Metabolic adjustment enhances food web stability

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¹ Abstract

Understanding ecosystem stability is one of the greatest challenges of ecology. Over several 2 decades, it has been shown that allometric scaling of biological rates and feeding inter-3 actions provide stability to complex food web models. Moreover, introducing adaptive 4 responses of organisms to environmental changes (e.q. like adaptive foraging that enables 5 organisms to adapt their diets depending on resources abundance) improved species per-6 sistence in food webs. Here, we introduce the concept of metabolic adjustment, *i.e.* the 7 ability of species to slow down their metabolic rates when facing starvation and to increase 8 it in time of plenty. We study the reactions of such a model to nutrient enrichment and 9 the adjustment speed of metabolic rates. We found that increasing nutrient enrichment 10 leads to a paradox of enrichment (increase in biomasses and oscillation amplitudes and 11 ultimately extinction of species) but metabolic adjustment stabilises the system by damp-12 ening the oscillations. Metabolic adjustment also increases the average biomass of the top 13 predator in a tri-trophic food chain. In complex food webs, metabolic adjustment has a 14 stabilising effect as it promotes species survival by creating a large diversity of metabolic 15 rates. However, this stabilising effect is mitigated in enriched ecosystems. Phenotypic 16 plasticity of organisms must be considered in food web models to better understand the 17 response of organisms to their environment. As metabolic rate is central in describing 18 biological rates, we must pay attention to its variations to fully understand the population 19 dynamics of natural communities. 20

21 Introduction

Identifying the mechanisms responsible for ecosystem stability is one of the main sci-22 entific tasks in ecology (de Ruiter, 2005; Montoya et al., 2006; Rooney and McCann, 23 2012; Loreau and de Mazancourt, 2013). Natural ecosystems are assumed to be stable 24 (in the sense of dynamic stability, defined by the equilibrium stability and the variability 25 (Pimm, 1984; McCann, 2000)) thanks to many mechanisms resulting from the diversity 26 of interacting species (MacArthur, 1955; Elton, 1958). However, mathematical models of 27 ecosystems predicted opposite results. For instance, the theoretical study performed by 28 May (1972) demonstrated that diversity, complexity (measured by the linkage probability 29 between pairs of species) and the average interaction strength decreased the stability of 30 random interaction networks (assessed by a linear stability analysis). Subsequently, many 31 mechanisms promoting food web stability were identified and two of them inspired us to 32 implement a new one in food web models. The first mechanism is the allometric scaling 33 of biological rates (e.q. metabolic rate, feeding strength), describing them as power func-34 tions of individual body mass (Yodzis and Innes, 1992; Brown et al., 2004; Savage et al., 35 2004; Brose et al., 2008; Pawar et al., 2012; Kalinkat et al., 2013). These relationships 36 provided a better prediction of species biomasses in empirical data than any other model 37 parametrisation (Boit et al., 2012; Hudson and Reuman, 2013). In addition, allometric 38 scaling coupled with size structured communities (*i.e.* consumers larger than their prey) 39 lead to more stable food webs with fewer extinctions (Brose et al., 2006; Brose, 2008; 40 Kartascheff et al., 2010). 41

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⁴³ The second mechanism is adaptive foraging. Kondoh (2003) included adaptive forag-⁴⁴ ing behaviour into food web models to enable the consumers to maximise their biomass ⁴⁵ income by preferentially hunting more abundant prey. The result is dramatic, with a

