

1 Vergence accuracy in an autostereoscopic display

2

3 Luca Lo Verde^{1,2} and Anthony M. Norcia^{1,2}

4

5 ¹ Department of Psychology, Stanford University

6 ² Wu Tsai Neurosciences Institute, Stanford University

7

8

9

10

11

12

13

14

15

16 **Acknowledgments:** Funded by a Stanford University Bio-X Interdisciplinary Initiatives Seed
17 Grants Program (IIP) grant.

18

19 **Address for Correspondence:** Anthony M. Norcia (amnorcia@stanford.edu); Wu Tsai
20 Neurosciences Institute, 290 Jane Stanford Way, Stanford, CA 94305. +1 (650) 725-2438.

21 **Abstract**

22

23 When fixating an object, observers typically under or over-converge by a small amount, a
24 phenomenon known as “fixation disparity”. Fixation disparity is typically measured with physical
25 fixation targets and dichotically presented nonius lines. Here we made fixation disparity
26 measurements with an autostereoscopic display, varying the retinal eccentricity and disparity of
27 the fixation targets. Measurements were made in a group of four practiced observers and in a group
28 of thirteen experimentally naïve observers. Fixation disparities with a zero-disparity target were in
29 the direction of fixation behind the plane of the screen and the magnitude of the fixation disparity
30 grew with the eccentricity of the fixation targets (1-5 deg in the practiced observers and 1 – 10 deg
31 in the naïve observers). Fixation disparity also increased with increasing disparity of the targets,
32 especially when they were presented at crossed disparities. Fixation disparities were larger overall
33 for naïve observers who additionally did not converge in front of the screen when vergence demand
34 was created by crossed disparity fusion locks presented at 5 and 10 deg eccentricities.

35

36 **Keywords:** stereoscopic display, vergence, binocular fusion, autostereoscopic display

37

38

39 **Introduction**

40 Observers with normal binocular vision typically fixate slightly in front of or behind an
41 objective of regard, a phenomenon known as fixation disparity (Hoffmann and Bielschowsky,
42 1900 ; Ogle et al., 1967). Fixation disparity is typically measured using dichoptic nonius lines to
43 read-out the perceived visual direction of each eye and this measurement is generally well
44 correlated with the pointing direction of the two eyes in observers with normal binocular vision
45 (Hillis and Banks, 2001).

46 Fixation disparity can be exaggerated by imposing different degrees of retinal disparity on
47 display elements. In the classical studies of fixation disparity, these image disparities were
48 produced through the use of prisms (Ogle et al., 1967). Fixation disparity has also been reported
49 to increase with increasing retinal eccentricity of disparate targets (Carter, 1964; Debysingh et al.,
50 1986; Ukwade, 2000).

51 Measures of fixation disparity are commonly measured clinically with physical cards or
52 devices and prisms (Mallett, 1964; Sheedy, 1980; Wesson and Koenig, 1983). Here we studied
53 fixation disparity using a large-format lenticular autostereoscopic display in practiced and
54 experimentally naïve observers. Changes on vergence demand were induced by disparate targets
55 presented over a range of retinal eccentricities. Fixation disparity increased with both increasing
56 vergence demand and retinal eccentricity of the stimulus to fusion, especially for crossed
57 disparities (increased convergence demand) and for experimentally naïve observer

58

59 **Methods**

60

61 **Participants**

62 Two groups of observers participated. Four highly practiced participants (2 females, mean
63 age: 42 ± 18 years; range 31-69; two observers were co-authors of this work) were tested to tune
64 the experimental parameters. These observers had normal- or corrected-to-normal vision, and
65 normal stereoacuity.

66 A second, experimentally naive group of thirteen participants (7 females, mean age: 19.9
67 ± 0.8 years; range: 19-21 years old) were tested after being screened for having normal or corrected
68 to normal visual acuity and stereoacuity (Bailey Lovie Eye Chart; Randot Stereotest). Consenting
69 and experimental procedures were approved by the Institutional Review Board of Stanford
70 University. The research conformed to the tenets of the Helsinki Convention.

