

1 **Instantaneous midbrain control of saccade kinematics**

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15 **Abstract**

16

17 The ability to interact with our environment requires the brain to transform spatially-represented sensory
18 signals into temporally-encoded motor commands for appropriate control of the relevant effectors. For
19 visually-guided eye movements, or saccades, the superior colliculus (SC) is assumed to be the final stage
20 of spatial representation, and instantaneous control of the movement is achieved through a rate code
21 representation in the lower brain stem. We questioned this dogma and investigated whether SC activity
22 also employs a dynamic rate code, in addition to the spatial representation. Noting that the kinematics of
23 repeated movements exhibits trial-to-trial variability, we regressed instantaneous SC activity with
24 instantaneous eye velocity and found a robust correlation throughout saccade duration. Peak correlation
25 was tightly linked to time of peak velocity, and SC neurons with higher firing rates exhibited stronger
26 correlations. Moreover, the strong correlative relationship was preserved when eye movement profiles
27 were substantially altered by a blink-induced perturbation. These results indicate that the rate code of
28 individual SC neurons can control instantaneous eye velocity, similar to how primary motor cortex
29 controls hand movements, and argue against a serial process for transforming spatially encoded
30 information into a rate code.

31

32 **Introduction**

33

34 Even when we wish to produce the same movement repeatedly, our action exhibits heterogeneity across
35 repetitions. This explains, in part, why intended identical swings of a tennis racket, for example, do not
36 result in identical trajectories of a ball. It is possible the variability could be the result of biological noise
37 in the effectors, although a more likely explanation points to a neural origin (Carmena et al., 2005;
38 Churchland et al., 2006; van Beers, 2007, 2008). While potential neural sources of movement variability
39 have been extensively studied for hand movements (for a review, see (Churchland, 2015)), less is known
40 about their impact on eye movements, particularly the ballistic type known as saccades.

41

42 The superior colliculus (SC), a laminar subcortical structure with a topographic organization of the
43 saccade motor map, is a central node in the oculomotor neuraxis (Gandhi and Katnani, 2011; Basso and
44 May, 2017). It is intimately linked to the spatiotemporal transformation, in which visuo-oculomotor
45 signals in the SC conform to a space or place code, while recipient structures in the brainstem exhibit a
46 rate code. In a slight modification to this framework - the so-called dual coding hypothesis (Sparks and
47 Mays, 1990) - saccade amplitude and direction are computed from the locus of population activity in the
48 SC, while movement velocity is a “determinant” of these neurons’ firing rates. The strongest evidence for
49 SC control of saccade velocity comes from causal studies demonstrating that peak eye velocity is
50 correlated with frequency or intensity of electrical microstimulation (Stanford et al., 1996; Katnani and
51 Gandhi, 2012) and that peak velocity is attenuated after inactivation of SC (Sparks et al., 1990). However,
52 these results only address the distribution in static saccade descriptors, falling short of explaining dynamic
53 properties of the movement (e.g. instantaneous velocity). On the other hand, the dynamic vector
54 summation algorithm (Goossens and Van Opstal, 2006) presents a framework in which the SC controls
55 the desired instantaneous displacement of the eye through a series of mini-vectors, but does not directly
56 address the possibility of instantaneous control of ocular kinematics.

57
58 In this study, we tested the hypothesis that SC activity dynamically controls the instantaneous velocity of
59 saccades. Time series correlation was first performed on individual trials by regressing the temporal
60 evolution of SC activity with eye velocity within each trial. This analysis, by definition, cannot reveal
61 which epoch(s) of the waveforms contribute most significantly to the correlation. We addressed this latter
62 limitation by correlating the instantaneous neural activity and eye velocity across trials, an ensemble
63 approach that calculates the correlation between firing rate and velocity on individual timepoint basis. We
64 found that instantaneous residual firing rate strongly correlates with instantaneous residual velocity for
65 both within-trial and across-trials analyses. The peak correlation was best aligned with the time of peak
66 eye velocity, and at a population level, the correlation was significant throughout the movement. Neurons
67 with the highest firing rates within individual penetrations displayed the strongest correlation. Finally,
68 the relationship was observed not only for ballistic-like, bell-shaped velocity waveforms of normal
69 saccades but also for profiles altered by blink perturbations. Thus, individual SC neurons exhibit a code
70 that can control instantaneous eye velocity, akin to how primary motor cortex controls hand velocity
71 (Ashe and Georgopoulos, 1994; Reina et al., 2001) Our finding also argues against a serial process for
72 transforming spatially encoded information into a rate code.

73 74 **Methods**

75
76 Two adult rhesus monkeys (*Macaca mulatta*, 1 male and 1 female, ages 8 and 10, respectively) were used
77 for the study. All procedures were approved by the Institutional Animal Care and Use Committee at the
78 University of Pittsburgh and were in compliance with the US Public Health Service policy on the humane
79 care and use of laboratory animals.