reversion of the pattern predicted by May: with adaptive foragers, increasing species 46 richness and complexity enhances species persistence. Furthermore, food webs with ran-47 domly set interactions and adaptive foraging converge towards size-structured food webs 48 with predators systematically larger than their prey (Heckmann et al., 2012). In such 49 models, species biomasses are not the only dynamic variables, food web structures and 50 interaction parameters are also dynamic (de Ruiter, 2005). However, one central param-51 eter has always been considered constant in food web models: the metabolic rate. The 52 closest examples to adjustable metabolic rates were given by Kuwamura et al. (2009), 53 Nakazawa et al. (2011) and Wang and Jiang (2014) who considered simple models with 54 a structured population of Daphnia including metabolically active adults and dormant 55 eggs. In nature, however, many organisms exhibit phenotypic plasticity in the expression 56 of metabolism (Brown et al., 2004; Glazier, 2005; Jeyasingh, 2007; Glazier, 2009a; Carey 57 et al., 2013; Norin et al., 2015). In fact, Makarieva et al. (2005) pointed out that or-58 ganisms with different body sizes can display similar metabolic rates depending on their 59 activity. Moreover, animals from all major phyla are able to slow down their activity to 60 face harsh conditions such as drought and starvation using body mass reduction (DeLong 61 et al., 2014b), torpor, diapause (depression of 60-95%) or cryptobiosis (depression of 99-62 100%) (Guppy and Withers, 1999). Considering the metabolic activity of organisms as a 63 constant parameter is a strong assumption despite its central role in food web models. In 64 this study, we model the plastic response of metabolism similarly to adaptive foraging. As 65 adaptive foraging maximises the growth rate of consumers by varying the foraging effort 66 for the different prey, we propose that metabolic adjustment maximises the growth rate 67 by varying the metabolic rate. 68

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⁷⁰ Based on prior studies on adaptive foraging, we can predict consequences of this ad-

justable metabolism for food web models. First, this adjustable behaviour should have a 71 substantial impact on population dynamics. For instance, when the population density 72 of the prey increases, consumers will raise their metabolic activity that is directly related 73 to their consumption rate. The consequence is an increase in the predation pressure and 74 top-down control imposed by consumers on their prey at high densities. On the contrary, 75 in periods of starvation, consumers slow down their metabolic rate to minimise their loss 76 in biomass caused by respiration, which keeps predator biomasses at a level high enough 77 to avoid extinction (Chesson and Huntly, 1989; Polis et al., 1996; Chesson, 2000). In this 78 study, we wonder whether the combination of these two effects stabilises the dynamics 79 of the species (decreased amplitude and increased minima of population oscillations). In 80 consequence our second prediction is that adaptive metabolic rates increase the persis-81 tence of complex food webs. As a measure of stability, we use the time variability of 82 species biomasses (existence of fixed points and amplitude of biomass oscillation) and 83 species persistence (proportion of surviving species in a food web). 84

⁸⁵ Material and Methods

We study the impact of metabolic adjustment on a simple tri-trophic food chain and complex food webs. Both are modified versions of the Allometric Trophic Network (ATN) (Brose et al., 2006). The complex food webs rely on the Williams and Martinez (2000) niche model for their structure and on the Yodzis and Innes (1992) predator-prey model for the dynamic equations and their parameters.

⁹¹ Food web construction

The construction of the complex food webs follows the niche model (Williams and Martinez, 2000; Brose et al., 2006; Heckmann et al., 2012; Binzer et al., 2016) as it successfully

⁹⁴ predicted the food web structures of natural communities. The trophic interactions across ⁹⁵ species are set according to the algorithm detailed by Williams and Martinez (2000) with ⁹⁶ an expected connectance equal to 0.15. The basal species described by Williams and Mar-⁹⁷ tinez (2000) are set as primary producers and the others as consumers. The niche values n_i ⁹⁸ (uniformly drawn in a [0, 1] interval for each of the 40 initial species) used to parametrise ⁹⁹ the niche model are also used to calculate species body mass as follows (Heckmann et al., ¹⁰⁰ 2012).

$$M_i = 10^{N.n_i} \tag{1}$$

Here N is equal to 6, that means the biggest species is one million times larger than the smallest ones.

