

336

# 337 Pathway size is affected by the set cover algorithm and Gene Coverage 338 setting

When *GC* was set to 100% the standard set cover algorithm represented all of the genes in the dataset using only 524 pathways (16% of the original pathway set).

- However, many of these were very large increasing the mean size to 87.2
- 342 (standard deviation 160.1). These pathways have reduced informativeness since
- 343 functional specificity is lost. Figure 4A illustrates the tendency of this algorithm to
- 344 select extremely large pathways.
- 345
- 346 The proportional set cover algorithm was designed to preferentially select
- 347 moderately sized pathways. This returned a cover set of 1,336 pathways with
- 348 controlled size variation (mean of 36.5, standard deviation 55.1) shown in Figure
- 349 4A. The hitting set cover algorithm was less able to control pathway size than the
- proportional set cover algorithm, returning 957 pathways with a mean size of 46.2(standard deviation 61.7).
- 352
- 353 Figures 4B D show that as *GC* is reduced the tendency of the standard set cover to
- 354 select very large pathways becomes more exaggerated. Decreasing *GC* also
- improves the ability of the proportional set cover algorithm to select moderately
- 356 sized pathways. The hitting set algorithm also tends to select smaller pathways
- 357 when *GC* is reduced, since larger pathways often contain more frequent genes.
- Reducing *GC* affects pathway size since in the later stages of the algorithm, fewer
- pathways are available to cover the remaining genes, reducing the available
- 360 options. Therefore, lowering *GC* has the ability to help control pathway size when
- the proportional set cover and hitting set cover algorithms are used.
- 362
- 363 Since the databases that contribute to CPDB contain pathways of different sizes, the set cover generated may
- 364 preferentially select pathways from some databases more than others.

365 Table 1 shows the proportion of pathways that come from each database in the cover set generated by each algorithm. All algorithms generate set covers with 366 367 reduced INOH and SMPDB pathways, showing that SMPBD's focus on small molecules and INOH's ontology-based approach tend to be ill-suited to the 368 369 generation of discrete pathway protein sets. The standard set cover algorithm generates sets containing large pathways, preferentially selecting pathways from 370 371 KEGG (median size 65, see Table 1) and Netpath (median size 51); while 372 proportional set cover tends to select smaller pathways from Reactome (median 373 size 17), HumanCyc (median size 5) and Signalink (median size 32), whilst 374 avoiding NetPath. 375

- 376 Table 1. Proportion of pathways from CPDB databases. Median size represents the
- 377 median sizes of the pathways in the CPDB dataset. CPDB % represents the proportion
- 378 of the pathways in the unaltered dataset that came from each database. The
- 379 following columns represent the proportion of pathways in the set cover generated
- 380 by the standard set cover algorithm, the hitting set cover algorithm and the
- 381 proportional set cover algorithm. Different results are obtained by altering the
- 382 proportion of the gene set covered, shown in subcolumns below the algorithm header.

383	2
20-	)

	Median size	CPDB %	Standard set cover				Hitting	Hitting set cover		
			100%	99%	95%	90%	100%	99%	95%	
BioCarta	15.0	6.3	6.3	4.6	0.5	0.0	4.7	4.8	5.4	
EHMN	32.5	1.6	3.2	3.4	2.6	1.0	2.1	2.3	1.8	
HumanCyc	5.0	8.2	6.5	7.7	2.6	0.0	10.1	10.9	12.9	
INOH	34.5	2.3	1.7	1.9	1.0	1.0	0.8	0.6	0.3	
KEGG	65.0	7.2	29.0	30.5	37.6	40.4	15.8	15.0	13.5	
NetPath	51.0	0.9	2.1	2.4	3.6	5.1	1.1	1.2	1.1	
PharmGKB	13.0	2.8	3.1	2.9	0.5	0.0	2.0	2.1	2.4	
PID	35.0	5.2	15.6	13.9	10.3	6.1	9.5	9.8	9.4	
Reactome	17.0	39.6	4.2	5.3	10.8	21.2	36.1	35.1	34.7	
Signalink	32.0	0.4	1.0	1.2	1.0	0.0	0.6	0.7	0.7	
SMPDB	11.0	16.7	1.7	1.4	0.5	0.0	1.6	1.5	1.4	
Wikipathways	26.0	8.8	25.6	24.9	28.9	25.3	15.6	16.0	16.2	