71

72 **Apparatus and Stimuli**

73 The experiment was performed in a quiet room in total darkness. The stimuli were
74 developed in MATLAB (The Mathworks, Inc., Natick, MA) using Psychtoolbox-3 (Brainard,
75 1997; Pelli and Vision, 1997; Kleiner et al., 2007) and delivered using a SeeFront autostereoscopic
76 3D monitor (SeeFront GmbH, Frankfurt, Germany; model SF3D320-MP). A schematic
77 representation of the stimulus configuration, depicted as a red/blue anaglyph for visualization
78 purposes, is shown in Figure 1A. Nonius lines were used as a high-precision subjective indicator
79 of vergence posture (McKee and Levi, 1987). The dichoptic nonius lines were gray, 21 minutes of
80 arc long and were vertically separated by 36.5 minutes of arc. The top nonius lines was delivered
81 to the right eye and fixed in position, always presented in the center of the screen and in the center

82 of the right eye fusion lock component. The participant could adjust the horizontal position of the
83 other nonius line using a track wheel device. The initial position of the adjustable nonius line
84 varied pseudo-randomly on each trial, with a maximum possible displacement of 14.4 arcmin from
85 the screen center. The background was black.

86 The binocular fusion lock consisted of a radial pattern composed of four circular sectors
87 surrounding the nonius lines. The fusion lock could be placed at different retinal eccentricities
88 around the nonius stimuli: four eccentricities for the pilot data collection (1°, 1.25°, 2.5° and 5°
89 of eccentricity) and three eccentricities for the main data pool (1°, 5° and 10° of eccentricity).
90 These eccentricities were defined as the distance from the screen center and the inner radius of
91 the four circular sectors around the nonius lines. The circular sector sizes were scaled to equate
92 their visibility according the cortical magnification factor (Baseler et al., 1994) and thus the
93 fusion locks presented at higher eccentricities were larger than the ones presented closer to the
94 center of the visual field. The equation used to estimate the cortical area A subtended by circular
95 sectors is the following:

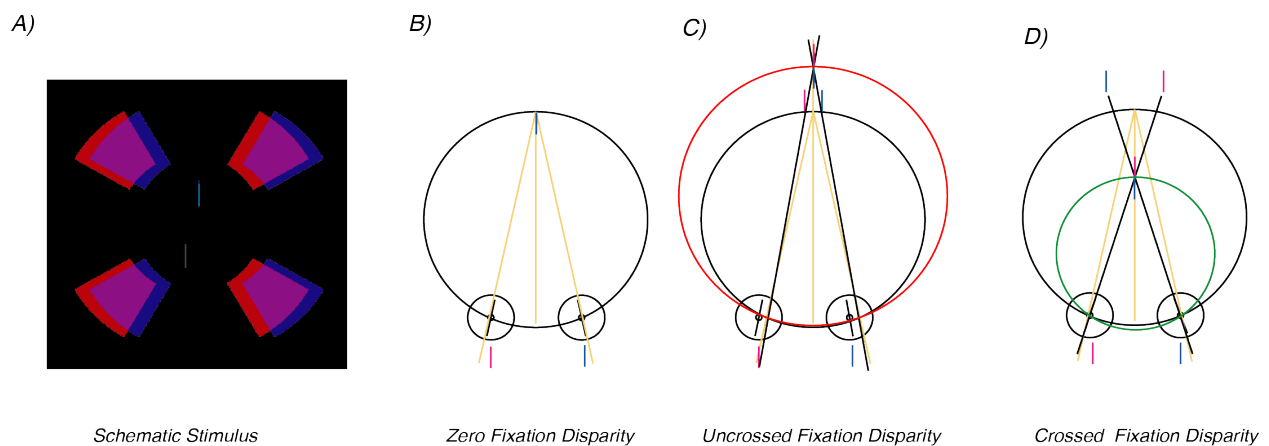
$$96 \quad A = 300 * \frac{2\pi}{360} * \theta * \left[\frac{0.75 * (r_o - r_i)}{(r_i + 0.75) * (r_o + 0.75)} + \ln \left(\frac{r_i + 0.75}{r_o + 0.75} \right) \right]$$

97
98 Where θ represents the angle of a given circular sector, r_i represents the inner radius between the
99 screen center and the inner margin of each circular sector, and r_o represents the outer radius
100 between the screen center and the outer margin of each circular sector. The fusion lock was
101 presented at thirteen different horizontal disparities (6 crossed and 6 uncrossed disparities plus
102 zero disparity: 0°, ±0.05°, ±0.1°, ±0.2°, ±0.4°, ±0.6° and ±0.8°).

