

fcfdr: an R package to leverage continuous and binary functional genomic data in GWAS

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1 **Abstract**

2 **Summary:** GWAS discovery is limited in power to detect associations that exceed the stringent
3 genome-wide significance threshold, but this limitation can be alleviated by leveraging relevant
4 auxiliary data. Frameworks utilising the conditional false discovery rate (cFDR) can be used to
5 leverage continuous auxiliary data (including GWAS and functional genomic data) with GWAS
6 test statistics and have been shown to increase power for GWAS discovery whilst controlling the
7 FDR. Here, we describe an extension to the cFDR framework for binary auxiliary data (such
8 as whether SNPs reside in regions of the genome with specific activity states) and introduce an
9 all-encompassing R package to implement the cFDR approach, `fcfdr`, demonstrating its utility in
10 an application to type 1 diabetes.

11

12 **Availability and implementation:** The `fcfdr` R package is freely available at: <https://github.com/annahutch/fcfdr>. Scripts and data to reproduce the analysis in this paper are freely available
13 at: https://annahutch.github.io/fcfdr/articles/t1d_app.html

15

16 **1 Introduction**

17 A stringent significance threshold is required to identify robust genetic associations in GWAS
18 due to multiple testing constraints. Leveraging relevant auxiliary data has the potential to boost
19 statistical power to exceed the significance threshold. The conditional FDR (cFDR) is a Bayesian
20 FDR measure that additionally conditions on auxiliary data to call significant associations. The
21 cFDR approach was originally developed to leverage GWAS p -values from related traits, thereby
22 exploiting genetic pleiotropy to increase GWAS discovery^{1,2,3}, and has been shown to increase
23 power for GWAS discovery whilst controlling the frequentist FDR¹¹.

24 Motivated by the enrichment of GWAS SNPs in particular functional genomic annotations¹⁴,
25 Flexible cFDR was developed to extend the usage of the cFDR approach to the accelerating field
26 of functional genomics⁹. However, at-present no cFDR methodology exists that permits binary
27 auxiliary data, meaning that the approach cannot currently be used to leverage auxiliary data with a
28 binary representation, such as whether SNPs are synonymous or non-synonymous or whether they
29 reside in regions of the genome with specific activity states.

30 Here we present an extension to the cFDR approach that supports binary auxiliary data and we
31 thus introduce a cFDR toolbox in the form of an R package ([https://github.com/annahutch/](https://github.com/annahutch/fcfd)
32 `fcfd`) that supports various auxiliary data types. We demonstrate the utility of our methods
33 and software by iteratively leveraging three distinct types of relevant auxiliary data with GWAS
34 p -values for type 1 diabetes (T1D)¹² to uncover new genetic associations.

35 **2 The cFDR framework**

36 Let $p_1, \dots, p_m \in (0, 1]$ be a set of p -values corresponding to the null hypotheses of no association
37 between the SNPs and a trait of interest (denoted by H_0). Let q_1, \dots, q_m be auxiliary data values
38 corresponding to the same m SNPs. Assume that p and q are realisations of random variables P, Q
39 satisfying:

$$(P|H_0) \sim U(0, 1) \tag{1}$$
$$P \perp\!\!\!\perp Q|H_0.$$

40 The cFDR is defined as the probability that a random SNP is null for the trait given that the
41 observed p -values and auxiliary data values at that SNP are less than or equal to values p and q
42 respectively^{1,2}. Bayes theorem and standard probability rules are used to derive:

$$\begin{aligned} cFDR(p, q) &= Pr(H_0|P \leq p, Q \leq q) \\ &= \frac{Pr(P \leq p|H_0, Q \leq q) \times Pr(H_0|Q \leq q)}{Pr(P \leq p|Q \leq q)} \\ &= \frac{Pr(P \leq p|H_0, Q \leq q) \times Pr(Q \leq q|H_0)Pr(H_0)}{Pr(P \leq p, Q \leq q)}. \end{aligned} \quad (2)$$

43 To construct a conservative estimator of the cFDR, approximate $Pr(P \leq p|H_0, Q \leq q) \approx p$ (from
44 property 1; note that if property 1 holds and P is correctly calibrated then this approximation is an
45 equality) and $Pr(H_0) \approx 1$ (since associations are rare in GWAS):

$$\widehat{cFDR}(p, q) = \frac{p \times \widehat{Pr(Q \leq q|H_0)}}{\widehat{Pr(P \leq p, Q \leq q)}}, \quad (3)$$

46 where $\widehat{}$ is used to denote that these are estimates under the assumption $H_0 \perp\!\!\!\perp Q|P$. The methods
47 used to estimate the cumulative densities in equation (3) vary across approaches. In the original
48 cFDR approach they are estimated using empirical cumulative density functions^{1,10,11} whilst in
49 Flexible cFDR they are estimated using kernel density estimation⁹.

