1 Comparison of neural population dynamics in the regression

2 subspace between continuous and categorical task

3 parameters

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32 Abstract

33 Neural population dynamics, presumably fundamental computational units in the 34 brain, provide a key framework for understanding information processing in the 35 sensory, cognitive, and motor functions. However, neural population dynamics is not 36 explicitly related to the conventional analytic framework for single-neuron activity, i.e., 37 representational models that analyze neuronal modulations associated with cognitive 38 and motor parameters. In this study, we applied a recently developed state-space 39 analysis to incorporate the representational models into the dynamic model in 40 combination with these parameters. We compared neural population dynamics 41 between continuous and categorical task parameters during two visual recognition 42 tasks, using the datasets originally designed for a single-neuron approach. We 43 successfully extracted neural population dynamics in the regression subspace, which 44 represent modulation dynamics for both continuous and categorical task parameters 45 with reasonable temporal characteristics. Furthermore, we combined the classical 46 optimal-stimulus analysis paradigm for the single-neuron approach (i.e., stimulus 47 identified as maximum neural responses) into the dynamic model, and found that the 48 most prominent modulation dynamics at the lower dimension were derived from 49 these optimal responses. Thus, our approach provides a unified framework for 50 incorporating knowledge acquired with the single-neuron approach into the dynamic 51 model as a standard procedure for describing neural modulation dynamics in the 52 brain.

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Keywords: monkey, neural population dynamics, regression subspace, orbitofrontal
cortex, hippocampus

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57 Introduction

Recent innovations in the state-space analysis applied to multi-neuronal activities 58 59 provide insight into the dynamic structure of information processing in a neural 60 population (Brendel et al., 2011; Churchland et al., 2012; Mante et al., 2013). The 61 identified dynamic structures of neural population activity are known as neural 62 population dynamics and are assumed to reflect some underlying computations 63 occurring in a neural network in the sensory, cognitive, and motor domains (Aoi et al., 64 2020; Churchland et al., 2012; Murray et al., 2017; Okazawa et al., 2021; Osako et 65 al., 2021; Raposo et al., 2014; Rossi-Pool et al., 2021). In the state-space analysis, 66 multi-neuronal interactions with fine temporal evolution have provided a different 67 perspective from the conventional analytical framework for single-neuron activity, 68 known as the representational model. In this conventional framework, the neuronal 69 discharge rate of a single neuron is assumed to reflect some mathematical 70 parameters presumably computed in a neural circuit, such as the Gabor function in 71 the visual cortices (Jones & Palmer, 1987; Tolhurst & Movshon, 1975), movement 72 direction (Georgopoulos et al., 1982) and muscle force (Fetz & Cheney, 1980) in the 73 motor cortices, reward value in the parietal cortex (Platt & Glimcher, 1999), and the 74 location of animals during navigation in the hippocampus (O'Keefe & Dostrovsky, 75 1971). As dynamic and representational models have rarely been analyzed 76 simultaneously, a fundamental question remains as to how these two different 77 approaches reflect putatively different or shared aspects of neural computation 78 employed by each neuron and the underlying neuronal network, as well as their 79 relationship.

Theoretical neuroscience has provided a quantitative basis for the computation of single neurons in the brain (Dayan & Abbott, 2001). The theory has been developed in parallel with the development of measurement technology for neuronal activity (Yuste, 2015). The early representative model was developed when

84 researchers observed only one neuron while animals performed a behavioral task or 85 were under anesthesia. As the single-neuron recording technique provides fine 86 neuronal activity in vivo (Evarts, 1968; Hubel & Wiesel, 1959; Mountcastle & 87 Henneman, 1949; Wurtz, 1968), an analytical and theoretical framework was 88 developed to describe the functional role of separately recorded single-neuron 89 activity. Recently, large-scale multi-channel recording technology has been 90 developed to measure a large number of isolated neurons (Buzsaki et al., 2015; Jun 91 et al., 2017) never imagined before. These simultaneously recorded single-neuron 92 activities in the tens of thousands motivated computational neuroscientists to pursue 93 a theoretical framework for neural computations that provides a different perspective 94 from the conventional representational model (Aoi & Pillow, 2018; Elsayed & 95 Cunningham, 2017; Keemink & Machens, 2019; Saxena & Cunningham, 2019; Vyas 96 et al., 2020).

97 Neural population dynamics, derived through dimensional reduction of neural 98 population activity and its projection onto parsimonious dimensions, describe the 99 temporal structures of neural response in fine time resolutions in the order of 100 approximately 10 ms, different from other conventional population analyses, e.g., 101 (Georgopoulos et al., 1982). Both analytic frameworks have described brain function 102 in various functional domains, but the relationship between the developing dynamic 103 model and the conventional representational model remains unclear. Indeed, we do 104 not really know whether and how the neural population described by the conventional 105 representational model is described from a dynamic-system perspective. Thus, it is 106 challenging to incorporate knowledge acquired from the representational model into 107 the dynamic model in the form of neural population dynamics.

We previously developed a variant of state-space analysis for continuous parameters (Yamada et al., 2021), which describes how neurons dynamically encode some cognitive parameters in the regression subspace at the population level.

111 Although the pseudo-population of neurons was composed of non-simultaneously 112 recorded single-neuron activity according to the representational framework, our 113 previous study successfully described neural modulation dynamics using continuous 114 parameters related to value-based decision making. Nevertheless, the other standard 115 parameter for single-neuron recordings, categorical, was not incorporated previously, 116 and thus, our previous analysis were not able to describe all types neural 117 modulations in a dynamic system perspective. Here, we applied our analysis to the 118 pre-existing datasets using a typical factorial design for conventional single-neuron 119 recordings, i.e., categorical task parameters, from the hippocampus in monkeys 120 performing a memory retrieval task (H. Chen & Naya, 2020). Our approach provided 121 the temporal structure of neural modulations for both types of task parameters 122 moment-by-moment, which would not be possible with the representational model, 123 while most aspects of neural modulation were dynamically described, consistent with 124 the conventional representational model. Thus, our analytic approach is beneficial to 125 analyze neural modulation dynamics for all types of pre-existing data allowing 126 researchers to incorporate the representational model into a dynamic system.

127

128 Results

129 Task, monkey's behavior and datasets

130 Details of the behavioral training, learning progress, and behavioral performance of 131 the animals in the cued lottery task (Exp. 1, Yamada et al., 2021) and in the item-132 location-retention (ILR) task (Exp. 2, Chen & Naya, 2020) have been previously 133 reported. Briefly, after completing training in Exp. 1, the monkeys learned to estimate 134 the expected value of the lottery, defined as a multiplicative combination of 135 probability and magnitude, and chose the option with higher expected values 136 (Yamada et al., 2021). This choice behavior was observed separately from the neural 137 recordings. We used the neural activity recorded from the central par of the

138 orbitofrontal cortex (cOFC) in the non-choice condition where a single lottery cue and 139 its outcome were provided to the monkeys (Figure 1A–C). In Exp. 2, the monkeys 140 learned to retain the types of visual items and their presented location during the 141 encoding phase, after which the monkeys indicated whether the sample item was 142 matched to the cued items by choosing the memorized location (Figure 1D). Six 143 visual items and four locations were used (Figure 1E). We used the neural activity 144 recorded from the HPC (Figure 1F), after which the sample stimulus was presented 145 to the monkeys during the encoding phase.

146 In this study, we constructed two pseudo-simultaneously recorded populations of 147 neurons by aligning the single-neuron activity of the cOFC (Figure 1C, 190 neurons) 148 and HPC (Figure 1F, 590 neurons) with respect to the lottery cue onset in the single-149 cue task (Figure 1A, gray bar) and the sample onset in the ILR task, respectively 150 (Figure 1D, gray bar), with a 0.6-s time window for each. Note that the HPC 151 population data in Exp. 2 has been analyzed and reported using a representational 152 model, but never analyzed using a dynamic model. Note also that the cOFC 153 population data in Exp. 1 has been analyzed using both representational and 154 dynamic models, and here, we repeated the same analysis with the shorter analysis 155 time window after the cue presentation (2.7 s time window was used in Yamada et al., 156 2021).

157

158 Conventional analyses for detecting task-dependent modulations

We first applied common conventional analyses such as the general linear model: linear regression in Exp. 1 and ANOVA in Exp. 2, respectively (see Methods). Detailed results from these conventional analyses have been previously reported (Figure 2E–O in Yamada et al., 2021, Figures 2 and 5 in Chen et al., 2020). In Exp. 1, the linear regression analysis showed that the cOFC neurons encode both probability and magnitude to some extent after cue onset, as shown in an example neuron 165 (Figure 2A–B, n = 119 trials, coefficient: intercept, -0.74, t = -0.72, P = 0.47; 166 probability, 8.55, t = 6.91, P < 0.001; magnitude, 11.1, t = 8.95, P < 0.001). This 167 conventional analysis showed whether the probability and magnitude cued by the 168 lottery, both continuous parameters, modulated neuronal activity in each neuron. In 169 the cOFC populations, approximately half of the neurons were modulated by the 170 probability and magnitude of rewards during the 1-s time window (0-1 s after cue 171 onset, probability: 44%, 84/190, magnitude: 49%, 94/190). The analysis with 0.02-s 172 time bins, used to analyze neural population dynamics latter, showed that the 173 percentages of neurons modulated by these two parameters increased and then 174 decreased during the 1.0 s after the onset of the lottery cue (Figure 2C).