103

104 Procedure

105 Participants sat comfortably 70 cm from the monitor. They held a rotary USB input device
106 used for collecting responses. Experimentally naive participants were familiarized with the stimuli
107 and task by having them perform 5 training trials. Practiced observers had extensive experience
108 with the task prior to data collection. Each trial began with a blank, dark screen, followed by the
109 appearance of the fusion lock stimulus, presented at zero disparity for 750 msec. Subsequently,
110 the fusion lock assumed the designated disparity for that trial and the nonius lines appeared in the
111 center of the screen. The participants were asked to focus on the central nonius lines and to ignore
112 the surrounding radial fusion lock pattern. These stimuli remained visible on the screen until the
113 end of the trial.



115

116 **Figure 1.** A) Schematic representation of the stimuli, in this case depicting the dichoptic fusion lock with 1 deg of
117 eccentricity and 0.2 degrees of uncrossed disparity. In this anaglyphic representation, the magenta portions of the
118 stimuli are delivered to the left eye while the blue ones are seen by the fellow eye (every component of the stimulus
119 was gray in the actual experiment). We manipulated both eccentricity and disparity of the fusion lock surrounding the
120 nonius lines. The upper nonius line was always a fixed reference, while the participants could adjust the horizontal
121 position of the lower, probe nonius line to perceptually align them. B) Zero fixation disparity. Physically aligned
122 nonius lines at the plane of the screen (black curve) are subjectively aligned with zero nonius offset. C) Uncrossed
123 fixation disparity. The eyes are diverged relative to the plane of the screen, subjectively aligned targets have a negative
124 nonius offset. D) Crossed fixation disparity. The eyes are converged relative to the plane of the screen, subjectively
125 aligned targets have a positive nonius offset.

126

127 The participants used the rotary input device to adjust the position of the probe nonius line
128 until they perceived the two nonius lines as vertically aligned. The device allowed them to
129 progressively and smoothly move the probe nonius line in either horizontal direction (step size: 1
130 pixel \approx 1.80 minutes of arc) to align the vertical nonius lines. The participants pressed a dedicated
131 button on the response device to proceed to the next trial once they were satisfied with the
132 perceived alignment of the nonius lines.

133 Figure 1B illustrates the case of zero fixation disparity. Here physically aligned nonius
134 lines are seen as subjectively aligned, indicating that vergence was on the plane of the screen,
135 indicated by the black Vieth-Müller circle presented as an approximation of the empirical horopter.
136 Fig. 1C indicates the case of uncrossed fixation disparity where the eyes are diverged relative to
137 the plane of the screen and subjective alignment occurs with a negative nonius offset, under our
138 convention. Fig. 1D indicates the case of a crossed fixation disparity where the eyes are converged
139 relative to the plane of the screen and subjective alignment occurs with a positive nonius offset,
140 under our convention.

141 There were no time constraints on the perceptual alignment task, and the participants were
142 instructed to achieve a stable alignment before finishing a given trial. Each experimental session
143 consisted of 6 trial repetitions for each of the 3 fusion lock eccentricities (4 fusion lock
144 eccentricities for the experienced observers pool) and the 13 fusion lock disparities, for a total of
145 246 trials per participant, split in 3 separate blocks each consisting of 82 trials.

146

147 **Conventions**

148 We adopted the disparity conventions in widespread use across classical optometry works (Ogle
149 et al., 1967) by assigning uncrossed fusion lock disparities to the positive range of the presented
150 disparity axis while the crossed disparity fusion locks are assigned negative values.

