## Senescence of multicellular individuals: imbalance of epigenetic and non-epigenetic information in histone modifications

Felipe A. Veloso (1) Facultad de Ciencias, Universidad Mayor, Santiago, Chile. (Dated: April 27, 2018)

Cellular aging has been progressively elucidated by science. However, aging at the multicellular-individual level is still poorly understood. A recent theory of individuated multicellularity describes the emergence of crucial information content for cell differentiation. This information is mostly conveyed in the non-epigenetic constraints on histone modifications near transcription start sites. According to this theory, the non-epigenetic content emerges at the expense of the information capacity for epigenetic content. However, it is unclear whether this "reassignment" of capacity continues after adulthood. To answer this question, I analyzed publicly available high-throughput data of histone H3 modifications and mRNA abundance in human primary cells. The results show that the "reassignment" continues after adulthood in humans. Based on this evidence, I present a falsifiable theory describing how continued "reassignment" of information capacity creates a growing epigenetic/non-epigenetic information imbalance. According to my theoretical account, this imbalance is the fundamental reason why individuated multicellular organisms senesce.

Keywords: aging; ageing; cancer; constraints; naked mole-rat; bristlecone pine; Turritopsis; gene regulation; epigenetics; teleodynamics

the immortality of cultured somatic cells was indeed a 17 widely-held belief [3]. That changed only when Hayflick & Moorhead showed that cultured human somatic cells do stop dividing and become less viable once their 20 divisions reach a certain number [4], a phenomenon known 21 today as the Hayflick limit [3]. This loss of replicative 22 capacity and, in general, the process of aging at the cellular level, have been found to correlate with telomere length [3,5,6]. Yet, the number of times human cells can divide in culture exceeds the number of times cells divide 26 throughout our lifespan; there is no significant correlation <sub>27</sub> between human cell replicative capacity and cell donor 28 age [7]. That is, we—and individuated multicellular <sup>29</sup> organisms in general—age before most of our cells do [8,9]. The outstanding question is why.

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Theoretical descriptions of senescence or aging at the 32 multicellular-individual level have been classified into 33 two categories: programmed senescence and senescence caused by damage/error [10]. Recently it has been 35 argued, however, that senescence is not programmed nor is it ultimately a consequence of damage or error in the organism's structure/dynamics [11]. Instead, may be a byproduct of maintenance and/or 40 in part by intracellular signaling pathways such as 41 the cell-cycle-related PI3K/AKT/mTOR pathway [11]. These pathways have been shown to modulate aging 43 at the cellular level in species such as the yeast 44 Saccharomyces cerevisiae [13].

analogous notion The of aging at $_{
m the}$ 46 multicellular-individual level as a byproduct

Our intellectual endeavors have entertained the 47 certain functional signaling pathways [11] is, in principle, prospect of unlimited lifespan for centuries [1], and the 48 supported by the fact that the deficiency of mTOR 15 scientific endeavor has been no exception [2]. In the 1950s, 49 kinase—a key component of the PI3K/AKT/mTOR 50 pathway—can double the lifespan of the roundworm 51 Caenorhabditis elegans [14]. However, the fundamental 52 dynamics that make individuated multicellular organisms 53 senescent after adulthood remain unclear and largely 54 lack falsifiable scientific theories. Falsifiability—the 55 possibility of establishing a hypothesis or theory as 56 false by observation and experiment [15]—allows the 57 objective rejection of existing scientific theories, fosters 58 the development of new ones, and constitutes the 59 most widely accepted demarcation between science 60 and non-science [16].

Using publicly available high-throughput data of 62 histone H3 modifications and mRNA abundance in human 63 primary cells to look for proof of concept, the issue of 64 senescence can also be approached from the angle of 65 theoretical biology. Thus, I conducted a statistical data 66 analysis in this study, which revealed that proof of concept 67 exists for the human species. These findings provide 68 empirical grounds for my theoretical work, suggesting that 69 senescence is a byproduct of functional developmental 70 dynamics as first described by a recently proposed 71 theory of individuated multicellularity [17]. Specifically, 72 I show that the byproduct is a post-ontogenetic, <sup>39</sup> developmental dynamics [11,12], themselves underpinned <sup>73</sup> growing imbalance between two different information 74 contents conveyed respectively in two different types of 75 constraints on histone post-translational modifications 76 near transcription start sites (TSSs). Constraints are 77 here understood as the local and level-of-scale specific 78 thermodynamic boundary conditions required for energy 79 to be released as work as described by Atkins [18]. 80 The concept of constraint is crucial because, according to 81 the theory of individuated multicellularity, a higher-order 82 constraint (i.e., a constraint on constraints) on changes 83 in histone modifications harnesses critical work that

Correspondence: veloso.felipe.a@gmail.com

89 the dynamics of the lower-order constraints must be 108 capacity of histone modifications to convey information 90 explicitly unrelated to each other (i.e., statistically 109 content, which has allowed the prediction of mRNA 91 independent) in order to elicit the emergence of 110 levels from histone modification profiles near TSSs with 92 the intrinsic higher-order constraint. Along with the 111 high accuracy [23]. 93 emergence of this intrinsic higher-order constraint, the 112 94 theory of individuated multicellularity describes the 113 nonnegative measure of multivariate statistical association 95 emergence of critical information content, named in the 114 known as total correlation [24] or multiinformation [25] <sub>96</sub> theory hologenic content, which is about the multicellular <sub>115</sub> (symbolized by C and typically measured in bits), the 97 individual as a whole in terms of developmental 116 overall observable histone crosstalk can be decomposed. 98 self-regulation. Thus, for the sake of brevity, I here refer 117 That is, histone crosstalk, if measured as a total hologenic theory.

102 histone modifications are generally known as histone 121 (i.e., explicitly unrelated to changes in gene expression).

104 be relevant for epigenetic changes [21], which are defined Under the theory of individuated multicellularity, 105 as changes in gene expression that cannot be explained the intrinsic higher-order constraint is the simplest 106 by (i.e., that are explicitly unrelated to) changes in the multicellular individual in fundamental terms. In addition, 107 DNA sequence [22]. This relevance is underpinned by the

Based on these considerations and the properties of the to the theory of individuated multicellularity as the  $_{118}$  correlation C, is the sum of two explicitly unrelated C components: one epigenetic (i.e., explicitly related to The constraints on the combinatorial patterns of 120 changes in gene expression) and the other non-epigenetic 122 This sum can be expressed as follows:

$$\underbrace{C(X_1,\ldots,X_n)}_{\text{Overall histone crosstalk}}$$
 (total correlation of  $X_1,\ldots,X_n$ )

Epigenetic histone crosstalk (total correlation of 
$$X_1, \ldots, X_n$$
 that is explicitly related to  $Y$ ), depends on DNA-nucleosome interactions (Ref. 17), and conveys

epigenetic information content

Non-epigenetic histone crosstalk (total correlation of 
$$X_1, \ldots, X_n$$
 that is explicitly unrelated to  $Y$ ), depends on protein/RNA-nucleosome interactions (Ref. 17), and conveys hologenic information content

(1)

124 histone modification levels in specific genomic positions 151 has a finite information capacity, which can be measured 130 and references therein).

132 component of histone crosstalk (represented by 159  $_{133}$   $C_Y(X_1,\ldots,X_n,Y)$  in the sum decomposition of Eq. 1) 160 condition for the evolution of individuated multicellular importantly, also for undifferentiated stem cells.

141 known to grow in magnitude during development until the 168 magnitude of the non-epigenetic histone crosstalk (i.e., the <sub>142</sub> organism's mature form is reached [17]. This component <sub>169</sub>  $C(X_1,\ldots,X_n|Y)$  summand in Eq. 1) within other 143 is described by the hologenic theory as conveying 170 cells' nuclei, and (iii) affected in their extracellular 144 information about the multicellular individual as a 171 diffusion dynamics by the geometrical complexity of the 145 whole—starting from the moment said individual emerges 172 extracellular space (i.e., constraints on diffusion at the 147 embryo's proliferating cells.

where  $X_1, \ldots, X_n$  are random variables representing  $n_{150}$  not infinite. In other words, the overall histone crosstalk with respect to the TSS and Y is a random variable 152 in bits. Moreover, the sum decomposition in Eq. 1 implies 126 representing either gene expression level, transcription 153 that the growth in magnitude (bits) of the hologenic 127 rate, or mRNA abundance level associated with the TSS. 154 (i.e., non-epigenetic) component must be accompanied These levels are equivalent for the decomposition because 155 by a decrease in magnitude of the epigenetic component. of the strong correlation that exists between them ([26] 156 That is, the capacity (in bits) for hologenic information 157 content in histone crosstalk is bound to grow at the The hologenic theory describes how the epigenetic 158 expense of the capacity for epigenetic information content.

