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2 **Astrocyte nanoscale morphology controls Ca^{2+}**
3 **signals at tripartite synapses**
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15 **Abstract**

16 Ca^{2+} signals in astrocytes can trigger the modulation of neuronal ac-
17 tivity. Recent developments in Ca^{2+} imaging and super-resolution mi-
18 croscopy have allowed to characterize the complex morphology of astro-
19 cyte branchlets that communicate with neurons and the associated Ca^{2+}
20 microdomains. Here, we use computational tools to investigate the causal
21 relationship between branchlet morphology and spatio-temporal profile of
22 Ca^{2+} signals. 3D reticular branchlet geometries were designed, alternating
23 between large (nodes) and thinner cellular compartments (shafts). Sim-
24 ulations confirm experimental observations that a decreased shaft width
25 is associated with a decreased diffusion flux from nodes, enhancing local
26 Ca^{2+} activity. Upon successive neuronal stimuli, a decreased shaft width
27 facilitates signal propagation in astrocyte branchlets. We further identify
28 parameters that decrease local Ca^{2+} activity, such as a discontinuous ER
29 geometry and an increased Ca^{2+} buffering. Overall, this study proposes
30 key parameters that regulate Ca^{2+} activity locally, potentially favoring
31 neuron-astrocyte communication at tripartite synapses.

32 **Introduction**

33 Astrocytes are glial cells of the central nervous system that are essential
34 for brain development and function, playing key roles in e.g ionic home-
35 ostasis, lactate metabolism and the uptake of neurotransmitters (see the
36 review from Verkhratsky & Nedergaard [1] for more details). Furthermore,
37 according to the concept of tripartite synapses [2], astrocytes take part in
38 information processing. In response to neuronal stimulation, Ca^{2+} signals
39 can be observed in astrocytes. The first Ca^{2+} signals that have been char-
40 acterized are Ca^{2+} waves that propagate, through gap junction coupling, in
41 astrocyte networks [3]. Ca^{2+} waves can also propagate within the branches
42 of a single astrocyte, sporadically propagating to the soma [4, 5]. The re-
43 cent development of Ca^{2+} imaging techniques that provide better spatial

44 and temporal resolution have revealed the existence of spatially-restricted
45 Ca^{2+} signals in astrocytes, referred to as microdomains or hotspots [5–15].
46 As one astrocyte can contact $\approx 20,000$ – $120,000$ synapses simultaneously in
47 the mouse hippocampus [16], up to two million in the human brain [17],
48 those local, fast Ca^{2+} signals could enable the astrocyte to powerfully yet
49 precisely control the flow of information through synaptic circuits.

50
51 80% of astrocyte Ca^{2+} signals, notably Ca^{2+} hotspots, occur in thin
52 branchlets, characterized by diameters that are $< 200\text{nm}$ [5], which appear
53 blurry when imaged using conventional light microscopy. The geometry
54 of those compartments, forming the gliapil, has thus first been character-
55 ized by electron microscopy (EM), which revealed their physical proximity
56 to neurons and their complex reticular morphology [16, 18, 19]. Astro-
57 cyte branchlets appeared to display an organized ultrastructure, forming
58 “glial microdomains” that wrapped around synapses, potentially restrict-
59 ing neuron-astrocyte communication [19]. This hypothesis is however hard
60 to test experimentally because of the small size of astrocyte branchlets
61 and because EM does not allow to study dynamical phenomena in live
62 tissue. Recently, Arizono et al. [15] have overcome those issues by combin-
63 ing confocal Ca^{2+} imaging and 3D-Super-Resolution Stimulated Emission
64 Depletion (STED) microscopy. Their results suggest that the propagation
65 of Ca^{2+} signals in astrocyte branchlets is influenced by their morphology.
66 They notably identified bulbous structures, referred to as nodes, as pref-
67 erential sites of Ca^{2+} activity in astrocytes. Whether there is a causal re-
68 lationship between astrocyte branchlet morphology and the characteristics
69 of Ca^{2+} signals however remains unclear and difficult to test experimen-
70 tally. As Ca^{2+} microdomains might allow astrocytes to finely modulate
71 neuronal communication at the single synapse level, elucidating the bio-
72 physical mechanisms that regulate their formation is crucial.

73
74 Here, we use computational tools to investigate the effect of the mor-
75 phology of astrocyte branchlets on Ca^{2+} activity. To account for the
76 stochasticity of molecular interactions in small volumes such as those of as-
77 trocyte branchlets, we use the voxel-based model of IP_3R -mediated Ca^{2+}
78 signals from Denizot et al. [20]. Idealized geometries of branchlets were
79 designed based on super-resolution microscopy images in live tissue [15].
80 Branchlets consist in alternations of structures referred to as nodes and
81 shafts. Our results suggest that molecular diffusion flux decreases with
82 shaft width, which enhances Ca^{2+} peak probability, duration and ampli-
83 tude in the stimulated node. In case of successive node stimulation events,
84 thin shafts allow signal propagation despite an omitted stimulus. Thin
85 shafts thus allow more robust signal propagation. Furthermore, we pro-
86 pose several mechanisms that decrease local Ca^{2+} activity in the gliapil:
87 an increased shaft width, a discontinuous ER geometry and an increased
88 Ca^{2+} buffering .

89
90 Overall, our results shed light on the mechanisms that can influence
91 local Ca^{2+} signals in astrocyte branchlets. Importantly, our results pro-
92 vide evidence that node compartmentalization, resulting from a reduced
93 diffusion flux from nodes connected to thin shafts, can increase Ca^{2+} ac-
94 tivity locally. This study provides a better understanding of the effect of
95 the morphology of the cell and of the organelles on Ca^{2+} signals at the
96 nanoscale.

97 Results

98 Geometrical representation of typical astrocyte branch- 99 lets

100 In order to investigate the effect of the geometry of astrocyte branch-
101 lets on the spatio-temporal properties of Ca^{2+} signals, we have designed
102 geometries of typical astrocyte branchlets, derived from the recent char-
103 acterization of their ultrastructure at high spatial resolution (50 nm in
104 x-y) in organotypic brain slices [15]. Geometries consist in alternations of
105 bulbous structures, nodes, connected to each other with cylindrical struc-
106 tures, referred to as shafts. Geometries with different shaft width d_{shaft} and
107 constant node width were designed (Fig 1A). Screenshots of the resulting
108 meshes are presented in Supplemental Fig S1. The geometry of the ER in
109 the gliapil has not been characterized in live tissue so far. Thus, as a first
110 approximation, ER geometry was considered to be identical to the geome-
111 try of the astrocyte branchlet: node/shaft successions. A sensitivity study
112 has been performed to investigate the effect of voxel size on the kinetics of
113 the molecular interactions modeled. Information on the voxel sizes of the
114 different meshes used is presented in Supplemental Table S1. Results are
115 presented in Supplemental Fig S2. Meshes that contained voxels that were
116 $< 50\text{nm}^3$ were characterized by aberrant kinetics, resulting in inaccurate
117 average numbers of molecules in a given state. We have thus made sure,
118 while meshing the geometries in which we ran the simulations, that no
119 voxels were $< 50 \text{ nm}^3$.

120

Table 1: **Characteristics of the geometries of astrocyte branchlets used in this study.** V_{cyt} is the cytosolic volume, S_{PM} is the area of the plasma membrane and S_{ER} is the area of the ER membrane. Volumes are expressed in nm^3 and areas in nm^2 .

| Geom | $V_{\text{cyt}} (\text{nm}^3)$ | $S_{\text{PM}} (\text{nm}^2)$ | $S_{\text{ER}} (\text{nm}^2)$ |
|--------------------------------------|--------------------------------|-------------------------------|-------------------------------|
| “5nodes” $d_{\text{shaft}} = d_0$ | 6.20×10^8 | 7.73×10^6 | 2.19×10^6 |
| “5nodes” $d_{\text{shaft}} = d_0/2$ | 2.63×10^8 | 4.95×10^6 | 1.28×10^6 |
| “5nodes” $d_{\text{shaft}} = d_0/3$ | 1.95×10^8 | 4.10×10^6 | 9.99×10^5 |
| “No ER” $d_{\text{shaft}} = d_0$ | 6.73×10^8 | 7.73×10^6 | 0.00 |
| “No ER” $d_{\text{shaft}} = d_0/2$ | 2.83×10^8 | 4.95×10^6 | 0.00 |
| “No ER” $d_{\text{shaft}} = d_0/3$ | 2.10×10^8 | 4.09×10^6 | 0.00 |
| “Node ER” $d_{\text{shaft}} = d_0$ | 6.67×10^8 | 7.75×10^6 | 4.17×10^5 |
| “Node ER” $d_{\text{shaft}} = d_0/2$ | 2.74×10^8 | 4.96×10^6 | 4.37×10^5 |
| “Node ER” $d_{\text{shaft}} = d_0/3$ | 2.00×10^8 | 4.11×10^6 | 4.41×10^5 |
| “Cyl ER” $d_{\text{shaft}} = d_0$ | 6.27×10^8 | 7.74×10^6 | 2.03×10^5 |
| “Cyl ER” $d_{\text{shaft}} = d_0/2$ | 2.77×10^8 | 4.95×10^6 | 8.78×10^5 |
| “Cyl ER” $d_{\text{shaft}} = d_0/3$ | 2.07×10^8 | 4.09×10^6 | 5.86×10^5 |