80
81 Extracellular spiking activity of SC neurons were recorded as head-restrained animals performed a
82 visually-guided, delayed saccade task under real-time control with a LabVIEW-based controller interface
83 (Bryant and Gandhi, 2005). Neural activity was collected with either a multi-contact laminar probe
84 (Alpha Omega; 16 channels, 150 μm inter-contact distance, $\sim 1\text{ M}\Omega$ impedance of each contact) or a
85 standard tungsten microelectrode (Microprobes, $\sim 1\text{ M}\Omega$ impedance). All electrode penetrations were
86 orthogonal to the SC surface, so that roughly the same motor vector was encoded across the layers. The
87 saccade target was presented either near the center of the neuron's movement field or at the diametrically
88 opposite location. This study reports analyses from 189 neurons, 145 of which were collected with a
89 laminar probe across 18 sessions, and the remaining 44 neurons were recorded with a single electrode
90 (Jagadisan and Gandhi, 2017). All neurons can be classified as visuomotor or motor neurons according to
91 standard criterion, which we have described previously (Jagadisan and Gandhi, 2016).

92
93 Blink perturbation data were only available for the 50 neurons, 44 of which were studied with the single
94 electrode setup and the remaining 7 from a single laminar electrode session. On approximately 15-20%
95 of the trials, an air-puff was delivered to one eye to invoke the trigeminal blink reflex. The puff was timed
96 to induce a blink around the time of saccade onset or even trigger the eye movement prematurely. In this
97 case, blink-triggered saccades provide a valuable control against spurious correlations, as the velocity
98 profile of the saccade is altered compared to that of a normal movement and endpoint accuracy is

99 preserved. Thus, if SC dynamically controls the kinematics of the saccade, the perturbed velocity
100 waveforms should be predicted by the SC activity as well. For full disclosure, the data from these 50
101 neurons are the same as those reported in a previous publication (Jagadisan & Gandhi 2017). The key
102 distinction is that the previous study assayed SC activity during the saccade preparation phase, and now
103 the focus is on the peri-saccade period.

104

105 Eye and eyelid movements were detected using the magnetic search coil method. Spike trains were
106 converted to a spike density waveform by convolution with a 5 ms Gaussian kernel. All movements were
107 aligned on saccade onset and standard velocity criteria were used to detect the onset and offset of normal
108 saccades. For blink-triggered movements, the onset of saccadic component was estimated as the time of a
109 deviation from a spatiotemporal template of a blink related eye movement induced during fixation
110 (Katnani and Gandhi, 2013). The movement profiles were then transformed into radial coordinates in
111 which positive values indicate vectorial velocity towards the movement field and negative values away
112 (Jagadisan and Gandhi, 2017); this differs from the common method in which vectorial velocity
113 representation is always positive and independent of the ideal saccade path towards the target. This
114 distinction is vital, as we were not able to observe the effects described later when using traditional
115 vectorial coordinates. To remove potential confounds of saccade amplitude on correlations between
116 spiking activity and radial velocity, we additionally limited each neuron's dataset to movements within
117 $\pm 5\%$ of the mean amplitude (range: 8-25 degrees; median: 12 degrees) and, for the analysis comparing
118 normal and blink-perturbed movements, at least 20 trials for each condition. All 189 neurons passed the
119 inclusion criteria, 50 of which also had amplitude-matched blink perturbation trials.

120

121 For each neuron we subtracted the session's mean velocity and spike density waveforms from each trial's
122 data to obtain the respective residuals. This important step removes spurious correlations from generally
123 similar shapes of SC activity and saccade velocity. For within-trial analysis, a Pearson's correlation was
124 determined for each trial's residual velocity and neural activity waveforms. The two residual vectors were
125 shifted relative to each other from 100 ms to -100 ms in 1 ms increments, and the Pearson's correlation
126 was calculated for each delay (Δt). A zero delay indicates that both vectors are aligned on saccade onset.
127 Negative delays signify instances when the neural activity preceded the velocity, which we refer to as a
128 efferent delay (ED). This analysis was performed for every residual neural activity – velocity waveform
129 pairing for each trial of each cell. For across-trials analysis, we created a vector of activity residuals at
130 time t and a corresponding vector of velocity residuals at time $t + \Delta t$, where the length of the vectors
131 equals the number of trials. The Pearson correlation between these two vectors was determined. We
132 repeated this procedure for every timepoint in the saccade and for every 1 ms shift, resulting in a
133 correlation coefficient for each combination of time relative to saccade onset and delay. This technique
134 allowed us to examine the SC effects on eye velocity at every timepoint of the saccade in 1 ms resolution.
135 We repeated both correlational analyses on blink-perturbed trials to see if the results persist even when
136 the saccade properties are altered.

137

138 To further validate that the influence of the SC on velocity continues throughout the entirety of the
139 saccade, we calculated the duration of significant correlation for each cell. To do this, we determined the
140 confidence threshold by performing the across-trial analysis on shuffled data for each cell one hundred

141 times. Then we determined that the correlation was significant at those points where the real correlation
142 exceeded 2 standard deviations around the mean of the shuffled results. Summing the instances at which
143 correlation was significant gave us the total duration of the correlation.

144

145 To determine the significance of the results of within-trial analysis, we randomly paired a residual
146 velocity trace of one trial with residual activity data of another trial from the same session's data and
147 determined the Pearson correlation for the span of delay values. For across-trials analysis, we randomly
148 shuffled the order of elements in each residual vector (instantaneous across-trial shuffle) before
149 determining the correlation coefficient. The shuffling procedures were repeated 100 times for both types
150 of analyses. Deviations of unshuffled correlation results outside 2 standard deviation bounds generated
151 from shuffled data were deemed statistically significant.