175 In Exp. 2, ANOVA showed that the HPC neurons could encode both types of 176 items and their presented locations to some extent, as shown in an example neuron 177 (Figure 2D–E, two-way ANOVA, n = 240 trials, item: $F_{(5,216)} = 79.50$, P < 0.001, 178 location: $F_{(3,216)} = 5.48$, P = 0.001). The analysis showed whether the items and 179 locations, both categorical parameters, modulated neuronal activity in each neuron. 180 In the HPC population, considerable proportions of neurons were modulated by these 181 two factors (0.08-1 s after sample onset, Item, 26%, 152/590, Position, 22%, 182 131/590). These proportions were significantly smaller than those of the cOFC 183 neurons modulated by the probability and magnitude in Exp. 1 (Chi-squared test, df 184 =1, P < 0.001 for all cases). In the 0.02-s time bins, the percentages of neurons 185 modulated by these two factors increased and then decreased during the 1.0 s after 186 the onset of the sample stimulus (Figure 2F).

In short, the general linear model detected neural modulations using continuous
 and categorical parameters, which are usually used in the standard representational
 model, but these analyses did not clearly provide temporal structure of neural
 population signals.

191

192 State-space analysis for detecting neural modulation dynamics at the 193 population level

194 State-space analysis originally provided temporal dynamics of neural population 195 signals related to cognitive and motor performances for whole neural activity changes 196 under an assumption of linear system (Churchland et al., 2012; Mante et al., 2013). 197 We previously developed a variant of the state-space analysis, which extracts the 198 temporal structure of neural modulation by the task-related continuous parameters, 199 probability and magnitude of rewards (Yamada et al., 2021). Here, we extend this 200 analysis to neural modulations by categorical parameters to describe how the HPC 201 neural population reflects item and location dynamically. We represented each 202 neural-population signal as a vector time series in the parsimonious dimensions in 203 two steps (Figure 3). First, we used a general linear model to project a time series of 204 each neural activity into a regression subspace composed of task parameters as 205 continuous (Figure 3A) and categorical (Figure 3B) (see Methods for details). This 206 step captures the across-trial variance caused by the task-related parameters 207 moment-by-moment at the population level. Note that this step requires an 208 orthogonal matrix for task parameters because the estimation of the regression 209 subspace is distorted given that the estimation of the regression matrix assumes 210 orthogonality between parameters. Second, we applied PCA once to the time series 211 of neural activities in the regression subspace in each neural population. This step 212 determined the main feature of the neural population signal moment-by-moment in 213 the predominant dimensions at the population level. Because neural activations are 214 dynamic over time, this analysis identified whether and how signal modulations occur 215 as a time-series of eigenvectors. These extracted time series of eigenvectors 216 captured how the main neural modulation evolved as a vector angle and size, and 217 their deviance at the population level (Figure 3C).

We evaluated the eigenvector properties in the first three principal components (PC1 to PC3) in each neural population in terms of vector angle, size, and deviance. We compared two neural populations recorded during two different cognitive tasks in terms of these vector properties.

222

223 **Neural population dynamics reflecting continuous and categorical parameters**

224 Our state-space analysis described the neural population dynamics in the cOFC 225 (Figure 4A–C) during the perception of visual lotteries. In our previous study, we 226 reported neural population dynamics during whole a cue period of 2.7 s (Yamada et 227 al., 2021), but here, we analyzed the dynamics only during the initial 0.6 s to ensure 228 that the neural population structures would be comparable between the cOFC and 229 HPC populations with continuous and categorical parameters. We first confirmed the 230 performance of the state-space analysis indicated by the percentages of variance 231 explained in the cOFC population (Figure 4A). The cOFC population exhibited high 232 performance, more than 40% of the variance was explained by PC1 and PC2 (see 233 gray arrowhead). This is consistent with our previous findings (Figure 7A in Yamada 234 et al., 2021, 27% in 0.02s bin during 2.7 s). We then characterized the whole 235 structure of the cOFC population by plotting its eigenvectors moment-by-moment 236 with the temporal order. As shown in Figure 4B, the eigenvectors for PC1 and PC2 237 evolved less than 0.2 s after the onset of the cues in both probability and magnitude, 238 while the eigenvectors shortened after approximately 0.3 s. These changes in 239 eigenvectors were very stable in terms of vector angle (Figure 4C, top), as seen in 240 the vector evolutions at 45° in angle between the PC1 and PC2 plane (see also 241 Figure 7B in Yamada et al., 2021), while the vectors changed in PC3 in the opposite 242 direction from positive to negative over time (Figure 4B and Figure 4C, bottom). Thus, 243 these stable structures in the top two dimensions are consistent with our previous 244 ones, even when the analysis window sizes differed.

245 Upon analysis of the HPC population as modulated by the two categorical 246 parameters, the performance of the analysis was lower than that in Exp. 1 (Figure 247 5A). The first two PCs only explained approximately 10% of the variance (see gray 248 arrowhead) possibly because the percentages of modulated neurons in the recorded 249 HPC population were not high compared to the cOFC populations (Figure 2C and F). 250 This might also be partly because of the larger data matrix composed of 10 vectors at 251 each time point (six items and four locations) and a larger neural population 252 containing 590 neurons: total X of size $N_{(590)} \times M_{(300)}$ because in our previous study, 253 PCA performance decreased as the matrix size increased (Figure 7A in Yamada et 254 al., 2021). We evaluate the effect of matrix size on PCA performance later in the 255 manuscript (Figure 9). The eigenvectors in the first three PCs appeared to describe 256 the neural population dynamics in the HPC. For example, the extracted eigenvectors 257 for each visual item evolved within a reasonable range of time; increase and then 258 decreased during approximately 0.2 to 0.5 s (Figure 5B), consistent with our previous 259 findings using typical conventional analysis (Figures. 2 and 3 in Chen and Naya, 260 2020). In clear contrast, the eigenvectors for locations did not show clear trends over 261 time (Figure 5C), as the location information was shown to the monkeys before the 262 sample presentations. When plotting the eigenvectors in the space of the first three 263 PCs, the eigenvectors consistently evolved in one direction in the spaces of PC1 and 264 PC2 (I2, I3, and I6) or in PC3 (I1, I4, and I5) (Figure 5D, left). In contrast, the 265 eigenvectors for the locations were positioned at a constant location across time 266 (Figure 5D, right). Unambiguously, arrangements of the eigenvectors for items and 267 locations were orthogonalized, as seen in the item representations in the second and 268 fourth quadrants and location representations in the first and third quadrants (Figure 269 5D, top row). Thus, our state-space analysis in the regression subspace successfully 270 described neural modulation dynamics in the HPC populations similar to the cOFC

271 populations, while they reflect continuous and categorical parameters in their neural

272 modulations.

273

274 Effect of shuffle control on PCA performance

275 To validate the significance of these findings, we used a shuffle control procedure in 276 three ways (see Methods for details), which determines the number of available 277 dimensions in the neural population. In shuffled conditions 1 and 2, information on 278 task-related parameters was partially shuffled in the regression subspace, matrix X. 279 In shuffle condition 1, random permutation of neuron, n, was performed at each time i, 280 eliminating the temporal neural modulation structure by condition C across each 281 neuron but retaining the effect of neural modulation at each time, *i*, at the population 282 level. In shuffle condition 2, random permutation of time, *i*, was performed in each 283 neuron, n, eliminating the temporal neural modulation structure by condition C in 284 each neuron but retaining the effect of neural modulation in each neuron, n, at the 285 population level. In shuffled condition 3, random permutation of both time i and 286 neuron n was performed. We evaluated the performance of the PCAs for each 287 condition of each experiment.

288 As shown in Figure 6, these three shuffle control procedures reproduced 289 different disturbances in neural populations. In shuffle conditions 1 and 3 (Figure 6A, 290 left and right), the explained variance decreased compared to those from the original 291 data in the cOFC population. In shuffle condition 2, a considerable amount of 292 variance was explained by PCA (Figure 6A, middle). These effects are consistent 293 with those of our previous study (Figure 5A, E, and I in Yamada et al., 2021). 294 Because the eigenvectors were very stable across time in the cOFC population 295 (Figures 4B and 4C), the shuffle within each neuron did not strongly affect PCA 296 performance (Figure 6A, middle). In contrast, the shuffle among neurons at each time 297 point, t, strongly reduced the performance of PCA because neural modulation

298 differed neuron-by-neuron (Figure 6A, left). The same effects of shuffle controls were 299 observed in the HPC population, for which categorical parameters were used (Figure 300 6B); a considerable amount of variance was explained by PCA in shuffled condition 2. 301 When examining the details of the decreased performance in each experiment, the 302 performances of the first three PCs and the first twelve PCs were better than those in 303 shuffled control condition 2 in Exp. 1 and Exp. 2, respectively (P < 0.05 for all these 304 cases). Thus, the total number of available dimensions differed between the 305 experiments. Note that all three shuffles destroyed the structured neural population 306 dynamics to some extent, consistent with our previous findings (Figure 5F and J in 307 Yamada et al., 2021).