151 We first computed deviations from each presented vergence demand by subtracting the actual
152 vergence demand from the final adjusted position of the participants-controlled nonius line
153 which had to be perceptually aligned with the other, fixed nonius line. Therefore, a positive
154 (negative) deviation indicates a failure to converge (diverge) the eyes enough to have each
155 dichoptic fusion mask lie on each corresponding points on the two retinae. We computed these
156 deviations for the three fusion lock eccentricities as a function of vergence load, as well as
157 having the deviations for each vergence load as a function of fusion lock eccentricity to better
158 visualize the influence of these variables on the task.

159

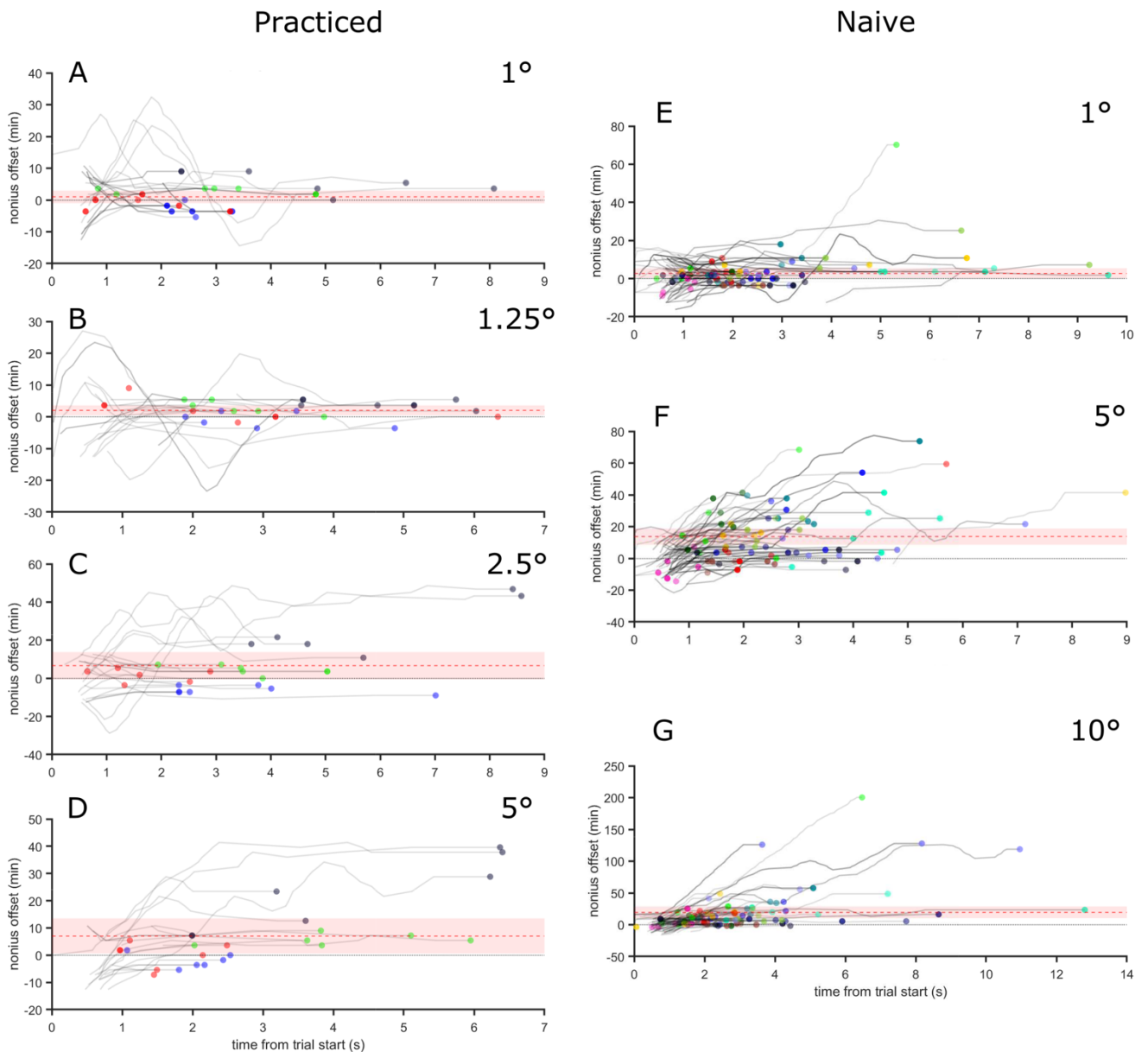
160 **Results**

161

162 The relative alignment of the nonius lines was continuously tracked until they were perceptually
163 aligned. Figure 2 A-D shows example time-courses of the alignment judgements for each of the
164 fusion lock eccentricities for the zero-disparity fusion lock condition (1.0, 1.25, 2.5 and 5 deg for
165 the practiced observers pool and 1.0, 5 and 10 deg for the naïve participants pool, respectively).

