

Dynamic trade-offs between biomass accumulation and division determine bacterial cell size and proteome in fluctuating nutrient environments

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1 **Abstract**

2 Bacteria dynamically regulate cell size and growth rate to thrive in changing environments. While much
3 work has been done to characterize bacterial growth physiology and cell size control during steady-state
4 exponential growth, a quantitative understanding of how bacteria dynamically regulate cell size and growth
5 in time-varying nutrient environments is lacking. Here we develop a dynamic coarse-grained proteome
6 sector model which connects growth rate and division control to proteome allocation in time-varying en-
7 vironments in both exponential and stationary phase. In such environments, growth rate and size control
8 is governed by trade-offs between prioritization of biomass accumulation or division, and results in the
9 uncoupling of single-cell growth rate from population growth rate out of steady-state. Specifically, our
10 model predicts that cells transiently prioritize ribosome production, and thus biomass accumulation, over
11 production of division machinery during nutrient upshift, explaining experimentally-observed size control
12 behaviors. Strikingly, our model predicts the opposite behavior during downshift, namely that bacteria
13 temporarily prioritize division over growth, despite needing to upregulate costly division machinery and
14 increasing population size when nutrients are scarce. Importantly, when bacteria are subjected to pulsatile
15 nutrient concentration, we find that cells exhibit a transient memory of the previous metabolic state due to
16 the slow dynamics of proteome reallocation. This phenotypic memory allows for faster adaptation back to
17 previously-seen environments when nutrient fluctuations are short-lived.

18

19 **Introduction**

20 In their natural environment, bacteria must be able to sense and adapt rapidly to time-varying environmen-
21 tal stressors to survive and proliferate. Not surprisingly, bacteria exhibit tight regulatory control over their
22 growth physiology and cell morphology [1, 2], and alter both in response to fluctuating nutrient perturba-
23 tions, resulting in dynamic growth rate and cell size changes in time-varying environments [3–6].

24 Significant research has gone into understanding how bacterial cell size is coupled to growth rate [7],
25 DNA replication [8, 9], and gene expression [10] at steady-state, and how size homeostasis is maintained

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26 despite division and growth rate noise [11, 12]. In addition, characterization of a large portion of the steady-
27 state bacterial proteome across different growth conditions has improved understanding of the resource
28 allocation strategies employed by bacteria in different environments [13–15]. Motivated by experimental
29 data, various coarse-grained models of cell physiology have been developed in recent years, which explain
30 the regulation of cellular growth rate and cell size control from underlying proteome allocation strategies at
31 steady-state [10, 16–19]. However, bacteria do not exist naturally in such conditions, but instead thrive in
32 rapidly changing environments. As a result, it remains unclear how cells sense changes in the environment
33 and dynamically regulate division and growth in response.

34 Bacteria reallocate their proteome to relieve metabolic or translational bottlenecks and increase growth
35 rate under a given nutrient limitation [20], but do not always allocate resources in order to optimize steady-
36 state growth rate [21]. For example, bacteria maintain a fraction of inactive ribosomes at steady state
37 regardless of nutrient condition, presumably as a reserve which can be deployed to quickly increase growth
38 rate during nutrient upshift [4, 22]. This apparent strategy highlights the challenges of resource allocation
39 in dynamic environments, specifically that organisms must weigh the trade-offs between optimizing growth
40 rate at steady-state and employing mechanisms that are costly at steady-state but that hasten adaptation
41 to environmental changes [4, 23]. In addition, the molecular mechanisms connecting dynamic resource
42 allocation to division control in bacteria are not clear, nor is our understanding of how these allocation
43 strategies are affected by the temporal pattern of environmental fluctuations. Furthermore, it is not clear if
44 bacterial size modulation is simply a byproduct of the complex cellular response to changing environmental
45 conditions, or if it serves as an adaptive mechanism employed by the cell to improve fitness in time-varying
46 environments.

47 To understand the dynamics of bacterial growth physiology and size control in dynamic nutrient en-
48 vironments, we have developed a coarse-grained proteome sector model which connects gene expression
49 to growth rate and division control, and accurately predicts the cell-level *E. coli* response to nutrient per-
50 turbations in both exponential and stationary phase seen in experimental data [5, 24]. This is done by
51 integrating the dynamics of biochemical elements such as amino acids, ribosomes, and metabolic enzymes
52 with decision-making rules for cell division. We applied this model to study how cells allocate intracellular
53 resources dynamically in response to time-varying nutrient conditions, and found that growth rate and cell
54 size control is governed by dynamic trade-offs between biomass accumulation and cell division. Specif-
55 ically, our model predicts that bacteria temporarily divert resources to ribosome production over division
56 protein production during nutrient upshift, resulting in a temporary delay in division and an overshoot in
57 added cell volume per generation as cells prioritize biomass accumulation. Conversely, in response to
58 nutrient downshift, cells prioritize division over growth, resulting in a rapid decrease in added volume

59 and interdivision time before relaxing to their steady-state values. As a result, population and single-cell
60 growth rates uncouple outside of steady-state, potentially serving as an adaptive mechanism in time-varying
61 environments. Lastly, when simulating pulsatile nutrient conditions, we find that growth rate and cell size
62 recovery time after pulse cessation both increase with increasing pulse duration. Our model suggests that
63 this transient memory of previous environments is a result of the slow dynamics of proteome reallocation,
64 and provides a passive mechanism for faster adaptation in fluctuating environments.

65

66 **Results**

67 **Dynamic proteome allocation in time-varying nutrient environment**

68 Bacterial cells integrate time-varying environmental information through a complex set of regulatory net-
69 works to control gene expression. Despite this complexity, steady-state proteomics reveals that the expres-
70 sion of proteins with similar function are regulated reciprocally in response to growth rate perturbations,
71 such that various proteome sectors can be defined which coarse-grain the cellular milieu into a limited
72 number of collective state variables [13–15]. To investigate *E. coli* cell size and growth rate control in time-
73 varying nutrient environments, we developed a dynamic model which coarse-grains the proteome into four
74 sectors: ribosomal, metabolic, division, and "housekeeping" (Figure 1A). In this framework, the environ-
75 ment contains time-varying nutrients with concentration c , which the cell imports and converts into amino
76 acids using metabolic proteins with protein mass fraction ϕ_P . We assume that the kinetics of protein transla-
77 tion are limited by the abundance of multiple metabolites, and so coarse-grain amino acid abundance into a
78 single group of amino acid precursors, with mass fraction a . These precursors are consumed by translating
79 ribosomes, with mass fraction ϕ_R , to synthesize each of the four proteome sectors. As a result, the ribosome
80 mass fraction sets the cellular exponential growth rate, $\kappa = d \ln M / dt = d \ln V / dt$, such that growth rate is
81 defined as

$$82 \quad \kappa = \kappa_t(a)(\phi_R - \phi_R^{\min}) - \mu_{\text{ns}}, \quad (1)$$

83 where ϕ_R^{\min} denotes the fraction of ribosomes which are not actively engaged in translation, and $\kappa_t(a)$ is
84 the translational efficiency, which is dependent on amino acid availability such that translation becomes
85 significantly attenuated at low intracellular amino acid levels (see Supporting Information Section I). Here
86 we also coarse-grain the effects of protein turnover and assume that it is governed by a constant, nonspecific
87 degradation rate constant, μ_{ns} .