308

309 **Preference ordering in compatible with the representational model**

310 To incorporate the conventional analytic framework into neural population dynamics, 311 we reconstruct the regression subspace in line with the conventional perspective, 312 such as neural preference to task conditions, item and location in this case. We 313 analyzed the most preferred to least preferred conditions for items and locations in 314 each neuron, in which item and location were remapped to the most preferred to 315 least preferred in each condition of item and location neuron-by-neuron, defined 316 using whole activity in the 0.08-0.6 s analysis window in each neuron. Thus, the 317 regression subspace became composed of the same size, total X of size $N_{(590)} \times N_{(300)}$, 318 but the condition, C, was changed to the most preferred to least preferred items and 319 the most preferred to least preferred locations.

The percent variance explained by the model for PC1 and PC2 was almost the same in the preference-ordering analysis (Figure 7A, 11%) compared to the original analysis (Figure 5A, 10%). The composition of the eigenvectors was also similar between the analyses in the PC1 and PC2 dimensions, locating at the second and fourth quadrants from the most preferred (lb, best item) to the least preferred (lw, worst item), but they were clearly different in the PC3 dimension, as seen in the most preferred item (lb) (Figure 7B, left bottom). The composition of eigenvectors for locations was not clearly changed by preference ordering, even for PC3 (Figure 7B, right bottom). Thus, preference ordering may affect the eigenvector compositions at higher dimensions, equal to or more than PC3.

330

331 Quantitative analyses of neural population dynamics between two neural 332 populations

To quantitatively examine these neural population structures, we compared the properties of the eigenvectors by estimating the vector size, angle, and deviance in each neural population (Figure 8). For this analysis, we used the rank-ordered HPC data shown in Figure 7, as well as the cOFC data shown in Figure 4. In the rankordered data, we evaluated the best and worst conditions as typically used in conventional representational analyses.

339 First, evaluation of vector size provided clear time-dependent structures in both 340 cOFC and HPC populations for probability and magnitude (Figure 8A) and for the 341 best and worst items (Figure 8B). Such time-dependent changes were not clearly 342 observed in the eigenvectors for the best and worst locations (Figure 8B, right and 343 second right columns), presumably because location information had already been 344 provided to the monkeys before the samples appeared. The vector sizes during 0.1 s 345 to 0.6 s after the onset of the lottery stimuli were not significantly different between 346 two continuous parameters, probability and magnitude of rewards (Figure 8C, 347 Wilcoxon rank sum test; PC1-2, n = 52, df = 51, W = 330, P = 0.892, PC2-3, n = 52, 348 df = 51, W = 341, P = 0.964), consistent with our previous findings (Yamada et al., 349 2021). In contrast, the vector sizes during 0.1 s to 0.6 s after the onset of the sample 350 stimuli significantly differed between the best and worst items (Figure 8D, Wilcoxon 351 singed rank test; PC1-2, item, n = 52, df = 51, W = 502, P = 0.002, PC2-3, item, n = 52, df = 51, W = 588, P < 0.001; PC1-2, location, n = 52, df = 51, W = 600, P < 0.001, PC2-3, item, n = 52, df = 51, W = 542, P < 0.001), possibly because the regression coefficients for the best conditions were considerably different from their means because the HPC responses were highly selective for one object (Figure 2D–E). Thus, the vector sizes captured the temporal changes in neural modulation at the population level.

358 The analyses of vector angles showed that all eigenvectors were very stable in 359 both populations in the top two dimensions (Figure 8E–F, top, Wilcoxon rank sum 360 test; cOFC, PC1-2, n = 52, df = 51, W = 62, P < 0.001; HPC, PC1-2, item, n = 52, df 361 = 51, W = 520, P < 0.001, location, n = 52, df = 51, W = 0, P < 0.001), as also shown 362 in Figures 4C top and 7B top. Their angles in the PC2-3 plane were not stable 363 (Figure 8E–F, bottom, Wilcoxon rank sum test; cOFC, PC2-3, n = 52, df = 51, W = 364 343, P = 0.935; HPC, PC2-3, item, n = 52, df = 51, W = 321, P = 0.765, PC2-3, 365 location, n = 52, df = 51, W = 312, P = 0.643, see also, Figure 4C, bottom and Figure 366 7B, bottom). Both neural populations showed considerable vector deviance smaller 367 than 0.1 with some statistical differences (Figure 8G-H, Wilcoxon rank sum test; 368 cOFC, PC1-2, n = 52, df = 51, W = 361, P = 0.683; PC2-3, n = 52, df = 51, W = 300, 369 *P* = 0.496; HPC, PC1-2, item, n = 52, df = 51, W = 459, *P* = 0.027; PC2-3, item, n = 370 52, df = 51, W = 581, P < 0.001, PC1-2, location, n = 52, df = 51, W = 352, P = 0.807; 371 PC2-3, location, n = 52, df = 51, W = 384, P = 0.408). Thus, our state-space analysis 372 in the regression subspace was capable of describing neural modulation dynamic in 373 the cOFC and HPC during two different cognitive tasks composed of continuous and 374 categorical parameters.

375

376 Matrix size control for PCA

Because the PCA performance was lower in the HPC than in the cOFC population,
we evaluated the effect of matrix size on the representational models. In our previous

379 study, the variance explained by the PCA decreased as the matrix size increased to 380 explain the same neural modulation (Figure 7A in Yamada et al., 2021). In the 381 present study, we reduced the matrix size of the HPC population by extracting the 382 best and worst conditions for item and location according to conventional 383 representational model analysis, although the regression matrix from the other conditions, 2nd preferred to 5th preferred, were removed. The regression subspace 384 385 was reduced from the large size, total X of size $N_{(590)} \times N_{(10\times30)}$, to $N_{(590)} \times N_{(4\times30)}$, similar 386 column size to the OFC population, $N_{(190)} \times N_{(2\times30)}$, in terms of the number of conditions. 387 In this smaller regression matrix, PCA performance improved (Figure 9A, 388 approximately 16% of the variance explained by PC1 and PC2), consistent with the 389 findings of our previous study where we used continuous parameters. The 390 eigenvector compositions developed in a clearly symmetric way, perhaps because 391 the variances from the other conditions were removed (Figure 9B). In this smaller 392 regression matrix, the principal components appeared to be rotated at an 393 approximately 135° angle from the original on the PC1-2 plane (Figures 9B and 7B). 394 The percent variance explained by the PCA clearly differed from that in the shuffled 395 conditions for the top three PCs, while the top six PCs significantly differed from 396 shuffled control in condition 2 (Figure 9C, see also Figure 6B, middle), indicating that 397 some neural population structures in higher dimensions were removed in this smaller 398 matrix.

In summary, our state-space analysis clearly described the neural modulation structures for both continuous and categorical task parameters. In both populations, using two standard task designs, we found stable evolutions of neural modulation structures in a relatively short period i.e., 0.6 s while the monkeys perceived visual items.

404

405 Discussion

406 In our previous study, we developed a variant of state-space analysis in the 407 regression subspace for continuous task parameters, which extracts neural 408 modulation dynamics at the population level. Here, we applied our state-space 409 analysis in the regression subspace to categorical task parameters and successfully 410 described the neural modulation dynamics for items and locations for the first time 411 (Figure 7). Comparisons of these results with those derived from continuous task 412 parameters (Figures 4 and 5) indicated that our analysis showed gradual 413 development (Figure 8A–B) and stable composition of the neural population 414 structures at different angles (Figure 8E-F, top). Moreover, the population analysis 415 using the best and worst conditions for items and locations showed that low-416 dimensional robust neural-modulation structures existed in this restricted neural 417 population, and some high-dimensional information seemed to disappear by 418 removing neural activity between the best and worst conditions (Figure 9A, and 419 Figures 7B vs 9B). Although both the cOFC and HPC neural populations were 420 pseudo-populations of neurons using repetitive single-neuron recordings for the 421 representational models, we successfully extracted both neural modulation dynamics 422 with the state-space analysis we developed. Our reliable extraction of neural 423 modulation dynamics indicated that any type of data can be re-analyzed and 424 evaluated to describe the temporal structure of neural modulations as dynamic 425 representational models.