166 The data are from the four practiced observers in panels A-D and the thirteen naïve observers in
167 E-G. The zero-disparity condition represents a conventional estimate of fixation disparity, but with
168 eccentric fixation locks. The average fixation disparity increased with the eccentricity of the fusion
169 lock (dashed line), as did the variability of the setting (red band). The dashed red lines indicate the

170 average of the final adjustment before trial end for each participant, and the red shade represents
171 the standard error of the means.



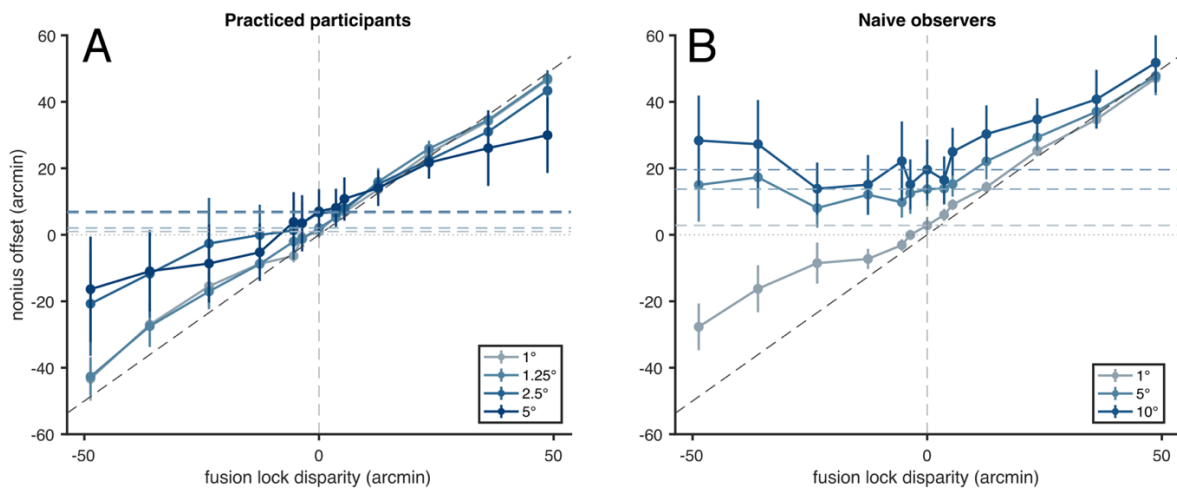
172

173

174 **Figure 2.** Time course of the nonius position adjustments from trial onset, plotted for each fusion lock eccentricities
175 (A: 1°; B: 1.25°; C: 2.5°; D: 5°) for the zero-disparity condition for the practiced participant pool. Each color
176 represents a single participant, the red dashed line represents the average of the final nonius position across all
177 participants, the light red area defines the standard error of the mean. E-G) data from the 13 naïve participants using
178 the same convention.

179

180 The full data sets over all fixation lock disparities and eccentricities are shown in Figure 3.
181 The dashed diagonal lines indicate the imposed disparity of the fusion lock and thus the vergence
182 demand. For both practiced and naïve observers, the nonius offset for subjective alignment
183 accurately tracks the disparity of the low-eccentricity, uncrossed fusion locks (1 deg in both groups
184 (light blue curves in both A and B) and additionally at 1.25 deg eccentricity in the practiced group
185 but undershoots it for crossed disparities especially in the naïve observers (compare Fig. 3 A to
186 B). As the eccentricity of the fusion lock increases to 2.5, 5 and 10 deg eccentricity, the nonius
187 offset setting increasingly fails to track the disparity of the fusion lock, especially for crossed
188 disparities (see Fig. 2 C, D and F, G). The divergence of the nonius settings from the imposed
189 demand implies that the eyes are less converged or diverged than the demand imposed by the
190 disparity of the fusion lock. Notably, in the naïve observers, the nonius offset for crossed fusion
191 locks are on the uncrossed side for the largest fusion lock disparities.