¹⁰³ Predator-prey model

The population dynamics of the food web follows the ATN model (Brose et al., 2006;
Williams et al., 2007).

$$\frac{dB_i}{dt} = r_i G_i B_i - \sum_{j=consumers} x_j y_j B_j F_{ji} / e_{ji}$$
(2a)

$$\frac{dB_i}{dt} = -x_i B_i + \sum_{j=prey} x_i y_i B_i F_{ij} - \sum_{j=consumers} x_j y_j B_j F_{ji} / e_{ji}$$
(2b)

These equations describe changes in relative, biomass densities of primary producers (2a) and consumer species (2b). In these equations B_i is the biomass of species *i*, r_i is the mass-specific maximum growth rate of primary producers, G_i is the logistic growth rate of primary producers (Equation (3)), x_i is *i*'s mass-specific metabolic rate, y_i is the maximum consumption rate of consumers relative to their metabolic rate, e_{ji} is j's assimilation efficiency when consuming population i and F_{ij} describes the realised fraction of i's maximum rate of consumption achieved when consuming j (equation (4)). Primary producers growth rate is modelled by a logistic growth with a shared carrying capacity K which ensures a comparable primary production among food webs, regardless the number of primary producers (equation 3).

$$G_i = (K - \sum_{\substack{j=primary\\producers}} B_j)/K$$
(3)

The consumption rate of prey depends on a Holling type II functional response with predator interference (Equation (4)). The preference of consumers for their prey ω_{ij} are set to $1/p_i$ with p_i the number of consumer *i*'s prey as we have no a priori information on preferences. Thus, all consumption rates are only driven by consumer body masses and prey biomass densities. ω_{ij} are recalculated after each extinction to follow the changes of the number of prey p_i .

$$F_{ij} = \frac{\omega_{ij}B_j}{B_0 + cB_iB_0 + \sum_{k=prey}\omega_{ik}B_k}$$
(4)

Here B_0 is the half-saturation density of *i* and *c* the predator interference.

Basically, mass specific biological rates (biomass production, metabolic rate and maximum consumption rate) follow the negative-quarter power-law relationship with species body masses as described by the metabolic theory of ecology (Brown et al., 2004; Savage et al., 2004). The time scale of the system is defined by normalising the biological rates to the mass-specific growth rate of the smallest primary producer as performed by Yodzis and

Innes (1992); Brose et al. (2006); Williams et al. (2007) (Equations 5a and 5b). Then
the maximum consumption rates are normalised by the metabolic rates (Equations 5c).
Thus, the loss due to respiration and the gain due to consumption both directly depend
on the metabolic rate (Equation (2b)).

$$r_i = \left(\frac{M_i}{M_{ref}}\right)^{-0.25} \tag{5a}$$

$$x_i = \frac{a_x}{a_r} \left(\frac{M_i}{M_{ref}}\right)^{-0.25} \tag{5b}$$

$$y_i = \frac{a_y}{a_x} \tag{5c}$$

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With M the body mass of species i, M_{ref} the body mass of the smallest primary producer, a_r , a_x and a_y are allometric constants (see Brose et al. (2006) and Williams et al. (2007) for more details on the normalisation).

136 Metabolic adjustment model

¹³⁷ We propose to model the metabolic adjustment by an optimisation of the mass-specific ¹³⁸ net growth rate g_i as in adaptive foraging models (Kondoh, 2003; Uchida et al., 2007) ¹³⁹ or in body mass plasticity models (DeLong et al., 2014b). Thus, the consumer adjusts ¹⁴⁰ its metabolic rate to maximise the balance between ingestion and respiration that both ¹⁴¹ depend on metabolic rate. Metabolic adjustment does not apply to primary producers ¹⁴² that are considered as basal resources species with constant resource supply (Equation

143 (2a)).

$$\frac{dx_i}{dt} = x_i X \frac{\partial g_i}{\partial x_i} = x_i X (-1 + \sum_{j=prey} e_{ij} y F_{ij})$$
(6a)

$$g_i = -x_i + \sum_{j=prey} e_{ij} x_i y F_{ij} \tag{6b}$$

With X the metabolic adjustment coefficient representing the speed of the adjustment. The higher X is, the faster the response of species to modifications of their growth rate is. The metabolic rate is bounded by 1 and 0.001 to ensure a minimum metabolic rate and to prevent a destabilising high metabolic rate. The values predicted by the equation 5b fall in this interval that is consistent with Makarieva et al. (2005) (Supplementary material Appendix B, Fig.B5, B6,B7,B8).