88 In response to changes in nutrient availability, the cell reallocates its proteome by altering the fraction
89 of translational flux, $J_i(t) = \kappa_t(\phi_R(t) - \phi_R^{\min})$, devoted to each sector, such that the time dynamics of each

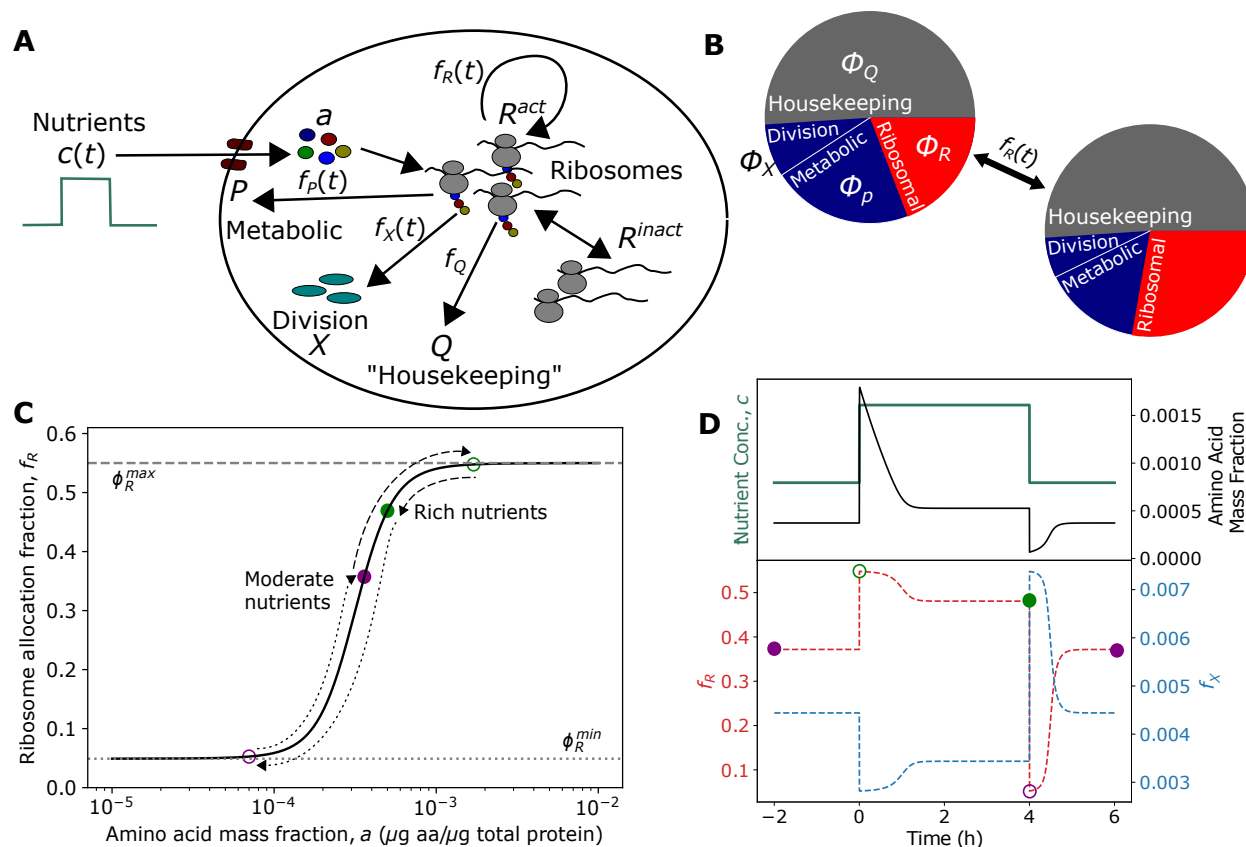


Figure 1. Dynamic resource allocation model for cell growth and division control in dynamic environments. (A) Schematic of coarse-grained model of bacterial cell size control and growth physiology. Nutrients (c) are imported by metabolic proteins (P) and converted to amino acid precursors (a), which are then consumed by ribosomes (R) to produce proteins via translation. Division occurs once a threshold amount of division proteins (X) have been accumulated. (B) By dynamically regulating the fraction of the total translational flux devoted to each proteome sector i , $f_i(a(t))$, in response to changes in a triggered by environmental changes, the cell alters its proteome composition, and thus its size and growth rate. (C) The dependence of f_R on a is the given by their steady-state relationship. The path of f_R in response to a nutrient-rich pulse is shown with colored circles corresponding to the timepoints shown in (D). f_R is initially given by its steady-state value in poor media (purple, closed). A shift to rich media results in a transient increase in f_R close to its maximum value (green, open), before relaxing back to its new steady-state value (green, closed). The path during upshift is given by the dashed line. A shift back to poor media results in a temporary drop in f_R close to its minimum value (purple, open), before relaxing back to the original steady-state value (purple, closed). The path during downshift is given by the dotted line. (D) Representative dynamics of amino acid mass fraction (top) and proteome allocation fractions (bottom) during a nutrient pulse. See Table I for a list of parameters. f_X is calculated by assuming that division timing is set by the protein FtsZ (see Supporting Information section V).

90 sector can be written as

$$91 \quad \frac{d}{dt} \boldsymbol{\phi}(t) = J_t(t)(\mathbf{f}(t) - \boldsymbol{\phi}(t)), \quad (2)$$

92 where the vectors $\boldsymbol{\phi}(t) = [\phi_R(t), \phi_P(t), \phi_X(t), \phi_Q(t)]$ and $\mathbf{f}(t) = [f_R(t), f_P(t), f_X(t), f_Q(t)]$ denote the protein
93 mass fraction and translational flux allocation fraction of each sector at time t , respectively. Proteomics data
94 from *E. coli* reveal that a significant fraction of the proteome is invariant to environmental perturbations
95 [13]. As a result, we define the "housekeeping" sector such that it contains all the proteins whose proteome
96 allocation is not growth rate dependent. Consequently, the mass fraction, ϕ_Q , and allocation fraction, f_Q ,
97 are equal and remain constant. This assertion constrains the dynamics of flux allocation such that $f_R(t) +$
98 $f_P(t) + f_X(t) = 1 - f_Q = \phi^{\max}$.

99 To model division control, we employ a threshold accumulation model of cell division in which division
100 is triggered after a cell accumulates a fixed number of division proteins (collectively referred to as X pro-
101 teins) [10, 17, 25, 26]. Since the total protein abundance per cell scales with growth rate [7, 8] and if the
102 threshold remains constant [5], the average protein mass fraction of division proteins per cell necessarily
103 decreases to maintain the constancy of the threshold, and thus must be part of the metabolic sector [12, 17].
104 Consequently, we assume that allocation to the division sector, $f_X(t)$, is given by a linear combination of
105 a basal allocation fraction, β , and a time-dependent fraction, $f_X^\alpha(t)$, whose expression is co-regulated as
106 part of a larger metabolic sector, $f_P^*(t) = \phi_R^{\max} - f_R(t)$. As a result, the flux allocation constraint can be
107 simplified such that $\phi_R^{\max} = \phi^{\max} - \beta$, where ϕ_R^{\max} represents the upper limit to allocation fraction devoted
108 to ribosomal proteins. Using the simplified constraint, $f_X(t)$ can be expressed such that its time dependence
109 is solely through $f_R(t)$, yielding

$$110 \quad f_X(t) = \alpha(\phi_R^{\max} - f_R(t)) + \beta, \quad (3)$$

111 where α is the fraction of the co-regulated sector $f_P^*(t)$ made up of division proteins. From Eq. (3), we
112 see that when the fraction of cellular resources allocated to ribosome production increases, metabolic and
113 division protein translational flux is necessarily downregulated, and vice versa (Figure 1B). This highlights
114 the trade-off that cells must make between biomass accumulation and division in dynamic environments.