The hologenic theory also maintains that a necessary conveys information about each cell's transcriptional 161 lineages was the appearance of a class of molecules profile. This component is, in information content 162 synthesized by the cells—called Nanney's extracellular terms, the dominating component for any eukaryotic 163 propagators (symbolized by  $F_N^{\rightarrow}$ ) in the theory [17]. colonial species (such as the alga Volvox carteri [27]) and, 164 These  $F_N^{\rightarrow}$  molecules are predicted to be, in a given 165 tissue and time period, (i) secretable into the extracellular The second, non-epigenetic component of histone 166 space, (ii) once secreted, capable of eliciting a significant crosstalk (represented by  $C(X_1,\ldots,X_n|Y)$  in Eq. 1) is 167 incremental change (via signal transduction) in the as an intrinsic higher-order constraint on the early 173 multicellular-individual level, which cannot be reduced to 174 constraints at the cellular level). Also under the hologenic Importantly, the overall observable histone crosstalk 175 theory, for the multicellular individual to develop and <sub>149</sub> magnitude (represented by  $C(X_1,\ldots,X_n)$  in Eq. 1) is <sub>176</sub> survive, both hologenic (developmental self-regulation of

cell's transcriptional profile) contents must coexist.

does. For this reason, histone crosstalk constraints were 204 as proof of concept. expected to have relevance for senescence but only at a 205 been studied in detail before.

192 "reassignment" of information capacity for epigenetic 210 positively correlated with cell donor age (over a range of 193 and non-epigenetic (i.e., hologenic) content stops when 211 0-90 years old) and (ii) no such statistically significant 194 development reaches the multicellular individual's mature 212 correlation exists for primary cancer cells (see Fig. 1).

177 the multicellular individual overall) and epigenetic (each 195 form or instead continues without interruption, one also 196 needs to investigate the "reassignment" (if any) in cancer One final but important consideration regarding 197 cells. One of the corollaries of the hologenic theory is histone crosstalk is that it is the result of constraints 198 a significant loss of hologenic content in cancer cells, which, as mentioned previously, are level-of-scale specific. 199 because they are no longer constrained by the multicellular 182 To exemplify this specificity, consider the example of an 200 individual that normal (i.e., non-cancerous) cells serve and 183 internal combustion engine: a single molecule in a cylinder 201 are constrained by. Thus, I developed a falsifiable theory wall does not embody a constraint on the expansion 202 of senescence based on the post-ontogenetic continuation 185 of the igniting gas, yet the cylinder-piston ensemble 203 of this "reassignment" process in human histone crosstalk

To test this theory, I formalized the proof of concept 188 specific level of scale. The specific level of scale in histone 206 into the following two hypotheses: (i) within genomic 189 crosstalk that is relevant for human senescence has not 207 regions adjacent to TSSs in primary normal cells, the 208 log-ratio between the non-epigenetic and epigenetic To investigate from a theoretical angle if the 209 histone H3 crosstalk magnitudes is significantly and

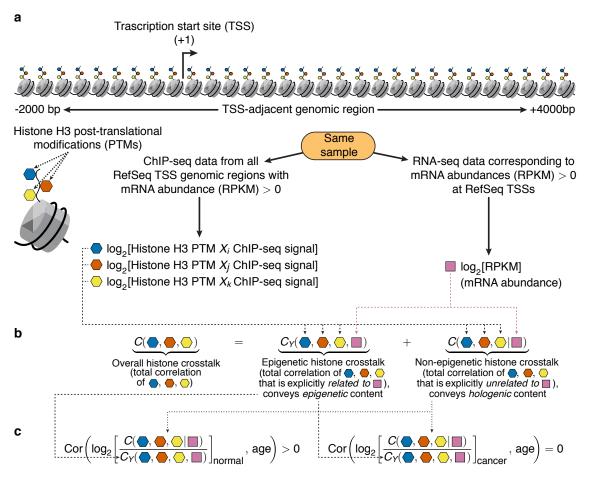


Fig. 1. Schematic for proof-of-concept hypotheses and computational analysis for testing. Publicly available ChIP-seq (chromatin immunoprecipitation followed by high-throughput DNA sequencing) and RNA-seq (transcriptome high-throughput sequencing) data for human primary cell samples allowed the computation, for each TSS, of position-specific histone H3 modification levels (at every 200bp) and its associated mRNA abundance level (a). After log-transforming these levels and taking into account all TSSs, the TSS-adjacent histone H3 crosstalk (triad-wise crosstalk depicted here) was represented as a total correlation [24] or information capacity in bits, which in turn was decomposed as the sum of two measurable and explicitly unrelated components: one epigenetic (explicitly related to transcriptional changes) and the other non-epigenetic (explicitly unrelated to said changes) (b). Taking into account all samples, the log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude was hypothesized to be positively correlated with cell donor age in normal cells (c, left) and also to be uncorrelated with cell donor age in cancer cells (c, right). The subsequent rejection of the statistical null hypothesis in (c, left) and the failure to reject the statistical null hypothesis in (c, right) provided proof of concept for the theory of senescence proposed in this paper.

Using these tandem ChIP-seq and RNA-seq data, quantified the non-epigenetic and epigenetic 228 histone H3 crosstalk magnitudes (Eq. 1) for triads of variables  $\{X_i, X_i, X_k\}$ . These variables represented 230 position-specific histone H3 modification i.e.,  $C(X_i, X_i, X_k | Y)$  and  $C_Y(X_i, X_i, X_k, Y)$ 232 the non-epigenetic and epigenetic histone crosstalk 233 components, respectively, where Y represents mRNA 234 abundance. Triads (as opposed to pairs or tetrads) were 235 first analyzed because a triad constitutes the number 236 of variables (i.e., position-specific histone modification 237 levels) found to possess both significant predictive 238 power and predictive synergy to resolve the statistical 239 uncertainty about the mRNA abundance level associated 240 with a given TSS (see details in Methods).

242 epigenetic histone H3 crosstalk magnitudes was thus 243 computed as the dimensionless quantity

$$\log_2 \left[ \frac{C(X_i, X_j, X_k | Y)}{C_Y(X_i, X_j, X_k, Y)} \right]. \tag{2}$$

Importantly, total correlation C captures all possible 245 associations in the set of variables  $\{X_i, X_i, X_k\}$  that may 246 exist starting from the pairwise level.

> The log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude is positively correlated with cell donor age in normal cells

ChIP-seq data for five histone H3 modifications 248 were used in all analyses: H3K4me1 (histone H3 249 lysine 4 monomethylation), H3K9me3 (histone H3 250 lysine 9 trimethylation), H3K27ac (histone H3 251 lysine 27 acetylation), H3K27me3 (histone H3 lysine 27 252 trimethylation), and H3K36me3 (histone H3 lysine 36 253 trimethylation). The ChIP-seq signals for these 254 modifications were computed for 30 200bp-long genomic 255 bins across a 6,000bp-long TSS-adjacent region (see Fig. 1). Thus, a total of 150 variables  $X_i$  representing

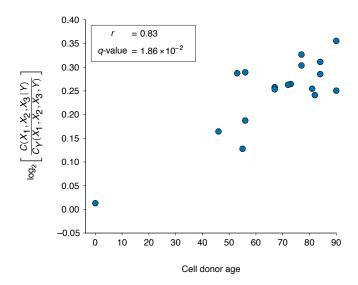


Fig. 2. Positive correlation between the log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude and cell donor age for one triad of position-specific histone H3 modification levels in normal cells. In this triad  $X_1$  represents  ${
m H3K27ac}$  (at  ${
m -1000bp}$ ),  $X_2$  represents  ${
m H3K36me3}$  (at  ${
m +1000bp}$ ), and  $X_3$  represents H3K4me1 (at +3200bp), which together comprise all TSSs. Regardless of the specific triad, Y always represents the mRNA abundance profile comprising all TSSs. Each data point in the figure corresponds to a primary cell sample.

position-specific histone H3 modification levels—each variable with signals for 18,220 RefSeq TSSs—were used when analyzing each cell sample. A total of 18 normal 260 cell samples and 17 cancer cell samples was included The log-ratio (base 2) between the non-epigenetic and  $^{261}$  in the analysis. The Pearson correlation coefficient r $_{262}$  between the log-ratio and the cell donor age was obtained 263 for each of the  $\binom{150}{3} = 551{,}300$  possible  $\{X_i, X_j, X_k\}$ <sup>264</sup> triads. The 551,300 p-values (one-sided Student's t-test)  $_{265}$  associated to these r values were then corrected for 266 multiple testing (Benjamini-Yekutieli correction, see Methods), obtaining q-values.