152

153 In a separate analysis we looked at the subset of data which was collected using laminar probes. This
154 subset allowed us to examine the effect of depth of SC neurons on our results. The number of channels
155 with neural data ranged from 4 to 16 per session. Since each session did not have enough channels for
156 sufficient statistical power, we de-meaned the data from each session and combined all channels. We then
157 used linear regression on the de-meaned correlation coefficients of these channels and the corresponding
158 FR to establish a trend.

159

160 **Results**

161

162 The relationship between SC activity and saccade dynamics can be intuitively queried by correlating the
163 firing rate with velocity for different transduction delays. Figure 1A plots the results of such within-trial
164 analysis for normal saccades across all 189 neurons in our database. The mean peak Pearson correlation
165 ($r = 0.179$) was observed for an efferent delay (ED) of 13 *ms*, equivalently $\Delta t = -13$ *ms*. The
166 correlation was significantly different from the pattern observed for shuffled data. This result therefore
167 indicates that the residuals of both SC activity and eye velocity fluctuate around the mean in a coherent
168 fashion and that SC activity can influence saccade velocity.

169

170 A major limitation of within-trial analysis is that it offers no information about the correlation at each
171 timepoint within the saccade. The correlation coefficient could peak if any sufficiently long sequence of
172 the activity correlates with the corresponding sequence in velocity. One can imagine that SC could,
173 perhaps, encode the accelerating phase of the eye movement and the deceleration phase could be
174 unaffected by SC activity, and rather be guided by muscle viscoelastic properties. In this case, the
175 correlation would peak at a particular ED because the first half of both signals is correlated, but would
176 provide little evidence to support our hypothesis that SC dynamically influences the entire saccade. We
177 therefore employed across-trials analysis to determine precisely the time-course of correlation between
178 activity and velocity.

179

180 Assembled across trials, the residual firing rates were correlated with residual eye velocities separated by
181 a delay. This procedure was repeated for a large range of delays and for all times points of a saccade.
182 Figure 1B shows the correlation coefficients for all combinations of saccade time points and ED values. A

183 horizontal band of high correlation values is noted for the duration of the saccade for an ED of 12 *ms*.
184 The correlation values in this band (Figure 1C) are even higher (peak: $r = 0.278$) than that found in
185 within-trial analysis. Results from the across-trials analysis therefore provide the strongest evidence that
186 SC dynamically influences eye velocity throughout the entire saccade. Additionally, it is prudent to
187 mention that this analysis is identical whether performed on residuals or raw data, thus providing a more
188 direct evidence of correlation as compared to the within-trials analysis.

189
190 Next, we explored the temporal characteristics of instantaneous activity-velocity correlations. We found
191 that the time of peak correlation was well aligned with the time of peak velocity, after accounting for the
192 efferent delay, for each neuron (Figure 2A). A paired *t*-test could not reject the null hypothesis that the
193 mean difference was zero ($p = 0.15$). In contrast, the duration of the SC influence over the saccade
194 velocity reveals a flat distribution (Figure 2B), and cells that had a shorter duration of significant
195 correlation tended to have a lower peak correlation (Figure 2C; $r = 0.53, p = 1.99 \times 10^{-33}$, [*f* –
196 *test*, *MATLAB regress function*]). The relationship between degree and duration of influence could be
197 explained by cells with higher correlation values having a higher likelihood of rising above the
198 significance level over time. Thus, SC neurons tend to exhibit most influence over eye kinematics around
199 the peak of the saccade velocity profile, and those cells which showed a higher peak correlation continued
200 to influence eye velocity well past the peak, to saccade completion.

201
202 We then studied which properties of the neuronal population contributed to significant correlations. When
203 examining the entire population of cells, simple linear models found no relationship between a cell's peak
204 correlation and its peak firing rate or its location along the rostral-caudal extent of the SC ($p = 0.088, f -$
205 *test*). However, when we isolated only the cells from a single laminar recording, we observed an
206 increasing trend between the cells FR and its peak correlation (Figure 3A). When data from the laminar
207 recordings was pooled by subtracting the average peak firing rate and correlation measures of each
208 session, a statistically significant linear relationship was observed (Figure 3B, $p = 7.4 \times 10^{-6}, f -$ *test*).
209 This suggests that there is a strong relationship between firing rate and instantaneous velocity within
210 individual columns of the SC.

211
212 To assess the robustness of the influence of SC activity over instantaneous eye velocity we turned to the
213 50 neurons for which we also had blink-perturbation data. Such saccades do not exhibit the stereotypical,
214 bell-shaped profile and therefore offer an opportunity to assess if the correlation persists even in the
215 presence of perturbation. The top row of Figure 4 displays the within- and across-trial analyses for normal
216 trials in the 50 neurons. The general trend is preserved, even with the majority of data removed. The best
217 EDs for the normal, unperturbed data were 11 *ms* and 12 *ms* and the peak correlations were $r = 0.267$
218 and $r = 0.441$ for within- and across-trial analyses, respectively. For the blink-perturbed data from the
219 same neurons, the peak correlations were $r = 0.210$ and $r = 0.386$ for both within- and across-trial
220 analyses, respectively; and the ED was 13 for both. Correlative relationship was largely intact despite the
221 blink-induced perturbation.