115 Critically, as all other proteome sectors are defined in terms of $f_R(t)$, the time-dependence of f_R must
116 be specified. To do so, we assume that dynamic reallocation is driven by gene-regulatory networks which
117 are dependent on the amino acid pool, such that the time dependence of f_R is given through its dependence
118 on the time-varying amino acid mass fraction a , thus $f_R(t) = f_R(a(t))$. The dynamics of a are coupled to
119 Eq. (2) and are given by the difference in the metabolic and translational fluxes, such that $da/dt = J_n - J_t$,
120 where the metabolic flux, J_n , is proportional to the metabolic sector mass fraction, ϕ_P . Using the proteome

121 constraint relationship above, the dynamics of a can be written in terms of the proteome mass fractions,
122 such that

$$123 \quad \frac{da}{dt} = \kappa_n(a)(\phi^{\max} - \phi_R - \phi_X) + \mu_{\text{ns}} - \kappa_t(a)(\phi_R - \phi_R^{\min}), \quad (4)$$

124 where $\kappa_n(a)$ is the nutritional efficiency (see Supporting Information Section I), and is dependent on a such
125 that nutrient import becomes significantly attenuated at high values of a to reflect end-product inhibition of
126 biosynthesis pathways and inactivation of nutrient importers at high intracellular amino acid concentrations
127 [27].

128 Changes in environmental nutrient availability result in a flux imbalance which alters the size of the
129 amino acid pool. In this way, a acts as a read-out of flux imbalance, and so by altering proteome allocation
130 in response to a , the cell can dynamically respond to nutrient changes. To obtain the functional form of
131 $f_R(a(t))$, we assume that $a(t)$ sets the allocation fraction $f_R(a(t))$ via the steady-state relation $f_R^*(a)$, such
132 that $f_R(a(t)) = f_R^*(a(t))$. Furthermore, we assume that the cell maximizes translational flux at steady-state,
133 which allows us to express f_R solely in terms of the amino acid mass fraction, a . $f_R^*(a)$ is shown graphically
134 in Figure 1C, and predicts that proteome allocation is altered to reduce growth bottlenecks. Namely, when
135 a is high, ribosome synthesis is prioritized in order to increase translation flux, but when a is low, metabolic
136 protein synthesis is prioritized to increase nutrient import. Mathematically, any monotonically increasing
137 function for $f_R(a)$ will produce this type of regulatory behavior. However, by choosing $f_R(a)$ to be given by
138 $f_R^*(a)$, we also ensure that translational flux is maximized at steady-state. This assumption of growth-rate
139 maximization at steady-state has proved fruitful in previous theoretical models to explain bacteria growth
140 laws [16, 27–31], and has been observed experimentally to be the case for many nutrient-limiting conditions
141 [21]. Furthermore, it has been experimentally observed that *E. coli* cells evolve their metabolism towards a
142 state that maximizes growth rate [32–34].

143 Using the above framework, the dynamics of proteome allocation can be simulated in time-varying
144 nutrient environments by numerically solving the coupled Eqs. (2) and (4) (Figure 1D). In response to a
145 pulse of nutrients, allocation to ribosome synthesis increases drastically to its maximum value before slowly
146 relaxing to its steady-state value in rich nutrients (Figure 1D). In contrast, allocation to division protein syn-
147 thesis drops significantly before slowly relaxing to a lower steady-state value. Following cessation of the
148 nutrient-rich pulse, the opposite trends occur for each allocation fraction, resulting in an overshoot in f_X and
149 undershoot in f_R before both returning to their initial values (Figure 1D). Mechanistically, this regulation
150 of ribosome expression is carried out by the signaling molecule guanosine tetraphosphate (ppGpp). ppGpp
151 is synthesized when charged tRNA levels are low [35, 36]. As charged tRNA abundance is proportional
152 to amino acid levels, ppGpp thus indirectly acts as a sensor of the amino acid pool. As a result, amino

153 acid abundance is inversely proportional to ppGpp concentration, such that $[\text{ppGpp}] \propto 1/a$. In response to
154 decreased amino acid levels, ppGpp levels increase and repress rRNA expression [35, 36]. Free ribosomal
155 proteins, which can no longer bind rRNA, bind to their own mRNA and suppress additional ribosome
156 translation [37]. Conversely, when amino acids are abundant, ppGpp levels decrease which de-represses
157 ribosome production. In this way, the cell is able to regulate gene expression, and thus translational flux, by
158 responding to changes in amino acid concentration.

159

160 **Growth-rate dependent increase in cell size arises from trade-off between biomass accumu-** 161 **lation and division protein synthesis**

162 To test the validity of our resource allocation model, we first examined if the model can reproduce ex-
163 perimentally observed steady-state physiological behaviors of bacterial cells, in particular the increase in
164 average cell size with growth rate under nutrient perturbations (Figure 2A) [1, 7, 8]. To model cell size
165 control, the dynamics of proteome allocation must be connected to the dynamics of the total number of
166 division proteins per cell, $X(t)$, as cells divide at $t = \tau$ after accumulating a fixed number of X proteins,
167 $X(\tau) = X_0$. Using the relation $X = \phi_X V \rho_c / m_X$, where ρ_c is the protein mass density of the cell and m_X is
168 the mass of division molecule X , the dynamics of ϕ_X can be used to identify the dynamics of the fraction of
169 the total number of division proteins required to trigger cell division, $\tilde{X} = X/X_0$,

$$170 \quad \frac{d\tilde{X}}{dt} = \gamma f_X J_I V - \mu_X \tilde{X}, \quad (5)$$

171 where $\gamma = \rho_c / X_0 m_X$ and μ_X is the degradation rate of the division protein. We thus identify the division
172 protein synthesis rate per unit volume as $k_P(t) = \gamma f_X(t) J_I(t)$. By numerically solving proteome allocation
173 and volume dynamics in conjunction with the division rules given by Eq. (5), single cell size and growth
174 rate dynamics can be simulated in fluctuating nutrient environments.

175 At steady-state, $f_R = \phi_R$ (Eq. 2), allowing the rate of division protein synthesis k_P to be written solely
176 as a function of growth rate. In moderate to fast exponential growth conditions, the effects of protein
177 degradation are negligible. Thus assuming $\kappa \gg \mu_X$ and $\kappa \gg \mu_{ns}$, we arrive at

$$178 \quad k_P(\kappa) = \gamma(\alpha(\Delta\phi - \kappa/\kappa_f) + \beta)\kappa, \quad (6)$$

179 where $\Delta\phi = \phi_R^{\max} - \phi_R^{\min}$. When $\kappa \gg \mu_X$, this model recapitulates the adder principle employed by *E. coli*
180 to achieve size homeostasis [12], in which a constant amount of volume, ΔV , is added each generation
181 irrespective of birth size, $\Delta V \approx V_0 \approx \kappa/k_P$. We discuss deviations from this size control behavior in slow
182 growth conditions, when degradation effects become important, in the last Results section. Substituting Eq.
183 (6) into the expression for birth size yields a novel formulation of the size law [7], which links nutrient-