> To determine whether the hypothesized positive 269 correlation between the non-epigenetic/epigenetic 270 histone H3 crosstalk log-ratio and cell donor age exists, 271 and also to illustrate the concept of positive correlation in 272 normal cells vs. no correlation cancer cells, I obtained all 273 possible 551,300 correlation values for triads (one-sided 274 Student's t-test). To exemplify, the results for the triad 275 {H3K27ac (at -1000bp), H3K36me3 (at +1000bp),  $_{276}$  H3K4me1 (at +3200bp)} are shown here, where the 277 correlation was positive (r=0.83) and highly significant  $_{278}$  ( $q=1.86\times10^{-2}$ ), as seen in Fig. 2, indicating that the 279 hypothesized correlation holds for this triad.

> Altogether, the 551,300 correlation values had a mean value  $\bar{r}=0.58$ , a median value  $\tilde{r}=0.67$ , and a standard 282 deviation value  $\sigma_r$ =0.24 (see statistical distribution  $_{283}$  of r in Fig. 3). From these correlation values, only  $_{284}$  24,185 (i.e.,  $\sim$ 4%) were nonpositive and none of them 285 was statistically significant (i.e., where  $r \le 0$ , q > 0.05). 286 In contrast, it was found that for 315,378 triads

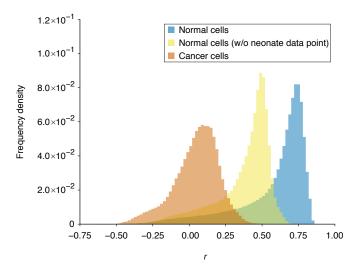


Fig. 3. Statistical distribution of the correlation coefficient between the log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude (triad-wise) and cell donor age. Histograms represent r values for all 551,300 possible triads in normal cells (blue), normal cells excluding the neonate data point (yellow), and cancer cells (orange).

 $_{287}$  (i.e.,  $\sim 57\%$ ) the correlation values were positive and statistically significant (i.e., r>0 and  $q\leq0.05$ ).

Importantly, I also found that the hypothesized positive 290 correlation between the log-ratio of non-epigenetic to <sup>291</sup> epigenetic histone H3 crosstalk and cell donor age verified 292 for triads of position-specific histone H3 modifications 293 in normal cells loses its strength for tetrads ( $\bar{r}=0.34$ ;  $\tilde{r}=0.35$ ;  $\sigma_r=0.27$ ). It is also no longer greater than <sup>295</sup> zero for pairs ( $\bar{r}=-0.30$ ;  $\tilde{r}=-0.38$ ;  $\sigma_r=0.40$ ) (Fig. 4). 296 These results for tetrads and pairs indicate that the 297 predicted positive correlation only holds for triads 298 (and it was predicted in the second proof-of-principle 299 hypothesis not to hold in cancer cells). Such specificity 300 was expected because if senescence can be explained 301 in terms of an imbalance of information-conveying 302 constraints that are level-of-scale specific like other 303 thermodynamic constraints, the imbalance itself also must 304 be level-of-scale specific.

### The log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude does not correlate with cell donor age in cancer cells

 $_{311}$  q=1; see Fig. 5), as hypothesized.

313 all triads of position-specific histone H3 modifications 324 as predicted, no significant correlation exists between 314 in cancer cells, the mean and median were close to 325 the log-ratio of non-epigenetic to epigenetic histone H3  $_{315}$  zero ( $\bar{r}$ =0.05;  $\tilde{r}$ =0.07), and the standard deviation was  $_{326}$  crosstalk magnitude and cell donor age in cancer cells.

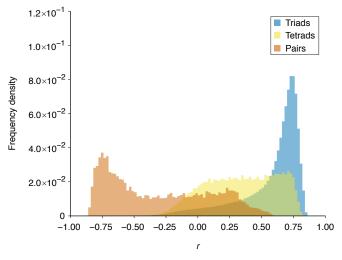


Fig. 4. Statistical distribution of the correlation coefficient between the log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude and cell donor age for triads, tetrads, and pairs of position-specific histone H3 modification levels. Histograms represent r values for all 551,300 possible triads (blue), 50,000 random tetrads (yellow), and all 11,175 possible pairs (orange).

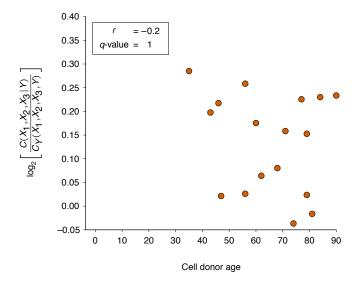


Fig. 5. No significant correlation between the log-ratio of non-epigenetic to epigenetic histone H3 crosstalk magnitude and cell donor age for one triad of position-specific histone H3 modification levels in cancer cells. This is the same triad of Fig. 2, i.e.,  $X_1$  representing H3K27ac (at -1000bp),  $X_2$  representing  ${
m H3K36me3}$  (at  ${
m +1000bp}$ ), and  ${
m X_3}$  representing  ${
m H3K4me1}$  (at  ${
m +3200bp}$ ).

When I analyzed the log-ratio of non-epigenetic to  $\sigma_r = 0.15$  (see statistical distribution of r in Fig. 3). epigenetic histone H3 crosstalk magnitude and cell 317 All associated p-values (two-sided Student's t-test) were donor age for cancer cells using the same exemplary 318 corrected and the resulting q-values were all equal to so triad (H3K27ac (at -1000bp), H3K36me3 (at +1000bp), sign 1 and hence non-significant. Similar results—i.e., all  $_{309}$  H3K4me1 (at +3200bp), I found that no significant  $_{320}$  q-values equal to 1—were obtained for all 11,175 pairs of 310 correlation exists between those two variables (r=-0.2; 321 position-specific histone H3 modification levels ( $\bar{r}=-0.04$ ;  $\tilde{r}=-0.05$ ;  $\sigma_r=0.23$ ) and for all 50,000 random tetrads For the 551,300 correlation values corresponding to  $_{323}$  ( $\bar{r}$ =0.08;  $\tilde{r}$ =0.11;  $\sigma_r$ =0.15). These results suggest that,

that corresponds to a neonate, with coordinates (0,0.01) 381 contraction" problem. in Fig. 2. In other words, whether the neonate data point 382 334 nonexistent difference between normal and cancer cells in 384 the primary cell samples analyzed given the different the analysis. 335

values corresponding to normal cells, excluding the 387 a theory of senescence presented in the Discussion. neonate data point. The mean, median, and standard deviation values obtained were  $\bar{r}=0.38$ ,  $\tilde{r}=0.44$ , and  $\sigma_r$ =0.19, respectively (see distribution of r in comparison with that for cancer cells in Fig. 3). This difference  $_{342}$  between r values for normal cells (neonate data point  $_{388}$ 243 excluded) and cancer cells was further tested and shown to 389 hypotheses in the present work provides empirical grounds be highly significant (Mann-Whitney U test:  $U=2.7\times10^{11}$ , 390 for the following falsifiable theory of senescence as a  $p < 2.2 \times 10^{-16}$ ). These findings suggest that the neonate 391 byproduct of developmental dynamics: Given that the <sup>346</sup> data point is not a statistical outlier among normal <sup>392</sup> "reassignment" process for information capacity in histone 347 cell samples let alone explains the difference between 393 crosstalk—i.e., a progressive gain of capacity for hologenic 348 normal and cancer cells in terms of the correlation 394 information content at the expense of that for epigenetic 349 values obtained.

