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KoT: an automatic implementation of the K/θ method for species delimitation

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ABSTRACT

¹ K/θ is a method to delineate species that rests on the calculation of the ratio between the
² average distance K separating two putative species-level clades and the genetic diversity
³ θ of these clades. Although this method is explicitly rooted in population genetic theory,
⁴ it was never benchmarked due to the absence of a program allowing automated analyses.
⁵ For the same reason, its application by hand was limited to small datasets of a few tens of
⁶ sequences.

⁷ We present an automatic implementation of the K/θ method, dubbed KoT (short for “K
⁸ over Theta”), that takes as input a FASTA file, builds a neighbour-joining tree, and returns
⁹ putative species boundaries based on a user-specified K/θ threshold. This automatic imple-
¹⁰ mentation avoids errors and makes it possible to apply the method to datasets comprising
¹¹ many sequences, as well as to test easily the impact of choosing different K/θ threshold
¹² ratios. KoT is implemented in Haxe, with a javascript webserver interface freely available at
¹³ <https://eeg-ebe.github.io/KoT/>

14 *Key words:* 4X rule, K/θ , species delimitation, molecular systematics, DNA taxonomy

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16 INTRODUCTION

17 Methods to delineate species from sets of DNA sequences have been an intense field of
18 research for the last 20 years (Sites and Marshall, 2003; Flot, 2015). Some methods delimit
19 species based on phylogenetic trees, other on genetic distances, and yet others on allele
20 sharing (Fontaneto et al., 2015). Among these methods, one called K/θ (Birky et al., 2010;
21 Birky, 2013; Birky and Maughan, 2020) stands out be resting on the genealogical species
22 concept, in which closely related populations are considered as distinct species when their
23 lineages for a given locus (or set of loci) are reciprocally monophyletic, that is, “if their
24 loci coalesce more recently within the group than between any member of the group and
25 any organisms outside the group” (Baum and Shaw, 1995). Of course, sampling all lineages
26 from a population is usually impossible, but population genetic theory provides ways to
27 calculate the probability that the lineages of two populations are monophyletic given the
28 observation that the sequences samples from these populations form clades in a phylogenetic
29 tree (Hudson and Coyne, 2002).

30 In particular, Rosenberg (2003) provides a formula that uses Watterson’s estimator
31 of genetic diversity $\theta = 4N_e\mu$ (Watterson, 1975) of each of two clades of sequences, the
32 number of sequences in each of them, and the mean pairwise sequence difference between
33 the two clades K to calculate the probability that the corresponding two populations are
34 reciprocally monophyletic, i.e. distinct species according to the genealogical species concept.
35 This formula is complex, but when the two θ values are similar and the number of sequences
36 in each clade is higher than three, a useful rule of thumb is that pairs of clades with a K/θ
37 ratio higher than 4 have a probability of at least 0.95 of belonging to different species. This
38 forms the basis of the so-called “4X rule” (Birky and Barraclough, 2009), which has been

39 widely used to delineate species in a variety of organisms. However, one may wish to choose
40 a more stringent threshold: for instance, a K/θ ratio higher than 6 entails a probability of
41 monophyly higher than 0.99 (according to equation 9 in Rosenberg, 2003).

42 Despite the theoretical appeal of this method based on an explicit criterion inspired
43 by population genetic, its practical application has been hampered by the lack of a program
44 performing the needed calculations automatically. To fill this gap, we introduce here KoT
45 (short for “K over Theta”), an automatic implementation of the K/θ method using the
46 programming language Haxe (Dasnois, 2011).

47 DESCRIPTION

48 KoT takes as input an alignment of DNA sequences in the FASTA file format. Users
49 can specify the K/θ threshold they wish to use to delineate species (by default, 4).

50 KoT starts by calculating all the pairwise nucleotide distances among the sequences
51 in the dataset. In case the input contains indels and/or missing data (encoded respectively as
52 “-” and as “N” or “?”), users can either ask KoT to filter out completely the corresponding
53 positions in the alignment (“complete deletion” mode) or to retain them (“pairwise deletion”
54 mode, in which case positions with missing or ambiguous data are ignored during pairwise
55 comparisons). From this set of pairwise distances, KoT then computes a neighbor-joining
56 (NJ) tree and the K/θ ratios of each pair of sister clades using the procedure outlined in
57 Birky and Maughan (2020).