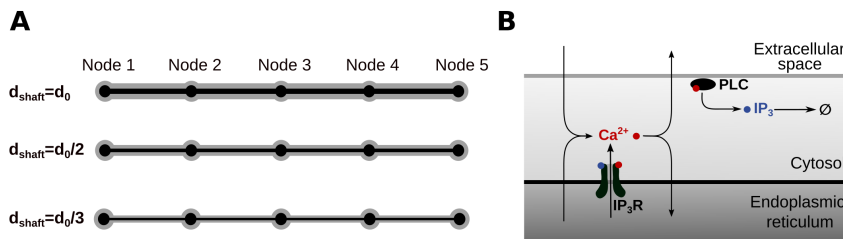


Fig 1: **Geometries and kinetic scheme used for simulating Ca^{2+} dynamics in node/shaft structures of the gliapil.** (A) Geometries reproducing node/shaft geometries of the gliapil [15, 21] were designed. Nodes are approximated as spheres of diameter 380 nm and shafts as $1\mu\text{m}$ -long cylinders. Conic geometries were added between spheres and cylinders in order to get smoother, more realistic geometries. The geometries designed in this study, referred to as “5 nodes”, contain 5 identical nodes and 4 identical shafts. Geometries were characterized by different shaft widths: $d_{\text{shaft}} = d_0 = 380\text{nm}$, $d_{\text{shaft}} = \frac{d_0}{2}$ and $d_{\text{shaft}} = \frac{d_0}{3}$. The associated cytosolic volume, plasma and ER membrane areas are presented in Table 1. (B) Biochemical processes included in the model. Ca^{2+} can enter/exit the cytosol from/to the extracellular space or the endoplasmic reticulum (ER), resulting from the activity of Ca^{2+} channels/pumps. Ca^{2+} and IP₃ diffuse in the cytosol following Brownian motion. The kinetics of IP₃R channels corresponds to the 8-state Markov model from [22], adapted from [23, 24]. When both IP₃ and Ca^{2+} are bound to IP₃R activating binding sites, the IP₃R is in open state and Ca^{2+} enters the cytosol. Ca^{2+} can activate Phospholipase C δ (PLC δ), which results in the production of IP₃. For more details, please refer to [22].

121 Thin shafts favor node compartmentalization

122 In order to test whether the geometries designed in this study are a
123 good approximation of the reticular ultrastructure of the gliapil, we have
124 compared molecular diffusion flux in those geometries with those reported
125 experimentally. To do so, we simulated photobleaching experiments and
126 compared our results to experimental results from Arizono et al. [15]. The
127 principle of bleaching simulations is presented in the Methods section and
128 in Supplemental Fig S3. Briefly, fluorescing molecules ZSGreen encounter
129 conformational changes at bleaching time, resulting in a decrease of the flu-
130 orescence level in the region of interest to I_0 . Then, because of the diffusion
131 of fluorescent ZSGreen into the region of interest, fluorescence increases un-
132 til it reaches I_{inf} (Supplemental Movie 1). Here, we refer to a high node
133 compartmentalization when the time to recovery after bleaching, τ , is high.

134
135 Bleaching traces in simulations are both qualitatively (Fig 2B) and
136 quantitatively (Fig 2C) similar to experimental bleaching traces, for shaft
137 width $d_{shaft} = d_0$ and $d_{shaft} = \frac{d_0}{2}$. Indeed, no significant difference of I_0
138 (Fig 2C1), I_{inf} (Fig 2C2) and τ (Fig 2C3) was observed between simu-
139 lations and experimental traces. Simulations were also performed with
140 $d_{shaft} = \frac{d_0}{3}$. Our simulations successfully reproduce experimental bleach-
141 ing experiments and suggest that τ , and thus node compartmentalization,
142 increases when shaft width decreases (Fig 2C3). This result is not surpris-
143 ing as a decreased shaft width results in a smaller size of the exit point for
144 diffusing molecules from the node. This is similar to e.g dendritic spines,
145 which compartmentalization is increased for thinner spine necks [25]. The
146 geometries that we have designed can thus be considered as a reasonable
147 approximation of the ultrastructure of the gliapil observed experimentally
148 in live tissue.

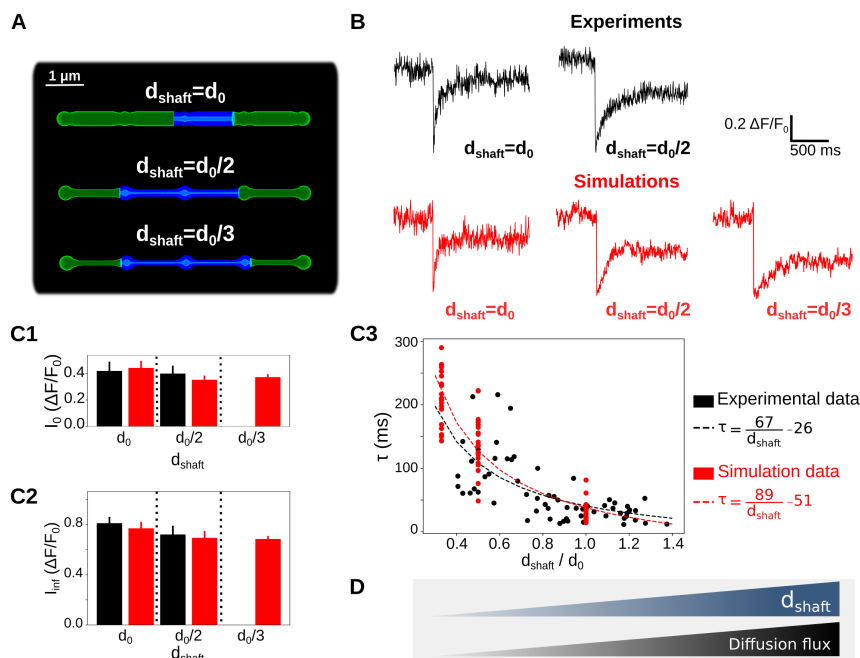


Fig 2: Simulations confirm that thin shafts favor node compartmentalization. (A) Geometries of different shaft widths d_{shaft} , $d_{\text{shaft}} = d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$, used in the bleaching simulations. Blue color represents the bleached volume, which varied depending on the value of d_{shaft} in order to fit experimental values of I_0 and I_{inf} . (B) Representative experimental (top) and simulation (bottom) traces for different shaft width values. Note that simulations were also performed for $d_{\text{shaft}} = \frac{d_0}{3}$. (C) Quantification of I_0 (C1), I_{inf} (C2) and τ (C3) values in simulations (red) compared to experiments (black). Note that no experimental data was available for $d_{\text{shaft}} = \frac{d_0}{3}$. In C1 and C2, $n=5 \times 2$ and 20×3 for experiments and simulations, respectively. Data are presented as mean \pm STD. In C3, $n=66$ and $n=20 \times 3$ for experiments and simulations, respectively. τ is negatively correlated to d_{shaft} in experiments ($n=66$ from 7 slices; Spearman $r=-0.72$, $p<0.001$ ***) and simulations ($n=60$; Spearman $r=-0.89$, $p<0.001$ ***). Black and red lines represent curve fit of τ as a function of d_{shaft} of the form $\tau = a * \frac{1}{d_{\text{shaft}}} + b$ for experiments and simulations, respectively. (D) Schematic summarizing the conclusion of this figure: diffusion flux increases with d_{shaft} . In that sense, thin shafts favor node compartmentalization. Data in panels C1 and C2 are represented as mean \pm STD, $n=20$ for each geometry.

149 Thin shafts are associated with increased Ca^{2+} activity 150 in nodes

151 80% of astrocyte Ca^{2+} activity occurs in thin branchlets of the gli-
152 apil [5], which suggests that most neuron-astrocyte communication occurs
153 at fine astrocyte branchlets. As we observed that a decreased shaft width is
154 associated with a decreased diffusion flux, i.e an increased compartmental-
155 ization of nodes, we have tested whether this effect influences Ca^{2+} activity
156 upon neuronal stimulation. To do so, we have first analyzed Ca^{2+} signals

157 resulting from the injection of IP_3 in one node (Node 1). Signals were
158 recorded both in the stimulated node and in the neighboring node (Node
159 2) (Fig 3A, Supplemental Movie 2). Representative Ca^{2+} traces in node 1
160 and 2 for $d_{\text{shaft}} = d_0, \frac{d_0}{2}$ and $\frac{d_0}{3}$ are displayed in Fig 3A. Our first notice-
161 able result is that Ca^{2+} peak probability increases when d_{shaft} decreases,
162 both in nodes 1 and 2 (Fig 3B1). The time to 1st peak increases with
163 d_{shaft} (Fig 3B2). On the contrary, peak amplitude (Fig 3B3) and duration
164 (Fig 3B4) increase when d_{shaft} decreases, both in nodes 1 and 2. Interest-
165 ingly, Ca^{2+} signals were not significantly different between node 1 and 2,
166 suggesting an "all-or-nothing" propagation to neighboring nodes. Indeed,
167 as soon as a Ca^{2+} peak was detected in node 1, an event of similar size
168 was always detected in node 2. In order to better understand the mecha-
169 nisms responsible for the increased Ca^{2+} peak probability, amplitude and
170 duration when d_{shaft} decreases, we have measured the frequency of IP_3R
171 opening in nodes 1 and 2. The frequency of IP_3R opening increases when
172 d_{shaft} decreases (Fig 3B5). Note that the duration of IP_3R opening and
173 the number of IP_3R open per Ca^{2+} peak did not vary with d_{shaft} . This
174 increase of IP_3R opening frequency when d_{shaft} decreases probably results
175 from the increased residency time of molecules in nodes connected to thin
176 shafts (Fig 3C). Indeed, a thin shaft can "trap" Ca^{2+} and IP_3 longer in
177 the node, thus locally increasing the probability of IP_3Rs to open, re-
178 sulting in larger Ca^{2+} peaks. For more details, the reader can refer to
179 the theoretical work investigating the narrow escape problem for diffusion
180 in microdomains [26]. Nodes connected to thinner shafts, despite being
181 characterized by a lower diffusion flux (Fig 2), could thus consist in sig-
182 nal amplification units, favoring the generation of larger signals, therefore
183 increasing Ca^{2+} peak probability, amplitude and duration both in the stim-
184 ulated node and in neighboring nodes.