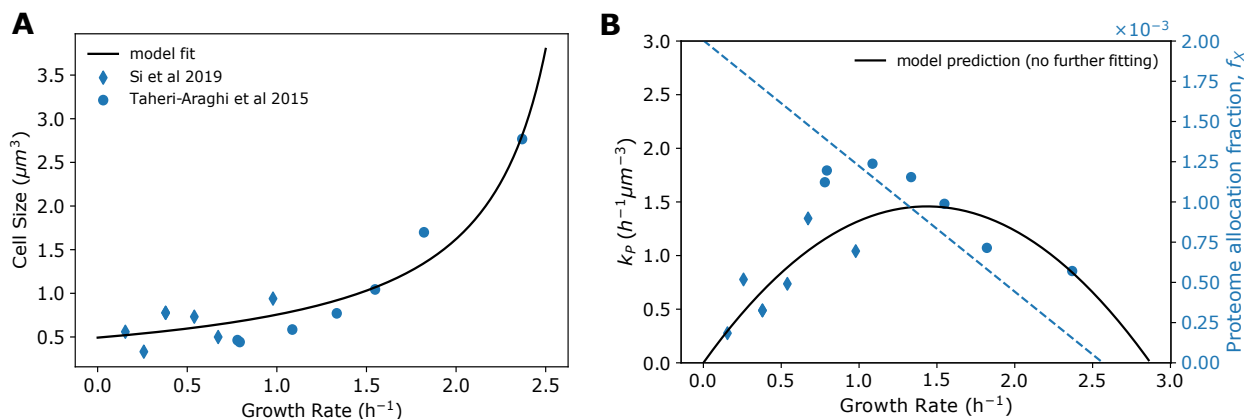


Figure 2. **Growth-rate dependent tradeoff between biomass accumulation and division protein synthesis sets steady-state bacterial cell size.** (A) Steady-state relationship between population average cell size at birth and growth rate. Solid line shows best fit of Eq. (7), yielding parameters $\gamma\alpha$, $\gamma\beta$, and κ_t , which are given in Table I. Experimental data are taken from Refs. [8, 12]. (B) Non-monotonic dependence of the division protein production rate, k_P , on growth rate, where k_P is estimated from experimental data as $\langle\kappa\rangle/\langle V_0\rangle$. Solid line given by Eq. (6), with parameters given by best fit from (A). The allocation fractions to the division protein sector is shown by dotted lines.

184 limited growth rate to cell size (Figure 2A), such that

$$185 \quad V_0(\kappa) = \frac{1}{\gamma\alpha(\Delta\phi - \kappa/\kappa_t) + \gamma\beta} \quad (7)$$

186 By fitting Eq. (7) to experimental data [8, 12] (Figure 2A), we determine the unknown model parameters $\gamma\alpha$,
 187 $\gamma\beta$, and κ_t (see Table I), which allows us to numerically predict the dependence of k_P on κ . Interestingly,
 188 Eq. (6) predicts a non-monotonic dependence of the division protein production rate on growth rate, which
 189 is seen in experimental data when considering a wide range of growth rates (Figure 2B). This behavior can
 190 be understood by considering the effects of both f_X and J_t , where here $J_t = \kappa$ when degradation effects
 191 are negligible. As growth rate decreases, translational flux allocation to division protein production, f_X ,
 192 increases while overall translational flux, J_t , decreases (Figure 2B). As such, at fast growth rates, decreasing
 193 κ results in an increase in k_P due to an increase in f_X . Conversely, at slow growth rates this increase in f_X
 194 is dominated by the decrease in J_t , resulting in a reduction in k_P . At intermediate growth rates translational
 195 flux and allocation are simultaneously moderately high, consequently yielding the maximum k_P value.

197 The expression for cell volume given in Eq. (7) predicts a maximum growth rate given by $\kappa_{\max} =$
 198 $\kappa_t(\Delta\phi + \beta/\alpha)$. This theoretical maximum, however, is nonphysical as it assumes that $f_X = \phi_X = 0$, which
 199 is never the case (Eq. 3). Growth rate is maximum when $\phi_R = \phi_R^{\max}$, thus giving an upper limit to the
 200 physical growth rate at $\kappa_{\max} = \kappa_t\Delta\phi$. Eq. (7) also implies that there is no bound on cell size. However, our
 201 expression for f_X constrains cell size to a finite value. When allocation to ribosomes is maximal, $\phi_X = \beta$,
 202 such that the maximum birth volume V_0 is given by $V_0^{\max} = 1/\gamma\beta$.

203

204 **Cells transiently prioritize biomass accumulation over division during nutrient upshifts**

205 Recent experimental results show that in response to nutrient upshift, bacteria transiently delay division
206 before increasing to a faster division rate in nutrient-rich media [5]. This behavior is seen clearly in the
207 overshoot in the average interdivision time (τ) and added volume (Δ) (Figure 3C-D). We hypothesized
208 that this delay in cell division upon nutrient upshift results from cells prioritizing ribosome production
209 over production of division proteins and metabolic proteins. Using our four-component proteome sector
210 model, we simulated single-cell growth and size dynamics in response to nutrient upshift, and were able to
211 quantitatively capture the experimental results (Figure 3A), as well as predict the dynamics of flux allocation
212 and proteome composition. Importantly, our model was also able to capture growth rate dynamics during
213 both upshift and downshift in many other experimental conditions examined recently by Erickson et al. [18]
214 (Supplementary Figure 3).

215 We simulated stochastic single-cell volume trajectories by introducing both growth rate and division
216 noise during the cell cycle, in which only one daughter cell was tracked after each division event (Figure
217 3A, bottom panel; see Supporting Information Section III). The single-cell level simulations quantitatively
218 capture the average value and noise profile of added volume (Δ), volume ratio (Δ/V_0), and the interdivision
219 time (τ) dynamics seen experimentally (Figure 3B-D). In particular, the simulations reproduce the over-
220 shoot in added volume and interdivision time following the nutrient upshift. As hypothesized, our model
221 predicts that in response to increased nutrient availability, bacteria transiently divert resources away from
222 division and metabolic protein production and instead prioritize ribosome production. This regulatory be-
223 havior occurs because an increase in nutrient availability transiently causes a mismatch in the translational
224 and metabolic fluxes, yielding a significant increase in the size of the amino acid pool, a . In response to
225 the increase in a , the cell allocates translational flux to ribosome production at the expense of division and
226 metabolic protein production (Figure 1C-D). This is seen in the temporary drop in division protein produc-
227 tion rate, k_P , and overshoot in ribosomal flux allocation, f_R , during the time period during which growth
228 rate increases, before both k_P and f_R relax to their new steady-state values (Figure 3A). Consequently, dur-
229 ing this transitional period, bacteria delay division and add significantly more biomass than their birth size
230 (Figure 3B). Importantly, a model in which division protein allocation is constant could not reproduce the
231 observed experimental results, and instead predicted that cell size is invariant to nutrient perturbations (Sup-
232 plementary Figure 4).

233

235 **Growth-rate and cell size recovery time increases with nutrient pulse duration**