### 384

385

### Reducing redundancy in pathway enrichment analysis

386 To demonstrate the ability of the set cover algorithm to handle enrichment data,

- 387 we applied the enrichment set cover algorithm to an osteoarthritis data set,
- retrieved from Dunn et al. (2016) [15]. From the osteoarthritis data set, 58.3% of
- the differentially expressed genes could be mapped to a CPDB pathway, which was

a 17% improvement on the GOseq [21] implemented data set. We retrieved 42
enriched pathways with a p-value lower than 0.05, following the BenjaminiHochberg correction for multiple testing. Set cover for enrichment analysis
reduced the number of pathways required to cover the differentially expressed
genes to 23 (supplementary table 1).

395

396 The heat map in Figure 5A shows the asymmetric overlap between the top ten 397 pathways before application of the algorithm. The p-values from pathway 398 enrichment determine the order in which pathways were considered for inclusion 399 in the cover set. Pathways were omitted if all of the differentially expressed genes 400 that they covered were also covered by more enriched pathways. Note that overlap 401 tends to be higher in the bottom left triangle as pathways added later were often 402 smaller subcomponents of larger pathways. We can see that 'extracellular matrix 403 organization', the most enriched pathway, was placed in the cover set first. Next was 'collagen biosynthesis and modifying enzymes'; however, all of the 404 405 differentially expressed genes in this pathway are also covered by the larger 406 pathway 'extracellular matrix organization', as indicated by the red cell in the 407 'collagen biosynthesis and modifying enzymes' row, 'extracellular matrix organization' column. The corresponding cell in the 'extracellular matrix 408 409 organization' row reveals that 24% of the differentially expressed genes in 'extracellular matrix organization' are also in 'collagen biosynthesis and modifying 410 411 enzymes'.

412

Figure 5B shows overlap between the top ten pathways after application of the 413 enrichment set cover algorithm. Because the differentially expressed genes 414 covered by the 'collagen biosynthesis and modifying enzymes' pathway are a 415 416 subset of those covered by the 'extracellular matrix organization' pathway, the 417 'collagen biosynthesis and modifying enzymes' pathway is removed from the cover 418 set (Figure 5B). The second pathway in this list therefore becomes 'GPCR signaling 419 g alpha q'. The 'collagen formation' and 'class b 2 secretin family receptors' 420 pathways are also removed because the differentially expressed genes they cover 421 are additionally covered by the more enriched pathways 'extracellular matrix 422 organization' and 'signal transduction' pathways (respectively). Additionally, 423 'GPCR signaling pertussis toxin' and 'GPCR signaling cholera toxin' are absent from 424 the returned list, as all of their differentially expressed genes are found in 'GPCR 425 signaling g alpha q' or 'signal transduction'. 426

Some pathways in the enrichment set cover do still show high levels of overlap, for
example 'wnt signalling network' is included despite 89% of its differentially

- 429 expressed genes being covered by 'signal transduction'. This is acceptable because
- 430 'signal transduction' is more highly enriched than 'wnt signalling network', yet the
- 431 'wnt signalling network' is worth including as it contains three differentially
- 432 expressed genes that are not in 'signal transduction'. If 'wnt signalling network'

had been excluded then these genes would not have been described by the most
significant pathway available to represent them. The unmodified top ten enriched
pathways only cover 78.0% of the enriched genes. Using the set cover enrichment
algorithm increases this figure to 85.2% without disrupting the pathway order

- 437 given by the enrichment p-values.
- 438

### 439 6. Discussion and conclusion

440 We described algorithms suitable for reducing overlap in large pathway data sets 441 allowing multiple databases to be amalgamated without excessive redundancy impeding the usefulness of the resource. Standard set cover is the best algorithm 442 to reduce the number of pathways required to cover the data set, but significantly 443 increases pathway size, which can be controlled by proportional set cover or 444 hitting set cover. The proportional set cover is the best algorithm for controlling 445 446 pathway size and the hitting set cover is the preferred choice for covering all of the genes in the dataset with minimal pathway redundancy. We showed that reducing 447 the *GC* parameter allows further reductions in pathway redundancy; for example, if 448 449 only 95% of the genes in the CPDB dataset were covered redundancy can be 450 reduced by up to 88%. In addition reducing GC increases pathway size control 451 when the proportional set cover and hitting set cover algorithms are used. 452