185
186 In order to better understand the variability of Ca^{2+} signals with d_{shaft} ,
187 the effect of the volume of the astrocytic process was tested. Geometries
188 with $d_{\text{shaft}} = d_0, \frac{d_0}{2}$ and $\frac{d_0}{3}$ are characterized by node/shaft width ratios δ
189 of 1, 2 and 3, respectively. Those geometries are further characterized by
190 different volumes: $V_1=0.620 \mu m^3$, $V_2=0.263 \mu m^3$ and $V_3=0.195 \mu m^3$. To
191 test whether the effect of node/shaft width ratio δ on Ca^{2+} signals resulted
192 from the decreased branchlet volume with δ , a subset of simulations were
193 performed in a geometry with $\delta=1$ and $V_1=0.258 \mu m^3$, which is similar to
194 V_2 and V_3 (see Methods). The results are presented in Supplemental Fig
195 S4 and suggest that it is node/shaft width ratio rather than shaft width
196 itself that influences Ca^{2+} residency time in nodes. A high node/shaft
197 width ratio results in a higher IP_3R opening frequency and a higher peak
198 amplitude in nodes. Further, our results illustrate that the increase of Ca^{2+}
199 activity when shaft width decreases mostly results from the associated
200 decrease of cellular volume.

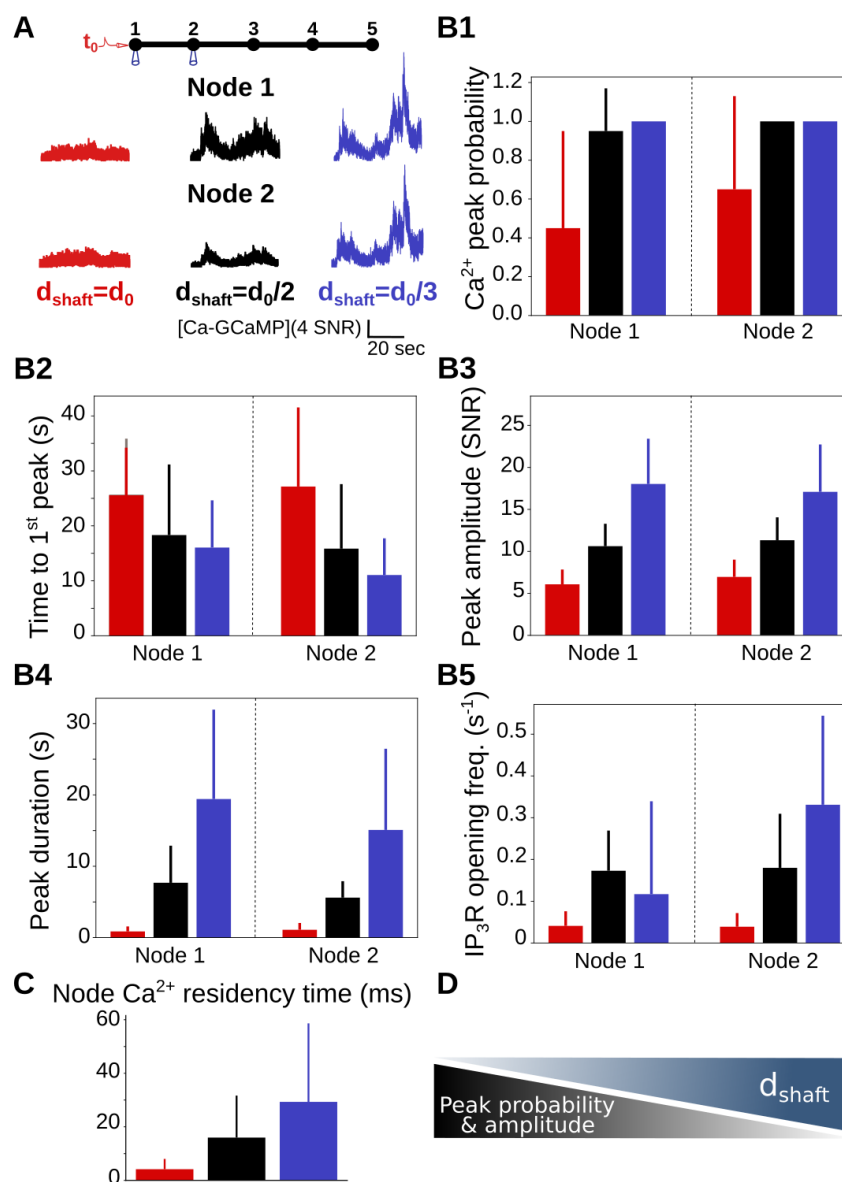


Fig 3: Ca²⁺ peak probability, amplitude and duration increase when shaft width decreases. (A) (Top) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at $t=t_0=1s$, while Ca²⁺ activity was monitored in nodes 1 and 2. Representative Ca²⁺ traces for shaft width $d_{\text{shaft}} = d_0$ (red), $\frac{d_0}{2}$ (black) and $\frac{d_0}{3}$ (blue) in node 1 (Middle) and node 2 (Bottom), expressed as SNR (see Methods). (B) Quantification of the effect of d_{shaft} on Ca²⁺ signal characteristics. Data are represented as mean \pm STD, $n=20$ for each geometry. (B1) Ca²⁺ peak probability increases when d_{shaft} decreases in both node 1 and 2 (***). (B2) Time to 1st peak increases with d_{shaft} in both Node 2 (*) and Node 1 (***). (B3) Peak amplitude increases when d_{shaft} decreases in both nodes 1 and 2 (***). (B4) Peak duration increases when d_{shaft} decreases in both nodes 1 and 2 (***). (B5) The frequency of IP₃R opening increases when d_{shaft} decreases in both nodes 1 and 2 (***). Ca²⁺ peak characteristics were not statistically different between node 1 and node 2, for $d_{\text{shaft}} = d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$. (C) Ca²⁺ residency time in node 1 increases when d_{shaft} decreases (***, $n=300$). (D) Schematic summarizing the main result from this figure: Ca²⁺ peak probability and amplitude increase when shaft width decreases. The effect of d_{shaft} on each Ca²⁺ signal characteristic was tested using one-way ANOVA. Significance is assigned by * for $p \leq 0.05$, ** for $p \leq 0.01$, *** for $p \leq 0.001$.

201 In the simulations presented in Fig 3, IP₃R density was constant. As
202 ER area varied with d_{shaft} (see Table 1) and as IP₃R density was kept constant,
203 the total number of IP₃R molecules differed and equaled 620, 363
204 and 283, for $d_{\text{shaft}} = d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$, respectively. To test whether the effect
205 of d_{shaft} on Ca²⁺ signals reported in Fig 3 resulted from the variation of
206 the number of IP₃R molecules with d_{shaft} , we have performed simulations
207 in which the number of IP₃R molecules did not vary with d_{shaft} . The results
208 are presented in Supplemental Fig S5 and confirm that Ca²⁺ peak
209 probability, duration and amplitude increase when d_{shaft} decreases. In order
210 to test the effect of reflective boundary conditions, we have performed
211 simulations in which the tetrahedra near the outer surface of Node 4 consisted
212 in clamped boundary conditions (Supplemental Fig S6). Similarly
213 to simulations with reflective boundary conditions, Ca²⁺ peak probability,
214 duration and amplitude increased when d_{shaft} decreased. Simulations in
215 which Node 3 was stimulated were also performed. Results are presented
216 in Supplemental Fig S7. Ca²⁺ peak probability, duration and amplitude
217 similarly increased when d_{shaft} decreased and Ca²⁺ peak characteristics
218 were similar in Node 3 and 4.

219
220 Finally, we have tested whether the increased Ca²⁺ activity of induced
221 signals in geometries with thin shafts could be observed for spontaneous
222 Ca²⁺ signals. To do so, 200 Ca²⁺ ions were infused in Node 1 at time
223 $t=t_0$, thus mimicking a Ca²⁺ signal resulting from the spontaneous opening
224 of Ca²⁺ channels. Ca-GCaMP signals were then monitored in nodes 1
225 and 2. The results are presented in Supplemental Fig S8. Simulation
226 results suggest that, similarly to neuronal-induced Ca²⁺ signals (Fig 3),
227 peak probability, amplitude and duration increase when d_{shaft} decreases,
228 both in nodes 1 and 2. Furthermore, the delay of Ca²⁺ peaks decreases
229 with d_{shaft} . Cellular geometry thus affects both spontaneous and induced
230 Ca²⁺ signals. Consistently with experimental results [15], we observe an
231 increase of the amplitude ratio of spontaneous Ca²⁺ signals between Node
232 2 and Node 1 with shaft width (Spearman $r=0.0006$, $p\text{-value} < 0.001$ ***).
233 This could result from the decreased diffusion flux from nodes connected
234 to thin shafts, so that a smaller proportion of molecules would reach the
235 neighboring node.