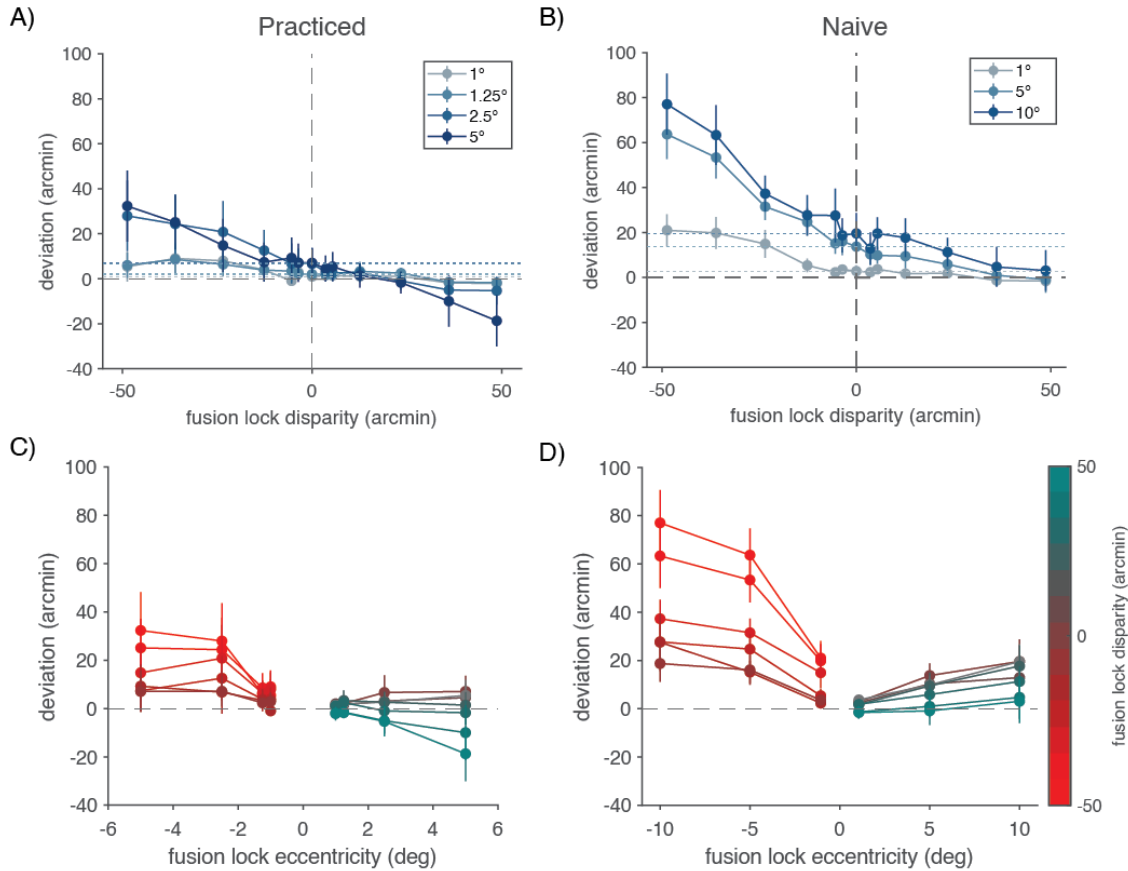
192

193 **Figure 3.** Nonius offset settings for practiced (A) and Naïve observers (B). Eccentricities in degrees are reported in
194 the legends.