236 In order to predict bacterial growth rate and cell size control in more complex time-varying environments,

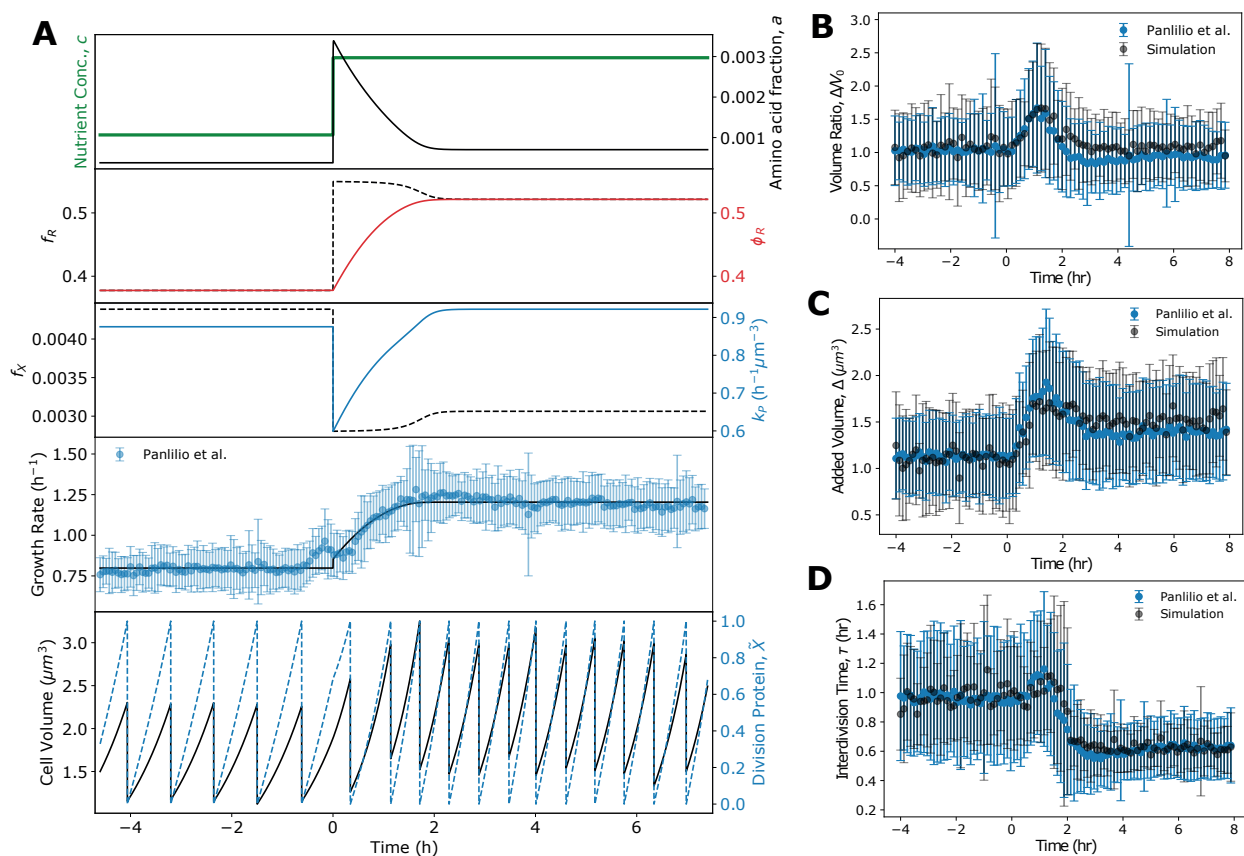


Figure 3. **Cell size and division dynamics during nutrient upshift.** (A) Simulation dynamics of average amino acid mass fraction, proteome composition, allocation fraction, and division protein production for *E. coli* cells experiencing nutrient upshift. Model parameters obtained by fitting growth rate dynamics to experimental data [5], and are provided in Table I. Bottom: Single-cell volume trajectories were simulated using the model by implementing division rules appropriate for *E. coli*. (B-D) Generation-averaged dynamics of cell volume ratio (B), added volume (C), and interdivision time (D) from single-cell volume trajectories agree well with experimental data. Error bars indicate the standard deviation of the time-binned mean for all time series.

237 we simulated single-cell trajectories experiencing a pulse of nutrient-rich media with duration τ_{feast} . For
 238 each trajectory with pulse-length τ_{feast} , we measured the time required (τ_{recovery}) for both the growth rate
 239 and cell volume added per generation to return to the pre-shift level following downshift (Figure 4A,B). In-
 240 terestingly, in both cases τ_{recovery} increased with increasing τ_{feast} until saturating at a constant value (Figure
 241 4D), showing that bacteria transiently retain memory of the previous nutrient environment across gener-
 242 ations, allowing for quicker recovery to optimal steady-state growth when experiencing short timescale
 243 perturbations in nutrient quality. As cellular growth rate is determined by ribosome abundance (Eq. 1), we
 244 hypothesized that this phenotypic memory is conferred by the slow dynamics of proteome reallocation and
 245 thus ribosome accumulation, which occur on a significantly slower timescale than translational flux reallo-