452

For pathway enrichment analysis we aimed to reduce redundancy while selectingthe most significantly enriched pathways based on p-values. As an application we

455 used the modified set cover algorithm to reduce the results of enrichment analysis

456 from a large osteoarthritis data set. We found that 5 out of the 10 top ranking

457 pathways could be omitted as they were subsets of more highly enriched

458 pathways. Overlap between pathways returned from enrichment data is not

459 always immediately obvious and requires further consideration. By reducing this

460 redundancy, data interpretation is made more intuitive. Reducing redundancy also

- allows the user to explore substantially more of the data set using the same
- 462 number of pathways.
- 463

464 The enrichment set cover algorithm presented within this study differs from

465 existing methods implemented by ReCiPa and Pathcards, since enrichment

466 analysis is performed prior to reduction of redundancy. This is because the

different sets of pathway boundaries available in the full dataset may optimally fit

- the differentially expressed genes. For example, comparison of the 'apoptosis'
- taken from KEGG, Reactome and Wikipathways, reveals that many of the proteins
- are specific to a single database [22]. This is due to the vague definition of pathway
- 471 boundaries, as well as differing experimental focus on cellular contexts, such as
- tissues or disease states. Following enrichment analysis the pathways that are
- 473 most significantly enriched are selected to represent the differentially expressed

474 genes and superfluous pathways are removed. This prevents the top results from

- being dominated by large numbers of highly similar pathways.
- 476

477 Set cover uses greedy heuristic methods, which provide good approximations of

- 478 the optimal solution in a time effective manner. These methods are extremely
- 479 efficient and can be run in a matter of minutes, however it should be noted that
- 480 they do not guarantee an optimal solution. This is particularly true for the
- 481 proportional set cover algorithm where the randomness of early selections
- 482 influences the result. However, all possible outcomes result in reduced
- 483 redundancy. The enrichment set cover algorithm is exempt from these
- 484 considerations unless multiple pathways have identical p-values.
- 485
- 486 We have provided a method to dramatically reduce redundancy in pathways
- 487 facilitating a more concise portrayal of cellular processes, while avoiding the issues
- 488 introduced by pathway merging. Our algorithms are publicly available and have
- 489 wide applicability to analysis of pathway datasets from any organism.
- 490

### 491 **7**. List of abbreviations

- 492 CPDB Consensus PathwayDB
- 493 GC Gene cover
- 494 SNP Single nucleotide polymorphism
- 495

### 496 8. Declarations

- 497 <u>Ethics approval and consent to participate</u> NA
- 498 <u>Consent for publication</u> NA
- 499 <u>Availability of data and materials</u>: https://github.com/RuthStoney/set-cover-and-
- 500 set-packing-to-reduce-redundancy-in-pathway-data
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- 507
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- 510

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577

578

### 579 10. Figure legends

- 580
- 581 Figure 1. Set cover A) A simple set of overlapping sets. B) The red set with 8
- 582 uncovered elements is selected first. C) The blue set with 3 elements is selected
- 583 second. D) The orange set then covers all the elements in the universe.
- Figure 2. Jaccard coefficient between pathway pairs in the cover set results produced
  by each algorithm.
- 586
- 587 Figure 3. Redundancy in set cover outputs given different GC values.

588

Figure 4. Pathway sizes in cover set when GC is set to A) 100%, B) 99%, C) 95% and
D) 90%. The boxes indicate the 25th and 75th percentiles and the whiskers indicate
the 5th and 95th percentiles.