195

196

197



198

199 **Figure 4.** Deviations of settings from vergence demand. A) Deviation as a function of fusion lock disparity for
 200 practiced observers. Deviation grows with increasing fusion lock, especially for larger crossed disparities. B)
 201 Deviation as a function of fusion lock disparity for naive observers. Trends in experience observers are exaggerated.
 202 C) Deviation as a function of fusion lock eccentricity for practiced observers. Deviation increases for more eccentric
 203 fusion locks, especially for crossed disparity. D) Deviation as a function of fusion lock eccentricity for naive observers.
 204 Trends in practiced observers are exaggerated in the naive observers. For visibility purposes, we translated the
 205 negative fusion lock disparities curves (plotted in shades of red) to negative eccentricities in C and D.
 206

207 To better visualize the magnitude of the biases, we transformed the nonius offsets in
 208 deviations from imposed vergence load and visualized the data of Figure 3 in two ways: first as a
 209 function of fusion lock disparity, with eccentricity as the parameter and then as a function of
 210 disparity with eccentricity as the parameter. At zero disparity and 1 degree of eccentricity, the
 211 fixation disparity in the practiced observers was 0.98 ± 1.97 arcmin and in the naive observers it
 212 was 2.82 ± 2.6 arcmin. At 5 deg, where both groups provided data, these values were 7.06 ± 6.44

213 arcmin and 13.73 ± 5.1 arcmin, respectively. At 10 degrees of eccentricity (for the naïve
214 participants pool), the fixation disparity was 19.58 ± 9.13 arcmin.

215 As the disparity of the fusion lock increases, nonius offset deviation remains essentially
216 constant for all uncrossed disparities when the fusion lock eccentricity is 1 deg in both groups and
217 1.25 deg in the practiced observers. At 2.5 deg and higher fusion lock eccentricities, the zone where
218 fixation disparity is small shrinks to disparities less than ≈ 5.41 arcmin. The fixation disparity
219 increases with eccentricity for all disparities, especially for crossed disparities and larger disparity
220 magnitudes in both groups. The asymmetry in settings between crossed and uncrossed disparities
221 is readily apparent when deviation is plotted as a function of eccentricity for the two disparity signs
222 (Fig 4 C, D).

223

224 **Discussion**

225

226 Our results with an autostereoscopic display qualitatively recapitulate results from the
227 clinical and psychophysical literatures. We find that the degree of nonius misalignment increases
228 with increasing disparity of the fusion locks. Increasing the disparity of the fusion lock mimics the
229 addition of prisms as used in clinical studies or the use of mirror deflectors (Schor et al., 1986),
230 but does not induce a shift of all visible elements over the visual field. In our case, only the fusion
231 lock stimuli varied in disparity, but the monitor bezel and the dimly lit room surround did not.

232 In both observer groups, fixation disparity measured with a zero-disparity fusion lock is
233 positive, meaning that the eyes are converged behind the plane of the display. The magnitude of
234 the fixation disparity increases in both groups as the fusion lock eccentricity increases, as observed
235 in previous studies (Carter, 1964; Debysingh et al., 1986; Ukwade, 2000).

236 As increasing disparity is introduced into the fusion lock, the nonius offset directly tracks
237 the magnitude of the imposed disparity for uncrossed fusion locks when the eccentricity of the
238 fusion lock is low (*e.g.* 1 to 1.25 deg). The uncrossed fusion locks are portrayed behind the plane
239 of the monitor. At larger eccentricities, the nonius offset fails to track the imposed disparity by
240 increasing amounts in the practiced observers (see Fig 3C and D). In the naïve observers the nonius
241 offset matches the largest of the imposed uncrossed disparities, but over- compensates in the
242 uncrossed direction for smaller fusion lock disparities (see Fig. 3 F and G).

243 The crossed disparity fusion locks render the images in front of the plane of the monitor.
244 In both observer groups, for the smallest fusion lock eccentricities, the nonius offset tracks the sign
245 of the disparity, but fails to keep up with the magnitude of the disparity (see Fig. 3 A,B and E). In
246 the practiced group, the function is shallower than the imposed disparity demand for both signs of
247 disparity and by 5 deg of eccentricity, the effect is approximately symmetric for crossed and
248 uncrossed disparities. In the naïve observers, the presentation of crossed disparity fusion locks fails
249 to drive convergence in front of the plane of the monitor at 5 and 10 deg eccentricities of the fusion
250 lock – fusion lock disparity has no effect and does not alter the fixation disparity value measured
251 for zero disparity.