58 To compute the genetic diversity θ of each clade, KoT starts by calculating the
59 nucleotide diversity π (Nei and Li, 1979) as the mean of all nucleotide-level differences π_{ij}
60 (number of nucleotide differences per nucleotide site between sequences i and j) among the
61 $\frac{n(n-1)}{2}$ pairs of sequences in a clade of n sequences, i.e. $\pi = \frac{2}{n(n-1)} \sum_{i=1}^n \sum_{j=1}^{i-1} \pi_{ij}$ (Equation
62 10.6 in Nei, 1987). An equivalent way to calculate π found in the literature is to compare all
63 pairs of haplotypes instead of all pairs of sequences: in that case, the formula above becomes
64 $\pi = \frac{1}{n(n-1)} \sum_{ij} (n \times x_i)(n \times x_j) \pi_{ij}$ (where x_i is the frequency of haplotype i in the clade),

65 which simplifies into $\pi = \frac{n}{n-1} \sum_{ij} x_i x_j \pi_{ij}$ (Equation 10.6 in Nei, 1987), i.e. the average
66 heterozygosity multiplied by a sample size correction $n/(n-1)$ (Nei and Tajima, 1981;
67 Korunes and Samuk, 2021). As KoT uses the direct formula comparing pairs of sequences,
68 however, no sample size correction is needed.

69 For clades made up of identical sequences (in which case $\pi = 0$), an upper bound of π
70 is sought by assuming that one sequence differs from the others by a single mutation, i.e. by
71 replacing one of the $\frac{n(n-1)}{2}$ pairwise distances with $1/L$, where L is the sequence length; in
72 such case π become $\frac{2}{Ln(n-1)}$ (Birky et al., 2010). As this ratio is not defined for $n = 1$, KoT
73 uses $n = 2$ (i.e. $\pi = 1/L$) for clades comprising a single sequence. To estimate the genetic
74 diversity θ associated with a specific clade, KoT uses the formula $\theta = \frac{1}{\frac{1}{\pi} - \frac{4}{3}}$ (Equation 9 in
75 Tajima, 1996), which corrects for multiple hits based on the Jukes-Cantor model of sequence
76 evolution (Jukes and Cantor, 1969).

77 To compute the genetic divergence K between sister clades A and B, KoT computes
78 the mean pairwise nucleotide distance $p = \sum_{i=1}^{n_A} \sum_{j=1}^{n_B} \pi_{ij}$ between the sequences in the
79 two clades, where n_A stands for the number of individuals in clade A and n_B stands for
80 the number of individuals in clade B, then corrects it for multiple substitutions using the
81 Jukes-Cantor formula $K = -\frac{3}{4} \ln(1 - \frac{4}{3}p)$ (Jukes and Cantor, 1969). Using the Jukes-Cantor
82 correction for calculating K is important to ensure that both terms of the ratio K/θ are
83 computed using the same evolutionary model.

84 Finally, KoT computes the K/θ ratios of clades A and B and compares the smallest
85 of the two with the threshold chosen by the user to delineate species. These calculations
86 are performed iteratively from the leaves of the tree all the way to its root. When a ladder
87 structure ((A,B)C) or a polytomy (A,B,C) is encountered, KoT starts by comparing the two
88 clades separated by the smallest distance K , i.e. A and B: if the result of the calculation
89 does not support the hypothesis that A and B are different species, the A+B clade is then
90 compared to C to find out whether they are conspecific or heterospecific; whereas if the result
91 of the calculation indicates that A and B are likely two distinct species, C is compared with

92 whichever of A and B has the smaller average distance K to C (Birky et al., 2010). If C is
93 then deemed to be distinct as well, the final result returned is three species A, B and C.
94 On the other hand, if the result of the calculation suggests that C is conspecific with e.g. B,
95 an additional comparison of C with A is warranted to ensure the transitivity of the result
96 (Dellicour and Flot, 2018). As the extra calculations this entails can take lots of time in
97 complex cases, this comparison is only performed if the box “transitivity” is checked by the
98 user prior to running the analysis. If the “transitivity” box is not checked (as by default),
99 KoT simply returns in such cases two species A and B+C; when the “transitivity” box is
100 checked, by contrast, KoT checks whether the K/θ ratio for the C vs. A comparison is also
101 above the user-selected threshold: if so, the final delimitation returned is a pair of species A
102 and B+C; whereas if the calculation does not support the monophyly of A vs. C, the final
103 result returned is a single species A+B+C.

104 KoT outputs a tree in which the θ values of each pair of clades being compared are
105 displayed on the tree next to the node uniting them, together with their K distance and
106 the K/θ ratio (obtained using the larger of the two θ values). Colors are applied to the tree
107 in order to visually delineate the different species. A partition list, i.e. a two-column table
108 indicating, for each sequence in the input FASTA, the species to which it was attributed
109 (Spöri and Flot, 2020), is also outputted below the tree where it can be easily copied/pasted
110 into other applications.