222
223 To further characterize the impact of blink perturbation, we computed for each neuron the linear
224 relationship between residual activity and velocity distributions across the duration of the movement.

225 Assuming the data contained n trials and the average duration of the amplitude-matched saccades is
226 d ms, a single regression was performed across nd points. The activity data were time shifted relative to
227 the velocity distribution to account for the neuron's ED. This was done separately for the normal and
228 blink-perturbed data from each of the 50 neurons. Figure 5A shows a scatter plot of the regression slopes
229 for each neuron in the two conditions. Overall, the slopes tended to be greater during the blink condition
230 (paired t-test $p=0.0013$). Moreover, we found a strong relationship between each neuron's regression
231 slope and the goodness of fit in both normal ($r=0.72$, $p=2.37\times 10^{-7}$) and perturbation ($r=0.35$, $p=0.02$)
232 conditions (Figure 5B).

233

234 Discussion

235

236 We revealed an intuitive yet, to our knowledge, unreported phenomenon on how SC activity exerts
237 instantaneous control over saccadic eye movements. We found a strong correlation between the motor
238 burst of SC neurons and eye velocity for an efferent delay of approximately 12 ms. The correlation was
239 noted for both within-trial and across-trials analyses. The latter approach, in particular, demonstrated that
240 the correlation remained high for the duration of saccade, lending support for SC control of instantaneous
241 eye speed and thereby modifying the notion of spatiotemporal transformation. In addition, this approach
242 revealed a robust distributed population coding scheme reminiscent of a synfire chain (Diesmann et al.,
243 1999; Shmiel et al., 2006), wherein individual neurons exert influence over saccade dynamics
244 sequentially at different times, collectively spanning the duration of the saccade. Comparable correlation
245 structure and ED were also observed for blink-perturbed movements, whose velocity profiles deviate
246 significantly from the stereotypical bell-shaped waveforms (Goossens and Van Opstal, 2000; Gandhi and
247 Bonadonna, 2005), although it was particularly important to project the velocity vector onto the preferred
248 vector of the SC neuron (Jagadisan and Gandhi, 2017). We also learned that, within individual collicular
249 columns, cells with higher FR tend to exhibit a stronger correlation with velocity, suggesting a
250 relationship based on the depth of each cell as well as its spiking properties. Finally, we uncovered the
251 interesting feature that regressions with the largest correlations also had the biggest slopes, implying that
252 eye velocity is more sensitive to firing rates of the more reliable neurons.

253

254 Previous studies have addressed relationships between neural activity and movement parameters in
255 several ways. For SC control of saccades, the focus has been on static parameters. For example, weaker
256 bursts of activity produce saccades with lower peak velocity (Edelman and Goldberg, 2001), peak
257 velocity is correlated with frequency or intensity of microstimulation (Stanford et al., 1996; Katnani and
258 Gandhi, 2012), and peak velocity is attenuated after inactivation of SC (Sparks et al., 1990). Modest
259 correlations with SC activity have also been reported for head movements (Walton et al., 2007; Rezvani
260 and Corneil, 2008) and electromyographic activity in proximal limb muscles (Stuphorn et al., 1999).
261 Instantaneous control of saccades has been studied or discussed for neurons downstream of the SC, in the
262 oculomotor brainstem (Cullen and Guitton, 1997; Sylvestre and Cullen, 1999; Sparks and Gandhi, 2003).
263 Such analyses are also more common in the skeletomotor system, with significant correlations identified
264 between neural activity waveforms in cortical areas and hand velocity profiles (Ashe and Georgopoulos,
265 1994; Reina et al., 2001). Trial-to-trial variability in eye and hand velocity has also been attributed to
266 variability in neural activity occurring earlier in the trial, for instance during sensory input (Osborne et al.,

267 2005; Huang and Lisberger, 2009) and motor preparation (Churchland et al., 2006; Jagadisan and Gandhi,
268 2017), but this perspective precludes insight into direct dynamic control during ongoing movements.

269
270 We believe our study is the first to quantify correlations informative of instantaneous control of saccades
271 by SC neurons. This finding does not conform readily to the standard role of SC in saccade generation,
272 that the spatial distribution of population activity in the deeper layers determines the saccade vector and
273 that downstream structures generate the firing patterns that reflect the velocity profile of the eye
274 movement. The result that SC activity does influence peak saccade velocity (cited above) somewhat
275 aligns to a modified framework, the dual coding hypothesis (Sparks and Mays, 1990), in which the level
276 of SC activity acts as a gain factor on the brainstem burst generator (Nichols and Sparks, 1996). However,
277 influencing saccade speed through a global gain is not equivalent to imposing instantaneous control. In
278 contrast, a dynamic vector summation algorithm (Goossens and Van Opstal, 2006; Goossens and van
279 Opstal, 2012) offers a more compelling framework in which the SC controls the *desired* instantaneous
280 displacement of the eye. Crucially, this model abstains from making direct statements about instantaneous
281 velocity control. It is possible this is because SC neurons do not have a relationship between the average
282 firing rate and the velocity of the saccade they code for. In other words, low firing cells could code for
283 high-velocity saccades, and high-firing cells could code for low-velocity saccades, depending on where
284 they reside in the collicular map. Our analysis circumvents this limitation by examining residuals. We
285 suggest that the static parameters of the saccade are controlled by traditionally understood methods (e.g.
286 dual coding hypothesis) while deviations from the optimal velocity profile are influenced by dynamic
287 fluctuations of neural activity residuals. This proposed framework is capable of functioning in tandem
288 with the aforementioned dynamic vector summation model, as long as the model accounts for the
289 fluctuations in the residual activity of each cell.