252 Previous research on the perception of depth from disparity has compared stereoacuity for
253 simple real-world targets and simulated versions of them presented in a stereoscope (McKee and
254 Taylor, 2010). For two unpracticed observers, depth thresholds in the stereoscope were much
255 worse than their real-space depth thresholds. Superiority of cue integration has also been reported
256 for real versus stereoscopically simulated displays (Buckley and Frisby, 1993). The
257 autostereoscopic and other types of dichoptic viewing system inherently present conflicts between
258 disparity cues and accommodation/proximity cues and this may affect the perception of depth from

259 the fusion locks. However, this can't be the whole explanation as cue conflict is equal over the
260 different fusion lock eccentricities. In the naïve observers, performance is relatively good for the
261 1 deg fusion lock eccentricity, but not for the 5 and 10 deg eccentricities. This suggests another
262 factor – peripheral disparity sensitivity – may be at play. Peripheral stereoacuity can improve more
263 than central visual acuity with practice, at least in some observers (Fendick and Westheimer, 1983)
264 and it is possible that the naïve observers are not as able to use peripheral disparity information in
265 the context of our experimental conditions.

266

267
268
269
270
271
272
273
274
275
276
277
278
279
280
281
282
283
284
285
286
287
288
289

References

- Baseler HA, Sutter EE, Klein SA, Carney T (1994) The topography of visual evoked response properties across the visual field. *Electroencephalogr Clin Neurophysiol* 90:65-81.
- Brainard DH (1997) The Psychophysics Toolbox. *Spat Vis* 10:433-436.
- Buckley D, Frisby JP (1993) Interaction of stereo, texture and outline cues in the shape perception of three-dimensional ridges. *Vision Res* 33:919-933.
- Carter DB (1964) Fixation Disparity with and without Foveal Fusion Contours. *Am J Optom Arch Am Acad Optom* 41:729-736.
- Debysingh SJ, Orzech PL, Sheedy JE (1986) Effect of a central fusion stimulus on fixation disparity. *Am J Optom Physiol Opt* 63:277-280.
- Fendick M, Westheimer G (1983) Effects of practice and the separation of test targets on foveal and peripheral stereoacuity. *Vision Res* 23:145-150.
- Hillis JM, Banks MS (2001) Are corresponding points fixed? *Vision Res* 41:2457-2473.
- Hoffmann FB, Bielschowsky A (1900) Ueber die der Willkur entzogenen Fusions-bewegungen der Augen. *Arch f d ges Physiol* 80:1-40.
- Kleiner M, Brainard D, Pelli D (2007) What's new in Psychtoolbox-3?
- Mallett RJF (1964) The investigation of heterophoria at near and a new fixation disparity technique. *Optician* 148:573-581.
- McKee SP, Levi DM (1987) Dichoptic hyperacuity: the precision of nonius alignment. *J Opt Soc Am A* 4:1104-1108.
- McKee SP, Taylor DG (2010) The precision of binocular and monocular depth judgments in natural settings. *J Vis* 10:5.

- 290 Ogle KN, Martens TG, Dyer TA (1967) Oculomotor Imbalance in Binocular Vision and Fixation
291 Disparity. Philadelphia: Lea and Febiger.
- 292 Pelli DG, Vision S (1997) The VideoToolbox software for visual psychophysics: Transforming
293 numbers into movies. *Spatial vision* 10:437-442.
- 294 Schor C, Wesson M, Robertson KM (1986) Combined effects of spatial frequency and retinal
295 eccentricity upon fixation disparity. *Am J Optom Physiol Opt* 63:619-626.
- 296 Sheedy JE (1980) Fixation disparity analysis of oculomotor imbalance. *Am J Optom Physiol Opt*
297 57:632-639.
- 298 Ukwade MT (2000) Effects of nonius line and fusion lock parameters on fixation disparity.
299 *Optom Vis Sci* 77:309-320.
- 300 Wesson MD, Koenig R (1983) A new clinical method for direct measurement of fixation
301 disparity. *South J Optom* 1:48-52.
302