111 BIOLOGICAL EXAMPLE

112 To investigate the behavior of KoT, we reanalyzed the COI dataset from one recent
113 article (Stoch et al., 2020). In this article, a dataset of 34 COI sequences of specimens
114 of the *Niphargus tatrensis* species complex was analyzed using a diversity of approaches:
115 mPTP Kapli et al. (2017) delimited seven putative species, ABGD (Puillandre et al., 2012)
116 returned ten of them, and bPTP (Zhang et al., 2013) and ST-GMYC (Pons et al., 2006)
117 delineated eleven species-level units. The methods chiefly differed in their delimitation of

118 species among the non-Austrian specimens included in the study but were largely congruent
119 in their treatment of the Austrian specimens, with mPTP, bPTP and ST-GMYC finding
120 four species and ABGD delimiting five species in Austria.

121 When run with a K/θ threshold ratio of 4 (Figure 1), KoT returned twelve species,
122 including five for Austria (separated by K/θ ratios of 21.39, 17.50, 4.52 and 5.98); with
123 a K/θ threshold ratio of 5 (Figure 2), the method returned eleven species, with precisely
124 the same putative boundaries as those obtained using bPTP and ST-GMYC (including
125 four species for Austria separated by K/θ ratios of 21.35, 17.44 and 5.94); finally, with a
126 K/θ threshold ratio of 6 (Figure 3) KoT returned eight species-level units, notably lumping
127 together all Austrian specimens into a single putative species. This highlights the sensitivity
128 of this method to the K/θ threshold parameter.

129 AVAILABILITY

130 KoT is written in Haxe. Its source code is available at <https://github.com/eeg-ebe/>
131 KoT, and a javascript webserver is freely accessible at <https://eeg-ebe.github.io/KoT/>.

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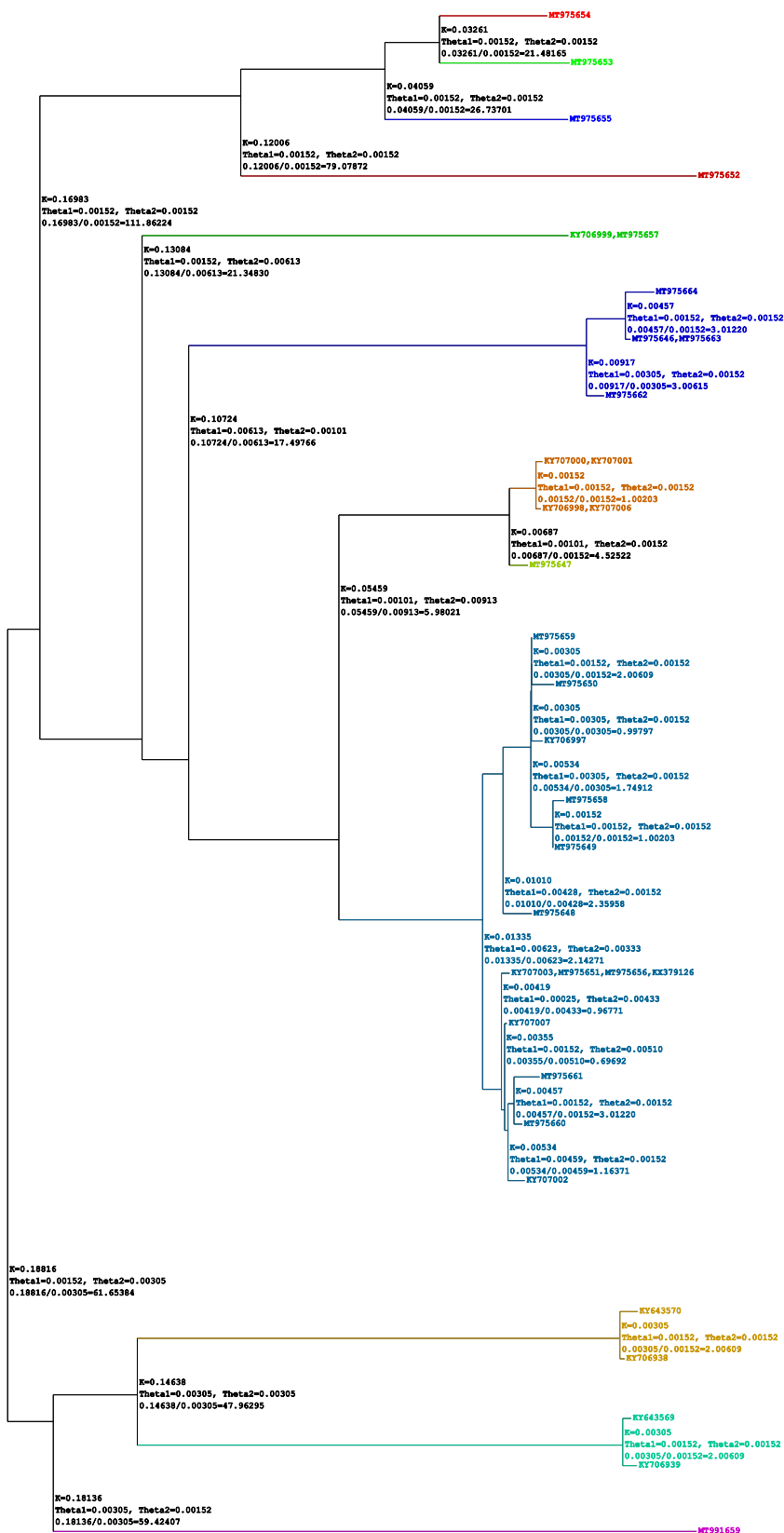