426

427 Two different types of task parameters yield comparable regression subspaces

In our state-space analysis, neural population activity was projected to the regression subspace, reflecting the across-trial variance caused by the task-related parameters at the population level. In this step, both continuous and categorical task parameters are reliably used within a framework in the general linear model. However, it was reliably performed with one critical limitation; the conditions in any parameters should

be orthogonalized as the experimental design (Grafen & Hails, 2002). In the linear
system assumed here, the concept of orthogonality is critical in terms of statistics and
to avoid the skewed projection of neural activity into the regression subspace, which
is part of the whole neural activity reflecting activity modulation by the task
parameters of interest.

438 Analysis of the regression subspace has been performed in a limited number of 439 studies (Aoi et al., 2020; Mante et al., 2013). These studies aimed at detecting the 440 regression subspace within a whole neural structure at a constant time point (Mante 441 et al., 2013), and the detected modulation axis is assumed to be projected 442 orthogonally and sometimes being stable through a task trial (Aoi et al., 2020). Our 443 results support these assumptions, which were not examined in the previous study, 444 as the cOFC and HPC showed stable evolution of these neural-modulation structures, 445 at least during the two cognitive tasks with continuous and categorical task 446 parameters. Thus, our approach encourages research that combines the 447 conventional representational model and the dynamic model by re-analyzing the 448 pseudo-population of recorded single-neuron activity to remap the dynamic neural 449 modulation structures for all pre-existing data.

450

451 Stable and fluctuating signals in neural modulation dynamics

452 In this study, we observed stable neural modulation dynamics in both the cOFC and 453 HPC populations. Although these tasks were designed with different types of task 454 parameters, both brain regions showed stable modulation structures during the visual 455 perception (Figures 4, 7, and 8). Why do these two distinct brain regions show stable 456 modulation dynamics? One possibility is that both the cOFC and HPC play a role in 457 accessing the memory for the expected values as a combination of probability and 458 magnitude in Exp. 1 and the association between stimulus and position for future 459 decisions in Exp. 2. These types of stable structures were observed in the

dorsolateral prefrontal cortex during a typical working memory task (Murray et al.,
2017). Thus, a key aspect of stable neural dynamics may be continuous access to
memory and its maintenance.

463 In our previous study, fluctuating neural population signals were observed in the 464 dorsal part of the striatum (DS) and medial part of the orbitofrontal cortex (mOFC) 465 because of signal instability or weakness (Figure 5A and B in Yamada et al., 2021). 466 Because the signal carried by the mOFC population was weak (Figure 8 bottom row 467 in Yamada et al., 2021), the eigenvector fluctuation in the mOFC population reflected 468 weak signal modulations by the probability and magnitude of rewards. In this case, 469 moment-by-moment vector fluctuation was observed, as there was no clear neural 470 modulation structure in the mOFC populations. In contrast, the fluctuating DS signal 471 seemed to reflect the functional role employed by the DS neural population in 472 detecting and integrating the probability and magnitude of rewards, related to the 473 control of some actions (Balleine et al., 2007). In the DS population, structural changes in eigenvectors occurred over time (Figure 8 in Yamada et al., 2021). We 474 475 need to elaborate on the stability of modulation dynamic functions in neural 476 processing in future studies to elucidate how neural circuitry actually operates and 477 computes (Ebitz & Hayden, 2021; Humphries, 2021).

478

479 Conclusions

Representational models have provided mounting evidence that neural modulation is associated with mathematical functions in every area of the brain. A dynamic-model approach that has been recently developed appears promising to account for different aspects of neural computation, but the relationship with the representational models remains unclear. Although a few studies have sought a connection between these two advances (X. Chen & Stuphorn, 2015; Churchland et al., 2012; Murray et al., 2017), more direct comparisons are necessary to understand the functional 487 significance of the neural population dynamics. Our results indicated that the neural 488 modulation dynamics observed in population ensemble activities are compatible with 489 representational models and encourage research aimed at incorporating traditional 490 representational models into the dynamic system.

491

492 Materials and Methods

493 Subjects and experimental procedures

494 Four macaque monkeys were employed for this study in two experiments 495 (Experiment 1: Macaca mulatta, SUN, 7.1 kg, male; Macaca fuscata, FU, 6.7 kg, 496 female; Experiment 2: Macaca mulatta, A, 9.3 kg, male; Macaca mulatta, D, 9.5 kg, 497 male). All experimental procedures were approved by the Animal Care and Use 498 Committee of the University of Tsukuba (Exp. 1, protocol no H30.336), and the 499 Institutional Animal Care and Use of Laboratory Animals approved by Peking 500 University (Exp. 2, project number Psych-YujiNaya-1) and performed in compliance 501 with the US Public Health Service's Guide for the Care and Use of Laboratory 502 Animals.

503

504 Behavioral task and Monkey electrophysiology

505 *Experiment* 1

506 *Cued lottery tasks.* Animals performed one of two visually cued lottery tasks: *a* 507 *single-cue task* or *a choice task.* Neuronal activity was recorded only during the 508 single-cue task.

At the beginning of trials during the single-cue task, the monkeys had 2 s to align their gaze to within 3° of a 1°-diameter gray central fixation target. After fixation for 1 s, a pie chart was presented for 2.5 s to provide information regarding the probability and magnitude of rewards at the same location as the central fixation target. The probability and magnitude of rewards were associated with the number of blue and

green 8° segments, ranging from 0.1 to 1.0 mL in 0.1-mL increments for magnitude and 0.1 to 1.0 in 0.1 increments for probability. With an interval of 0.2 s after the removal of the pie chart, either a 1 kHz or 0.1 kHz tone of 0.15-s duration was provided to indicate reward or no-reward outcomes, respectively. With an interval of 0.2 s after the high tone, a fluid reward was delivered. After a low tone, no reward was delivered. An inter-trial interval of 4–6 s followed each trial.

In the trials during choice task, the animals were instructed to choose between two peripheral pie charts providing information regarding the probability and magnitude of rewards for each of the two target options were presented for 2.5 s, at 8° to the left and right of the central fixation location. The animals received a fluid reward, indicated by the green pie chart of the chosen target, with the probability indicated by the blue pie chart; otherwise, no reward was delivered.

526 One hundred pie charts were used in the experiments. In the single-cue task, 527 each pie chart was presented once in a random order. In the choice task, two pie 528 charts from the 100 pie charts were randomly allocated to the two options. During 529 one session of electrophysiological recording, approximately 30 to 60 trial blocks of 530 the choice task were interleaved with 100 to 120 trial blocks of the single-cue task.

531 We used conventional techniques for recording single-neuron activity from the 532 central part of the orbitofrontal cortex (cOFC, area 13M). A tungsten microelectrode 533 $(1-3 M\Omega, FHC)$ was used to record single-neuron activity. Electrophysiological 534 signals were amplified, band-pass filtered (at 50-3000 Hz), and monitored. Single-535 neuron activity was isolated based on the spike waveforms. We recorded from the 536 cOFC of a single hemisphere in each of the two monkeys: 190 cOFC neurons (98, 537 SUN and 92, FU). The activity of all single neurons was sampled when the activity of 538 an isolated neuron demonstrated a good signal-to-noise ratio (>2.5). Blinding was not 539 performed. The sample sizes required to detect effect sizes (number of recorded 540 neurons, number of recorded trials in a single neuron, and number of monkeys) were

estimated based on previous studies (X. Chen & Stuphorn, 2015; Yamada et al.,
2013; Yamada et al., 2018). Neural activity was recorded during 100–120 trials of the
single-cue task. Neural activity was not recorded during the choice trials. In this study,
we analyzed the cOFC activity data during 600 ms after cue onset from Yamada et al.
(2021) for comparison with the activity data in Exp. 2.

546

547 Experiment 2

548 Item location-retention (ILR) task. The animals performed the task under dim light in 549 an electromagnetically shielded room. The task started with an encoding phase, 550 which was initiated by the animal pulling a lever and fixating on a white square (0.6°) 551 presented within one of the four quadrants at 12.5° (monkey A) or 10° (monkey D) from the center of the touch screen (3M[™] MicroTouch[™] Display M1700SS, 17 inch), 552 553 situated approximately 28 cm from the subjects. Eye position was monitored using an 554 infrared digital camera with a sampling frequency of 120 Hz (ETL-200, ISCAN). After 555 fixation for 0.6 s, one of the six items (3.0° for monkey A and 2.5° for monkey D, 556 radius) was presented in the same quadrant as a sample stimulus for 0.3 s, followed 557 by another 0.7-s fixation on the white square. If the fixation was successfully 558 maintained (typically, $< 2.5^{\circ}$), the encoding phase ended with the presentation of a 559 single drop of water.