150 Simulations

The model is coded in C + + and the simulations performed with the GSL ODE solver. 151 The simple tri-trophic food chain only contains a primary producer, a herbivore and a 152 carnivore. Their body masses are respectively set to 1, 10^2 and 10^4 . For the complex food 153 webs, each simulation is independent from the other and only differs in the body mass 154 distribution and the architecture of the food web. The system starts with 40 species with 155 initial biomass of 0.1 and the metabolic rates are initialised with the values predicted by 156 the metabolic theory of ecology (Equation 5). The simulations are performed for 10,000 157 time steps and only the last 1000 steps are recorded. Species persistence is the proportion 158 of the 40 initial species that survives until the end of the simulation. Each combination 159 of parameters is tested for 100 different food webs. 160

161 Results

¹⁶² Effect of adaptive metabolic rate on species dynamics

The first system we consider is a simple tri-trophic food chain containing a primary pro-163 ducer, a herbivore and a carnivore. The effects of the resource availability on species dy-164 namics are represented by bifurcation diagrams (Fig.1). The food chain without metabolic 165 adjustment (X = 0) displays large biomass oscillations whose amplitude increases with the 166 carrying capacity K (Fig.1A) and the minima reaches extremely low values, especially for 167 the herbivore (Supplementary material Appendix A, Fig.A1A). As there is no metabolic 168 adjustment, the metabolic rates are constant (Fig.1B) and their values are those predicted 169 by the metabolic theory of ecology (Equations 5a,b,c). The food chain with metabolic 170 adjustment (X = 2) has fixed points for $K \leq 7$ and oscillations for K > 7 (Fig. 1A). 171 Despite the multi-period oscillations, the system is not chaotic (Supplementary material 172 Appendix A, Fig.A4A). The amplitude of oscillations increases with the carrying capacity 173 for all species but remains lower than in the food chain without metabolic adjustment. 174 The biomass minima increases with higher values of the metabolic adjustment coefficient 175 (Supplementary material Appendix A, Fig.A1A). The herbivore metabolic rate remains 176 constantly at the maximum value allowed by the model, whereas the carnivore metabolic 177 rate increases with carrying capacity K until it oscillates for K > 7 (Fig.1B). 178

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The tri-trophic food chain has fixed points along a gradient in metabolic adjustment coefficients for a carrying capacity K = 2 (Fig.2), except for X = 0 (origin of the x-axis corresponding to the situation described in Fig.1A). Increasing the metabolic adjustment coefficient increases the biomass of the herbivore and of the carnivore while it decreases the biomass of the primary producer. However, we observe an increase in the primary producer biomass and a decrease in the herbivore biomass for the low values of X. The

metabolic rate of the herbivore is maximum for X > 0 and the metabolic rate of the 186 carnivore first sharply increases with the increasing metabolic adjustment coefficient X18 and then it decreases (Fig.2B). The response is similar for K = 5 and X < 4 but for 188 $X \ge 4$ the system oscillates (Fig.2A), yet it is not chaotic (Supplementary material Ap-189 pendix A, Fig.A4B). Increasing the metabolic adjustment coefficient does not increase 190 the amplitude of biomass oscillations, it even decreases them for the primary producer. 191 The biomass of the carnivore increases with X, the amplitude of the oscillations of its 192 metabolic rate increases (Fig.2B) while the amplitude of its biomass oscillations remains 193 mostly unchanged. Increasing the metabolic adjustment coefficient also increases the 194 biomass minima of each species (Supplementary material Appendix A, Fig.A1B). 195

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¹⁹⁷ Effect of adaptive metabolic rates on persistence

The response of stability to metabolic adjustment and enrichment in complex food webs is 198 assessed through the average species persistence (Fig.3A). In food webs without metabolic 199 adjustment (X = 0), increasing K does not significantly change species persistence that 200 stays around 0.3. In food webs with metabolic adjustment (X > 0), for a fixed carrying 201 capacity K, increasing X promotes species persistence, especially at low values of K where 202 all species can survive. If K > 3, species persistence first decreases and then increases as 203 X increases. For a fixed value of X, increasing K decreases species persistence and thus 204 leads to an example of the paradox of enrichment. To sum up, enrichment through the 205 increase of the carrying capacity has a destabilising effect on species persistence, whereas 206 metabolic adjustment increases it substantially. 207