592

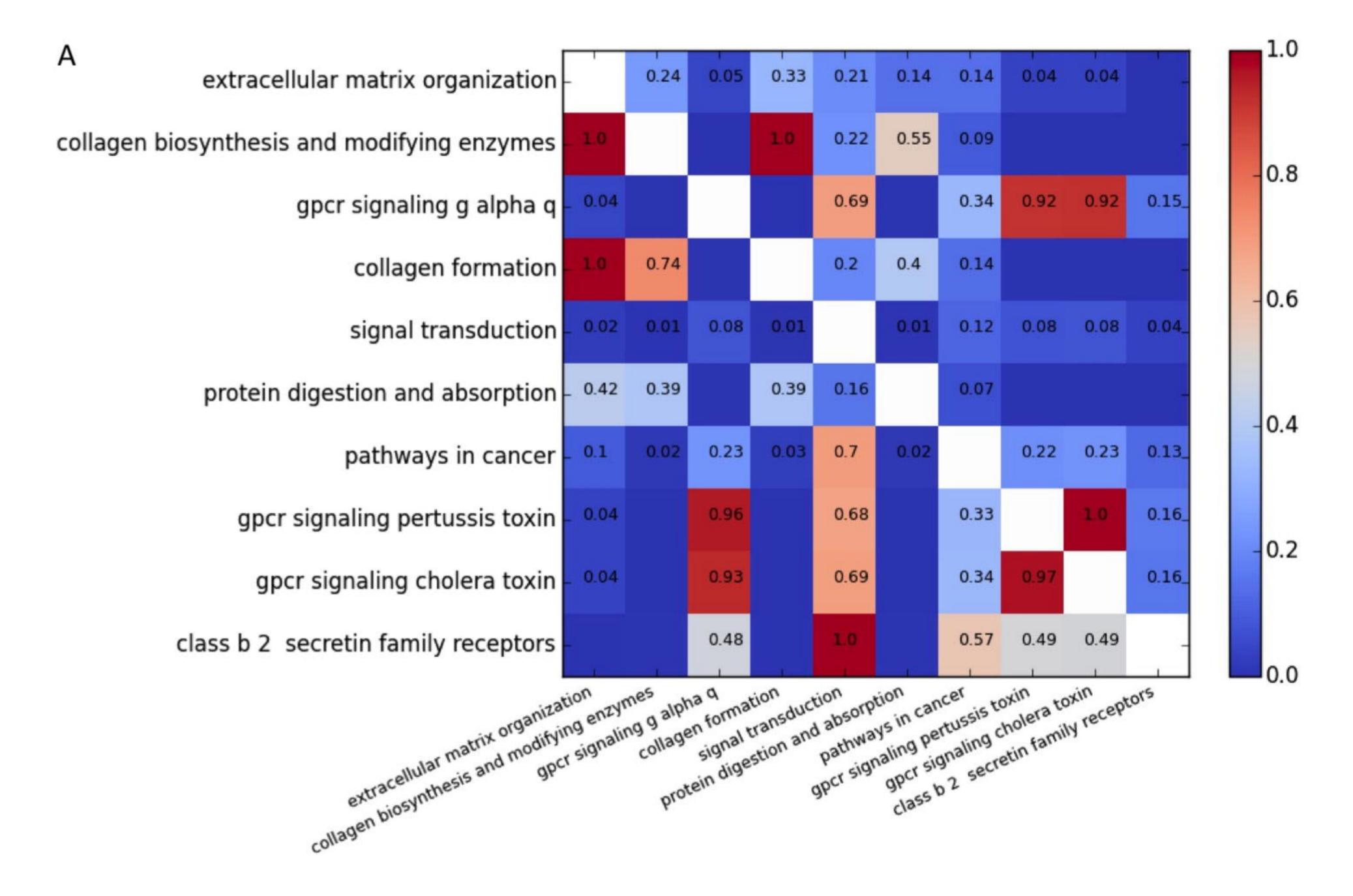
Figure 5. Pathway redundancy heat maps. (A) Pathway overlap for top ten enriched
pathways. (B) Pathway overlap for top ten enriched pathways after application of set
cover. The values represent asymmetric overlap, i.e. for each pathway shown on the
left axis, values represent the proportion of genes that are also included in the
pathway shown on the bottom axis.