236 Overall, our results suggest that a decreased shaft width, although resulting
237 in a decreased diffusion flow from nodes, increases Ca²⁺ peak probability,
238 amplitude and duration.

239

240 **Discontinuous ER geometry is associated with decreased** 241 **Ca²⁺ activity**

242 As the ultrastructure of the ER in the geometries presented in Fig 1
243 was arbitrary, we have next investigated to what extent the effect of shaft
244 width d_{shaft} reported in Fig 3 depends on ER geometry. To do so, we
245 have created geometries with the same cellular geometry as in Fig 1 while
246 varying the geometry of the ER (Fig 4A, Fig S7A). Simulations performed
247 in the geometries used so far in this study, in which the ER consists in
248 alternations of nodes and shafts, are here referred to as “Node/shaft ER”.
249 A subset of simulations, referred to as “Cyl ER”, has been performed in
250 meshes that contain continuous, cylindrical ER, with a length of $l_{\text{ER}} = 6274$
251 nm and a diameter of 108, 54 and 36 nm, for $d_{\text{shaft}} = d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$, respec-

252 tively. Another subset of simulations, referred to as “Node ER”, contained
253 discontinuous ER, which consisted in spheres with a diameter of 54 nm, lo-
254 cated in nodes. Finally, simulations referred to as “No ER” were performed
255 without any ER. Node 1 was stimulated at $t=t_0=1s$, while Ca^{2+} activity
256 was monitored in nodes 1 and 2. Note that no signals occur in the “No
257 ER” geometry, as there are no IP_3R channels. Ca^{2+} signals qualitatively
258 (Fig 4B) and quantitatively (Fig 4C) varied depending on ER geometry.
259 Time to 1^{st} is higher (Fig 4C2) and Ca^{2+} peak probability (Fig 4C1),
260 amplitude (Fig 4C3) and duration (Fig 4C4) as well as the frequency of
261 IP_3R opening (Fig 4C5) are lower in geometries with discontinuous com-
262 pared to continuous ER geometry. Note that IP_3R opening frequency was
263 larger in simulations in “Node ER” geometry than in “Node/shaft ER”
264 geometry with IP_3Rs located in nodes, although not resulting in any sig-
265 nificant difference of peak characteristics. Similarly to “Node/shaft” ER
266 geometry, there was no significant difference between peak characteristics
267 in Node 1 compared to Node 2 and Ca^{2+} peak probability, amplitude
268 and duration increased when d_{shaft} decreased, for all ER geometries tested
269 (Supplemental Fig S9B-C). Ca^{2+} peak probability, amplitude and dura-
270 tion were larger in “Cyl ER” geometries than in “Node ER” geometry
271 but lower than in “Node/shaft ER” geometry (Supplemental Fig S9B-C).
272 Interestingly, Ca^{2+} node residency time did not vary depending on ER
273 morphology (Supplemental Fig S10A), suggesting that the increased Ca^{2+}
274 activity in branchlets containing continuous ER might not result from ER
275 morphology itself. To further understand those results, as ER surface area
276 is increased in “Node/shaft ER” geometry compared to “Node ER” geom-
277 etry, we have tested whether the increased Ca^{2+} dynamics in branchlets
278 with continuous ER results from the associated increase of the number of
279 IP_3R channels in the branchlet. For example, there are 283 and 125 IP_3R
280 channels in “Node/shaft ER” and “Node ER” geometry with $d_{shaft}=\frac{d_0}{3}$,
281 respectively. To do so, simulations were performed in “Node/shaft ER”
282 and “Node ER” with the same amount of IP_3R channels, 300, located in
283 nodes. Ca^{2+} signals did not vary depending on ER morphology in those
284 simulations (Supplemental Fig S10B). Those results suggest that the de-
285 creased Ca^{2+} activity in branchlets with discontinuous ER mainly results
286 from the associated decreased surface area compared to continuous ER ge-
287 ometries.

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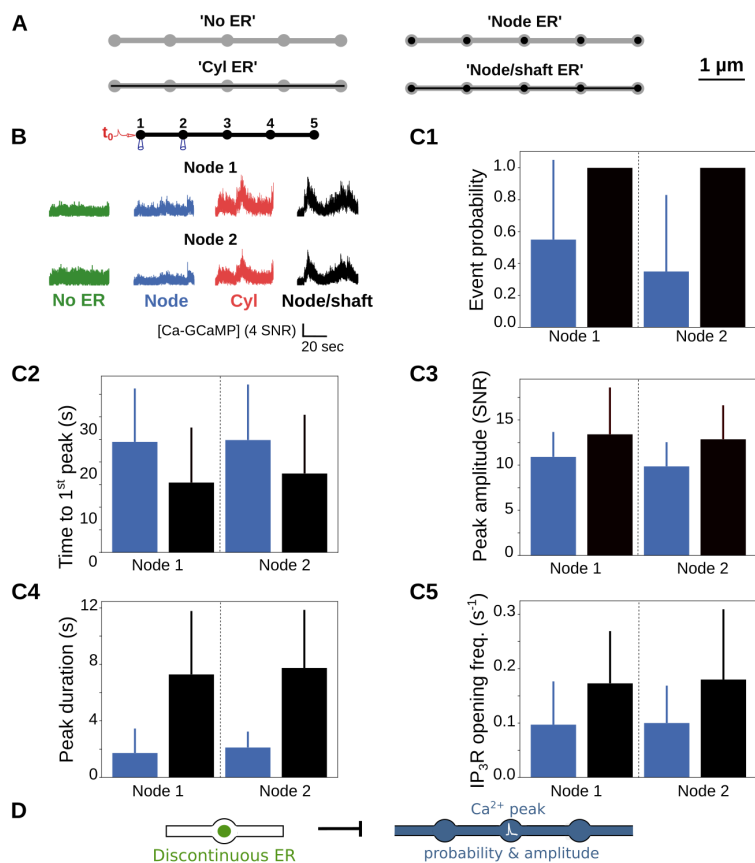


Fig 4: ER discontinuity is associated with decreased Ca^{2+} peak probability, amplitude and duration. (A) Simulations were performed in geometries with various ER geometries: “No ER”, “Node ER” and “Node/shaft ER”, in which there was no ER, discontinuous ER in nodes or nodes consisting in node/shaft alternations, respectively. (B) (Top) Neuronal stimulation protocol simulated for each geometry: Node 1 was stimulated at $t=t_0=1\text{s}$, while Ca^{2+} activity was monitored in nodes 1 and 2. (Bottom) Representative Ca^{2+} traces in nodes 1 and 2, in “No ER” (green), “Node ER” (blue) and “Node/shaft ER” (black) geometries, for $d_{\text{shaft}} = \frac{d_0}{2}$, expressed as SNR (see Methods). (C) Quantification of peak characteristics depending on ER geometry, $d_{\text{shaft}} = \frac{d_0}{2}$ (“Node ER” in blue and “Node/shaft” in black). (C1) Ca^{2+} peak probability is higher in geometries with continuous compared to discontinuous ER, both in node 1 and 2 (***). (C2) Time to 1st peak does not significantly change with ER geometry in Node 1 (p-value=0.59) but is higher in “Node/shaft ER” compared to “Node ER” geometry in Node 2 (p-value=0.04 *). (C3) Peak amplitude is increased in “Node/shaft ER” compared to “Node ER” geometry, both, both in nodes 1 and 2 (***). (C4) Peak duration is increased in “Node/shaft ER” compared to “Node ER” geometry, both in nodes 1 and 2 (***). (C5) The frequency of IP₃R opening is increased in “Node/shaft ER” compared to “Node ER” geometry, both in node 1 (p-value=0.01 *) and 2 (p-value=0.02 *). Ca^{2+} peak characteristics were not statistically different between node 1 and 2. (D) Schematic summarizing the conclusion of this figure: discontinuous ER geometry is associated with decreased Ca^{2+} peak probability and amplitude. Data are represented as mean \pm STD, n=20 for each geometry. Significance is assigned by * for $p \leq 0.05$, ** for $p \leq 0.01$, *** for $p \leq 0.001$.

289 Overall, our simulation results highlight the effect of both cellular and
290 ER geometry on Ca^{2+} peak amplitude and probability. A discontinuous
291 ER geometry is associated with a decreased peak probability, duration and
292 amplitude. Those results highlight the importance of investigating the ul-
293 trastructure of intracellular Ca^{2+} stores in live tissue, as it might strongly
294 influence local Ca^{2+} activity in the gliapil.
295