### The total information capacity of triad-wise histone H3 crosstalk does not correlate with cell donor age

Finally, I assessed whether the total information capacity (represented by  $C(X_1, \ldots, X_n)$  in Eq. 1 and 352 measured in bits) of overall histone H3 crosstalk 353 (triad-wise) is significantly correlated with age, in particular, whether it is positively correlated. This potential correlation is important, because if total information capacity increases with cell donor age,  $_{408}$ for epigenetic content would not be necessarily a problem. That is, a proportionally smaller and smaller information capacity for epigenetic content within histone crosstalk would not generate an information content imbalance—hypothesized in the Introduction—as long as a growing total capacity provides enough room for epigenetic content in absolute terms.

TSS-adjacent histone H3 crosstalk, computed as

$$C_Y(X_i, X_j, X_k, Y) + C(X_i, X_j, X_k | Y),$$
 (3)

was obtained for all 551,300 triads of position-specific  $^{422}$ histone H3 modifications for normal cells.

 $_{371}$  have mean, median, and standard deviation values  $\bar{r}$ =0.21,  $_{425}$  precision of transcription in the cells with respect to <sub>373</sub> q-values were equal to 1 and thus non-significant. <sup>427</sup> accuracy (i.e., closeness of the mean mRNA level to the For cancer cells, all correlation values were also 428 mean level functional for the multicellular individual) is non-significant (q=1). Their mean, median, and standard 429 reached with age at the expense of precision (i.e., closeness deviation values were  $\bar{r}$ =0.01,  $\tilde{r}$ =0.04, and  $\sigma_r$ =0.18, 430 of the resulting mRNA levels from the same pattern

I also evaluated whether the stark difference of the 377 respectively. These results suggest that senescence correlation values between normal—i.e., r markedly 378 would indeed be an information capacity "reassignment" positive—and cancer cells—i.e., r close to zero—was only 379 problem—creating in turn an information-content attributable to the data point (for normal cell samples) 380 imbalance, as hypothesized—rather than a "total capacity

Taken together, the statistical strength of all the results was simply a statistical outlier that created an otherwise 383 obtained—notwithstanding the heterogeneous origin of 385 tissues from different individuals—provides proof of For this purpose, I recomputed all 551,300 correlation 386 concept and underpins a strong falsifiable prediction for

#### DISCUSSION

The successful testing of the two proof-of-concept 395 content—continues without interruption throughout 396 the multicellular individual's lifespan, a growing and 397 ultimately lethal information content imbalance is created 398 in the cells' nuclei. Importantly, this "reassignment" 399 process is underpinned by constraints on the extracellular 400 diffusion of  $F_N^{\rightarrow}$  molecules, and the constraints are 401 embodied only at the multicellular-individual level. 402 That is, in histone crosstalk there is a time-correlated 403 loss of capacity for epigenetic information (i.e., less and 404 less epigenetic constraints on histone crosstalk), which  $_{405}$  causes a global and progressive impairment of biological 406 functions at the multicellular-individual level, eventually  $_{\rm 407}$  causing the death of the individual.

The nature of the epigenetic constraints on histone an age-correlated decrease of the proportion available  $_{\rm 409}$  crosstalk strongly implicates this time-correlated loss 410 of capacity for epigenetic information content (and 411 concurrent gain of that for hologenic content) as the 412 fundamental cause of senescence. Epigenetic constraints 413 are explicitly related to transcriptional/gene expression 414 changes and represented by the  $C_Y(X_1,\ldots,X_n,Y)$ 415 summand in Eq. 1. Because they depend on the 416 interactions between the histone-modified nucleosomes To test this possibility, the correlation value r between  $_{417}$  and the DNA wrapped around them—allowing or cell donor age and total information capacity (in bits) of  $_{418}$  preventing transcription—the epigenetic information 419 content they embody allows precise mRNA (and, 420 ultimately, gene expression) levels from histone 421 modification patterns.

This age-correlated hologenic/epigenetic information 423 imbalance in histone crosstalk can also be understood The analysis revealed that the correlation coefficients r 424 in terms of an imbalance between the accuracy and  $\tilde{r}$ =0.21, and  $\sigma_r$ =0.24, respectively, and that all associated 426 the needs of the multicellular individual. That is, more

because (i) the relative growth of  $C(X_1,\ldots,X_n|Y)$  490 under the falsifiable theory presented in this paper, this 433 implies an increasing constraint on (i.e., regulation 491 consensus is fundamentally incorrect. Indeed, senescence 434 of) histone modification patterns with respect to the 492 at the multicellular-individual level is, I suggest, not 435 multicellular individual [17], thus making transcription 493 the result of relaxed selection but instead an intrinsic 436 more accurate and (ii) the concurrent relative decrease of 494 developmental byproduct that would have been already  $^{457}$   $C_Y(X_1,\ldots,X_n,Y)$  means histone modification patterns  $^{495}$  observable theoretically in the emergence of the very 439 turn making transcription less and less precise to the 497 by the hologenic theory [17]. In other words, had the individual (see schematic in Fig. 6a).

where the dysfunctional effect is typically characterized 503 relaxed-selection hypothesis. in terms of the dysregulation of transcription and gene  $_{504}$ expression [28,29].

449 falsifiability of the theory of senescence: Within genomic 507 few yet crucial events where unprecedented forms of 450 regions adjacent to TSSs in primary normal cells from 508 biological individuality have emerged throughout the 451 any given tissue in any individuated multicellular species, 509 history of life on Earth. One of these events—as discussed 452 a significant positive correlation will be observed between 510 here—is the emergence of the individuated multicellular 458 may vary among species. It is predicted to be the level that 516 by Darwin from the scope of his original theory [36]—with 460 synergy (see Methods) on mRNA levels. Moreover, 518 dynamics that first enabled natural selection [44], and 461 since hologenic information content is described as 519 the emergence of the mind [37], which—through synthetic 462 emerging locally and independently in each developmental 520 biology—could at some point elicit the appearance of 463 process [17], the statistical strength of the predicted 521 new species in the evolutionary process without any all primary cell samples are obtained from the same tissue 524 with their evolutionary consequences. of the same individual throughout its lifespan.

469 above are a few species able to undergo reverse 527 level can be dynamically stopped. The answer suggested 474 reverse. Another exception for the prediction are species 532 could be developed to, for example, artificially increase 475 displaying extremely slow or potentially negligible 533 the dynamical range of nucleosome-DNA interactions 477 bristlecone pine Pinus longaeva [32], the freshwater 535 content in histone crosstalk at the expense of that for polyp *Hydra vulgaris* [33], and the naked mole-rat 536 hologenic content). 479 Heterocephalus glaber [34], which, after adulthood, are 537 480 predicted to display a significant but very weak positive 538 significant loss of hologenic content is a necessary 481 correlation (in cases where senescence is extremely slow), 539 condition for the onset of cancer. If this is correct, 483 (i.e., no correlation in cases where senescence is truly 541 also under hologenic theory, the in vivo balance 484 negligible; Fig. **6b**).

486 consequence of the relaxation of selection on traits that 544 cell-type-specific, and also confined to small functional 457 maintain/repair the multicellular individual's functions in 545 ranges. Thus, there could be an inherent high risk of

431 of histone modifications). This trade-off is unavoidable 489 in the wild with the hazards it imposes [35]. However, become worse and worse predictors of mRNA levels, in 496 first individuated multicellular organisms as described point of dysfunctionality with respect to the multicellular 498 first individuated multicellular organisms been free from 499 any extrinsic hazard in the wild, they would have begun Thus, we can characterize senescence under this theory 500 to senesce significantly after reaching a mature form in as a global transcriptional over-regulation with respect to 501 their development, as opposed to displaying extremely the multicellular individual's needs—as opposed to cancer, 502 slow or negligible senescence as can be inferred from the

If correct, the evolutionary account of senescence 505 suggested here underscores the need for modern The following general prediction applies to the 506 evolutionary theory to incorporate the effects of the the log-ratio of non-epigenetic to epigenetic histone 511 organism [17] with senescence as its developmental crosstalk magnitude and the age of the individual 512 byproduct, and its influence on the population renewal from whom the cells were obtained. The specific level 513 process. Other emergence events where new forms of of crosstalk—i.e., number of position-specific histone 514 individuality can arise with significant evolutionary modifications involved—at which this correlation exists 515 consequences include the origin of life—explicitly excluded possesses both significant predictive power and predictive 517 its unprecedented self-regulating and self-reproducing positive correlation will be further increased—and 522 involvement of natural selection. These latter two events, underpinned by a monotonically increasing function—if 523 and potentially others, remain to be fully elucidated along