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²⁰⁹ We can identify two groups of species in complex food webs: 'slow species' with a low

biomass (< 10^{-2}) and a low metabolic rate (< $10^{-2.5}$) and 'fast species' with a high 210 biomass $(> 10^{-2})$ and a high metabolic rate $(> 10^{-2.5})$ (Fig.3B and 3C). Increasing 211 the carrying capacity K does not seem to change the repartition of species in these 212 two categories (Fig.3B) while more species are in an intermediate category (low biomass 213 and high metabolic rate) at low values of metabolic adjustment coefficient X (Fig.3C). 214 This difference is confirmed in Fig.3D where three groups of species can be identified for 215 X > 0.002: (a) species with minimum or low metabolic rate, (b) species with intermediate 216 metabolic rate and (c) species with maximum metabolic rate. (a) species correspond to 217 the slow species, (b) and (c) to the fast species. Such a non-differentiation of the metabolic 218 profile of species for low metabolic adjustment coefficients may be the origin of the first 219 decrease of species persistence with increasing X for K > 3 (Fig.3A). 220

221 Discussion

We studied the consequences of an adaptive metabolic rate for different aspects of food web 222 stability. We predicted that metabolic adjustment enables species to fit their metabolic 223 rate to their energy budget and the resource availability. In times of bonanza, it allows 224 species to increase their activity and then to exploit more resources. In harsh times, 225 however, metabolic adjustment also lets organisms slow down their activity to save their 226 energy until the next season of plenty (Polis et al., 1996). This behaviour is typically 227 the case for microbial organisms that can get encysted or can produce spores (Dawes and 228 Ribbons, 1962; Fenchel and Finlay, 1983; Glazier, 2009b) but also larger organisms that 229 can shift between resting and activity metabolism (Glazier, 2008; Hudson et al., 2013) or 230 hibernating (Guppy and Withers, 1999). In the case of our models, adjustable metabolic 231 rates reduce the magnitude of biomass oscillations and increase the average biomass of 232 carnivores. Additionally, they greatly increase the stability of complex food webs by 233

²³⁴ increasing species persistence at low resource densities.

²³⁵ Effect of adaptive metabolic rate on species dynamics

Our first aim was to provide a mechanistic insight in the consequences of metabolic ad-236 justment for population dynamics. We followed prior studies employing tri-trophic food 237 chains with allometric scaling of population parameters, which provides a fully determin-238 istic and easily tractable system (Otto et al., 2007; Binzer et al., 2012). First, enrichment, 239 through the increase of the carrying capacity K, has a destabilising effect on population 240 dynamics (Rall et al., 2008; Schwarzmüller et al., 2015). Such a destabilisation, called 241 paradox of enrichment, is due to the unbalance between the growth and the mortality of 242 organisms (Rosenzweig, 1971; DeAngelis, 1992; Roy and Chattopadhyay, 2007; Rip and 243 McCann, 2011). However, this destabilising effect is dampened by metabolic adjustment 244 that promotes fixed points or reduces the amplitude of biomass oscillations and increases 245 the biomass minima. Increasing the speed of adjustment (*i.e.* increasing the metabolic 246 adjustment coefficient X) is destabilising because it promotes biomass oscillations, but 247 it also increases the biomass of carnivores. We can compare our results to prior studies 248 using adaptive foraging that inspired our modelling of metabolic adjustment (Kondoh, 249 2003, 2010; Křivan and Diehl, 2005; Mougi and Nishimura, 2008). The adaptability of 250 predator attack rates or prey defences (Vos et al., 2004; Verschoor et al., 2004) also 251 decreases in the amplitude of biomass oscillations, increases the average biomass of carni-252 vores and keeps the minima away from the extinction threshold (Mougi and Nishimura, 253 2007). The outcome of these processes are similar because both rely on growth rate opti-254 misation, which seems to highly improve the persistence of higher trophic levels that are 255 generally most prone to extinction (Binzer et al., 2011). However, metabolic adjustment 256 affects both the growth and the mortality rates of consumers while adaptive foraging only 257