50 However, the \widehat{cFDR} values do not directly control the FDR¹⁰. Instead, a method proposed by
51 Liley and Wallace¹¹ can be used to generate v -values, which are essentially the probability of
52 a newly-sampled realisation (p, q) of P, Q attaining an as extreme or more extreme \widehat{cFDR} value
53 than that observed, given H_0 . The v -values are therefore analogous to p -values and can be used in
54 any conventional error-controlling multiple testing procedure that allows for slightly dependent
55 p -values (e.g. the Benjamini-Hochberg procedure). The derivation of v -values also allows for the
56 method to be applied iteratively to incorporate additional layers of auxiliary data.

57 Since binary auxiliary data can only take two values, we introduce an alternative methodology
58 called “Binary cFDR” which is based on finding optimal rejection regions to derive v -values
59 (see Supplementary Methods for full details on the Binary cFDR methodology). We show in a
60 simulation-based analysis that applying Binary cFDR iteratively over informative auxiliary data

61 increases power whilst controlling the frequentist FDR (Supplementary Results, Supplementary
62 Fig. 2).

63 **3 R package and T1D application**

64 We present an R package that implements both Flexible cFDR and Binary cFDR, named `fcfdr`
65 (<https://github.com/annahutch/fcfd>), and demonstrate its utility in an application to T1D
66 which is fully reproducible (see https://annahutch.github.io/fcfd/articles/t1d_app.html).
67 `html`).

68 We used p -values from an Immunochip study of T1D¹² as our primary data set. In the first iteration
69 we used Flexible cFDR to leverage Immunochip p -values for a genetically related trait, rheumatoid
70 arthritis (RA)⁶ (Fig. 1A). In the second iteration we used Binary cFDR to leverage data measuring
71 SNP overlap with regulatory factor binding sites^{5,8,7} (Fig. 1B) and in the third iteration we used
72 Flexible cFDR to leverage average enhancer-associated H3K27ac fold change values derived from
73 ChIP-seq experiments conducted in T1D-relevant cell types⁴ (Fig. 1C) (see Supplementary Methods
74 for full details on the data).

75 Our implementation of cFDR identified 101 SNPs as newly genome-wide significant ($FDR \leq$
76 $3.3e - 06$ which corresponds to $p \leq 5e - 08$; Supplementary Methods). These SNPs had relatively
77 small p -values for RA (median $p = 0.007$ compared with median $p = 0.422$ in full data set), were
78 more likely to be found in regulatory factor binding sites (mean binary value was 0.406 compared
79 to 0.234 in full data set) and had larger H3K27ac fold change values in T1D-relevant cell types
80 (median fold change value was 1.44 compared with 0.576 in full data set). Similarly, 45 SNPs
81 were identified as newly not significant (i.e. they were significant in the original GWAS data set
82 but became not significant after applying cFDR). These SNPs had relatively high p -values for RA
83 (median $p = 0.620$), were less likely to be found in regulatory factor binding sites (mean binary
84 value was 0.044) and had smaller H3K27ac fold change values in T1D-relevant cell types (median
85 fold change value was 0.431).

86 The original GWAS identified 38 significant genomic regions (based on our definition of genomic
87 regions, see Supplementary Methods). All of these were found to be significant in the cFDR analysis,
88 which additionally identified 4 genomic regions that were newly significant (with lead variants:

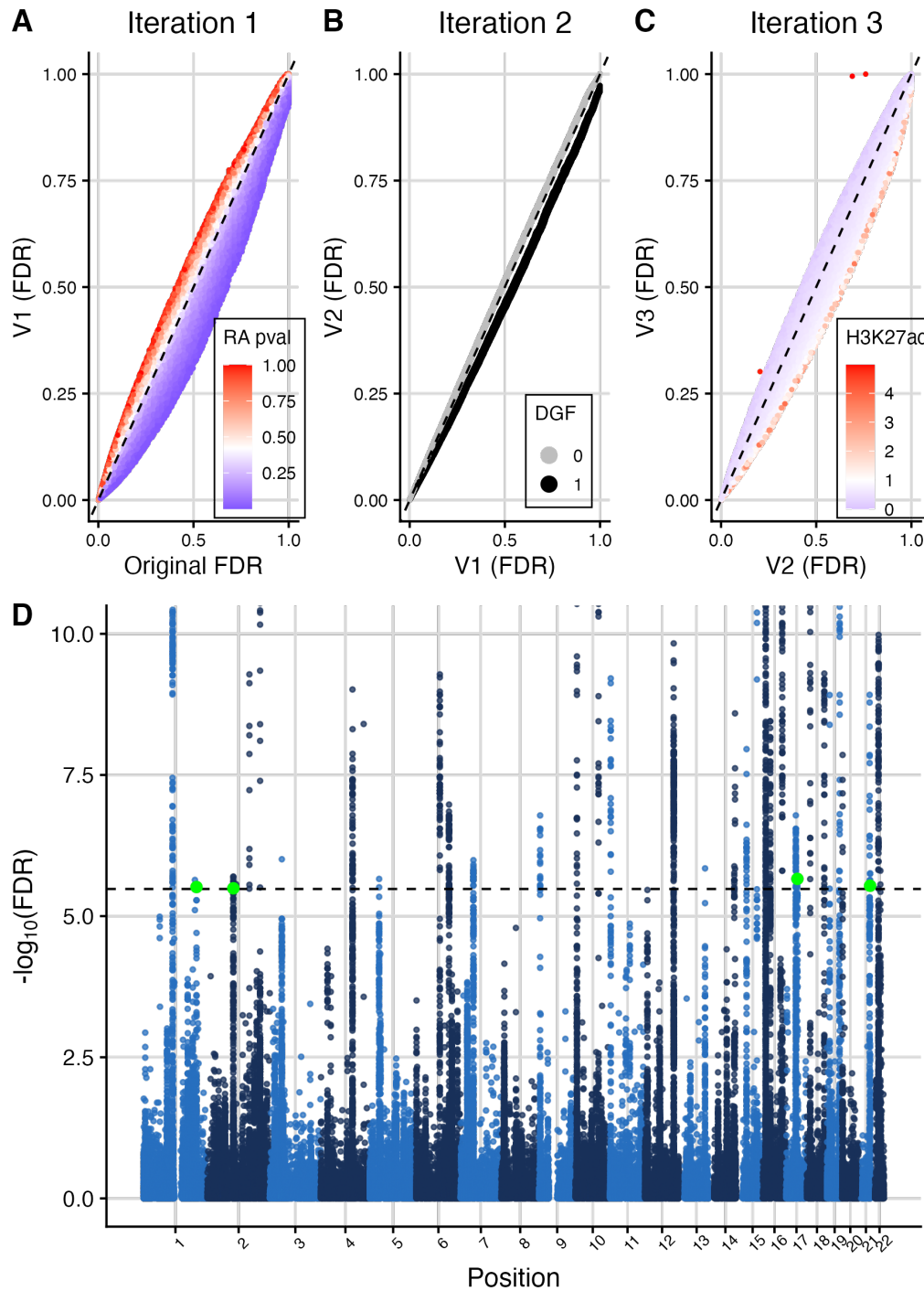


Figure 1: Summary of cFDR results for T1D application. “FDR values” were obtained from the raw p -values and v -values from each iteration of the cFDR approach using the Benjamini-Hochberg procedure. Top panel shows FDR values before and after (A) iteration 1 (B) iteration 2 and (C) iteration 3 of the method, coloured by the value of the auxiliary data (p -values for RA in iteration 1, DGF annotation values in iteration 2 and average H3K27ac fold change values relative to expected background counts in iteration 3). (D) Manhattan plot of ($-\log_{10}$ transformed) FDR values. Green points indicate the four lead variants that were newly FDR significant after cFDR. Black dashed line at FDR significance threshold ($FDR = 3.3e - 06$; which was the maximum FDR value amongst SNPs with raw p -values $\leq 5e - 08$ - see Supplementary Methods). y -axis has been truncated in panel (D) to aid visualisation.

89 rs1052553, rs3024505, rs6518350 and rs13415583). Three of these SNPs had small p -values for
90 RA (rs1052553: RA $p = 0.007$; rs6518350: RA $p = 0.06161$ and rs13415583: RA $p = 1.913e - 06$
91 whereas rs3024505 had RA $p = 0.6008$) and two of these SNPs had high H3K27ac fold change
92 values (rs3024505 had 87.4th percentile and rs6518350 had 72.7th percentile of H3K27ac fold
93 change values). Two of the lead variants overlapped regulatory factor binding sites (rs1052553
94 and rs3024505). When using a larger ImmunoChip study of T1D for validation (16,159 T1D cases
95 compared to 6,670)¹³, we found that three out of the four lead variants were present and that
96 these had smaller p -values in the validation GWAS data set than the discovery GWAS data set:
97 rs1052553 had $p = 1.649e - 15$, rs3024505 had $p = 9.127e - 14$, rs13415583 had $p = 4.764e - 09$
98 in the validation data set¹³ compared to $p = 8.156e - 08$, $p = 6.394e - 08$ and $p = 1.062e - 07$
99 respectively in the discovery data set¹².

100 **4 Conclusion**

101 We have described a novel implementation of the cFDR approach that supports binary auxiliary
102 data and have introduced an all-encompassing R package, `fcfdr`, that can be used to implement
103 the cFDR approach for a wide variety of auxiliary data types. We have demonstrated the versatility
104 of this tool in an application to T1D where we uncovered new genetic associations.

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