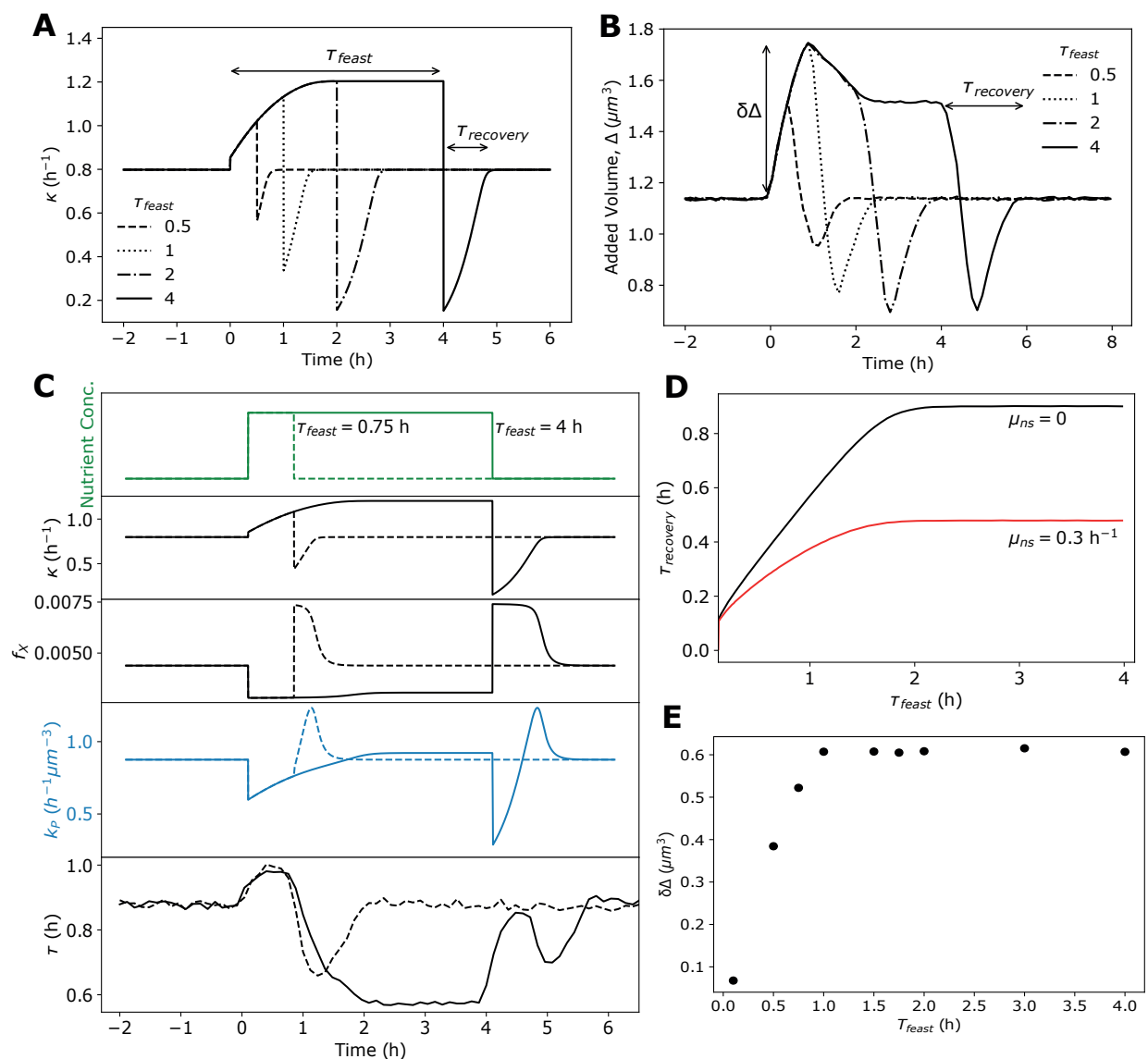


Figure 4. **Proteome reallocation and cell size regulation in pulsatile nutrient environment.** (A) Average single-cell growth rate simulations of bacteria experiencing a nutrient-rich pulse of duration τ_{feast} . For each trajectory with pulse-length τ_{feast} , the time required following downshift for the growth rate to return to within 99% of the pre-shift level was measured, given by τ_{recovery} . (B) Average dynamics of added volume, Δ , for 300 single-cell trajectories experiencing a nutrient-rich pulse as shown in (A). The time required to stabilize at the initial added volume after pulse cessation is again given by τ_{recovery} . (C) Example dynamics of simulation where $\tau_{\text{feast}} = 0.75$ h, and $\tau_{\text{feast}} = 4$ h. In both cases, the top four panels are deterministic simulations of average intracellular dynamics, whereas the bottom panel is the average dynamics of 300 single-cell stochastic simulations. (D) Quantification of the relationship of τ_{feast} and τ_{recovery} from the simulations in (A) for two different degradation rates. (E) Quantification of the relationship of τ_{feast} and τ_{recovery} from the simulations in (B). See Table I for a list of model parameters.

246 cation due to the half-life of proteins far exceeding that of mRNA [38]. As such, even though translation
247 proceeds largely at the same rate as transcription in bacteria [39], the stability of previously translated genes
248 allows for transmission of previous metabolic information across time by increasing the time required to
249 reshape proteome composition [23]. In agreement with this hypothesis, we found that the time period over
250 which cells maintain a memory of the previous state is equal to the time required to reshape the proteome to
251 become optimal in the new environment (Figures 3A and 4D). In addition, simulations were repeated while
252 including the nonspecific degradation rate, μ_{ns} , and the increase in protein turnover resulted in a reduction in
253 the recovery time and the duration of the phenotypic memory (Figure 4D). These results show that the delay
254 between translational flux reallocation and reorganization of the proteome incurs a short term fitness cost
255 by slowing adaptation, but confers a fitness advantage in fluctuating conditions as it allows cells to quickly
256 return to optimal growth in the previous condition if the nutrient perturbation is short-lived. This phenotypic
257 memory is also predicted to occur during starvation (Supplemental Figure 5), and is seen experimentally
258 [40].

259 As with τ_{recovery} , the overshoot in added volume, $\delta\Delta$, is also dependent on nutrient pulse length, such that
260 increasing τ_{feast} increases $\delta\Delta$ before saturating at a constant value (Figure 4E). This again is a consequence
261 of the slow dynamics of proteome reallocation and stems from the prioritization of ribosome production
262 over production of division machinery in response to nutrient upshift. This dynamic allocation strategy
263 results in delayed division events, and thus an overshoot in added volume.

264

265 **Cell division is prioritized over biomass accumulation during nutrient downshift**

266 Following the cessation of the nutrient-rich pulse, our model makes the interesting prediction that division
267 protein synthesis is prioritized over ribosome production and biomass accumulation during downshift, as
268 allocation to division protein synthesis transiently becomes maximal at the expense of ribosome allocation
269 (Figure 1D). This behavior can be understood by recalling that f_X and f_P are co-regulated, and that an in-
270 crease in f_X necessarily requires a decrease in f_R (Eq. 3). As a result, there is temporary increase in division
271 rate (undershoot in τ) caused by an overshoot in k_P (Figure 4C), while biomass accumulation temporarily
272 slows (undershoot in κ , Figure 4C), leading to a rapid reduction in cell size (undershoot in Δ , Figure 4B).
273 This prioritization of division protein synthesis is a surprising prediction given that following downshift
274 cells are experiencing harsher environmental conditions. We propose explanations for this behavior in the
275 Discussion section.

276 Remarkably, our model predicts distinctly different recovery behavior in interdivision time following
277 cessation of the nutrient-rich pulse, which is dependent on the time period of the nutrient pulse. This
278 can be seen clearly by comparing the simulation dynamics of bacteria experiencing nutrient-rich pulses

279 of 0.75 and 4 hrs (bottom panel, Figure 4C). Specifically, cells experiencing longer pulse lengths exhibit
280 a non-monotonic recovery of interdivision time, τ , which is not observed at shorter pulse durations. This
281 behavior can be understood by considering the impacts of both the overall translational flux ($J_t = \kappa$) and the
282 division protein allocation fraction (f_X) on division protein synthesis rate, given by $k_P = \gamma J_t f_X$. Under both
283 conditions, f_X behaves similarly immediately following downshift, namely that allocation to division pro-
284 tein production transiently increases before relaxing to its steady-state value (third panel from top, Figure
285 4C). As k_P is proportional to f_X , at short pulse lengths the increase in f_X causes an overshoot in k_P follow-
286 ing downshift (fourth panel from top, Figure 4C). Importantly, there is a temporary undershoot in growth
287 rate following downshift under both conditions, however the magnitude of this growth rate undershoot is
288 significantly larger at longer pulse lengths (second panel from top, Figure 4C) due to a greater mismatch
289 in metabolic and translational fluxes. As k_P is also proportional to κ , at longer pulse lengths the initial
290 drop in k_P is due to a temporary halt of translation. This is followed by a translation flux ramp-up in which
291 division is prioritized, resulting in a temporary overshoot in k_P , and an overall non-monotonic recovery
292 behavior in τ . Importantly, when the quality of the nutrient-rich media is reduced but the pulse length
293 remains long, there is a reduced growth rate undershoot following pulse cessation, and the non-monotonic
294 recovery in τ is not seen (Supplemental Figure 6). Thus, this pulse length-dependent division control is a
295 direct consequence of the dependence of k_P on both f_X and κ .

296

297 **Cell size-dependent protein synthesis regulates recovery from stationary phase under pulsed** 298 **nutrient supply**

299 When the environmental nutrient supply has been exhausted, bacteria halt growth and enter stationary phase.
300 Bacterial division control and size homeostasis behavior is markedly different in stationary phase compared
301 to exponential phase, and a robust mechanistic model which captures size control dynamics in both phases
302 of growth is still lacking. As such, we were interested if our model for dynamic proteome allocation would
303 successfully predict cell size and division control upon exit from stationary phase. Under such conditions,
304 the effects of protein turnover on cell physiology become crucial [41]. From Eq. (1) we see that although
305 bacterial growth vanishes in stationary phase ($\kappa = 0$), protein production does not cease completely, but
306 is balanced by the degradation rate such that the translational flux is given by $J_t = \mu_{ns} = \kappa_i(\phi_R - \phi_R^{\min})$.
307 This implies that a small fraction of ribosomes remain active and that amino acid supply comes solely
308 from protein turnover. Importantly, division protein production scales with cell volume and persists in
309 stationary phase, with $k_P = \gamma f_X \mu_{ns}$. As a result, the concentration of division proteins, c_X , at steady-state in
310 stationary phase is set by the relative rates of protein production and degradation, namely $c_X = k_P X_0 / \mu_X$,
311 predicting that cells maintain a constant concentration of division proteins in stationary phase, regardless of
312