Fig. 1. Output of KoT when run on the COI dataset of Stoch et al. (2020) with a K/θ threshold of 4

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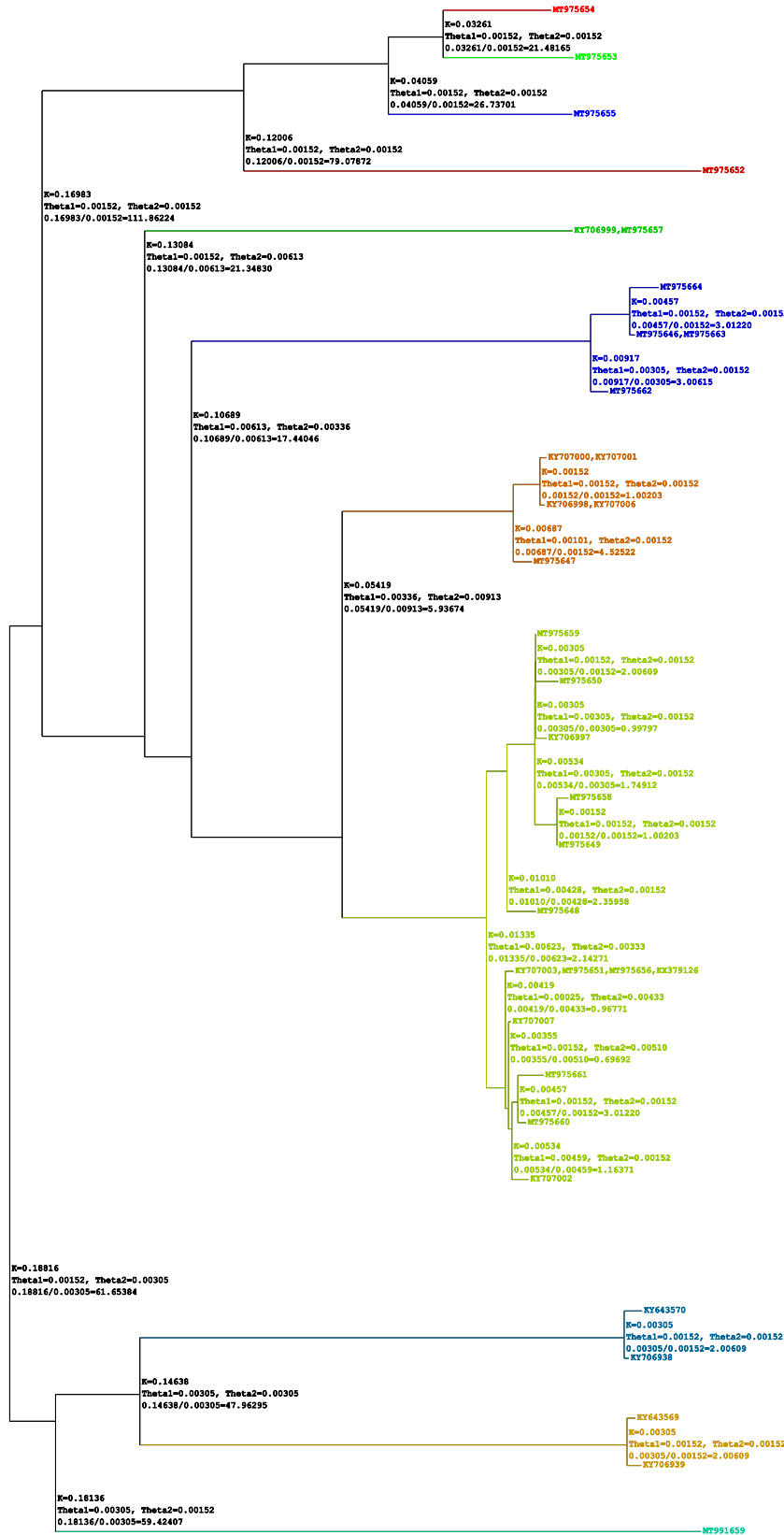