525 Any theory of senescence is bound to address the The notable exceptions to be made for the prediction 526 question of whether aging at the multicellular-individual developmental processes from adult to juvenile stages. 528 here is that achieving a dynamical arrest of senescence One such species is the jellyfish Turritopsis nutricula [30], 529 is not a fundamental impossibility but it may well which is predicted to display an analogous negative 550 be a technical impossibility because of a therapeutic correlation in the processes, i.e., "reassignment" in 531 safety issue. From a fundamental point of view, methods senescence processes [31]. Examples of these are the 534 (thus increasing the capacity for epigenetic information

Yet, the hologenic theory also predicts that a or an hologenic/epigenetic log-ratio invariant with age 540 a potentially unsurmountable safety problem arises: 542 between hologenic and epigenetic information content Senescence is widely regarded as an evolutionary 543 is predictably "fine-tuned" as it is individual-specific, 488 later life, because later life would have been rarely realized 546 greatly increasing cancer incidence with the slightest



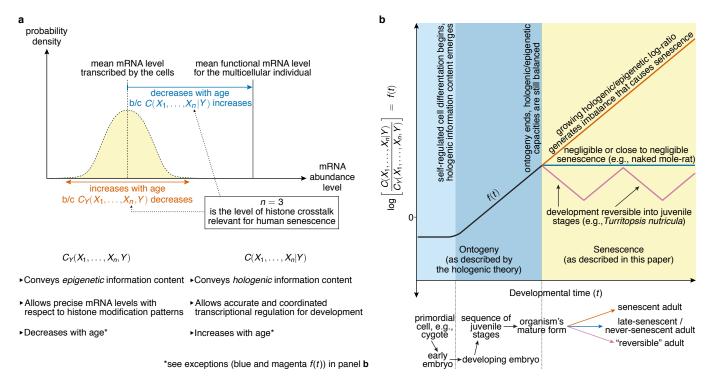


Fig. 6. Schematic of the imbalance between information capacity for hologenic content and epigenetic content in TSS-adjacent histone modification crosstalk as the cause of senescence. (a) The age-correlated increase in  $C(X_1,\ldots,X_n|Y)$  and concurrent decrease in  $C_Y(X_1,\ldots,X_n,Y)$  over-regulates the transcriptional response with respect to the multicellular individual's needs, i.e., the response becomes more and more accurate (blue) but less and less precise (orange) to the point of dysfunctionality. This unavoidable trade-off is explained by histone modification patterns becoming more constrained by regulation at the multicellular-individual level while at the same time becoming worse predictors of mRNA levels. The specific critical level of histone modification crosstalk (i.e., the value of n in  $\{X_1, \ldots, X_n\}$ ) at which this phenomenon occurs is n=3 (i.e., triads of position-specific histone modifications) in humans, but may vary for other species. (b) The log-ratio of non-epigenetic to epigenetic histone crosstalk magnitude increases during development as the embryo grows (black f(t) in darker blue area). After the organism reaches its mature form (yellow area), the log-ratio continues to increase (orange f(t))—with a few notable exceptions (blue and magenta f(t)). This continuous increase in turn creates an increasing dysfunctional imbalance of information contents that translates into senescence and, eventually, into death.

548 content imbalance. This problem resides in that hologenic 572 specific dynamics that would underpin the "pushback" 550 as a byproduct, are the very constraints preventing an 574 indeed falsifiable by means of the following secondary otherwise likely onset of cancer [17].

development can be reversed at least into juvenile 582 of the theory as a whole.) 559 developmental stages [30] and that of the naked 583 562 however exceptional.

564 information described here may shed light on the 588 it is worth noting that in the naked mole-rat both 565 well-known positive correlation between cancer incidence 589 senescence [34] and cancer incidence [40,41] have been 566 and age [39]: if the senescent multicellular individual 590 described as negligible or close to negligible. 567 attempts to correct its growing hologenic/epigenetic 591 568 content imbalance too strongly, it may elicit the onset 592 the explanatory limitations [42] of the Armitage-Doll 569 of cancer. Thus, age-related cancer would be the result 593 multistage model of carcinogenesis, which regards the 570 of a strong enough "pushback" from the multicellular 594 accumulation of genetic mutations as the cause of

547 extrinsic attempt to correct for the hologenic/epigenetic 571 individual against its own senescence. Although the constraints, whose growth in magnitude has senescence 573 are beyond the scope of this paper, this hypothesis is 575 prediction: the observed log-ratio of non-epigenetic to Based on a mathematical model of intercellular 576 epigenetic histone crosstalk magnitude in the normal 553 competition, Nelson and Masel have argued that stopping 577 (i.e., non-cancerous) cells closest to an age-related stage I senescence, even if possible, will always elicit the onset of 578 malignant tumor will be significantly lower than said cancer and that senescence is ultimately inevitable [38]. 579 log-ratio observed in the other (i.e., tumor-nonadjacent) Nevertheless, the existence of individuated multicellular 500 normal cells of the same tissue. (Note: The falsification of 557 species such as Turritopsis nutricula demonstrates that 551 this secondary prediction does not imply the falsification

In turn, the "pushback"-against-senescence hypothesis mole-rat suggests that senescence is reversible in some 584 for age-related cancer has, if correct, an implication we 561 cases and negligible or close to negligible in others, 585 should not overlook. Namely, stopping senescence and 586 eliminating the incidence of age-related cancer should be The delicate balance between hologenic and epigenetic 587 one and the same technical challenge. In this respect,

Rozhok and DeGregori have recently highlighted

 $_{595}$  age-related cancer [43]. They further argued that  $_{643}$  bigWigToWig ightarrow wig2bed --zero-indexed ightarrow $_{596}$  age-related cancer should rather be understood as a  $_{644}$  sort -k1,1 -k2,2n ightarrow bedtools map -o median <sup>597</sup> function of senescence-related processes [42]. However, 598 their description of age-related cancer is based on Darwinian processes and thus differ from the account 600 suggested here, which can be understood within the 601 concept of teleodynamics [37,44]—a framework of 602 biological individuality based on the emergence of intrinsic 603 higher-order constraints, such as that described in the 604 hologenic theory [17].

Apart from the proof of concept presented here, if the 606 main prediction of this paper resists falsification attempts 607 consistently, further research will be needed to elucidate 608 the specific molecular dynamics embodying hologenic and 609 epigenetic constraints within histone crosstalk completely. 610 Such insights will be necessary to decide whether the 611 hologenic/epigenetic information content imbalance can 612 be corrected without compromising the multicellular 613 individual's health or survival.

#### **METHODS**

#### Data collection

The genomic coordinates and associated transcript 615 lengths of all annotated RefSeq mRNA TSSs for the hg19 616 (Homo sapiens) assembly were downloaded from the 617 UCSC (University of California, Santa Cruz) database [45]. 618 All ChIP-seq and RNA-seq data downloaded, processed, 619 and analyzed in this work were generated by the 620 Canadian Epigenetics, Epigenomics, Environment and 621 Health Research Consortium (CEEHRC) initiative 622 funded by the Canadian Institutes of Health 623 Research (CIHR), Genome BC, and Genome Quebec. 624 CEEHRC protocols and standards can be found at 625 http://www.epigenomes.ca/protocols-and-standards, 626 and specific details on ChIP-seq antibody validation 627 can be found on this link. Further information 628 about the CEEHRC and the participating 629 investigators and institutions can be found 630 http://www.cihr-irsc.gc.ca/e/43734.html. For 631 full list of source data files with their respective URLs 632 for downloading, see Supplementary Information.

Cell sample data sets in the CEEHRC database were 634 selected based on the following criteria: (i) only data 635 sets with associated age were included and (ii) among 636 these data sets, the group (for both normal and cancer 637 cells) that maximized the number of specific histone H3 638 modifications present in all data sets was chosen.

#### ChIP-seq datafile processing

The original ChIP-seq binary datafile format was 640 bigWig. For mapping its ChIP-seq signal into the hg19 641 assembly, each datafile was processed with standard 642 bioinformatics tools [46–48] in the following pipeline:

-null 0 -a hg19\_all\_tss.bed/hg19\_all\_tss\_control.bed 646 to generate an associated BED (Browser Extensible Data) 647 file. (Note: The hg19\_all\_tss.bed file is a 200bp-per-bin 648 BED reference file with no score values to perform 649 the final ChIP-seq histone modification data mapping 650 onto the 6,000bp-long TSS-adjacent genomic regions. 651 The hg19\_all\_control.bed file is an analogous BED 652 reference file for mapping the ChIP-seq input data onto 653 200-bp, 1-kbp, 5-kbp, and 10-kbp genomic windows, 654 see ChIP-seq read profiles and normalization.)