290
291 The efferent delay is indicative of the transduction time of neural signals from the SC to the extraocular
292 muscles. Studies of SC stimulation have established a 25 – 30 *ms* latency for movement initiation
293 (Stanford et al., 1996; Katnani and Gandhi, 2012) and a shorter 10 – 12 *ms* delay for perturbing an
294 ongoing movement (Munoz and Wurtz, 1993; Miyashita and Hikosaka, 1996; Gandhi and Keller, 1999).
295 The ED that yielded the strongest correlation from our neural recording data was approximately 12 *ms*.
296 Crucially, it remained relatively constant throughout the movement, although we did observe a broader
297 range of ED values with higher correlation coefficients around saccade onset (Figure 1B). While the ED
298 values may seem different for microstimulation and recordings studies, a direct comparison should be
299 avoided because underlying network level processes associated with movement preparation, which are
300 implicitly incorporated in neural activity, may be different when microstimulation is used to trigger a
301 movement.

302
303 We are intrigued by the observation that peak correlation between activity and velocity increased as a
304 function of peak firing rate, but only for neurons within a SC “column” and not across the entire
305 population (Figure 3A). Analyses from separate, unpublished work in our laboratory indicate that peak
306 firing rate of the motor burst changes nonlinearly with depth, reaching a maximum in the intermediate
307 layers and decreasing gradually for dorsal and ventral locations. Neurons with the highest firing rates

308 resemble the classical saccade-related burst neurons, some with buildup activity, and are likely those that
309 project to the gaze centers in the brainstem (May, 2005; Rodgers et al., 2006).

310

311 Finally, we found it interesting that the regression slopes tended to be higher for blink-perturbation trials
312 than for unperturbed movements (Figure 5A). We speculate that reacceleration of saccades in the blink-
313 perturbation condition (Goossens and Van Opstal, 2000; Gandhi and Bonadonna, 2005) produces
314 residuals that likely increase the regression slope. However, we also note that the variance accounted for
315 (r^2) by these fits were lower for the blink condition (Figure 5B). This suggests that although SC activity
316 is updated to reflect the change in velocity, this compensation is likely not complete and that additional
317 temporal control signals are added downstream in the brainstem burst generator.

318

319 In summary, we present here compelling evidence that the SC has dynamic influence over every aspect of
320 the saccade. The result impacts the notion of spatiotemporal transformation, which is thought to be a
321 serial process of first encoding the movement in a retinotopic reference frame (place code) and then
322 transforming it into a rate code to control its dynamics (Groh, 2001). The SC is considered the last stage
323 of the spatial representation and gaze centers in the lower brainstem employ the temporal algorithm. Our
324 analyses show a clear role of the SC in also exerting temporal control over the duration of the movement,
325 casting a shadow on a simplistic and serial sensorimotor transformation framework. In doing so, the
326 result aligns well with observations from skeletomotor research, where it was demonstrated decades ago
327 that neurons in the cortex encode velocity of hand movement (Ashe and Georgopoulos, 1994; Reina et al.,
328 2001).

329

330

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332

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334 R01 EY024831, and F31 EY027688.

335

336 **Figure legends**

337

338 **Figure 1: Summary of within- and across-trial correlation analyses for normal saccades. (A)**

339 Within-trial correlation analysis. Black line denotes the correlation coefficient between activity and
340 velocity residuals as a function of the temporal shift. The gray outline is two standard errors around the
341 mean patterns from 189 neurons. Pink line and outline represent the mean correlation coefficients and two
342 standard deviations from the mean of the shuffled data. (B) Across-trials correlation analysis. Heatmap of
343 correlation coefficients between SC activity and eye velocity residuals for each timepoint during the
344 saccade (abscissa) and temporal shift between the two residual vectors (ordinate). Arrow and horizontal
345 dashed line mark the efferent delay at which the average correlation was highest (-12ms). Left and right
346 vertical red lines indicate respectively the beginning and the end of the shortest saccade in the dataset.
347 Data past rightmost red bar excludes saccades which have terminated prior to the timepoints on the x-
348 axis. (C) Correlation coefficients as a function of saccade timepoints for the optimal ED shown in (B).

349 Pink line and outline represent the mean and two standard deviations for the across-trials analysis
350 performed on shuffled data.