increases the growth rate and inducible defences decrease the mortality rate. In conse-258 quence, adaptive metabolic rates enables a better control of species dynamics, especially 259 for top consumers whose loss rate only depends on metabolic rate and not on predation. 260 In our tri-trophic food chain, carnivores have a highly variable metabolic rate while the 261 herbivore's metabolic rate always stays at the upper limit of metabolic rate range. This 262 can be attributed to a trophic cascade: the carnivore controls the herbivore population 263 and the primary producer thrives. Thus, the herbivore always has plenty of resources, 264 and increasing the metabolic rate increases more the ingestion rate and the growth rate 265 compared to the loss rate. 266

²⁶⁷ Effect of adaptive metabolic rate on species persistence

Our second aim was to address the impact of an adjustable metabolic rate on the species 268 persistence of complex food webs. The null model is a classic allometric model (Brose 269 et al., 2006) that displays an increase in persistence with increasing carrying capacity 270 and increase in the energy flow in the system (Dunne et al., 2005; Rall et al., 2008). 271 As expected, adding an adjustable metabolic rate increases the species persistence at 272 low resources levels. Similarly to the results of studies on adaptive foraging (Kondoh, 273 2003; Heckmann et al., 2012), higher adjustment coefficients (the metabolic adjustment 274 in our case) increase species persistence. Such an increase in persistence can be partially 275 attributed to the slow species with a low biomass and a low metabolic rate described in 276 our study. However, no positive relationship between density and metabolic rate has been 277 reported in previous studies (DeLong et al., 2014a; Yashchenko et al., 2016). Alternatively, 278 these slow species could just be slow in getting extinct because of their very low metabolic 279 rate (which is the loss rate in our model). However, the large diversity of metabolic rates 280 in the fast species enables these species to better adapt to the specific situation concerning 281

top-down control and resource availability of each food web, leading to an increased species persistence. The improvement in species persistence by the metabolic adjustment slips away as the carrying capacity increases. Our results obtained for the tri-trophic food chain demonstrate that metabolic adjustment dampens the paradox of enrichment but does not resolve it as in models with adaptive foraging (Mougi and Nishimura, 2007, 2008).

287 Conclusion and perspectives

Previous models studied mechanisms similar to the metabolic adjustment by using struc-288 tured populations of consumers with active adults and dormant eggs (Kuwamura et al., 289 2009; Nakazawa et al., 2011; Wang and Jiang, 2014). In these models, the resting eggs act 290 as a refuge for the consumer, enabling them to escape from starvation. This mechanisms 293 is very different of our representation of metabolic adjustment because metabolic adjust-292 ment is an energy budget optimisation process while the production of resting eggs forms 293 a seed bank maintaining a high biodiversity (Jones and Lennon, 2010). This difference 294 is emphasised by our divergent results. In fact, Nakazawa et al. (2011) found that the 295 production of resting eggs leads to more stable population dynamics as it responds more 296 to seasonality than to non-seasonal variation in resource availability (in this case the effect 297 of resting eggs is weak). Metabolic adjustment (*i.e.* response to resource availability) in 298 food webs deeply changes the outcome of the model. In fact, adjustable metabolic rates 299 greatly increase stability regarding many criteria: they increase the average biomass of 300 top trophic levels, decrease the variability in population biomass density and increase the 301 minima of population biomass density, keeping them away from the extinction threshold. 302 Including metabolic adjustment in food web models improves the representation of the 303 diversity of organisms whose metabolic activity is not predicted by the metabolic theory 304 of ecology (Guppy and Withers, 1999; Glazier, 2005; Makarieva et al., 2008; DeLong et al., 305