296 **Thin shafts favor more robust signal propagation**

297 A single astrocyte branchlet can be in close contact to multiple synapses
298 simultaneously [15, 27–29]. The frequency of stimulation of the branchlet
299 could vary depending on the activity of the adjacent synapses, so that a
300 connection of astrocytic nodes to co-active synapses would result in a high
301 node stimulation frequency. We have thus tested the influence of the fre-
302 quency of neuronal stimulation of neighboring nodes on the propagation
303 of Ca^{2+} signals in branchlets. In order to do so, we have performed sim-
304 ulations in which neighboring nodes were successively stimulated after a
305 time period τ_{IP3} , that varied from 50 ms to 5s (Fig 5A), while Ca^{2+} sig-
306 nals were recorded in a remote node (Node 5). Representative Ca^{2+} traces
307 in Node 5 depending on shaft width d_{shaft} and on τ_{IP3} are presented in
308 Fig 5A. Our first noticeable result is that the time to 1st peak in Node 5
309 decreases with d_{shaft} , whatever the value of τ_{IP3} (Fig 5B1). More specifi-
310 cally, time to 1st peak is higher for $d_{\text{shaft}}=d_0$ compared to both $d_{\text{shaft}}=\frac{d_0}{2}$
311 and $\frac{d_0}{3}$, while differences between $d_{\text{shaft}}=\frac{d_0}{2}$ and $\frac{d_0}{3}$ are not as striking.
312 Moreover, the difference between $d_{\text{shaft}}=d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$ increases with τ_{IP3} .
313 This suggests that geometries with $d_{\text{shaft}}=d_0$ better discriminate slow from
314 fast frequency of node stimulation compared to geometries with thinner
315 shafts. Geometries with $d_{\text{shaft}}=d_0$ are further characterized by a lower
316 Ca^{2+} peak probability in Node 5 compared to geometries with $d_{\text{shaft}}=\frac{d_0}{2}$
317 and $\frac{d_0}{3}$ (Fig 5B2). More precisely, Ca^{2+} peak probability decreases as τ_{IP3}
318 increases for $d_{\text{shaft}}=d_0$. This suggests that geometries with larger shafts
319 could be associated with decreased signal propagation to remote nodes in
320 case of successive node stimulation at low frequency ($\tau_{\text{IP3}} > 2\text{s}$). In order
321 to test the effect of our reflective boundary conditions, we have performed
322 the same stimulation protocol in geometries in which the tetrahedra near
323 the outer surface of Node 4 formed clamped boundary conditions (Supple-
324 mental Fig S11). The effect of d_{shaft} and of τ_{IP3} on Ca^{2+} peak probability
325 and on the delay of signal onset was similar to simulations with reflective
326 boundaries. Note that Ca^{2+} peak probability was lower and time to 1st
327 peak higher compared to simulations with reflective boundary conditions.
328

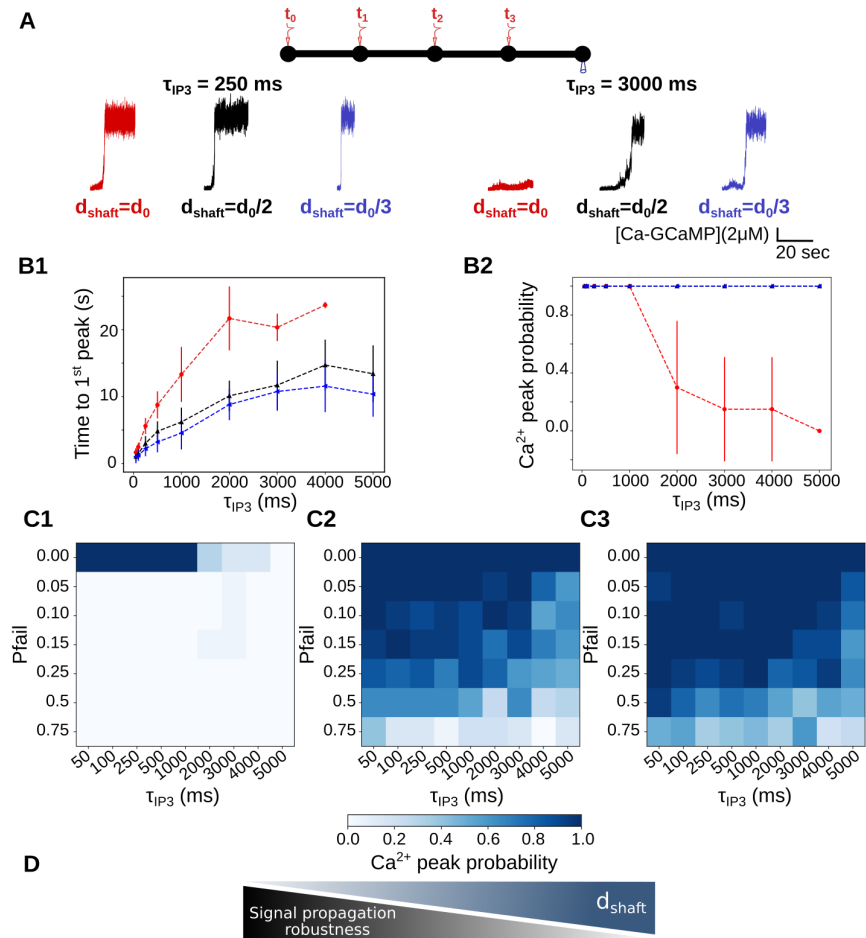


Fig 5: Thin shafts are associated with a more robust signal propagation upon successive neuronal stimuli. (A) (Top) Neuronal stimulation protocol: Node 1 is stimulated at $t=t_0=5s$, Node 2 at $t_0 + \tau_{IP3}$, Node 3 at $t_0 + 2\tau_{IP3}$ and Node 4 at $t_0 + 3\tau_{IP3}$. Ca^{2+} activity is recorded in Node 5. (Bottom) Representative Ca^{2+} traces in Node 5 for shaft width $d_{shaft} = d_0$ (red), $\frac{d_0}{2}$ (black) and $\frac{d_0}{3}$ (blue), with $\tau_{IP3}=250ms$ (left) and 3000ms (right), expressed as SNR (see Methods). (B1) Time to 1st peak increases with τ_{IP3} for $d_{shaft}=d_0$ (***) , $\frac{d_0}{2}$ (***) and $\frac{d_0}{3}$ (***) . T-tests revealed that for any value of τ_{IP3} , time to 1st peak is higher for $d_{shaft}=d_0$ compared to $d_{shaft}=\frac{d_0}{2}$ and $\frac{d_0}{3}$. Time to 1st peak is significantly higher when $d_{shaft}=\frac{d_0}{2}$ compared to $d_{shaft}=\frac{d_0}{3}$, for most values of τ_{IP3} ($p=0.032^*$, 0.0025^{**} , 0.034^* , 0.016^* and 0.019^* for $\tau_{IP3}=250, 500, 1000, 4000$ and 5000 , respectively). (B2) Ca^{2+} peak probability in Node 5 is lower for $d_{shaft}=d_0$ compared to $d_{shaft}=\frac{d_0}{2}$ and $\frac{d_0}{3}$. Ca^{2+} peak probability decreases as τ_{IP3} increases for $d_{shaft}=d_0$ (***) . (C) Ca^{2+} peak probability in Node 5 (colorbar) as a function of τ_{IP3} and of the probability of failure of node stimulation p_{fail} , for $d_{shaft}=d_0$ (C1), $d_{shaft}=\frac{d_0}{2}$ (C2) and $d_{shaft}=\frac{d_0}{3}$ (C3), with $p_{fail} \in [0, 1]$. (D) Schematic summarizing the main conclusion of this figure: decreased shaft width allows signal propagation despite omitted node stimulation, thus favoring more robust signal propagation. Data are represented as mean \pm STD, $n=20$ for each value of d_{shaft} and of τ_{IP3} . Lines in panel B are guides for the eyes. The effect of d_{shaft} on each Ca^{2+} signal characteristic was tested using one-way ANOVA. Significance is assigned by * for $p \leq 0.05$, ** for $p \leq 0.01$, *** for $p \leq 0.001$.

329 For $\tau_{IP_3}=4s$ and $d_{shaft}=\frac{d_0}{3}$, signals were detected in Node 5 $11.55 \pm$
330 3.89 s after the stimulation of Node 1, which means that they occurred
331 before the stimulation of Node 4 ($t=t_0 + 12s$ for $\tau_{IP_3}=4s$). This phe-
332 nomenon was not observed for $d_{shaft}=d_0$, for which time to 1st peak when
333 $\tau_{IP_3}=4s$ was 23.67 ± 0.47 s. This suggests that for $d_{shaft}=\frac{d_0}{3}$, contrary
334 to $d_{shaft}=d_0$, one node stimulation could be omitted without having any
335 consequence on Ca^{2+} peak probability in Node 5. In order to test this hy-
336 pothesis, we have performed simulations in which the stimulation of Nodes
337 2, 3 and 4 occurred with a given probability of failure p_{fail} . Simulations
338 were performed for $p_{fail}=0, 0.05, 0.1, 0.15, 0.25$ and 0.75 . Ca^{2+} peak prob-
339 ability in Node 5, depending on p_{fail} and on τ_{IP_3} is presented in Fig 5C, for
340 $d_{shaft}=d_0$ (Fig 5C1), $d_{shaft}=\frac{d_0}{2}$ (Fig 5C2) and $d_{shaft}=\frac{d_0}{3}$ (Fig 5C3). As ex-
341 pected, Ca^{2+} peak probability, despite high values of p_{fail} , increases when
342 d_{shaft} decreases. Thus, thin shafts can favor signal propagation by allowing
343 the omission of a node stimulation. In that sense, geometries displaying
344 thin shafts are characterized by a more robust signal propagation (Fig 5D).

345
346 Together, our results suggest that, in the context of successive node
347 stimulation, thin shafts are associated with an increase of Ca^{2+} peak prob-
348 ability in more remote nodes, with a lower delay of signal onset, suggest-
349 ing an increased signal propagation. Geometries with thick shafts (here
350 $d_{shaft}=d_0$) are associated with lower signal propagation in case of low stim-
351 ulation frequency (time period $> 2s$), potentially favoring the formation of
352 local Ca^{2+} hotspots. Our results further suggest that geometries with thick
353 shafts could impair signal propagation when a branchlet is stimulated by
354 different neuronal populations. In that sense, astrocyte branchlets with
355 thick shafts would be better detectors of the surrounding neuronal stimuli.
356 On the contrary, branchlets with thin shafts would allow less discriminating
357 and more robust signal propagation events.