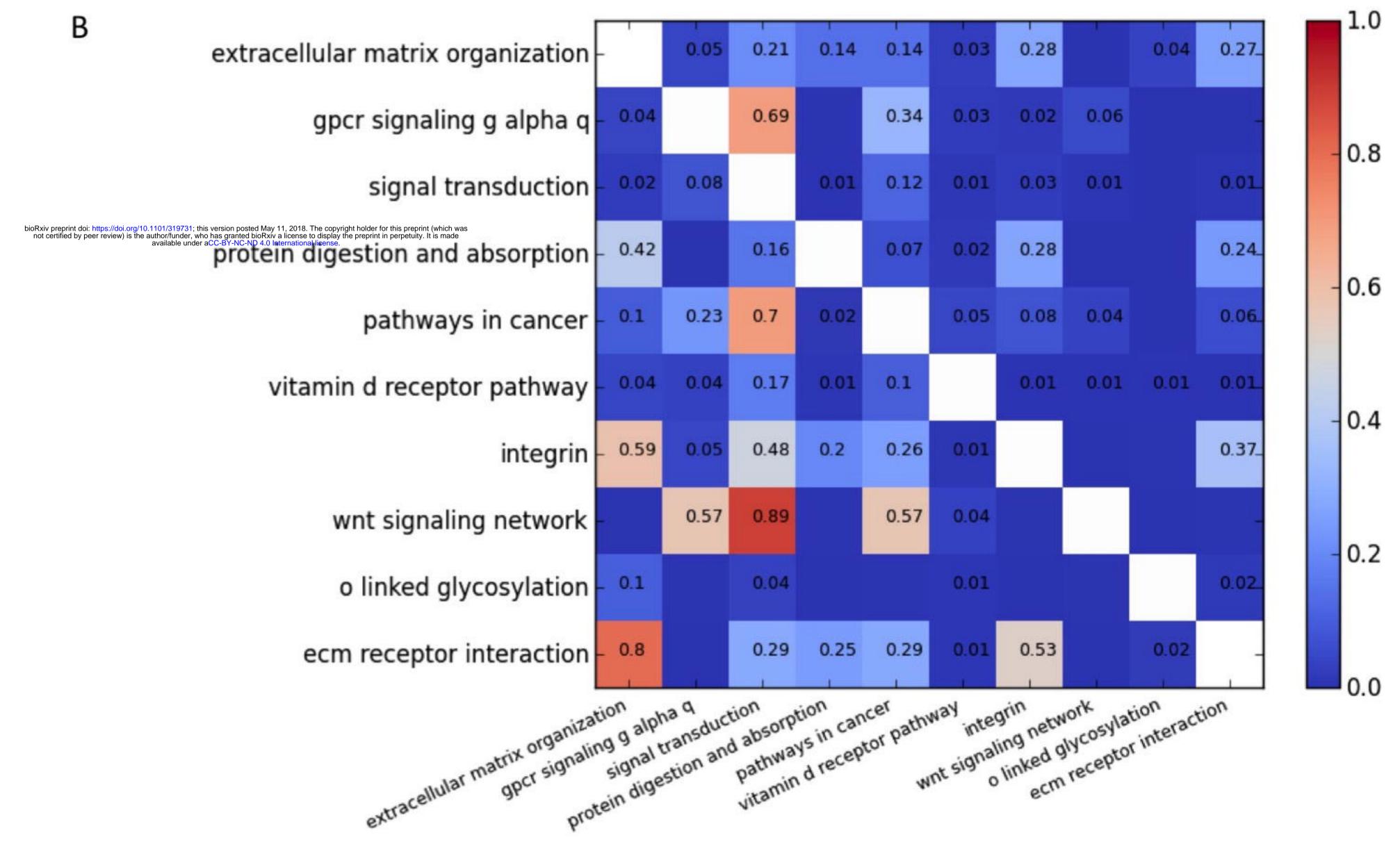
598

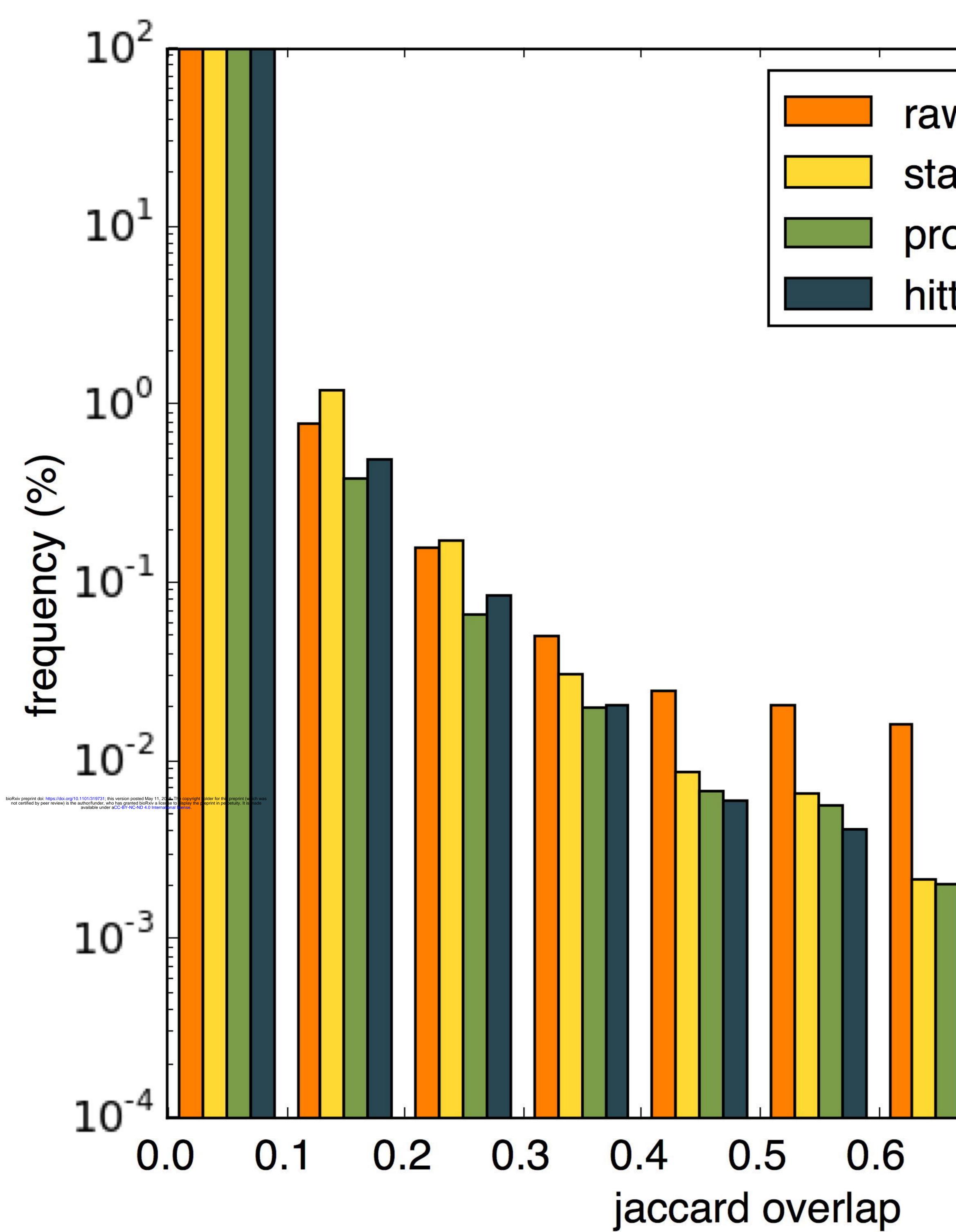
### 599 11. Additional material

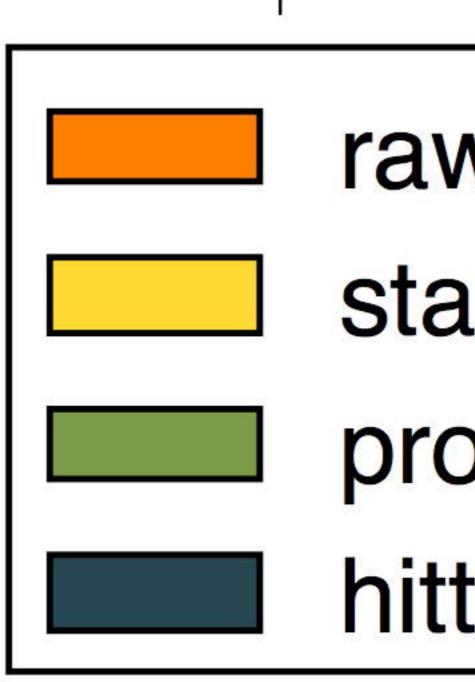
- 600 Supplementary table 1: Enriched pathways from the osteoarthritis dataset (p-
- value<0.05). The set cover column indicated the 23 pathways that were included
- 602 in the set cover. Found in additional file 1.docx.