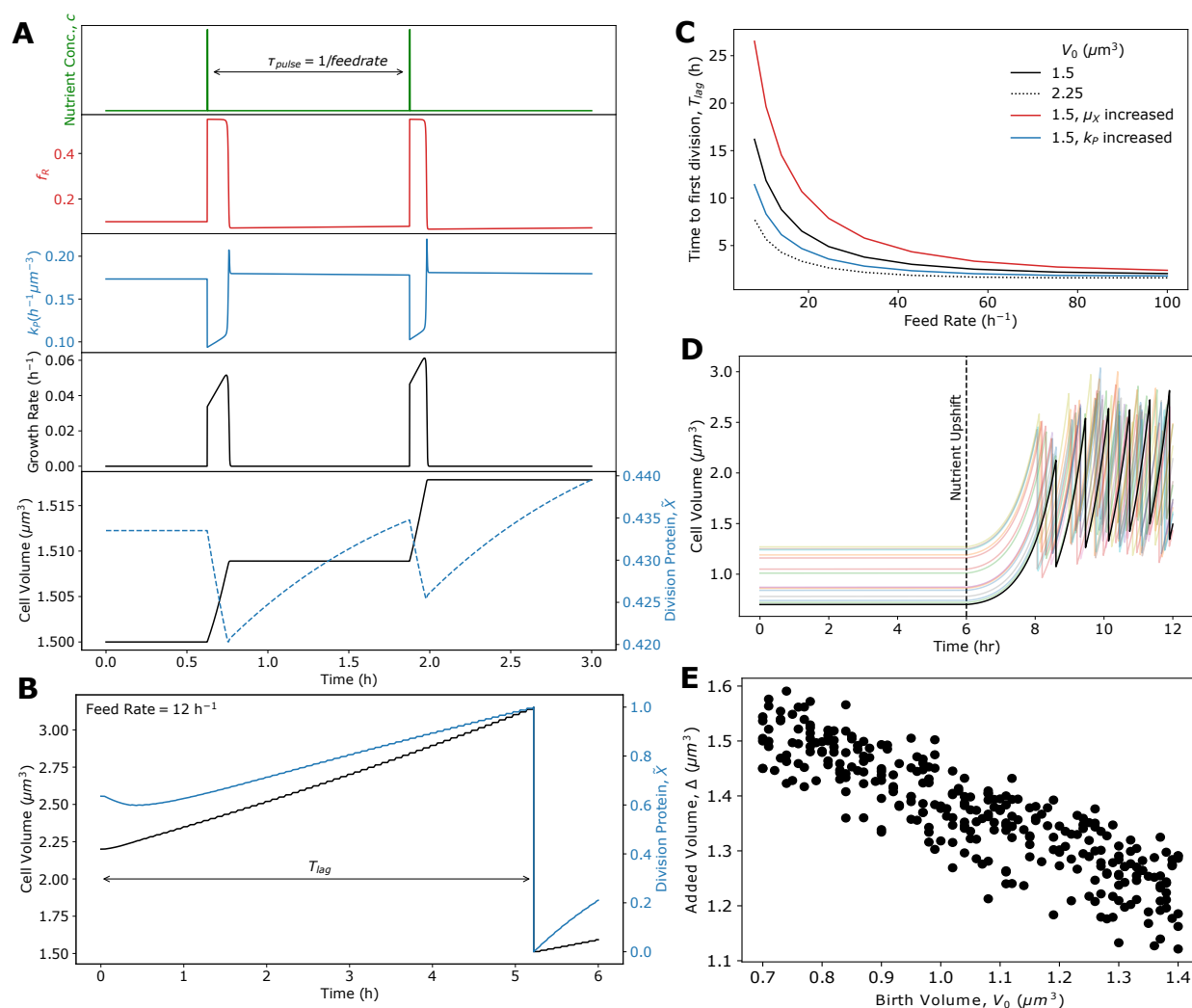


Figure 5. Cell size and division control during exit from stationary phase. (A) Single-cell simulation dynamics of ribosome allocation fraction, division protein production, growth rate, volume, and normalized X protein abundance for *E. coli* experiencing pulses of nutrients with delay τ_{pulse} starting from stationary phase. In response to an influx of nutrients, the cell temporarily decreases k_p in order to produce ribosomes. (B) Cell volume and normalized division protein abundance dynamics for a feed rate of 12 h^{-1} . (C) Using the simulation setup shown in (A), the time from pulsing onset until the first division event, T_{lag} (example trajectory shown in (B)), was measured as a function of pulse frequency (feed rate) for several initial volumes, degradation rates, and division protein production rates. For increased degradation, $\mu_X = 1 \text{ h}^{-1}$. For increased k_p , $\gamma\alpha = 2.875 \mu\text{m}^{-3}$ and $\gamma\beta = 0.875 \mu\text{m}^{-3}$. (D) Example single-cell trajectories of cells with randomized initial volumes exited stationary phase via a single nutrient shift (dotted line). (E) Negative correlation between birth volume and added volume shows that *E. coli* exhibit sizer dynamics when exiting stationary phase, which is in agreement with experimental observations [42]. See Table I for a list of model parameters.

313 cell size. Because division is dependent on the total number of division proteins and not its concentration,
314 we therefore expect larger cells to divide faster upon nutrient exposure.

315 To examine if our model was able to capture cell division dynamics in different growth regimes, we
316 simulated cell size dynamics of bacterial cells exiting stationary phase (i.e. starting at steady-state when
317 $\kappa = 0$ and $c = 0$) through pulsatile nutrient exposure of constant duration with a variable separation time,
318 τ_{pulse} (Figure 5A). As an increase in available nutrients results in an increase in the intracellular amino
319 acid mass fraction (Supplemental Figure 7) [24], our model predicts that bacteria transiently prioritize ribo-
320 some production over division immediately following pulse exposure, similar to nutrient upshift behavior
321 predicted in exponential phase (Figure 5A, Figure 3, Supplemental Figure 7). Consequently, immediately
322 following nutrient influx, k_p drops and the degradation rate dominates, resulting in a sharp decrease in the
323 division protein number, X . Importantly, in the time between pulses, X increases significantly due to an
324 increase in the division protein production rate caused by an increase in cell volume. This stands in contrast
325 to a previous model for division control in stationary phase [24], which assumed that bacteria immediately
326 allocate resources to division during nutrient upshift, causing the division protein production rate to tran-
327 siently increase before falling to some basal value if the pulse rate is of insufficient frequency. Despite the
328 stark differences in molecular details between these models, we find that the time from pulse onset to first
329 division, T_{lag} (Figure 5B), monotonically decreases with increasing feedrate (decreasing τ_{pulse} , Figure 5C),
330 which is observed experimentally [24]. This behavior occurs because although bacteria initially prioritize
331 ribosome production over division when exiting stationary phase, once the ribosome bottleneck is relieved,
332 cells then upregulate division machinery. As a faster feedrate relieves this bottleneck quicker, a faster fee-
333 drate results in a shorter lag time until division. Also consistent with experimental results [24], we find that
334 increasing the division protein degradation rate (μ_x) increases T_{lag} , while increasing the protein production
335 rate (k_p) decreases T_{lag} (Figure 5C), highlighting the importance of the degradation and volume-specific
336 protein synthesis rates in controlling division timing.

337 As cells in stationary phase maintain a constant concentration of division proteins regardless of size, our
338 model predicts that T_{lag} is dependent on initial volume in stationary phase, V_0 , such that larger cells divide
339 faster (Figure 5C). Importantly, this dependence of division timing on initial cell size is seen experimen-
340 tally [42], and is not captured by the model proposed in Ref. [24]. To more specifically investigate size
341 control mechanisms when exiting stationary phase, we simulated single-cell volume trajectories of bacteria
342 exiting stationary phase via a single nutrient upshift (Figure 5D; see Supporting Information Section III).
343 Importantly, we found that the adder model for cell size control did not hold under this growth regime,
344 but rather cells exhibited sizer-like behavior, which is characterized by the added volume being negatively
345 correlated with birth volume (Figure 5E). This behavior has been observed experimentally [42], and again

346 can be understood from our threshold accumulation model, now considering the limit when $\mu_X \gg \kappa$. In
347 such environments, bacteria divide once reaching a set size given by $V_d = \mu_X/k_P$.