Fig. 2. Output of KoT when run on the COI dataset of Stoch et al. (2020) with a K/θ threshold of 5

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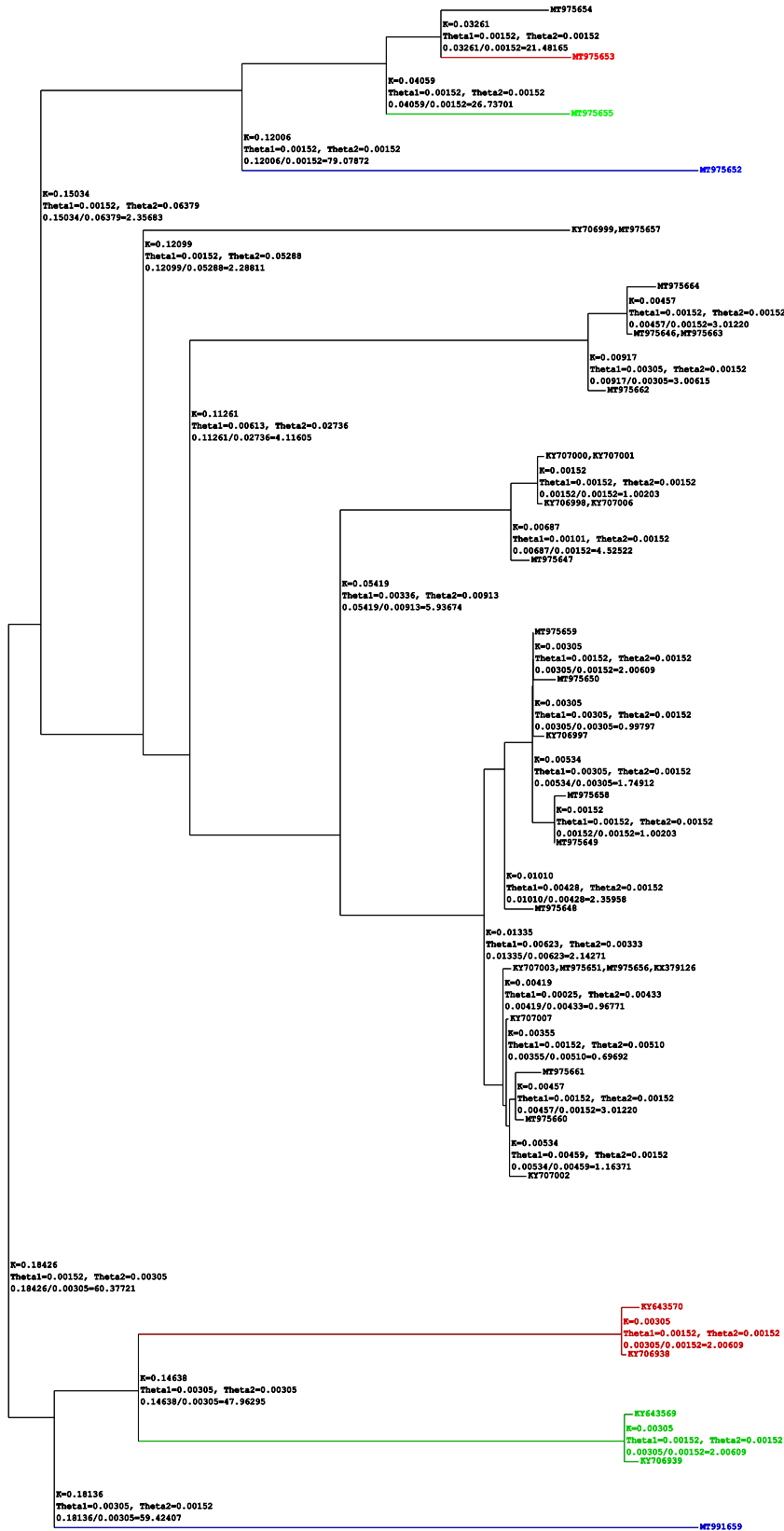


Fig. 3. Output of KoT when run on the COI dataset of Stoch et al. (2020) with a K/θ threshold of 6