358 Ca^{2+} indicators alter Ca^{2+} peak characteristics

359 In order to measure Ca^{2+} signals, experiments rely on the use of Ca^{2+}
360 indicators, such as GCaMP, which correspond to molecules that fluoresce
361 when bound to Ca^{2+} . The variations of fluorescence with time are moni-
362 tored and normalized over the basal level of fluorescence ($\Delta F/F_0$). Those
363 methods thus do not measure the exact variations of free Ca^{2+} concentra-
364 tion [Ca^{2+}] but the variations of the concentration of Ca^{2+} bound to the
365 indicator, here [Ca-GCaMP]. The resulting signal strongly depends on the
366 concentration and kinetics of the indicator [20].

367 Here, in order to investigate the effect of d_{shaft} on free Ca^{2+} signals rather
368 than on signals mediated by GCaMP, we have performed simulations in
369 which no GCaMP molecules were added in the cytosol. Free Ca^{2+} dynam-
370 ics was then monitored in node 1, while stimulating node 1 (Fig 6A). Free
371 Ca^{2+} signals were qualitatively (Fig 6A) and quantitatively (Fig 6B) differ-
372 ent from Ca-GCaMP signals. No effect of d_{shaft} was observed on free Ca^{2+}
373 peak probability (Fig 6B1). Similarly to Ca-GCaMP signals, time to 1st
374 peak decreased (Fig 6B2), IP_3R opening frequency (Fig 6B5), free Ca^{2+}
375 peak amplitude (Fig 6B3) and duration (Fig 6B4) increased when d_{shaft}
376 decreased. Consistently with previous reports [20,30,31], free Ca^{2+} signals
377 strongly differed from Ca-GCaMP signals. More precisely, free Ca^{2+} sig-
378 nals were characterized by a higher peak amplitude and frequency of IP_3R
379 opening as well as a lower peak duration and delay of peak onset than

380 Ca-GCaMP signals.

381 Overall, our results suggest that the use of Ca^{2+} indicators, and more
382 generally Ca^{2+} buffering, is associated with an increased Ca^{2+} peak dura-
383 tion and a decreased peak probability and amplitude (Fig 6D). Note that,
384 even though free Ca^{2+} signals strongly differ from Ca-GCaMP signals,
385 Ca-GCaMP signals can still provide relevant information on the qualita-
386 tive effect of shaft width on Ca^{2+} dynamics, such as the increased peak
387 probability, duration and amplitude when d_{shaft} decreases. As it is cur-
388 rently impossible to measure free Ca^{2+} signals experimentally, our study
389 highlights the importance of using computational tools for improving our
390 understanding of Ca^{2+} signals.

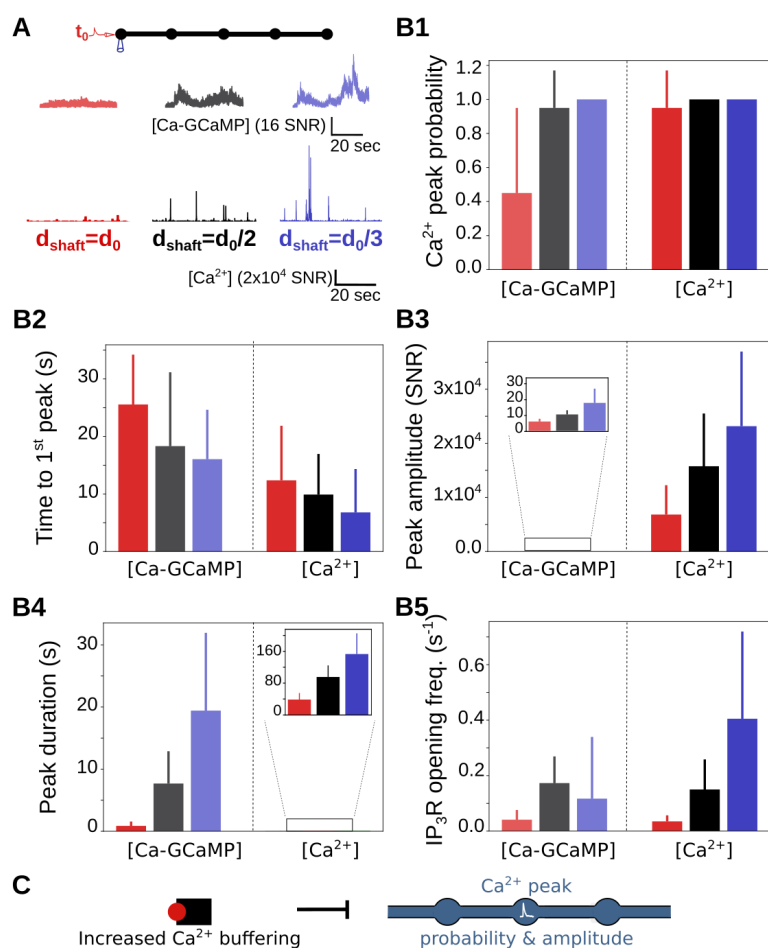


Fig 6: Ca^{2+} indicators alter Ca^{2+} peak probability, duration and amplitude. (A) In order to investigate free Ca^{2+} peak probability, no GCaMP molecules were added to the model. (Top) At $t=t_0=1\text{s}$, Node 1 was stimulated while Ca^{2+} concentration was monitored in node 1. (Middle) Representative Ca-GCaMP traces in node 1, in simulations containing GCaMP molecules in geometries with shaft width $d_{\text{shaft}} = d_0$ (light red), $\frac{d_0}{2}$ (grey) and $\frac{d_0}{3}$ (light blue). (Bottom) Representative free Ca^{2+} traces in node 1, in the absence of GCaMP molecules, in geometries with shaft width $d_{\text{shaft}} = d_0$ (red), $\frac{d_0}{2}$ (black) and $\frac{d_0}{3}$ (blue). The amplitude of Ca-GCaMP and free Ca^{2+} signals is expressed as SNR (see Methods). (B) Characteristics of free Ca^{2+} signals depending on d_{shaft} . Ca-GCaMP signals measured in simulations from Fig 3 are presented for comparison. (B1) Free Ca^{2+} peak probability does not vary with d_{shaft} (p-value=0.22). Ca-GCaMP peak probability is lower than free Ca^{2+} peak probability for $d_{\text{shaft}} = d_0$ (***). (B2) Time to 1st free Ca^{2+} peak increases with d_{shaft} (***). Time to 1st Ca-GCaMP peak is higher than time to 1st free Ca^{2+} peak, for any value of d_{shaft} (***). (B3) Free Ca^{2+} peak amplitude increases when d_{shaft} decreases (***). Ca-GCaMP peak amplitude is lower than free Ca^{2+} peak amplitude, for any value of d_{shaft} (***). (B4) Free Ca^{2+} peak duration increases when d_{shaft} decreases (***). Ca-GCaMP peak duration is higher than free Ca^{2+} peak duration, for any value of d_{shaft} (***). (B5) The frequency of IP_3R opening increases when d_{shaft} decreases (***). (C) Schematic summarizing the main result from this figure: increased Ca^{2+} buffering is associated with decreased Ca^{2+} peak probability and amplitude. Data are represented as mean \pm STD, $n=20$ for each geometry. The effect of d_{shaft} on each free Ca^{2+} signal characteristic was tested using one-way ANOVA. Significance is assigned by * for $p \leq 0.05$, ** for $p \leq 0.01$, *** for $p \leq 0.001$.

391 Discussion

392 This study outlines the effect of the nanoscale morphology of astrocyte
393 branchlets on the characteristics of Ca^{2+} signals. More precisely, the
394 reticular morphology of branchlets, alternating between large and thinner
395 cellular compartments [15,19,21], seems to increase Ca^{2+} peak probability,
396 duration, amplitude and propagation (Fig 7A). We further propose plausible
397 mechanisms that are associated with a decreased local Ca^{2+} activity:
398 an increased shaft width, discontinuous ER geometry and increased Ca^{2+}
399 buffering (Fig 7B). Our results, in accordance with experimental data, sug-
400 gest that thin shafts are associated with a decreased diffusion flux, i.e an
401 increased compartmentalization of nodes. Thus, nodes, similarly to den-
402 dritic spines [25], act as diffusion traps when shaft width is low. Note that,
403 more than the value of shaft width itself, our results emphasize the effect
404 of the ratio between node and shaft diameter on Ca^{2+} activity. The ge-
405 ometries designed and used in this study, based on recent super-resolution
406 images of the gliapil [15], emerge as interesting tools to investigate the in-
407 fluence of the ultrastructure of fine astrocyte branchlets on the local Ca^{2+}
408 dynamics. By recording Ca^{2+} activity upon neuronal stimulation in small
409 cellular compartments of the gliapil, which cannot be performed experi-
410 mentally, our simulation results shed light on the mechanisms by which
411 astrocyte morphology influences the frequency, amplitude and propagation
412 of Ca^{2+} signals at the nanoscale.