#### ChIP-seq read profiles and normalization

To quantify and represent ChIP-seq read signal 656 profiles for the histone H3 modifications, data were 657 processed with the same method used in the EFilter 658 multivariate algorithm [23] to predict mRNA levels with 659 high accuracy ( $R \sim 0.9$ ). Steps in this method comprise 660 (i) dividing the genomic region from 2 kbp upstream 661 to 4 kbp downstream of each TSS into 30 200-bp-long 662 bins, in each of which ChIP-seq reads were later counted; 663 (ii) dividing the read count signal for each bin by its 664 corresponding control (ChIP-seq input) read density to 665 minimize artifactual peaks; (iii) estimating the control 666 read density within a 1-kbp window centered on each bin, 667 if the 1-kbp window contained at least 20 reads; otherwise, 668 a 5-kbp window, or else a 10-kbp window was used if the 669 control reads were less than 20. When the 10-kbp length 670 was insufficient, a pseudo-count value of 20 reads per 10 671 kbp was set as the control read density. This implies that the denominator (i.e., control read density) is at least 0.4 673 reads per bin.

## RNA-seq datafile processing

For each strand in the DNA, original datafiles contained 675 mRNA abundances in RPKM (reads per kilobase of 676 transcript per million mapped reads) in bigWig format. 677 These datafiles were thus processed analogously to the ChIP-seq datafiles, i.e., using the pipeline

 $_{679}$  bigWigToWig ightarrow wig2bed --zero-indexed ightarrowsort -k1,1 -k2,2n  $\rightarrow$  bedtools map -o median -null 0 -a refseq\_pos.bed/refseq\_neg.bed

obtain associated BED files. (Note: The 683 refseq\_pos.bed and refseq\_neg.bed files are BED 684 reference files for each strand, with no score values, to 685 perform the final RPKM calculation for each RefSeq 686 mRNA in the hg19 assembly.)

When two or more mRNAs shared the same TSS 688 (i.e., transcription start site with same genomic position 689 and strand) the mean of the respective RPKM values was 690 computed and associated with the corresponding TSS.

# Using the RPKM values processed in this work, a 692 subset TSS<sub>def</sub> of all RefSeq mRNA TSSs displaying 721 $^{695}$ TSSs in this subset TSS<sub>def</sub> was 18,220, indicating that $^{724}$ with mRNA levels. $\sim$ 70% of the 26,048 RefSeq mRNA TSSs annotated in 697 the hg19 assembly had an associated mRNA abundance 698 greater than zero in all (i.e., both normal and cancer) 699 samples. The obtained TSS<sub>def</sub> subset thus provided the 700 data analysis with a common basis for all samples that 725 702 human genome.

for defined and denoted by the distance (bp) between their  $_{729}$  P(X) its uncertainty (also known as Shannon entropy) is 705 5'-end and their respective TSS<sub>def</sub> genomic coordinate: 730 defined as "-2000", "-1800", "-1600", "-1400", "-1200", "-1000", 707 "-800", "-600", "-400", "-200", "0" (TSS<sub>def</sub> or '+1'), 708 "200", "400", "600", "800", "1000", "1200", "1400", "1600", "1800", "2000", "2400", "2600", "2800", "2800", "2800", "2800", "3400", "3 710 "3000", "3200", "3400", "3600", and "3800". Then, for 711 each sample data entry, the ChIP-seq read signal was 712 computed for all bins and for all histone modifications  $_{713}$  (30 bins×5 modifications=150 signal values) in all TSS<sub>def</sub> 714 genomic regions. Data input tables—comprising the 715 histone H3 modifications H3K4me1, H3K9me3, H3K27ac, 716 H3K27me3, and H3K36me3—were thus generated for 717 each sample entry as exemplified next:

The tables were then written to tab-delimited datafiles, 719 which were subsequently classified into two groups: normal 720 and cancer cells (see Table 1).

group	datafiles			
	CEMT0032.nm.dat	CEMT0033.nm.dat		
	CEMT0034.nm.dat	CEMT0040.nm.dat		
	CEMT0042.nm.dat	CEMT0044.nm.dat		
normal	CEMT0050.nm.dat	CEMT0051.nm.dat		
(n = 18)	CEMT0052.nm.dat	CEMT0053.nm.dat		
	CEMT0054.nm.dat	CEMT0055.nm.dat		
	CEMT0056.nm.dat	CEMT0057.nm.dat		
	CEMT0058.nm.dat	CEMT0059.nm.dat		
	CEMT0060.nm.dat	CEMT0061.nm.dat		
	CEMT0004.nm.dat	CEMT0005.nm.dat		
	CEMT0006.nm.dat	CEMT0019.nm.dat		
	CEMT0021.nm.dat	CEMT0025.nm.dat		
	CEMT0026.nm.dat	CEMT0027.nm.dat		
cancer	CEMT0028.nm.dat	CEMT0029.nm.dat		
(n = 17)	CEMT0030.nm.dat	CEMT0047.nm.dat		
	CEMT0063.nm.dat	CEMT0064.nm.dat		
	CEMT0065.nm.dat	CEMT0066.nm.dat		
	CEMT0067.nm.dat			

Table 1. Datafiles generated in this work containing normalized ChIP-seq signal values and RPKM values. The 'nm' suffix in the filename refers to the 'NM' RefSeq label for messenger RNAs, as opposed to non-coding RNAs.

#### Shannon measures of statistical uncertainty and statistical association

Shannon measures of statistical uncertainty and measured abundance (i.e., RPKM > 0) in all normal 722 statistical association were used in this work in order to 694 and cancer samples was determined. The number of 723 quantify histone H3 crosstalk at TSSs and its relationship

#### Statistical uncertainty

C.E. Shannon's seminal work, among other things, comprises most protein-coding genes annotated in the 726 introduced the notion of—and a measure for—the <sub>727</sub> uncertainty about discrete random variables [49]. For a For each sample data entry, 30 genomic bins were 728 discrete random variable X with probability mass function

$$H(X) := -\sum_{x \in X} P(x) \log_b[P(x)], \tag{4}$$

731 where P(x) is the probability of X=x and b is the  $_{732}$  logarithm base. When b=2 (the base used in this work). 733 the unit for this measure is the bit. H(X) can also 734 be interpreted as the amount of information necessary 735 to resolve the uncertainty about the outcome of X.  $_{736}$  Shannon uncertainty was the measure used to estimate 737 the uncertainty about the mRNA abundance level to be 738 resolved in normal cells.

H(X) is typically called marginal uncertainty because 740 it involves only one random variable. In a multivariate 741 scenario, the measure  $H(X_1,\ldots,X_n)$  is called the joint 742 uncertainty of the set of discrete random variables  $\{X_1,\ldots,X_n\}$ , and it is analogously defined as

$$H(X_1, \dots, X_n) := -\sum_{x \in X_1} \dots \sum_{x \in X_n} P(x_1, \dots, x_n) \log_b [P(x_1, \dots, x_n)].$$
(5)

744 Another measure important to this work is the conditional  $_{745}$  uncertainty about a discrete random variable Y, with 746 probability mass function P(Y), given that the value 747 of another discrete random variable X is known. This conditional uncertainty H(Y|X) can be expressed

$$H(Y|X) = -\sum_{x \in X} \sum_{y \in Y} P(x, y) \log_b \left[ \frac{P(x)}{P(x, y)} \right], \quad (6)$$

where P(x,y) is the joint probability of X=x and Y=y. 751 Importantly, any measure of Shannon uncertainty (or any 752 other derived Shannon measure) that is conditional on a random variable X can also be understood as said measure 754 being explicitly unrelated to, or statistically independent 755 from, the variable X.