2014b). More broadly, considering phenotypic plasticity (as it was extensively done for 306 adaptive foraging or inducible defences for instance) is crucial to better understand the 30 fast response of organisms to environmental changes (Marshall and McQuaid, 2011; Mar-308 shall et al., 2011; Magozzi and Calosi, 2015). Interesting future directions in this research 309 agenda would be to extend metabolic adjustment to primary producers depending on the 310 supply of non-biotic resources affected by seasonality (e.q. nutrients, sun light, water...) 311 or to include more parameters such as the attack rate in the list of biological rates di-312 rectly affected by the adjustable metabolic rate. Finally, it would also be interesting to 313 set the metabolic adjustment coefficient X as an allometric parameter because single cell 314 organisms are expected to respond faster than large animals for instance. Overall, ad-315 justable metabolic rates holds great potential to represent the biology of many species in 316 natural communities as metabolic rate plays a central role in describing species biological 317 functions. 318

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326 Data accessibility

All data are included in the manuscript and its supporting information. The codes are available on Zenodo and GitHub (doi:10.5281/zenodo.1170138).

329 Supplementary materials

³³⁰ Supplementary material (available online as Appendix XXXXX (insert manuscript num³³¹ ber) at LÄNK). Appendix 1–2

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Variable	Value	Description			
B_i	$\rm kg.m^{-2}$	biomass density of species i			
r_i	dimensionless	scaled mass specific maximum growth rate of species i			
x_i	dimensionless	scaled mass specific metabolic rate of species i			
y_i	8	scaled mass specific maximum consumption rate			
e_{ji}	0.45	assimilation efficiency of species i by species j (herbivores)			
	0.85	assimilation efficiency of species i by species j (carnivores)			
G_i	dimensionless	density dependent growth rate of species i			
F_{ij}	dimensionless	functional response of species i feeding on species j			
B_0	$0.5~\rm kg.m^{-2}$	half saturation density for consumer functional response			
c	$0.5 \ {\rm m^2.kg^{-1}}$	predator interference			
ω_{ij}	$1/\mathrm{nbr}$ prey	predator i preference for species j			
a_x/a_r	0.138	metabolic rate allometric constant (primary producers)			
	0.314	metabolic rate allometric constant (invertebrates consumers)			
X	dimensionless	metabolic adjustment coefficient			
K	$\rm kg.m^{-2}$	carrying capacity of primary producers			

Table 1	Parameters	and	variables	used	in	the model
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Note: All these parameters come from Brose et al. (2006).

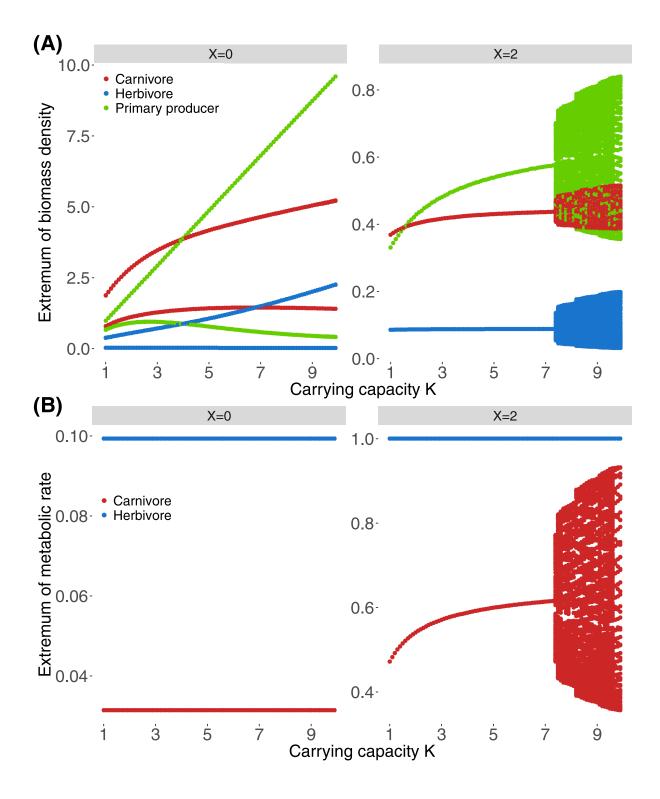


Figure 1: Bifurcation diagrams of the tri-trophic food-chain containing a primary producers (green), a herbivores (blue) and a carnivores (red). The bifurcation is performed along gradients in the carrying capacity K for **A**) biomass density and **B**) metabolic rate for a metabolic adjustment coefficient X = 0 or X = 2.