413

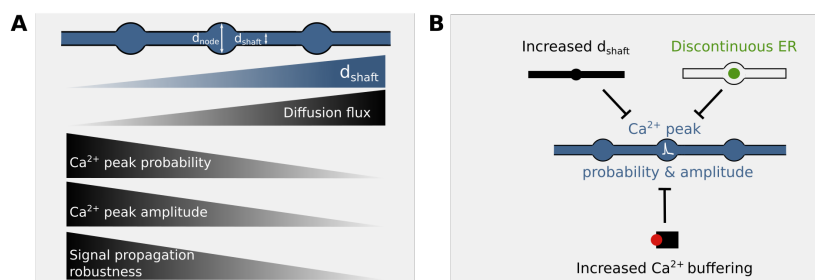


Fig 7: **Proposed mechanisms that regulate astrocytic Ca^{2+} activity at tripartite synapses.** (A) Proposed effects of shaft width d_{shaft} on Ca^{2+} signals. A decreased shaft width results in a decreased diffusion flux of molecules from nodes. This results in an increase of Ca^{2+} peak probability, amplitude and duration in the stimulated node. Finally, thinner shafts allow signal propagation despite omitted node stimulation upon successive stimuli, thus allowing more robust signal propagation. (B) Proposed mechanisms that decrease Ca^{2+} peak probability and amplitude: an increased shaft width d_{shaft} , a discontinuous ER geometry and an increased Ca^{2+} buffering.

414 Experimental Ca^{2+} recordings of astrocyte activity suggest that as-
415 trocyte branchlets display both highly localized microdomain signals and
416 propagating Ca^{2+} waves [5,9]. Our simulations suggest that the morphol-
417 ogy of the cell and of its organelles can influence the formation of those
418 diverse spatio-temporal properties. Notably, thinner shafts allow less dis-
419 criminating and more robust signal propagation upon successive stimuli

420 compared to larger shafts. Thinner shafts indeed allow signal propagation
421 despite the omission of some stimuli or when the time interval between
422 successive stimuli is large. On the contrary, geometries with thick shafts
423 seem to be more discriminating, potentially favoring the propagation of
424 signals resulting from successive stimuli from co-active synapses. Cellular
425 morphology thus emerges as a key parameter that regulates the active prop-
426 agation of Ca^{2+} signals. Further quantification is required to better charac-
427 terize the inter- and intra-cellular variability of the ultrastructure of astro-
428 cyte branchlets and of its connectivity to the neighboring synapses. This
429 will be crucial to better understand the integration of signals within astro-
430 cytes and how specialized their communication with individual synapses is.

431
432 In neurons, both experimental [32–34] and modelling [25, 35–41] stud-
433 ies have suggested that spine morphology, more precisely thin neck width,
434 favors the compartmentalization of Ca^{2+} signals within single spine heads.
435 It has been proposed that the presence of small compartments, such as
436 astrocyte nodes and spine heads, enables a 2 orders of magnitude faster
437 homogenization of the concentration of second messengers, such as Ca^{2+} ,
438 compared to larger compartments [32]. According to our simulation re-
439 sults, nodes connected to thin shafts could favor the emergence of large
440 signals at the site of neuron-astrocyte communication. Interestingly, we
441 further propose that those amplified signals in nodes, instead of resulting
442 in Ca^{2+} hotspots, favor active signal propagation. In response to spike
443 timing-dependent plasticity (STDP) protocols [42] and after long-term po-
444 tentiation [34], the neck of dendritic spines become wider and shorter.
445 Recent *in vitro* and *in vivo* studies have reported that the geometry of the
446 ER in neurons is also highly dynamic [43], experiencing fast fission and
447 fusion events. The geometries of dendrites and of their organelles, which
448 influence local signals, are thus highly dynamic. Further, the ER is variably
449 distributed in spines, being preferentially present in large spines associated
450 with strong synapses [44]. The variability of the geometry of astrocyte
451 branchlets and of their organelles depending on physiological conditions
452 remains to be uncovered and, according to our results, could strongly im-
453 pact Ca^{2+} dynamics.

454
455 Genetically encoded Ca^{2+} indicators (GECI) have been used exten-
456 sively to investigate Ca^{2+} dynamics in astrocytes. They are presently the
457 best tools for detecting Ca^{2+} signals in the whole astrocyte territory, in-
458 cluding the very fine distal branchlets, while bulk-loading of Ca^{2+} indica-
459 tors can only report signals in the soma and major branches, leaving $\approx 90\%$
460 of astrocyte area unsampled [10, 45]. Furthermore, using GECIs avoids the
461 risk of altered cell physiology associated with bulk-loading [46] and can be
462 used to image Ca^{2+} signals *in vivo* [5, 9, 10, 14, 47]. GECIs however present
463 a major drawback: as they are genetically encoded, their exact concen-
464 tration and distribution within the cell is unknown and thus generally
465 not reported. Our results, in agreement with previous reports [20, 48, 49],
466 highlight the modulation of Ca^{2+} signals by Ca^{2+} buffers such as GECIs.
467 Interestingly, the increased Ca^{2+} peak probability, duration and ampli-
468 tude of Ca-GCaMP peaks when d_{shaft} decreases was still observed for free
469 Ca^{2+} signals. As the concentration of GCaMP, $[\text{GCaMP}]$, can influence
470 the size of Ca-GCaMP peaks [20], we have tested the sensitivity of our
471 results to $[\text{GCaMP}]$ (Supplemental Fig S12). The amplitude and duration
472 of Ca-GCaMP signals varied with $[\text{GCaMP}]$, in accordance with previous

473 reports [20]. Importantly, the increase of peak amplitude and duration as
474 well as the decrease of time to 1st peak when d_{shaft} decreases was observed
475 for all tested values of [GCaMP]. This study highlights the importance of
476 computational tools to investigate free Ca^{2+} signals and to quantify the
477 effect of Ca^{2+} indicators on signal readout.

478
479 Overall, our simulations illustrate how the morphology of fine astro-
480 cyte branchlets, notably shaft width, and of their organelles influence local
481 Ca^{2+} activity. Importantly, this study highlights the counter-intuitive sig-
482 nal amplification in compartmentalized nodes, resulting from a reduced
483 diffusion flux from nodes connected to thin shafts. This study provides
484 a better understanding of the mechanisms that govern Ca^{2+} dynamics in
485 small volumes, which is notably crucial for disentangling neuron-astrocyte
486 communication at tripartite synapses.

487 Methods

488 Stochastic spatially-explicit voxel-based simulations

489 In order to model astrocyte Ca^{2+} signals in astrocyte branchlets, we
490 have used the voxel-based “GCaMP” implementation of the Inositol 3-
491 Phosphate (IP_3) receptor-dependent Ca^{2+} signaling model from Denizot
492 et al [20], using the same reaction scheme and parameter values (Fig 1B).
493 Briefly, we model Ca^{2+} fluxes in and out of the cytosol, mediated by Ca^{2+}
494 channels and pumps on the endoplasmic reticulum (ER) and on the plasma
495 membrane. Ca^{2+} signals occur when some IP_3R channels are in the open
496 state. IP_3 can be synthesized by the Ca^{2+} -dependent activity of phospho-
497 lipase C δ ($\text{PLC}\delta$) and the removal of IP_3 molecules from the cytosol is
498 expressed as a single decay rate. IP_3R kinetics is described by a Markov
499 model, derived from De Young & Keizer’s model [23]. Each IP_3R molecule
500 contains one IP_3 binding site and two Ca^{2+} binding sites. An IP_3R is in
501 the open state when in state {110} (first Ca site and IP_3 bound, second
502 Ca site free). Depending on the simulation, other diffusing molecules were
503 added to the model, such as the fluorescent molecule ZSGreen and fluores-
504 cent Ca^{2+} indicators, here $10\ \mu\text{M}$ of GCaMP6s. GCaMPs are genetically-
505 encoded Ca^{2+} indicators (GECIs) that are derived from the fluorescent
506 protein GFP and the Ca^{2+} buffer calmodulin (see [50] for a review on
507 GECIs). For further details on the kinetic scheme and model assumptions,
508 please refer to Denizot et al. 2019 [20].

509
510 The model was implemented using STEPS (<http://steps.sourceforge.net/>),
511 a python package performing exact stochastic simulation of reaction-diffusion
512 systems [51]. More precisely, STEPS uses a spatialized implementation of
513 Gillespie’s SSA algorithm [52–54]. Simulations in STEPS can be performed
514 in complex geometries in 3 spatial dimensions. Space is divided into well-
515 mixed tetrahedral compartments, referred to as voxels. Reactions between
516 2 molecules can only occur if they are located within the same voxel. Dif-
517 fusion events are modeled as a decrease of the number of molecules in the
518 original voxel and an increase in the number of molecules in its neighboring
519 voxel. Boundary conditions, except when specified otherwise, were reflect-
520 ive. STEPS enables to compute, in complex 3D geometries, reactions and
521 diffusion in the cytosol as well as reactions between cytosolic molecules and
522 molecules located at the plasma or ER membrane.