603 604

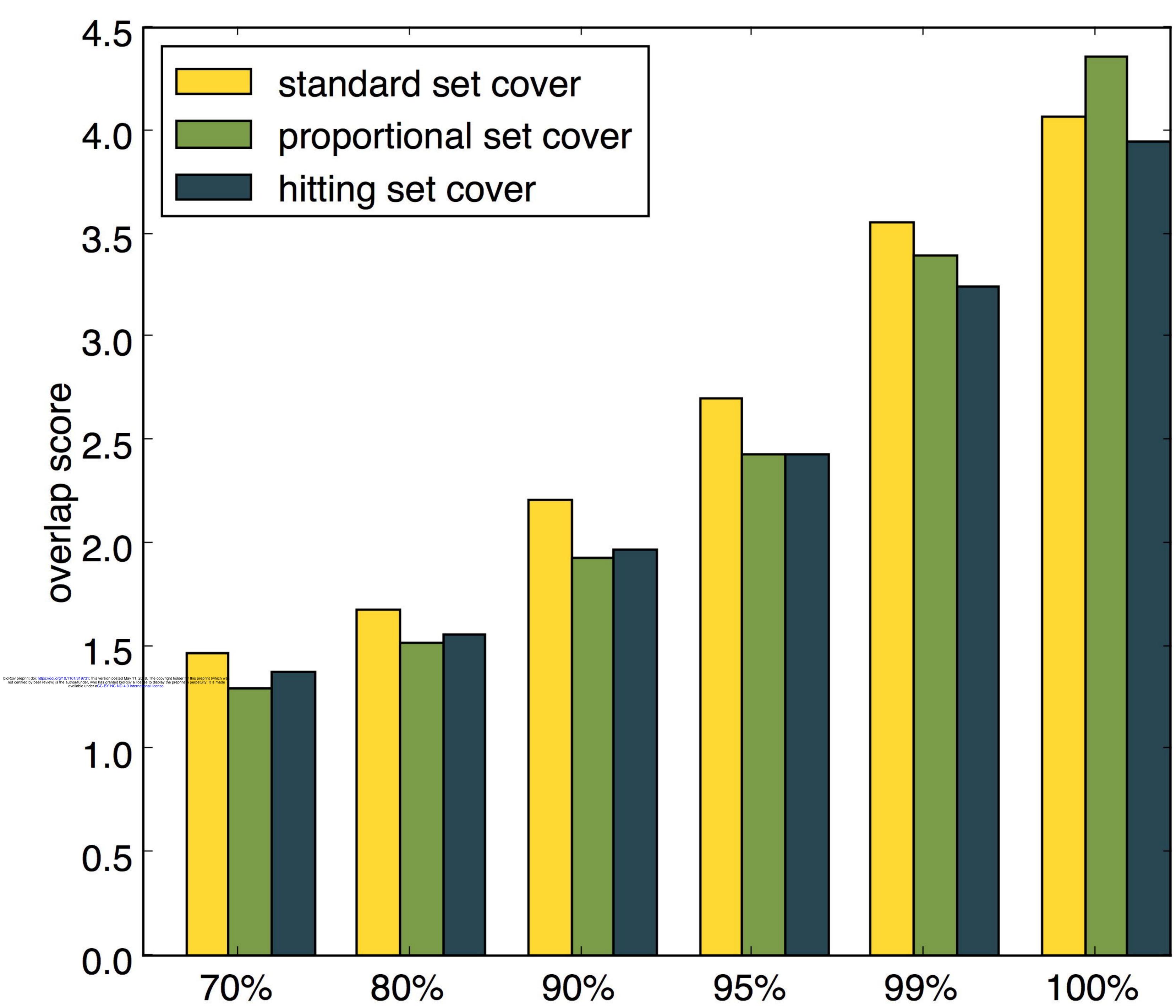




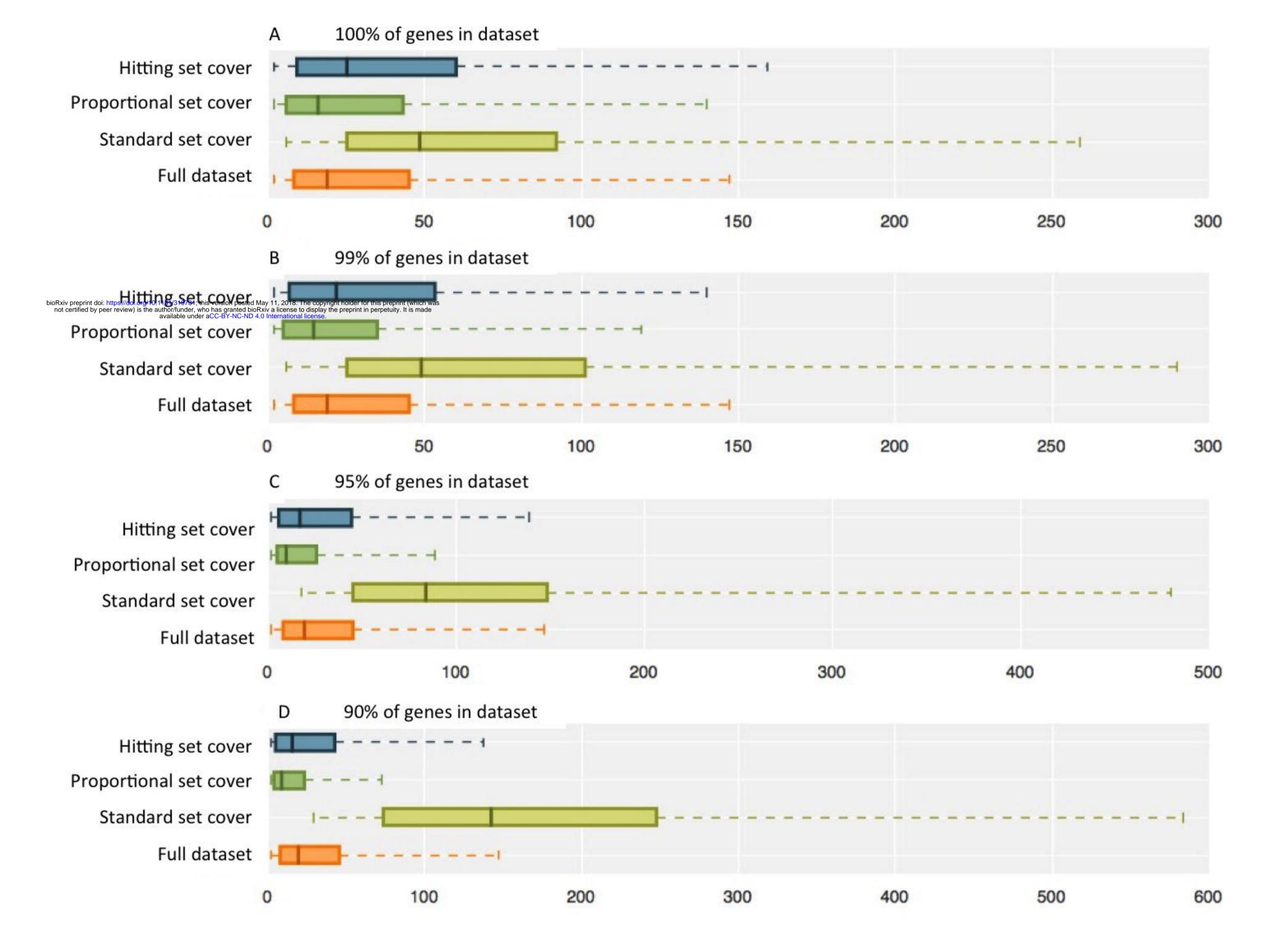




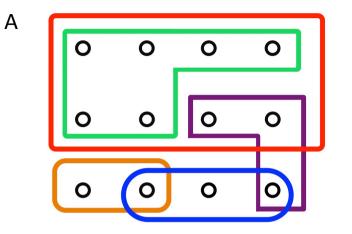
# raw data standard set cover proportional set cover hitting set cover 0.7 **0.8** 0.9 1.0

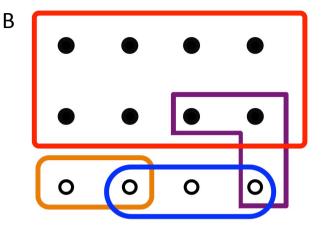


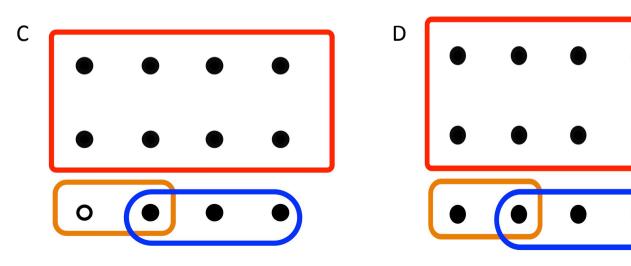
% genes for data set covered



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Set Cover Start with  $\mathbf{R} = \mathbf{U}, \mathbf{C} = \emptyset$  and  $\mathbf{SC} = \emptyset$ while |C| / |U| \* 100 < GC do Select set  $s_i$  that maximizes  $v_i$ Add  $s_i$  to SCAdd the elements in  $s_i$  to C Delete the elements in  $s_i$  from Rend

Return SC