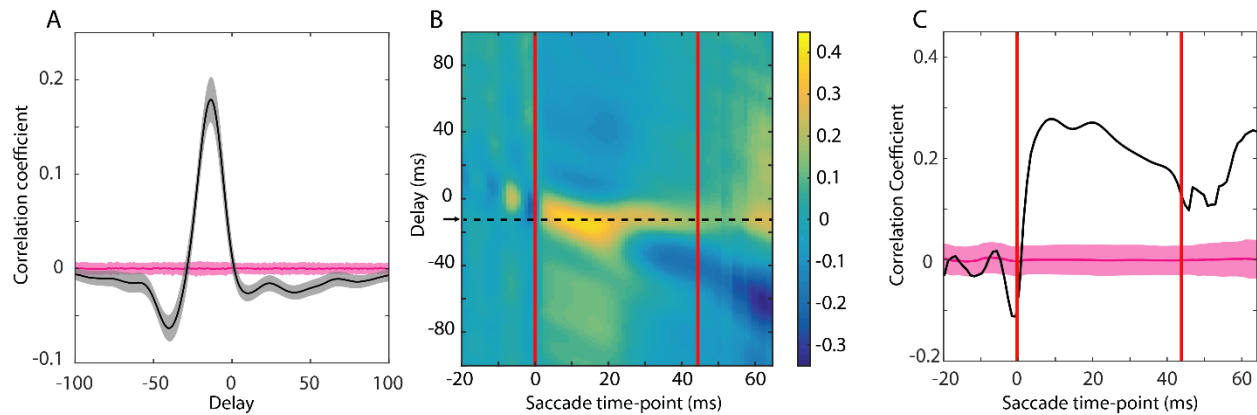
351 **Figure 2: Temporal characteristics of activity-velocity correlation.** (A) Histogram of average peak
352 correlation time relative to average peak velocity time for each neuron. The count on y-axis indicates the
353 number of neurons. (B) Histogram of cumulative duration (as proportion of total saccade length) for
354 which the correlation remained above significance level. (C) Relationship between peak correlation and
355 the duration of the correlation. Each point indicates one neuron. Blue line is the best fit line to the data.

356 **Figure 3: Analysis of data recorded from laminar probes.** (A) Peak correlation of each SC neuron is
357 plotted against the average peak firing rate of that neuron. Neurons recorded in the same penetration are
358 plotted as the same color, each color represents data from different sessions. The best fit line to each
359 session's data is shown in the matching color. (B) Data from (A) de-meanded and pooled across sessions.
360 Each de-meanded value is obtained after subtracting the respective average across all neurons in its track.
361 The dashed red line is the best fit line.

362 **Figure 4: Comparison of correlation analyses for blink-perturbed and normal saccades.** Within-trial
363 correlation between activity and velocity residuals for (A) normal and (D) blink-perturbed saccades
364 available for 50 of 189 neurons. The heatmaps of correlation coefficients obtained from across-trials
365 analysis for (B) normal and (E) blink-perturbed movements. Correlation coefficients as a function of
366 saccade timepoints for the optimal ED for (C) normal and (F) blink-perturbed saccades. The plots follow
367 the same conventions used in Figure 1.

368 **Figure 5: Linear regression features between SC activity and eye velocity.** (A) A pairwise comparison
369 of the regression slopes obtained for normal (x-axis) and blink-perturbed (y-axis) conditions for each
370 neuron. Every neuron had a statistically significant slope for at least one of the two conditions. Cyan:
371 normal trials only; magenta: blink perturbation trials only; black: both types of trials. The dashed line
372 represents the unity relationship. (B) Relationship between slope and R^2 values. Cyan: normal trials.
373 Magenta: blink perturbation trials.

374



375

376 **Figure 1: Summary of within- and across-trial correlation analyses for normal saccades. (A)**