523

524 Geometries

525 Typical astrocyte branchlet geometries were designed from their recent
526 experimental characterization in live tissue at high spatial resolution (50
527 nm in x-y) [15]. Those geometries consist in alternations of bulbous struc-
528 tures, nodes, connected to each other with cylindrical structures, shafts.
529 Geometries with different shaft widths d_{shaft} were designed using Trelis soft-
530 ware (<https://www.csimsoft.com/trelis>, Fig 1A). The geometry of a node
531 was approximated as being a sphere of diameter 380 nm. Shaft geome-
532 try consisted in a $1\mu\text{m}$ long cylinder. Shaft diameter was defined relative
533 to node diameter. For example, shaft diameter was the same as node
534 diameter, i.e $d_{\text{shaft}}=d_0=380$ nm. Similarly, shaft diameter was 190 nm
535 and 127 nm for $d_{\text{shaft}}=\frac{d_0}{2}$ and $\frac{d_0}{3}$, respectively. Cones were positioned
536 between spheres and cylinders in order to create a smoother transition
537 between nodes and shafts, better approximating the geometry observed
538 experimentally. Cytosolic volume was thus $V_1=0.620\mu\text{m}^3$, $V_2=0.263\mu\text{m}^3$
539 and $V_3=0.195\mu\text{m}^3$, for $d_{\text{shaft}}=d_0$, $\frac{d_0}{2}$ and $\frac{d_0}{3}$, respectively. A subset of sim-
540 ulations were performed in a geometry with $V_1=0.258\mu\text{m}^3$. This geometry
541 is characterized, similarly to geometries with $d_{\text{shaft}}=d_0$, by a node/shaft
542 width ratio of 1. It contains cylinders of length 750 nm, diameter 285 nm
543 and spheres of diameter 285 nm. As a first approximation, ER geometry
544 was considered to be identical to the geometry of the astrocyte branchlet:
545 node/shaft successions. ER nodes were aligned with cytosolic nodes. As
546 no quantification of the ER volume compared to cellular volume was found
547 for astrocytes in the literature, ER volume was 10% of the total branchlet
548 volume, based on available data in neurons [55]. The cytosolic volume,
549 plasma and ER membrane areas of the different “5Nodes” geometries are
550 presented in Table 1.

551 In a subset of simulations, ER geometry varied. The shape of the cell
552 was the same as in “5nodes” geometries (Fig 1). ER geometry consisting
553 of node/shaft alternations, described above, is referred to as “Node/shaft
554 ER”. “No ER” geometry contains no ER. “Node ER” is characterized by
555 a discontinuous ER geometry, consisting in spheres of diameter 54 nm,
556 located in cellular nodes. “Cyl ER” corresponds to a cylindrical ER, of
557 length $l_{\text{ER}}=6274$ nm and a diameter of 108, 54 and 36 nm, for $d_{\text{shaft}}=d_0$,
558 $\frac{d_0}{2}$ and $\frac{d_0}{3}$, respectively. The associated cytosolic volume, ER and plasma
559 membrane area are presented in Table 1.

560 Protocol for simulating bleaching experiments

561 In order to test whether the idealized geometries presented in Fig 1 are a
562 good approximation of the spongiform ultrastructure of astrocyte branch-
563 lets, we have simulated their fluorescence recovery after photobleaching
564 (FRAP) experiments. The principle of those experiments is summarized
565 in Supplemental Fig S3A. Briefly, laser pulses are simulated on a node (re-
566 gion of interest) while the fluorescence level is being recorded. At bleaching
567 time, the fluorescence level in the region of interest decreases to I_0 . Then,
568 because of the diffusion of fluorescent molecules into the region of inter-
569 est, fluorescence increases until it reaches a new steady state, I_{inf} . We
570 characterize node compartmentalization by measuring the time τ taken by
571 fluorescing molecules to diffuse into the node to reach I_{inf} . In other words,

572 a high node compartmentalization will be associated with a high value of
573 τ . Thus, 3 main parameters characterize bleaching traces: I_0 , τ and I_{inf} .

574
575 To mimic bleaching experiments in fine branchlets performed by Ari-
576 zono et al [15], ZSGreen molecules were added to simulation space. After
577 2 seconds of simulation, providing the basal level of fluorescence, 60% of
578 ZSGreen molecules were bleached. In order to fit I_0 and I_{inf} that were mea-
579 sured experimentally, and as bleaching time lasted 10 ms in experiments
580 and 1 ms in simulations, the bleached volume in simulations was adjusted
581 depending on the geometry (see Fig 2A). Bleaching was simulated as a tran-
582 sition from ZSGreen molecules to ZSGreen-bleached molecules, the latter
583 being considered as non-fluorescing molecules. Screenshots of simulations,
584 illustrating the diffusion of ZSGreen and ZSGreen-bleached molecules, are
585 presented in Fig S2B. The number of ZSGreen molecules in the central
586 node was recorded over simulation time and a fit was performed following
587 equation 1 to determine the values of I_0 , I_{inf} and τ .

$$I(t) = I_0 - (I_0 - I_{\text{inf}})e^{-t/\tau} \quad (1)$$

588 , where $I(t)$ is the level of fluorescence measured at time t . The coeffi-
589 cient of diffusion, D_{ZSGreen} , and the concentration, $[\text{ZSGreen}]$, of ZSGreen
590 were adjusted to fit experimental data. Indeed, the amplitude of $[\text{ZSGreen}]$
591 fluctuations at steady state is inversely proportional to the number of ZS-
592 Green molecules in the geometry. In other words, fluorescence signals are
593 more noisy when $[\text{ZSGreen}]$ is low. Moreover, the autocorrelation of those
594 fluctuations depends on the coefficient of diffusion of ZSGreen, D_{ZSGreen} .
595 If D_{ZSGreen} increases, the autocorrelation of Lag, where Lag is the au-
596 tocorrelation delay, will decrease faster as Lag increases. Comparing the
597 fluctuations of $[\text{ZSGreen}]$ and its autocorrelation in experiments and in sim-
598 ulations thus enabled to find the values of D_{ZSGreen} and of $[\text{ZSGreen}]$ that
599 allowed for the best fit to experimental data. In the simulations presented
600 here, $D_{\text{ZSGreen}}=90 \mu\text{m}^2 \cdot \text{s}^{-1}$ and $[\text{ZSGreen}]=25 \mu\text{M}$.

601 Protocols for simulating neuronal stimulation

602 In order to investigate the propagation of Ca^{2+} signals from nodes that
603 contact neuronal spines, we have developed 2 different protocols for our
604 simulations, performed in the geometries presented in Fig 1. As nodes
605 were the site of Ca^{2+} signal initiation [15] and as most spines contacted
606 nodes rather than shafts, we have simulated neuronal stimulation in nodes.

- 607
608 • In the first protocol, 100 IP_3 molecules were infused in Node 1, at
609 $t=t_0=1\text{s}$, while Ca^{2+} activity was monitored in Node 1 and in the
610 neighboring node, Node 2 (see e.g Fig 3A). Simulations were per-
611 formed in geometries with varying shaft width d_{shaft} .
- 612 • In the second protocol, we have investigated signal propagation in
613 the node/shaft geometry depending on shaft width d_{shaft} when sev-
614 eral nodes were successively stimulated. In “5nodes” geometries, 50
615 IP_3 molecules were infused at $t_0=5\text{s}$, $t_0 + \tau_{\text{IP}_3}$, $t_0 + 2\tau_{\text{IP}_3}$, $t_0 + 3\tau_{\text{IP}_3}$ in
616 Nodes 1, 2, 3 and 4, respectively. During the whole simulation time,
617 Ca^{2+} activity was recorded in Node 5 (see Fig 5). In a subset of sim-
618 ulations, stimulation of Nodes 2, 3 and 4 occurred with a probability
619 $1 - p_{\text{fail}}$, with $p_{\text{fail}} \in [0, 1]$.

620 Peak detection and analysis

621 The same strategy as developed by Denizot et al. [20] was used for de-
622 tecting and analysing Ca^{2+} signals. Briefly, basal concentration of Ca^{2+} ,
623 $[Ca]_b$, was defined based on a histogram of the number of Ca^{2+} ions in
624 the absence of neuronal stimulation. Peak initiation corresponded to the
625 time when $[Ca^{2+}]$ was higher than the following threshold: $[Ca]_b + n\sigma_{Ca}$,
626 where σ_{Ca} is the standard deviation of $[Ca^{2+}]$ histogram in the absence
627 of neuronal stimulation. The value of n was set by hand depending on
628 signal/noise ratio of the simulation of interest. Peak termination corre-
629 sponded to the time when $[Ca^{2+}]$ decreased below the peak threshold.
630 Several parameters were analyzed to characterize Ca^{2+} signals. Peak am-
631 plitude, A , corresponds to the maximum $[Ca^{2+}]$ measured during the peak
632 duration. It is expressed as signal to noise ratio $SNR = \frac{A - [Ca]_b}{[Ca]_b}$. Peak
633 duration corresponds to the time between peak initiation and peak termi-
634 nation. Time to 1st peak corresponds to the delay between the beginning
635 of the simulation and the first peak detection, measured in the cellular
636 compartment of interest. Peak probability corresponds to the fraction of
637 simulations in which at least one peak was detected during simulation time
638 in the region of interest. Ca^{2+} residency time was measured by performing
639 $n=300$ simulations for each value of d_{shaft} , in which only 1 Ca^{2+} ion was
640 added to node 1, without other molecular species. Ca^{2+} residency time
641 corresponds to the time taken for the ion to diffuse away from node 1.

642 Statistical analysis

643 For each parameter set, 20 simulations, with different seeds, were gener-
644 ated. Each parameter describing Ca^{2+} dynamics was expressed as mean
645 \pm standard deviation. The effect of d_{shaft} on each Ca^{2+} signal characteris-
646 tic was tested using one-way ANOVA. Comparison between two different
647 conditions was performed using unpaired Student T-test if values followed
648 a Gaussian distribution, Mann-Whitney test otherwise. Significance is as-
649 signed by * for $p \leq 0.05$, ** for $p \leq 0.01$, *** for $p \leq 0.001$.

650 Simulation code

651 The simulation code, implemented with STEPS 3.5.0, and the meshes
652 are available on ModelDB [56] at <http://modeldb.yale.edu/266928>, access
653 code: lto42@tpk3D?. The original model from Denizot et al. [20] is avail-
654 able at <http://modeldb.yale.edu/247694>.

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868 **Competing Interests statement**

869 The authors declare no competing financial interests.