A classic Shannon measure of statistical association of <sub>757</sub> any two discrete random variables X and Y is that of 758 mutual information I, defined as

$$I(X;Y) := -\sum_{x \in X} \sum_{y \in Y} P(x,y) \log_b \left[ \frac{P(x,y)}{P(x)P(y)} \right]$$
 (7)

$$= H(X) + H(Y) - H(X,Y)$$
 (8)

$$= H(Y) - H(Y|X). \tag{9}$$

Note that if and only if X and Y are statistically solution where  $C_Y(X_1,\ldots,X_n,Y)$  is the sum (analogous to that <sup>760</sup> independent then I(X;Y)=0, H(X,Y)=H(X)+H(Y), <sup>802</sup> of Eq. 13) of all interaction information quantities I but and H(Y|X)=H(Y). To analyze the magnitude of 803 now including the random variable Y in each combination 762 histone H3 crosstalk at TSSs, the two best known 763 multivariate generalizations of mutual information were 764 used in this work. The first is interaction information [50] 765 or co-information [51], also symbolized by I, which is 766 defined analogously to Eq. 8 for a set V of n discrete 767 random variables as

$$I(V) := \sum_{U \subset V} (-1)^{|U|+1} H(U), \tag{10}$$

where |U| is the cardinality (in this case, the number 769 of random variables) of the subset U. In the case of 808  $_{770}$  interaction information I, Shannon uncertainty H is thus  $_{809}$  chosen as the measure of statistical association to 771 summed over all subsets of V (the uncertainty of the 810 assess TSS-adjacent histone crosstalk because (i) C is <sub>772</sub> empty subset is  $H(\varnothing) = 0$ ). Importantly, the interaction <sub>811</sub> non-negative and thus easier to interpret conceptually, <sub>773</sub> information of the random variables  $\{X_1,\ldots,X_n\}$  can be <sub>812</sub> (ii) C is equal to zero if and only if all random variables it  $_{774}$  decomposed with respect to another random variable Y  $_{813}$  comprises are statistically independent, (iii) C captures 775 as follows:

$$I(X_1; ...; X_n) = I(X_1; ...; X_n; Y) + I(X_1; ...; X_n | Y).$$
(11)

776 Interaction information  $I(X_1; ...; X_n)$  captures the 5777 statistical association of all variables  $\{X_1, \ldots, X_n\}$  taken <sup>778</sup> at once, i.e., excluding all lower-order associations, and it 779 can also take negative values in some cases. Interaction 780 information was used in this work as a means to compute total correlation values.

To specifically quantify the magnitude of histone H3 crosstalk, the second multivariate generalization of mutual 784 information used in this work was total correlation [24] 785 (symbolized by C) or multiinformation [25], which is 786 defined as

$$C(X_1, \dots, X_n) := \left[ \sum_{i=1}^n H(X_i) \right] - H(X_1, \dots, X_n), (12)$$

787 i.e., as the sum of the marginal uncertainties of the random 829 uncertainty about Y when  $\{X_1,\ldots,X_n\}$  are known—or, 788 variables  $\{X_1,\ldots,X_n\}$  minus their joint uncertainty. 830 equivalently, the fraction of bits in Y that can be predicted <sub>789</sub> Importantly, and unlike interaction information I, total <sub>831</sub> by  $\{X_1, \ldots, X_n\}$ —and it can take values from 0 to 1. <sub>790</sub> correlation C captures all possible statistical associations <sub>832</sub>  $U(Y|X_1,\ldots,X_n)=0$  implies the set  $\{X_1,\ldots,X_n\}$  has <sub>791</sub> including lower-order associations or, equivalently, all <sub>833</sub> no predictive power on Y, whereas  $U(Y|X_1,\ldots,X_n)=1$ <sub>792</sub> possible associations between any two or more random <sub>834</sub> implies  $\{X_1,\ldots,X_n\}$  can predict Y completely. 793 variables in the set  $\{X_1,\ldots,X_n\}$ . This is because the 794 definition of interaction information I in Eq. 10 allows

795 total correlation C to be rewritten as a sum of quantities I796 for all possible combinations of variables in  $\{X_1, \ldots, X_n\}$ :

$$C(X_1, \dots, X_n) = \sum_{i,j} I(X_i; X_j) + \sum_{i,j,k} I(X_i; X_j; X_k) + \dots + I(X_1; \dots; X_n).$$
(13)

This expression for total correlation C as a sum of 798 interaction information quantities I along with the sum 799 decomposition of I in Eq. 11 allows C to be decomposed

$$C(X_1, \dots, X_n) = C_Y(X_1, \dots, X_n, Y) + C(X_1, \dots, X_n | Y),$$
(14)

804 of variables in  $\{X_1, \ldots, X_n\}$ , i.e.,

$$C_Y(X_1, \dots, X_n, Y) = \sum_{i,j} I(X_i; X_j; Y) + \sum_{i,j,k} I(X_i; X_j; X_k; Y) + \dots + I(X_1; \dots; X_n; Y),$$
(15)

and where  $C(X_1,\ldots,X_n|Y)$  is the sum of all conditional 806 interaction information quantities I given Y for each sor combination of variables in  $\{X_1, \ldots, X_n\}$ , i.e.,

$$C(X_1, \dots, X_n | Y) = \sum_{i,j} I(X_i; X_j | Y) + \sum_{i,j,k} I(X_i; X_j; X_k | Y) + \dots + I(X_1; \dots; X_n | Y).$$
(16)

For this work's purposes, total correlation C was 814 all possible associations up to a given number of variables 815 (in this work, position-specific histone modification levels) and, (iv) C can be decomposed, as shown in Eq. 14,  $_{817}$  as a sum of two C quantities: one explicitly related to  $_{818}$  a certain variable Y and the other explicitly unrelated 819 to Y. Property (iv) was useful to decompose the overall 820 histone crosstalk as a sum of an epigenetic and other 821 non-epigenetic component (see Introduction).

An additional Shannon measure of statistical 823 association was used to assess the predictive power 824 of TSS-adjacent histone modification levels on mRNA 825 abundance levels (such power has already been used 826 to predict mRNA levels with high accuracy [23]). The uncertainty coefficient U [52] is defined as

$$U(Y|X_1,...,X_n) := \frac{H(Y) - H(Y|X_1,...,X_n)}{H(Y)}, \quad (17)$$

828 i.e.,  $U(Y|X_1,...,X_n)$  is the relative decrease in

## Levels of possible statistical associations when assessing histone crosstalk magnitudes

and non-epigenetic histone crosstalk components is the 872 called redundancy [53]. Based on previous work [23], high 837 specific range of possible statistical associations. In other 873 predictive power on mRNA levels and yet no synergy are 838 words, the choice of the number n of TSS-adjacent, 874 thus expected to happen with a large enough n. From all position-specific histone H3 modification levels when 875 possible singletons (4), pairs (6), and triads (4) that exist  $C_Y(X_1,\ldots,X_n,Y)$  and  $C(X_1,\ldots,X_n|Y)$ . 876 within a tetrad, the explanatory power on mRNA levels  $_{841}$  To this end, the minimal n able to predict mRNA  $_{877}$  of a non-redundant set of only one triad and five pairs significantly 843 corresponds to the level of histone crosstalk able 879 844 to convey a non-neglectable amount of epigenetic 880 may not always be a suitable unit of mRNA abundance 845 information content—was first determined. This value is 881 when studying differential gene expression. Specifically, 846 straightforward to assess using the uncertainty coefficient 882 it was shown that, if transcript size distribution 847  $U(Y|X_1,\ldots,X_n)$ , where Y represents mRNA levels.