560 The encoding phase was followed by a blank interphase delay interval of 0.7-1.4 561 s during which no fixation was required. The response phase was initiated with a 562 fixation dot presented at the center of the screen. One of six items was then 563 presented at the center for 0.3 s as a cue stimulus. After another 0.5-s delay period, 564 five disks were presented as choices, including a blue disk in each quadrant and a 565 green disk at the center. When the cue stimulus was the same as the sample 566 stimulus, the animal was required to choose by touching the blue disk in the same 567 quadrant as the sample (i.e., match condition). Otherwise, the subject was required

568 to choose the green disk (i.e., non-match condition). If the animal made a correct 569 choice, four to eight drops of water were provided as a reward; otherwise, an 570 additional 4 s was added to the standard intertrial interval (1.5-3 s). During the trial, a 571 large gray square (48° on each side, Red, Green, Blue value: 50, 50, 50, luminance: 572 3.36 cd/m^2) was presented at the center of the display (backlight luminance: 0.22) 573 cd/m²) as a background. After the end of the trial, all stimuli disappeared, and the 574 entire screen displayed a light red color during the intertrial interval. The start of a 575 new trial was indicated by the reappearance of the large gray square on the display, 576 upon which the monkey could start pulling the lever, triggering the appearance of a 577 white fixation dot. In the match condition, sample stimuli were pseudo-randomly 578 chosen from six well-learned visual items, and each item was presented pseudo-579 randomly within the four quadrants, resulting in 24 (6×4) configuration patterns. In 580 the nonmatch condition, the location of the sample stimulus was randomly chosen 581 from the four quadrants, and the cue stimulus was randomly chosen from the five 582 items that differed from the sample stimulus. The match and non-match conditions 583 were randomly presented at a ratio of 4:1, resulting in 30 (24 + 6) configuration 584 patterns. The same six stimuli were used during all recording sessions.

To record single-unit activity, we used a 16-channel vector array microprobe (V1 X 16-Edge, NeuroNexus), a 16-channel U-Probe (Plexon), a tungsten tetrode probe (Thomas RECORDING), or a single-wire tungsten microelectrode (Alpha Omega). We recorded 590 hippocampal (HPC) neurons, of which the recording sites appeared to cover all its subdivisions (i.e., dentate gyrus, CA3, CA1, and subicular complex). We applied state-space analysis to the HPC population and compared to the results from the cOFC population.

592

593 Statistical analysis

594 For statistical analysis, we used the statistical software package R (Exp. 1) and

595 MATLAB (MathWorks) (Exp. 2). All statistical tests for the neural analyses were two

- 596 tailed.
- 597

598 Behavioral analysis

- 599 Exp. 1. We previously reported that monkey behavior depends on the expected
- values defined as probability time magnitude (Yamada et al 2021).
- 601 Exp. 2. We previously reported that two monkeys learned to retain the item and
- location information of the sample stimulus (H. Chen & Naya, 2020).
- 603 No new behavioral results were included in this study.
- 604

605 Neural analysis

606 Peristimulus time histograms were drawn for each single-neuron activity aligned at 607 the visual stimulus onset. The average activity curves were smoothed for visual

608 inspection using a Gaussian kernel.

609

610 **Conventional analyses to detect neural modulations in each neuron**

We analyzed neural activity during the 1-s time window (0-1 s after cue onset, Exp. 1) and during the 0.92 s time window (0.08-1 s after sample onset, Exp. 2), respectively, respectively. These activities were used for the conventional analyses below. No Gaussian kernel was used.

615 *Exp. 1.* Neural discharge rates (*F*) were fitted using a linear combination of the 616 following parameters:

617 $F = b_0 + b_p$ Probability + b_m Magnitude (1)

where Probability and Magnitude are the probability and magnitude of the rewards indicated by the pie chart, respectively. b_0 is the intercept. If b_p and b_m were not 0 at *P*

< 0.05, the discharge rates were regarded as being significantly modulated by that
variable. These results have been previously reported (Yamada et al., 2021).

Based on the linear regression, activity modulation patterns were categorized into several types: "Probability" type with a significant b_p and without a significant b_m ; "Magnitude" type without a significant b_p and with a significant b_m ; "Both" type with significant b_p and b_m .

Exp. 2. For neural responses during the encoding phase after the sample presentation, we evaluated the effects of "item" and "location" for each neuron using two-way analysis of variance (ANOVA) (P < 0.01 for each). We analyzed neurons that we tested in at least 60 trials (10 trials for each stimulus, 15 trials for each location). On average, we tested 100 trials for each neuron (n = 590). The results have been previously reported (H. Chen & Naya, 2020).

Based on the ANOVA, activity modulation patterns were categorized into several types: "Item" type only with a significant main effect of Item; "Location" type only with a significant effect of Location; "Both" type with a significant effect of Item and Location or with a significant effect of interaction.

636

637 **Population dynamics using principal component analysis**

We analyzed neural activity during a 0.6 s time period from cue onset (Exp. 1) and sample onset (Exp. 2). To obtain a time series of neural firing rates within this period, we estimated the firing rates of each neuron for every 0.02-s time bin (without overlap) during the 0.6-s period. No Gaussian kernel was used.

642

Regression subspace. We used a general linear model to determine the probability and magnitude of rewards (Exp. 1) and item and location (Exp. 2) affecting the activity of each neuron in the neural populations. Each neural population was composed of all recorded neurons in each brain region.

647 Exp. 1. We first set the probability and magnitude at 0.1 and 1.0 and 0.1 to 1.0 mL,

respectively. We then described the average firing rates of neuron i at time t as a

649 linear combination of the probability and magnitude in each neural population:

650
$$F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)} \text{Probability}_{(k)} + b_{2(i,t)} \text{Magnitude}_{(k)}$$
 (2)

where $F_{(i,t,k)}$ is the average firing rate of neuron *i* at time t on trial *k*, Probability_(k) is the probability of reward cued to the monkey in trial *k*, and Magnitude_(k) *is* the magnitude of reward cued to the monkey in trial *k*. The regression coefficients $b_{O(i,t)}$ to $b_{2(i,t)}$ describe the degree to which the firing rates of neuron *i* depend on the mean firing rates (hence, firing rates independent of task parameters), probability of rewards, and magnitude of rewards, respectively, at a given time *t* during the trials.

Exp. 2. We first set six items and four locations as categorical parameters. We then described the average firing rates of neuron *i* at time *t* as a linear combination of item and location in each neural population:

 $F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)} |\text{tem}_{(k)} + b_{2(i,t)} |\text{Location}_{(k)}, \quad (3)$

661 where $F_{(i,t,k)}$ is the average firing rate of neuron i at time t on trial k, Item_(k) is the type 662 of item cued to the monkey on trial k, and Location(k) is the type of location cued to 663 the monkey on trial k. Each of the regression coefficients $b_{0(i,t)}$, $b_{1(i,t)}$, and $b_{2(i,t)}$ 664 describe the degree to which the firing rates of neuron *i* depend on the mean firing 665 rates (hence, firing rates independent of task parameters, probability, and magnitude 666 of rewards), the degree of the firing rate in each item relative to the mean firing rates, 667 and the degree of firing in each location relative to the mean firing rates, respectively, 668 at a given time t during the trials. Note that the interaction term was not included in 669 the model.

We used the regression coefficients (i.e., the regression table in the ANOVA) described in Eqs. 2 and 3 to identify how the dimensions of neural-population signals were composed of information related to probability and magnitude (Exp. 1) and were composed of information related to item and location (Exp. 2) as aggregated

674 properties of individual neural activity. This step constructs an encoding model where 675 the regression coefficients could be explained by a temporal structure in the neural 676 modulation of two continuous parameters (Exp. 1) or two categorical parameters 677 (Exp. 2) at the population level. Our procedures are analogous to the state-space 678 analysis performed by Mante et al. (Mante et al., 2013), in which the regression 679 coefficients were used to provide an axis (or dimension) of the parameters of interest 680 in multi-dimensional state space obtained through principal component analysis 681 (PCA). In this study, our orthogonalized task design allowed us to reliably project the 682 neural firing rates into the regression subspace. Note that our analyses were not 683 aimed at describing the population dynamics of neural signals as a trajectory in multi-684 dimensional task space but were aimed at describing the neural-modulation 685 dynamics as in a representational model.

686

687 Preference ordering. In Exp. 2, each neuron had a preferred item and location. As in 688 the conventional representational-model analysis, we defined the preferred item and 689 location in each neuron to construct matrix X. We constructed X with and without 690 rank order. Items 1 to 6 were rank-ordered from the most preferred to least preferred, 691 defined as the mean firing rates during a whole analysis time window from 0.08 to 0.6 692 s. Thus, Item_(k) was the rank-ordered item cued to the monkey on trial k. In the same 693 way as the definition of Item, Location_(k) was the rank-ordered location cued to the 694 monkey on trial k. Note that this preference ordering was never changed through 695 time t in each neuron n.