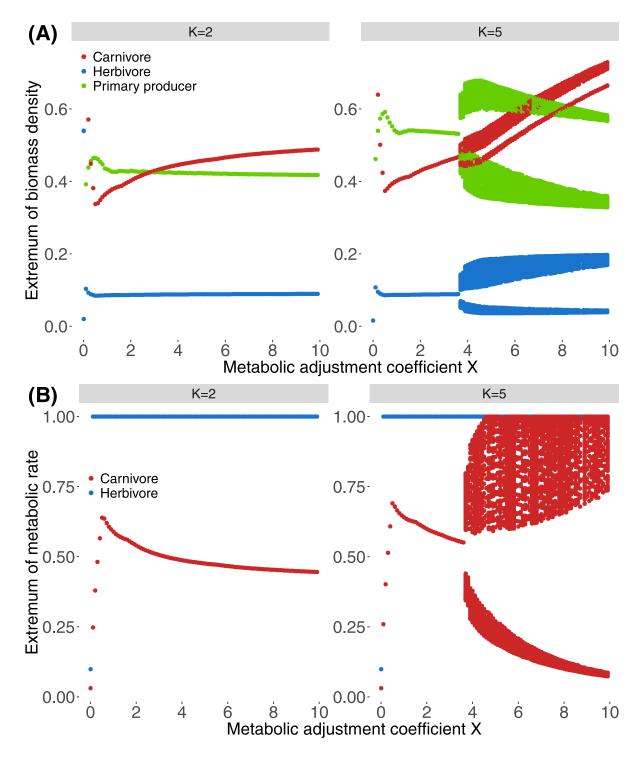


Figure 2: Bifurcation diagrams of the tri-trophic food-chain containing a primary producers (green), a herbivores (blue) and a carnivores (red). The bifurcation is performed along gradients in the metabolic adjustment coefficient X for A) biomass density and B) metabolic rate for a carrying capacity K = 1 or K = 2.

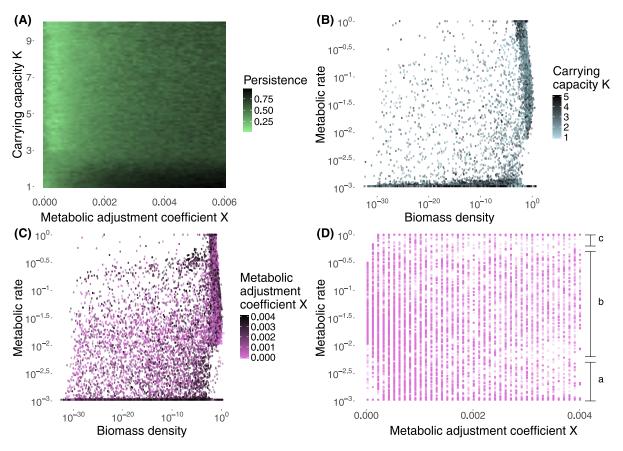


Figure 3: Effects of metabolic adjustment on complex food webs. **A)** Persistence of species for different values of metabolic adjustment coefficient X and carrying capacity K. Each square represent the average persistence for 100 replicates. **B)** Metabolic rate versus biomass density along gradient in carrying capacity K (X = 0.004). **C)**Metabolic rate versus biomass density along a metabolic adjustment coefficient gradient (K = 1.5). Each point represents one species and 100 food webs are tested for each combination of K and X. **D)** Distribution of the average metabolic rate of each species along a metabolic adjustment coefficient gradient (K = 1.5). The domains a, b and c represent respectively species with minimum or low metabolic rate, species with intermediate metabolic rate and species with maximum metabolic rate.