849 the predictive power of pairs of position-specific 885 an alternative abundance unit TPM (transcripts per histone modification levels,  $U(Y|X_i,X_j,X_k)$  quantifies  $^{886}$  million)—which is an invertible linear transformation of 851 the predictive power of triads, etc.  $U(Y|X_1,\ldots,X_n)$  887 the RPKM value for each sample—was introduced [55]. 852 values were thus computed for singletons, pairs, triads, 888 Nonetheless, this issue was not a problem for the 853 and tetrads. Singeltons were calculated for descriptive 889 present work because Shannon measures are invariant <sub>854</sub> purposes only, because histone crosstalk is not measurable <sup>890</sup> under any invertible transformation of the discrete 855 for them. On average, a triad (i.e., when n=3) of 891 random variables.) 856 position-specific histone H3 modification levels was found 857 to have (i) significant predictive power on mRNA levels 858  $(U(Y|X_i, X_j, X_k)=0.63)$  and, importantly, (ii) at least 2.3 859 times more predictive power than all possible singletons 860 (3) and pairs (3) that exist within a triad taken together, 892 861 i.e.,

$$\frac{U(Y|X_i, X_j, X_k)}{\sum_{i} U(Y|X_i) + \sum_{i,j} U(Y|X_i, X_j)} \ge 2.3,$$
 (18)

a phenomenon known as synergy of a set of <sub>863</sub> predictor variables [53] (see Table 2).

level	set	U(Y V) [mean]	κ	U(Y V) measured in
singleton	$V=\{X_i\}$	0.02	154	all 150 singletons
pair	$V=\{X_i,X_j\}$	0.07	441	all 11,175 pairs
triad	$V = \{X_i, X_j, X_k\}$	0.63	325	all 551,300 triads
tetrad	$V = \{X_i, X_j, X_k, X_l\}$	0.95	379	50,000 random tetrads

Table 2. Predictive power (quantified as  $U(Y|V) \in [0,1]$ ) of different sets  $V = \{X_1, \dots, X_n\}$  of TSS-adjacent, position-specific histone H3 modification levels on mRNA levels (represented by Y) in normal cells. For each instance of the set V, U(Y|V) was averaged over the 18 normal cell samples analyzed. The distribution of U(Y|V) in the interval [0, 1] for each family V of sets (singletons, pairs, triads, and tetrads) was parameterized and described here in terms of the mean  $\bar{x}$  and the concentration parameter  $\kappa$ , which are derived from the respective beta distribution  $_{908}$ Beta $(\alpha, \beta)$ , with  $\kappa = \hat{\alpha} + \hat{\beta}$  [54]. Point estimators  $\hat{\alpha}$  and  $\hat{\beta}$  were computed using the method of moments, i.e.,  $\hat{\alpha} = \bar{x}^2 \left( \frac{1-\bar{x}}{\sigma^2} - \frac{1}{\bar{x}} \right)$ and  $\hat{\beta} = \hat{\alpha} \left( \frac{1}{\bar{x}} - 1 \right)$ , where  $\sigma^2$  is the variance.

Pairs (i.e., when n=2) were also found to possess predictive synergy, but this synergy is smaller than that  $_{911}$  which is known to follow a Student's t-distribution found for triads  $\left(1.75 \le \frac{U(Y|X_i,X_j)}{\sum_i U(Y|X_i)} < 2.3\right)$ . The average  $\frac{912}{912}$  with n-2 degrees of freedom, and where n is the  $\frac{913}{913}$  number of data pairs [56]. For the hypothesized

substantially lower  $(U(Y|X_i,X_i)=0.07)$ . On the other hand, tetrads (i.e., when n=4) were found to have high predictive power  $(U(Y|X_i, X_j, X_k, X_l)=0.95)$  but they An important aspect of quantifying the epigenetic 871 possess no synergy whatsoever and display instead what is and non-redundantly—which 878 already exceeds the explanatory power of the tetrad.

(Note: In previous work it has been argued that RPKM 883 varies significantly among the samples, RPKM might In effect,  $U(Y|X_i, X_j)$  (i.e., where n=2) quantifies <sup>884</sup> introduce significant biases [55]. To overcome this problem,

#### Theoretical methods

The elaboration of the main falsifiable prediction took 893 into account two observations for human primary cells 894 in this work. Namely, (i) the uniqueness of triads of 895 position-specific histone modification levels in terms of 896 significant predictive power and predictive synergy and 897 (ii) the post hoc result that triads constitute precisely the 898 level n at which the predicted correlation between the 899 non-epigenetic/epigenetic histone H3 crosstalk log-ratio 900 and cell donor age actually exists. In this way, the main 901 prediction was formulated with explicit dependence on the 902 level of scale: "For any given tissue in any individuated 903 multicellular species a positive correlation between the 904 non-epigenetic/epigenetic histone H3 crosstalk log-ratio and cell donor age will be observed at the level n of histone 906 crosstalk that possesses both significant predictive power 907 and predictive synergy on mRNA levels."

#### Statistical tests

The statistical significance of each Pearson correlation  $_{909}$  coefficient r obtained was assessed using the statistic t

$$t := r\sqrt{\frac{n-2}{1-r^2}},\tag{19}$$

 $_{867}$  predictive power of pairs on mRNA levels is also  $_{914}$  positive correlation between the non-epigenetic/epigenetic

 $^{915}$  histone H3 crosstalk log-ratio and age, the statistical null  $^{916}$  hypothesis was tested against the alternative hypothesis  $^{917}$  that the correlation is greater than zero (i.e., one-sided  $^{918}$  Student's t-test). For the hypothesized non-significant  $^{919}$  correlation between the overall histone H3 crosstalk  $^{920}$  magnitude and age, the statistical null hypothesis  $^{921}$  was tested against the alternative hypothesis that the  $^{922}$  correlation is greater or less than zero (i.e., two-sided  $^{923}$  Student's t-test).

On the other hand, the distribution of correlation coefficients (r) is known to be non-Gaussian [57], which can be easily appreciated in Fig. 3. For this reason, the statistical comparison of r for normal cells (neonate data point excluded) and cancer cells was performed using the non-parametric Mann-Whitney U test [58].

#### Correction for multiple testing

The analysis of histone crosstalk involved  $^{931}$  5 histone H3 modifications  $\times$  30 genomic bins = 150  $^{932}$  TSS-adjacent, position-specific histone H3 modification  $^{933}$  levels. Thus, assessing the statistical significance of the  $^{934}$  correlation values involved a large number of tests of  $^{935}$  the null hypothesis (for triads, tetrads, and pairs) under  $^{936}$  general dependence. This dependence derives from the  $^{937}$  fact that different histone modification levels are known  $^{938}$  to be highly correlated (this is the phenomenon of histone  $^{939}$  crosstalk itself).

The resampling-based procedure by Benjamini and Yekutieli [59] provides control of the false discovery rate (FDR) [60] under general dependence conditions. This was the method thus used in this work in order to correct for multiple testing.

#### Code availability

Standard bioinformatics tools [46–48] and the Perl language were used to process the ChIP-seq and RNA-seq source data and to generate the \*.nm.dat files displayed in Table 1. The R software [61] and its infotheo package [62] were used for the computation of Shannon measures of statistical uncertainty and statistical association from the \*.nm.dat files. Marginal and joint Shannon uncertainties and all the other derived Shannon measures were computed using maximum likelihood (ML) estimation [63] and bias-corrected with the Miller-Madow method [64]. All the R code and the \*.nm.dat files necessary for a full reproduction of the results are available as Supplementary Information.

#### Sample metadata

sample ID	disease status	cell donor age	sex	cell type/tissue
CEMT0032	normal	0	N/A	hematopoietic (cord)
CEMT0033	normal	82	F	colon
CEMT0034	normal	73	M	colon
CEMT0040	normal	67	F	thyroid
CEMT0042	normal	46	F	thyroid
CEMT0044	normal	55	M	thyroid
CEMT0050	normal	53	M	colon
CEMT0051	normal	67	M	colon
CEMT0052	normal	72	M	colon
CEMT0053	normal	81	F	colon
CEMT0054	normal	90+	F	colon
CEMT0055	normal	90+	F	colon
CEMT0056	normal	84	F	colon
CEMT0057	normal	84	F	colon
CEMT0058	normal	56	F	colon
CEMT0059	normal	56	F	colon
CEMT0060	normal	77	M	colon
CEMT0061	normal	77	M	colon
CEMT0004	cancer	74	M	peripheral blood
CEMT0005	cancer	68	F	peripheral blood
CEMT0006	cancer	60	M	peripheral blood
CEMT0019	cancer	46	F	brain
CEMT0021	cancer	35	M	brain
CEMT0025	cancer	62	F	peripheral blood
CEMT0026	cancer	79	M	peripheral blood
CEMT0027	cancer	71	M	peripheral blood
CEMT0028	cancer	79	F	peripheral blood
CEMT0029	cancer	47	M	colon
CEMT0030	cancer	56	F	peripheral blood
CEMT0047	cancer	43	M	brain
CEMT0063	cancer	81	F	colon
CEMT0064	cancer	90+	F	colon
CEMT0065	cancer	84	F	colon
CEMT0066	cancer	56	F	colon
CEMT0067	cancer	77	M	colon

Table 3. Metadata for each primary cell sample analyzed. Note: Age entries originally tabulated as 90+ were entered as 90 into the computational analysis. Metadata source: CEEHRC.

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