696

Principal Component Analysis We used PCA to identify the dimensions of the neuralpopulation signal in the orthogonal spaces composed of the probability and magnitude of rewards in Exp. 1 and of the item and location in Exp. 2, respectively, in each of the four neural populations. In each neural population, we first prepared a

701 two-dimensional data matrix X of size $N_{(0)} \times M_{(CxT)}$; the regression coefficient vectors, $b_{1(i,t)}$ and $b_{2(i,t)}$, in Eqs. 2 and 3, whose rows correspond to the total number of 702 703 neurons (n) in each neural population and columns correspond to C, the total number 704 of conditions (i.e., two: probability and magnitude in Exp. 1; 10: six items and four 705 locations in Exp. 2), and T as the total number of the analysis windows (i.e., 30 bins: 706 0.6 s divided by the window size bin, 0.02 s). A series of eigenvectors was obtained 707 by applying PCA once to data matrix X in each of the neural populations. The 708 principal components (PCs of this data matrix are vectors $v_{(a)}$ of length $N_{(n)}$, and the 709 total number of recorded neurons if $M_{(C \times T)}$ is > $N_{(n)}$; otherwise, the length is $M_{(C \times T)}$. 710 The PCs were indexed from the principal components, explaining most of the 711 variance to the least variance. The eigenvectors were obtained using the prcomp () 712 function in R software. Note that we did not include the intercept term $b_{O(i,t)}$ to focus on 713 the neural modulation by the interested parameters.

714

715 *Eigenvectors.* When we applied PCA to data matrix X, we decomposed the matrix 716 into eigenvectors and eigenvalues. Each eigenvector has a corresponding 717 eigenvalue. In our analysis, the eigenvectors at time t represent a vector in the space 718 of probability and magnitude in Exp. 1 and of item and location in Exp. 2, respectively. 719 The eigenvalues at time t for the probability and magnitude in Exp. 1 and of item and 720 location in Exp. 2, respectively, were scalars, indicating the extent of variance in the 721 data in that vector. Thus, the first PC is the eigenvector with the highest eigenvalue. 722 We mainly analyzed eigenvectors for the first three PCs (PC1 to PC3) in the following 723 analyses, as the top three PCs had been analyzed previously (Okazawa et al., 2021). 724 Note that we applied PCA once to each neural population, and thus, the total 725 variances contained in the data differed among the neural populations.

726

727 Analysis of eigenvectors. We evaluated the characteristics of eigenvectors for PC1 to 728 PC3 in each neural population in terms of the vector angle, size, and deviance in the 729 space of probability and magnitude in Exp. 1 and of the item and location in Exp. 2, 730 respectively. The angle is the vector angle from the horizontal axis from 0° to 360° 731 against the main PCs. Size is the length of the eigenvector. The deviance is the 732 difference between vectors. We estimated the deviance from the mean vector for 733 each neural population. These three characteristics of the eigenvectors were 734 compared in each population at P < 0.05 using the Kruskal–Wallis and Wilcoxon 735 rank-sum tests. The vector during the first 0.1 s was extracted from these analyses.

736

737 Shuffle control for PCA. We performed three shuffle controls to examine the 738 significance of population structures described with PCA. A two-dimensional data 739 matrix X was randomized by shuffling in three ways. In shuffled control 1, matrix X 740 was shuffled by permutating the allocation of neuron n at each time i. This shuffle 741 provided a data matrix X of size $N_{(0)} \times M_{(C \times T)}$, eliminating the temporal structure of 742 neural modulation by condition C in each neuron but retaining the neural modulations 743 at time t at the population level. In shuffled control 2, matrix X was shuffled by 744 permutating the allocation of time *i* in each neuron *n*. This shuffle provided a data 745 matrix X of size $N_{(neuron)} \times M_{(C\times T)}$, eliminating the neural modulation structure under 746 condition C maintained in each neuron but retaining the neural modulation in each 747 neuron at the population level. In shuffled control 3, matrix X was shuffled by 748 permutating the allocation of both time *i* and neuron *n*. In these three shuffle controls, 749 matrix X was estimated 1,000 times. PCA performance was evaluated by 750 constructing the distributions of explained variances for PC1 to PC12. The statistical 751 significance of the variances explained by PC1 and PC3 was estimated based on the 752 95th percentile of the reconstructed distributions of explained variance or bootstrap 753 standard errors (i.e., standard deviation of the reconstructed distribution).

754

755 Matrix Size Control for PCA Because the original matrix sizes of X, $N_{(n)} \times M_{(C\times T)}$, differed 756 between the cOFC (X of size $N_{(190)} \times M_{(2\times 30)}$) and HPC (X of size $N_{(590)} \times M_{(10\times 30)}$) populations, 757 we controlled for matrix size. In this control, we used only two columns in each bin, the most 758 preferred and least preferred, for each condition C, item, and location; thus, matrix X was (X 759 of size $N_{(590)} \times M_{(4\times30)}$). This corresponds to the conventional analysis usually used in the 760 representational model, which compares the neural responses between the most preferred 761 and least preferred conditions. We evaluated the percentage explained by the model between 762 the original matrix and size-controlled matrix in the HPC.

763

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Author Contributions: H.Y. conceptualized the study. H.Y. and Y.N. designed the experiments. H.Y., H.C., Y.I., Y.H., and T.M. conducted the experiments. M.M. conducted a part of experiments. H.Y. developed the analytic tools. H.Y. and H.C. analyzed the data. H.Y., H.C., J.K., T.O., T.M., and Y.N. evaluated the results. H.Y., H.C., J.K., T.O., and T.M. wrote the manuscript. All authors edited and approved the final manuscript.

781 Data availability: All data and analysis codes in this study are available from the

782 corresponding authors.

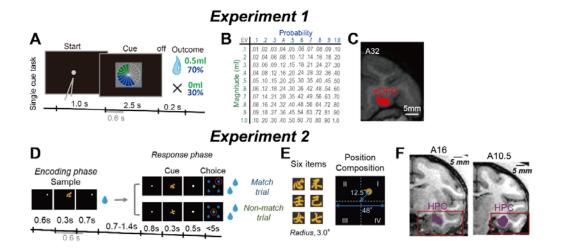
784 **References**

785	Aoi, M. C., Mante, V., & Pillow, J. W. (2020). Prefrontal cortex exhibits
786	multidimensional dynamic encoding during decision-making. Nat Neurosci,
787	23(11), 1410-1420. doi:10.1038/s41593-020-0696-5
788	Aoi, M. C., & Pillow, J. W. (2018). Model-based targeted dimensionality reduction
789	for neuronal population data. Adv Neural Inf Process Syst, 31, 6690-6699.
790	Balleine, B. W., Delgado, M. R., & Hikosaka, O. (2007). The role of the dorsal
791	striatum in reward and decision-making. J Neurosci, 27(31), 8161-8165.
792	Brendel, W., Romo, R., & Machens, C. K. (2011). Demixed Principal Component
793	Analysis. Advances in Neural Information Processing Systems, 24, 2654-2622.
794	Buzsaki, G., Stark, E., Berenyi, A., Khodagholy, D., Kipke, D. R., Yoon, E., & Wise,
795	K. D. (2015). Tools for probing local circuits: high-density silicon probes
796	combined with optogenetics. Neuron, 86(1), 92-105.
797	doi:10.1016/j.neuron.2015.01.028
798	Chen, H., & Naya, Y. (2020). Forward Processing of Object-Location Association
799	from the Ventral Stream to Medial Temporal Lobe in Nonhuman Primates.
800	Cereb Cortex, 30(3), 1260-1271. doi:10.1093/cercor/bhz164
801	Chen, X., & Stuphorn, V. (2015). Sequential selection of economic good and action in
802	medial frontal cortex of macaques during value-based decisions. Elife, 4.
803	doi:10.7554/eLife.09418
804	Churchland, M. M., Cunningham, J. P., Kaufman, M. T., Foster, J. D., Nuyujukian,
805	P., Ryu, S. I., & Shenoy, K. V. (2012). Neural population dynamics during
806	reaching. Nature, 487(7405), 51-56. doi:10.1038/nature11129
807	Dayan, P., & Abbott, L. (2001). Theoretical neuroscience: computational and
808	mathematical modeling of neural systems.
809	Ebitz, R. B., & Hayden, B. Y. (2021). The population doctrine in cognitive
810	neuroscience. Neuron, 109(19), 3055-3068. doi:10.1016/j.neuron.2021.07.011
811	Elsayed, G. F., & Cunningham, J. P. (2017). Structure in neural population
812	recordings: an expected byproduct of simpler phenomena? Nat Neurosci,
813	20(9), 1310-1318. doi:10.1038/nn.4617
814	Evarts, E. V. (1968). A technique for recording activity of subcortical neurons in
815	moving animals. <i>Electroencephalogr Clin Neurophysiol</i> , 24(1), 83-86.