348

349 **Discussion**

350 We have developed a coarse-grained proteome sector model which quantitatively captures experimentally
351 observed growth rate and size control dynamics in response to nutrient upshift in both exponential (Figure 3)
352 and stationary phases (Figure 5). Our model highlights an important resource allocation trade-off that cells
353 must make between optimizing for biomass accumulation or division in dynamic nutrient environments. In
354 response to nutrient upshift, we predict that bacteria prioritize ribosome production in both exponential and
355 stationary phase, resulting in faster biomass accumulation but delayed division. At the single-cell level, this
356 results in a transient overshoot in both added volume and interdivision time. Interestingly, when simulating
357 population level growth dynamics (see Supporting Information Section IV), we find that upshift results in a
358 temporary reduction in population growth rate (Figure 6). This raises the question, in response to increased
359 nutrient availability, why do bacteria temporarily slow proliferation? One possible explanation is that by
360 delaying division, cellular resources are freed up which can be reallocated to quickly alleviate the growth
361 bottleneck caused by a lack of ribosomes. As a result, cells are optimized for biomass accumulation instead
362 of population growth, which allows for individual cells to adapt quickly to new environments. A second ex-
363 planation is that because bacteria can quickly inactivate ribosomes [22] and recycle the amino acids through
364 degradation, cells prioritize ribosome production as a method of energy storage when the environment is
365 transiently nutrient-rich. Thus by producing ribosomes in response to nutrient upshift, bacteria simultane-
366 ously relieve the growth bottleneck caused by lack of ribosomes, while also being able to quickly convert
367 metabolites into proteins which can be reallocated in the future after the nutrients have been exhausted. This
368 strategy could allow for bacterial survival in harsher fluctuating environments, when nutrients are few and
369 far between.

370 With our model able to capture nutrient upshift dynamics, we simulated bacterial growth rate and size
371 control dynamics in response to pulsatile nutrient exposure to predict how resources are allocated in more
372 complicated time-varying environments. In such conditions, growth rate recovery time following nutrient
373 downshift, increased with increasing pulse length (Figure 4), showing that bacteria exhibit a transient mem-
374 ory of the previous metabolic state. This phenotypic memory arises from the slow dynamics of proteome
375 reallocation, and although it incurs a short term fitness cost, this passive mechanism can confer a fitness
376 advantage in fluctuating conditions, as it allows cells to quickly return to optimal growth in the previous
377 condition if the nutrient perturbation is short-lived.

378 Our simulations also yielded surprising predictions for the size control dynamics following cessation

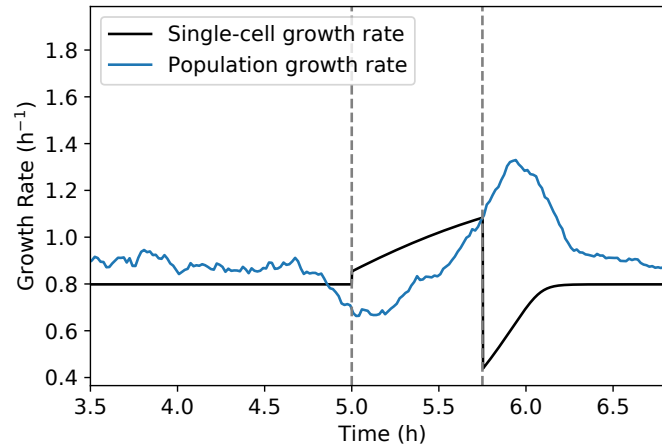


Figure 6. **Cell proliferation dynamics during nutrient up-shift.** Comparison of single-cell growth rate (black) and population growth rate (blue) dynamics in response to nutrient-rich pulse, where the population growth rate is given by the number of cell divisions per time. Dotted lines correspond to the start and end of the nutrient-rich period. See Table I for a list of model parameters.

379 of nutrient-rich exposure (Figure 4C). In particular, our model predicts that bacteria transiently prioritize
380 production of division proteins over production of ribosomes, resulting in a temporary undershoot in in-
381 terdivision time and added volume. This result is striking, because it predicts that in response to onset of
382 harsher environmental conditions, bacteria transiently upregulate the production of costly division machin-
383 ery instead of prioritizing energy storage. In addition, this prioritization of division results in a temporary
384 overshoot in population growth rate (Figure 6), meaning that the number of cells that must compete with
385 each other for nutrients sharply increases in the new, less-favorable, environment. Several potential ex-
386 planations for this behavior warrant exploration in future experimental and theoretical studies. First, by
387 increasing division events, cells rapidly decrease cell size and thus increase surface-to-volume ratio [3, 43].
388 As a higher surface-to-volume ratio results in greater nutrient influx [44, 45], decreasing cell size may
389 confer an important fitness advantage despite the metabolic cost associated with upregulating division
390 protein production. Second, bacteria may employ this increased rate of division as a population bet-hedging
391 strategy which facilitates adaptation to fluctuating environments. Previous work has shown that partitioning
392 of cellular contents at division is a major determinant of phenotypic heterogeneity [46]. Thus, by transiently
393 increasing the number of division events, a bacterial population temporarily will exhibit a broader range
394 of phenotypes. Phenotypic heterogeneity increases in adverse environments in both prokaryotic and eu-
395 karyotic populations, and previous work has shown that heterogeneity promotes adaptation to time-varying
396 stress by facilitating development of resistance-conferring mutations and/or by alleviating the fitness cost
397 of constitutive expression of unnecessary proteins [47–50]. These results suggest that bacterial cells utilize

Table I. Model parameters. See Supporting Information for more details.

Parameter	Description	Value	Growth condition	Figure number
ϕ_R^{\min}	inactive ribosome fraction [16]	0.049	all	all
ϕ_R^{\max}	maximum flux allocation to ribosome production [16]	0.55	all	all
a_t	translation attenuation threshold [27]	10^{-4}	all	all
a_n	feedback inhibition threshold [27]	10^{-3}	all	all
κ_t^0 (h^{-1})	translational efficiency rate constant	2.6	all	1, 3-6
		5.1	all	2
$\kappa_{n,low}^0$ (h^{-1})	nutritional efficiency rate constant in nutrient-poor media	5.29	exponential	1, 3, 4, 6
		0	stationary	5
$\kappa_{n,high}^0$ (h^{-1})	nutritional efficiency rate constant in nutrient-rich media	10	all	1
		62.8	all	3-6
μ_{ns} (h^{-1})	nonspecific degradation rate	0	exponential	1, 2-4, 6
		0.1	stationary	5
μ_X (h^{-1})	division protein degradation rate	0.6	all	1, 3-6
$\gamma\alpha$ (μm^{-3})	fitting parameter, contribution to k_P from co-regulated portion of f_X	2.3	all	1, 3-6
		3.6	all	2
$\gamma\beta$ (μm^{-3})	fitting parameter, contribution to k_P from basal allocation fraction of f_X	0.7	all	1, 3-6
		0.2	all	2

398 division control to increase population heterogeneity in response to harsh environmental perturbations, thus
 399 facilitating adaptation to new environments and conferring increased population fitness in time-varying
 400 environments.

401

402 Author Contributions

403 J.C.K. and S.B. designed and developed the study. J.C.K. carried out the simulations and analyzed the data.

404 J.C.K. and S.B. wrote the article.

405

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410

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