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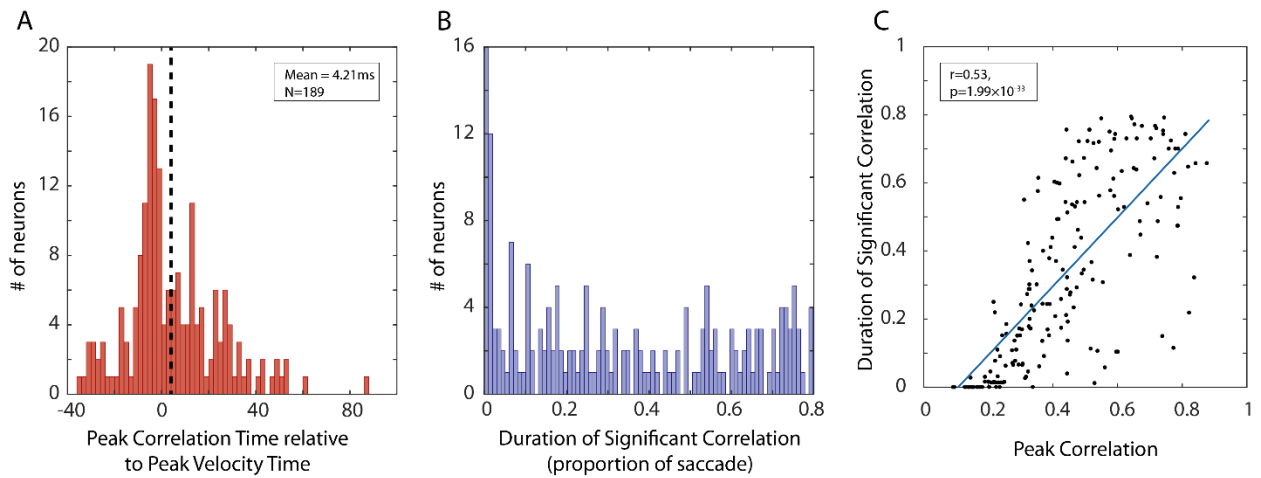
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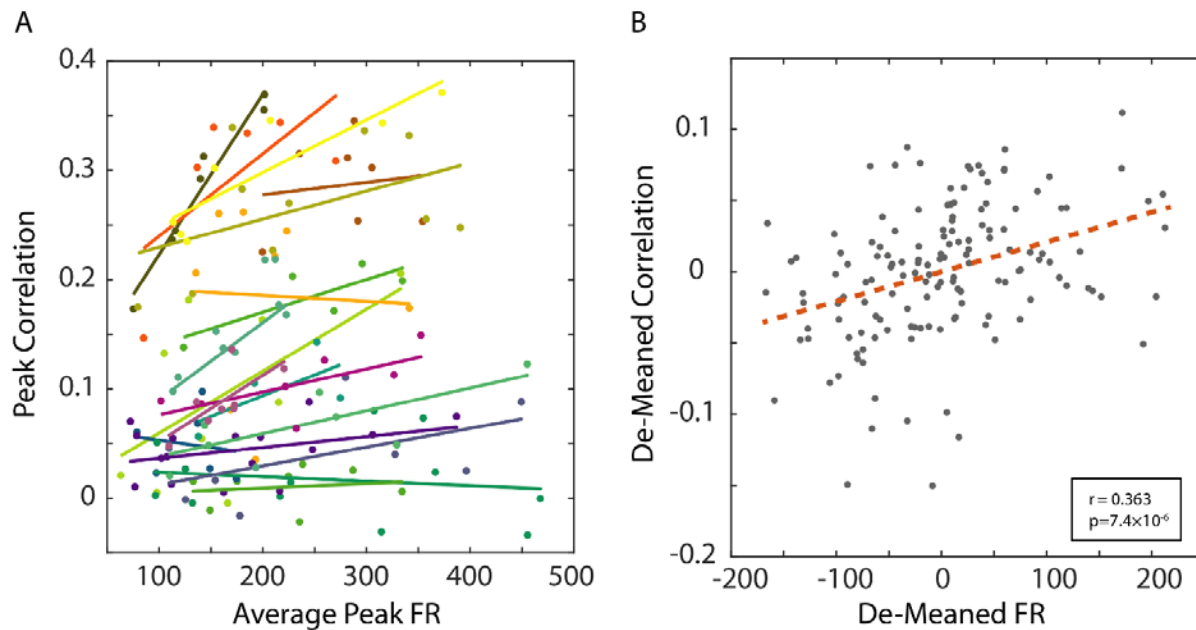
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388 performed on shuffled data.