816	Fetz, E. E., & Cheney, P. D. (1980). Postspike facilitation of forelimb muscle activity
817	by primate corticomotoneuronal cells. J Neurophysiol, 44(4), 751-772.
818	doi:10.1152/jn.1980.44.4.751
819	Georgopoulos, A. P., Kalaska, J. F., Caminiti, R., & Massey, J. T. (1982). On the
820	relations between the direction of two-dimensional arm movements and cell
821	discharge in primate motor cortex. J Neurosci, 2(11), 1527-1537.
822	Grafen, A., & Hails, R. (2002). Modern Statistics for the Life Sciences. New York:
823	Oxford university press.
824	Hubel, D. H., & Wiesel, T. N. (1959). Receptive fields of single neurones in the cat's
825	striate cortex. J Physiol, 148, 574-591. doi:10.1113/jphysiol.1959.sp006308
826	Humphries, M. D. (2021). Strong and weak principles of neural dimension reduction.
827	Neurons, Behavior, Data analysis, and Theory, 5(2).
828	Jones, J. P., & Palmer, L. A. (1987). An evaluation of the two-dimensional Gabor
829	filter model of simple receptive fields in cat striate cortex. J Neurophysiol,
830	58(6), 1233-1258. doi:10.1152/jn.1987.58.6.1233
831	Jun, J. J., Steinmetz, N. A., Siegle, J. H., Denman, D. J., Bauza, M., Barbarits, B.,
832	Harris, T. D. (2017). Fully integrated silicon probes for high-density recording
833	of neural activity. Nature, 551(7679), 232-236. doi:10.1038/nature24636
834	Keemink, S. W., & Machens, C. K. (2019). Decoding and encoding (de)mixed
835	population responses. Curr Opin Neurobiol, 58, 112-121.
836	doi:10.1016/j.conb.2019.09.004
837	Mante, V., Sussillo, D., Shenoy, K. V., & Newsome, W. T. (2013). Context-
838	dependent computation by recurrent dynamics in prefrontal cortex. Nature,
839	503(7474), 78-84. doi:10.1038/nature12742
840	Mountcastle, V., & Henneman, E. (1949). Pattern of tactile representation in thalamus
841	of cat. J Neurophysiol, 12(2), 85-100. doi:10.1152/jn.1949.12.2.85
842	Murray, J. D., Bernacchia, A., Roy, N. A., Constantinidis, C., Romo, R., & Wang, X.
843	J. (2017). Stable population coding for working memory coexists with
844	heterogeneous neural dynamics in prefrontal cortex. Proc Natl Acad Sci USA,
845	114(2), 394-399. doi:10.1073/pnas.1619449114
846	O'Keefe, J., & Dostrovsky, J. (1971). The hippocampus as a spatial map. Preliminary
847	evidence from unit activity in the freely-moving rat. Brain Res, 34(1), 171-
848	175. doi:10.1016/0006-8993(71)90358-1

849	Okazawa, G., Hatch, C. E., Mancoo, A., Machens, C. K., & Kiani, R. (2021).
850	Representational geometry of perceptual decisions in the monkey parietal
851	cortex. <i>Cell</i> , 184(14), 3748-3761 e3718. doi:10.1016/j.cell.2021.05.022
852	Osako, Y., Ohnuki, T., Tanisumi, Y., Shiotani, K., Manabe, H., Sakurai, Y., &
853	Hirokawa, J. (2021). Contribution of non-sensory neurons in visual cortical
854	areas to visually guided decisions in the rat. Curr Biol, 31(13), 2757-2769
855	e2756. doi:10.1016/j.cub.2021.03.099
856	Platt, M. L., & Glimcher, P. W. (1999). Neural correlates of decision variables in
857	parietal cortex. Nature, 400(6741), 233-238.
858	Raposo, D., Kaufman, M. T., & Churchland, A. K. (2014). A category-free neural
859	population supports evolving demands during decision-making. <i>Nat Neurosci</i> ,
860	17(12), 1784-1792. doi:10.1038/nn.3865
861	Rossi-Pool, R., Zainos, A., Alvarez, M., Diaz-deLeon, G., & Romo, R. (2021). A
862	continuum of invariant sensory and behavioral-context perceptual coding in
863	secondary somatosensory cortex. Nat Commun, 12(1), 2000.
864	doi:10.1038/s41467-021-22321-x
865	Saxena, S., & Cunningham, J. P. (2019). Towards the neural population doctrine.
866	Curr Opin Neurobiol, 55, 103-111. doi:10.1016/j.conb.2019.02.002
867	Tolhurst, D. J., & Movshon, J. A. (1975). Spatial and temporal contrast sensitivity of
868	striate cortical neurones. Nature, 257(5528), 674-675. doi:10.1038/257674a0
869	Vyas, S., Golub, M. D., Sussillo, D., & Shenoy, K. V. (2020). Computation Through
870	Neural Population Dynamics. Annu Rev Neurosci, 43, 249-275.
871	doi:10.1146/annurev-neuro-092619-094115
872	Wurtz, R. H. (1968). Visual cortex neurons: response to stimuli during rapid eye
873	movements. Science, 162(3858), 1148-1150.
874	doi:10.1126/science.162.3858.1148
875	Yamada, H., Imaizumi, Y., & Matsumoto, M. (2021). Neural Population Dynamics
876	Underlying Expected Value Computation. J Neurosci, 41(8), 1684-1698.
877	doi:10.1523/JNEUROSCI.1987-20.2020
878	Yamada, H., Inokawa, H., Matsumoto, N., Ueda, Y., Enomoto, K., & Kimura, M.
879	(2013). Coding of the long-term value of multiple future rewards in the
880	primate striatum. J Neurophysiol, 109(4), 1140-1151.
881	doi:10.1152/jn.00289.2012

- 882 Yamada, H., Louie, K., Tymula, A., & Glimcher, P. W. (2018). Free choice shapes
- 883 normalized value signals in medial orbitofrontal cortex. *Nat Commun, 9*(1),
- 884 162. doi:10.1038/s41467-017-02614-w
- 885 Yuste, R. (2015). From the neuron doctrine to neural networks. Nat Rev Neurosci,
- 886 *16*(8), 487-497. doi:10.1038/nrn3962
- 887

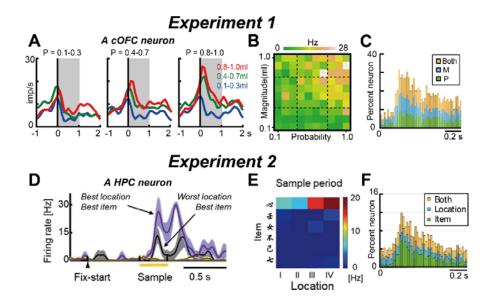


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Figure 1. Behavioral task and recording location of neurons.

890 (A) Sequence of events during the single-cue task in Exp. 1. A single visual pie chart 891 having green and blue pie segments was presented to the monkeys. Neural activity 892 was analyzed during 0.6 s after cue onset, i.e., for the same duration as in Exp. 2. 893 (B) Payoff matrix – each of the magnitudes was fully crossed with each of the 894 probabilities resulting in a pool of 100 lotteries. (C) Illustration of neural recording 895 areas based on coronal magnetic resonance (MR) images for the cOFC (13M, 896 medial part of area 13) at the A31–A34 anterior–posterior (A–P) level. (D) Sequence 897 of events during the ILR task in Exp. 2. The cue stimulus during the response phase 898 was the same as the sample stimulus during the encoding phase in the match trial, 899 while the two stimuli differed in the nonmatch trial. Neural activity was analyzed 900 during 0.6 s after sample onset, i.e., for the same duration as in Exp. 1. (E) Six visual 901 item stimuli and spatial composition during the sample period. (F) Coronal MR 902 images from monkey A for the HPC population showing the recording area at A16-903 A10.5 depicted by purple color in the red boxes. Figure 1A was published in Yamada 904 et al., 2021. Figure 1D-F was published in Chen et al., 2020.

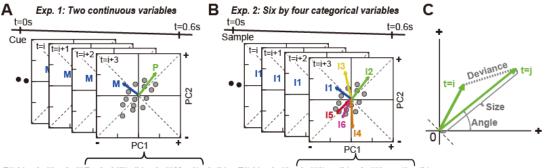
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907 Figure 2. Example activity of neurons during the single-cue and ILR tasks.

908 (A) Example activity histogram of a cOFC neuron modulated by the probability and 909 magnitude of rewards during the single-cue task. The activity aligned to the cue 910 onset is represented for three different levels of probability (0.1-0.3, 0.4-0.7, 0.8-911 1.0) and magnitude (0.1–0.3 mL, 0.4–0.7 mL, 0.8–1.0 mL) of rewards. Gray hatched 912 time windows indicate the 1-s time window used to estimate the neural firing rates 913 shown in **B**. Histograms are smoothed using a Gaussian kernel ($\sigma = 50$ ms) (**B**) 914 Activity plot of the cOFC neuron during the 1-s time window shown in **A** against the 915 probability and magnitude of rewards. (C) Percentages of neural modulation type: the 916 probability (P), magnitude (M), and both (Both) in the 0.02-s time bin during 1.0 s 917 after cue onset. The scale bar indicates the 0.2 s. (D) Example of an HPC neuron 918 showing sample-triggered sample-location signals and item signals. A 0.08-0.38 s 919 time window was used to estimate the neural firing rates shown in E. Histograms are 920 smoothed using a Gaussian kernel ($\sigma = 20$ ms). (E) Activity plot of the HPC neuron 921 during the 0.3-s time window shown in A against items and locations. (F) 922 Percentages of neural modulation types: item, location, and both (Both) in the 0.02-s 923 time bin during 1.0 s after sample onset. Figure 2A-C was published in Yamada et 924 al., 2021. Figure 2D-E was published in Chen et al., 2020.

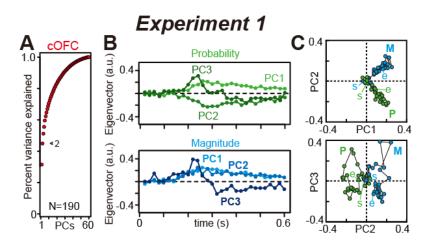


 $F(t,k) = b_0(t) + b_1(t)Probability(k) + b_2(t)Manitude(k) \qquad F(t,k) = b_0(t) + b_1(t)Item(k) + b_2(t)Location(k)$

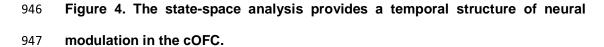
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Figure 3. Schematic depictions for the analysis of neural-population dynamics using PCA.

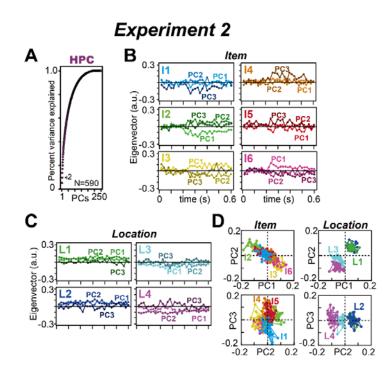
928 (A) Time series of neural population activity projected to a regression subspace 929 composed of probability and magnitude. The eigenvectors for probability and 930 magnitude were plotted after coordinate transformation against PC1 and PC2. A 931 series of eigenvectors was obtained by applying PCA once to the cOFC population. 932 The number of eigenvectors obtained by PCA was 0.6 s divided by the analysis 933 window size, 0.02 s, for probability (P) and magnitude (M), hence 30 eigenvectors for each. The regression equation is shown at the bottom (see Methods for details). (B) 934 935 Time series of neural population activity projected to a regression subspace 936 composed of items and locations. The eigenvectors for six items (I1 to I6) were 937 plotted after coordinate transformation against PC1 and PC2 (the eigenvector for 938 locations are not shown). A series of eigenvectors was obtained by applying PCA once to the HPC population. The number of eigenvectors obtained by PCA was 0.6 s 939 940 divided by the analysis window size, 0.02 s, for the six items and four locations, 941 hence 30 eigenvectors for each. The regression equation is shown at the bottom 942 (see Methods for details). (C) Characteristics of the eigenvectors evaluated 943 quantitatively. Angle: vector angle from the horizontal axis obtained from -180° to 180°. 944 Size: eigenvector length. Deviance: difference between vectors.



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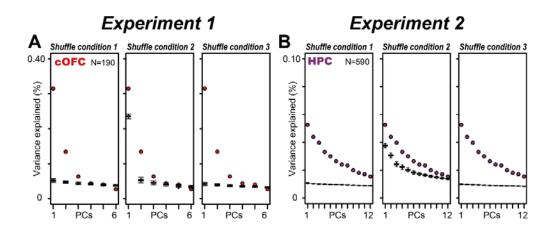
(A) Cumulative variance explained by PCA in the cOFC population. The arrowhead
indicates the percentages of variances explained by PC1 and PC2. (B) Time series
of eigenvectors for PC1 to PC3 in the cOFC population. (C) Series of eigenvectors
for PC1 to PC3 are plotted against the PC1 and PC2 and PC2 and PC3 dimensions
in the cOFC population. Plots at the beginning and end of the series of vectors are
labeled as start (s) and end (e), respectively. In A–B, a.u. indicates arbitrary unit.



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955 Figure 5. Temporal structure of neural modulation in the HPC population.

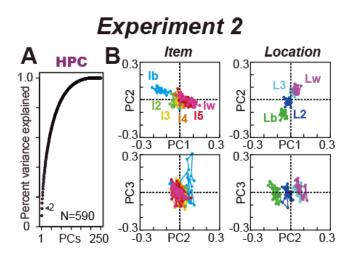
(A) Cumulative variance explained by PCA in the HPC population. The arrowhead
indicates the percentages of variances explained by PC1 and PC2. (B) Time series
of eigenvectors for six items in the HPC population. The top three PCs are shown.
(C) Same as B but showing the eigenvectors for the four locations. (D) Series of
eigenvectors for PC1 to PC3 are plotted against the PC1 and PC2 and PC2 and PC3
dimensions in the HPC population. In B–C, a.u. indicates arbitrary unit.



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964 Figure 6. Explained variances by PCA in shuffled controls.

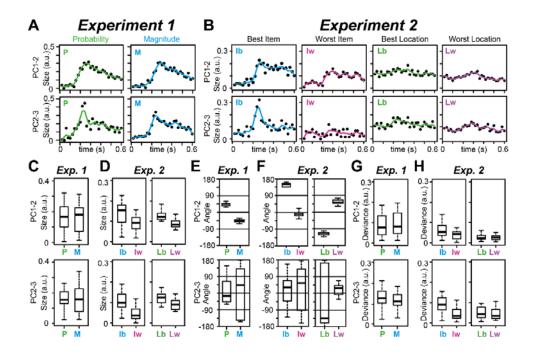
965 (A) Boxplot of explained variances by PCA for PC1 to PC6 for the cOFC population
966 under the three shuffled conditions (see Methods for details). The plot is not
967 cumulative. The boxplot was made with 1,000 repeats of the shuffle in each condition.
968 (B) Same as A, but for the HPC population. In A and B, the colored circles indicate
969 the variances explained by PCA in each neural population without the shuffles.



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971 Figure 7. Effects of preference ordering on the HPC categorical data.

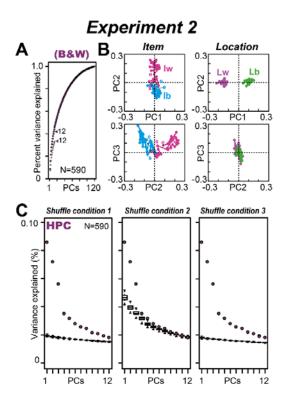
972 (A) Cumulative variance explained by PCA in the HPC population when item and 973 location are ordered according to their activity preferences (see Methods). The 974 arrowhead indicates the percentages of variances explained by PC1 and PC2. (B) 975 Series of eigenvectors for PC1 to PC3 when item and location are ordered according 976 to their preferences plotted against the PC1 and PC2 and PC2 and PC3 dimensions 977 in the HPC population. Ib and Iw indicate the best and worst items, respectively. I2 to 15 indicate the 2nd to 5th best items. Lb and Lw indicate the best and worst locations, 978 979 respectively. L2 and L3 indicate the 2nd and 3rd best locations, respectively. 980



981

Figure 8. Quantitative evaluations of eigenvector properties in the cOFC and
HPC populations.

984 (A) Time series of vector size estimated in the cOFC population for probability (P) 985 and magnitude (M) of rewards. The vector sizes are estimated in the PC1 to PC2 986 plane (top) and PC2 to PC3 plane (bottom), respectively. a.u. indicates arbitrary unit. 987 The solid colored lines indicate interpolated lines using a cubic spline function to 988 provide a resolution of 0.005 s. (B) Same as A, but for the best and worst items and 989 the best and worst locations in the HPC population. (C) Box plots of vector size 990 estimated in the cOFC population for probability and magnitude of rewards. (D) 991 Same as C, but for the best and worst items and the best and worst locations in the 992 HPC population. (E-F) Same as C-D, but for the vector angle estimated in the cOFC 993 and HPC populations. (G-H) Same as C-D, but from the vector deviance for the 994 mean estimated in the cOFC and HPC populations. In C-H, data after 0.1 s are used.



995

996 Figure 9. Effects of matrix size control in the HPC population.

997 (A) Cumulative variance explained by PCA in the HPC population when the best and 998 worst conditions for item and location are used for the regression subspace. The gray 999 dots indicated the percent variance explained by the PCA when using the full matrix. The first 12 PCs are shown. (B) Time series of eigenvectors for PC1 to PC3 when 1000 1001 the best and worst items and the best and worst locations are used. Ib and Iw 1002 indicate the best and worst items, respectively. Lb and Lw indicate the best and worst 1003 locations, respectively. s and e indicate the start and end of the time series of vectors, 1004 respectively. (C) Boxplot of explained variances by PCA for PC1 to PC12 under the 1005 three shuffled conditions (see Methods for details). The plot is not cumulative. The 1006 boxplot was made with 1,000 repeats of the shuffle in each condition. The colored 1007 circles indicate the variances explained by PCA in the HPC population without the 1008 shuffles.