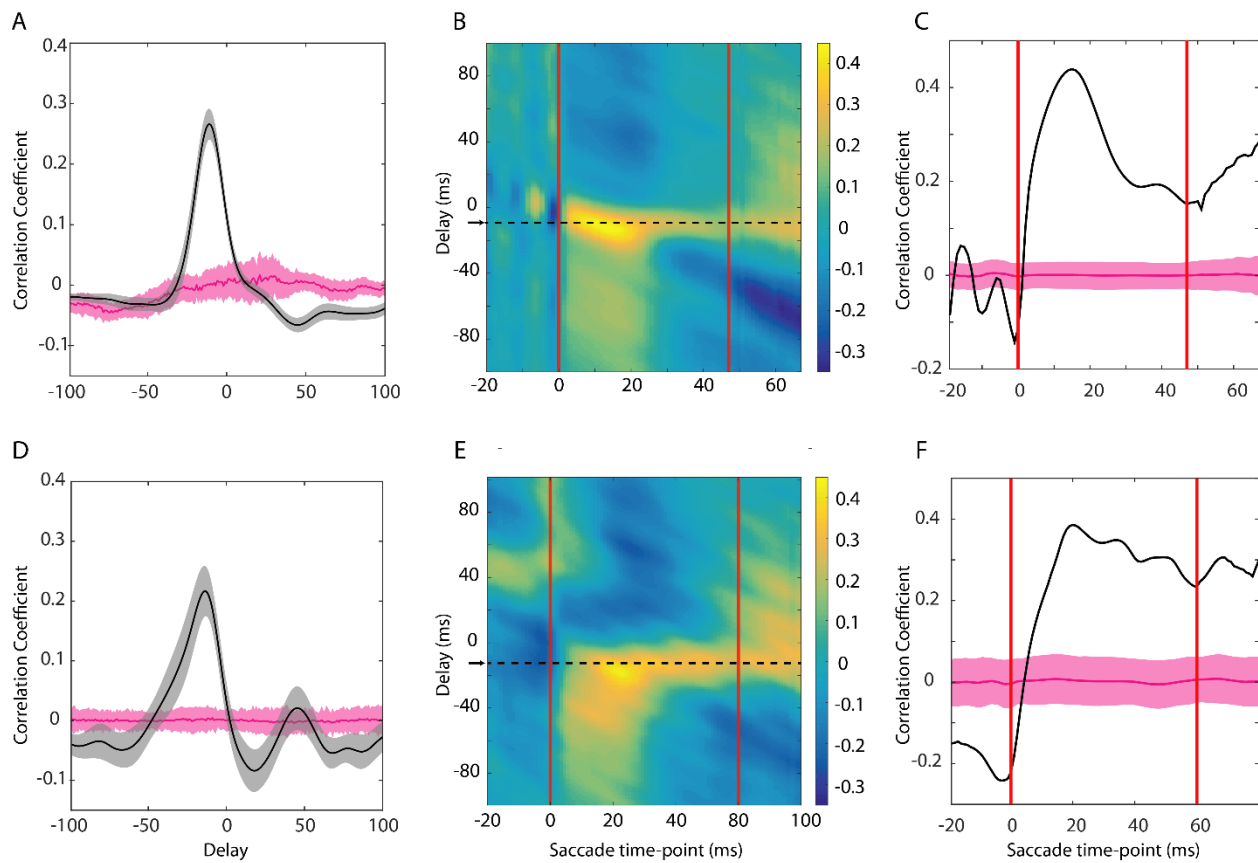
389

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393 which the correlation remained above significance level. (C) Relationship between peak correlation and
394 the duration of the correlation. Each point indicates one neuron. Blue line is the best fit line to the data.



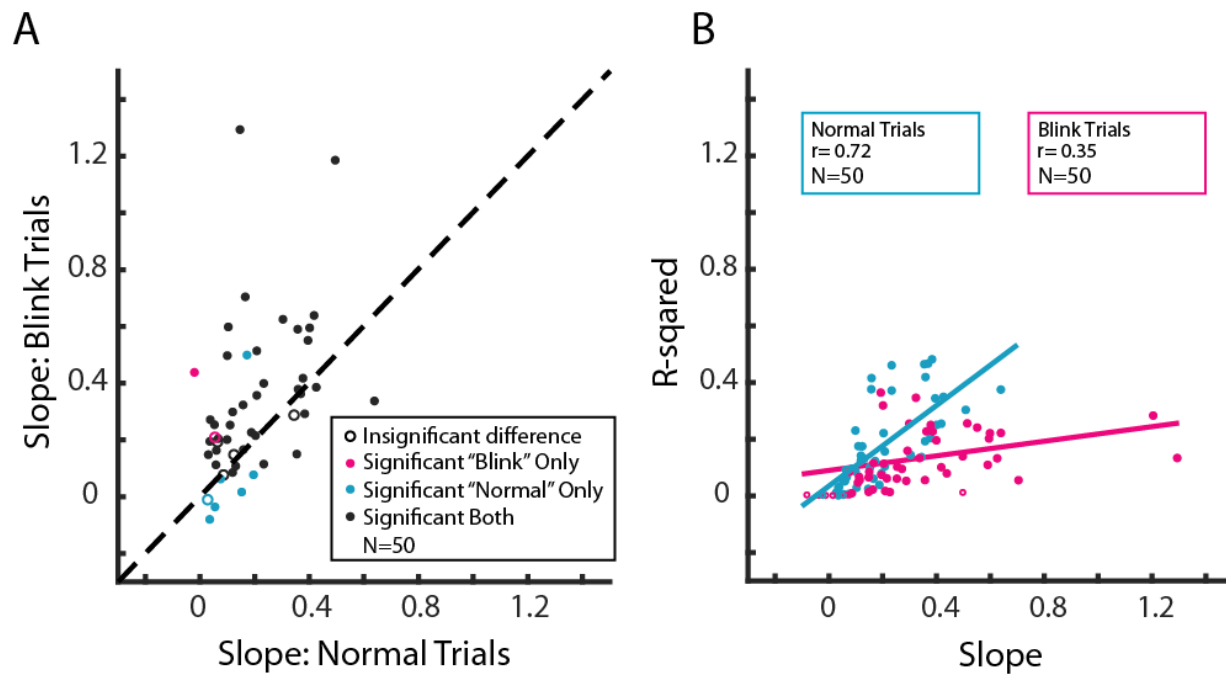
395

396 **Figure 3: Analysis of data recorded from laminar probes.** (A) Peak correlation of each SC neuron is
397 plotted against the average peak firing rate of that neuron. Neurons recorded in the same penetration are
398 plotted as the same color, each color represents data from different sessions. The best fit line to each
399 session's data is shown in the matching color. (B) Data from (A) de-meaned and pooled across sessions.
400 Each de-meaned value is obtained after subtracting the respective average across all neurons in its track.
401 The dashed red line is the best fit line.



402

403 **Figure 4: Comparison of correlation analyses for blink-perturbed and normal saccades.** Within-trial
404 correlation between activity and velocity residuals for (A) normal and (D) blink-perturbed saccades
405 available for 50 of 189 neurons. The heatmaps of correlation coefficients obtained from across-trials
406 analysis for (B) normal and (E) blink-perturbed movements. Correlation coefficients as a function of
407 saccade timepoints for the optimal ED for (C) normal and (F) blink-perturbed saccades. The plots follow
408 the same conventions used in Figure 1.



409

410 **Figure 5: Linear regression features between SC activity and eye velocity.** (A) A pairwise comparison
411 of the regression slopes obtained for normal (x-axis) and blink-perturbed (y-axis) conditions for each
412 neuron. Every neuron had a statistically significant slope for at least one of the two conditions. Cyan:
413 normal trials only; magenta: blink perturbation trials only; black: both types of trials. The dashed line
414 represents the unity relationship. (B) Relationship between slope and R^2 values. Cyan: normal trials.
415 Magenta: blink perturbation trials.

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