Activity-mediated accumulation of potassium induces a switch in firing pattern and neuronal excitability type

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Abstract

During normal neuronal activity, ionic concentration gradients across a neuron's membrane are often assumed to be stable. Prolonged spiking activity, however, can reduce transmembrane gradients and affect voltage dynamics. Based on mathematical modeling, we here investigate the impact of neuronal activity on ionic concentrations and, consequently, the dynamics of action potential generation. We find that intense spiking activity on the order of a second suffices to induce changes in ionic reversal potentials and to consistently induce a switch from a regular to an intermittent firing mode. This transition is caused by a qualitative alteration in the system's voltage dynamics, mathematically corresponding to a co-dimension-two bifurcation from a saddle-node on invariant cycle (SNIC) to a homoclinic orbit bifurcation (HOM). Our electrophysiological recordings in mouse cortical pyramidal neurons confirm the changes in action potential dynamics predicted by the models: (i) activity-dependent increases in intracellular sodium concentration directly reduce action potential amplitudes, an effect that previously had been attributed soley to sodium channel inactivation; (ii) extracellular potassium accumulation switches action potential generation from tonic firing to intermittently interrupted output. Individual neurons thus may respond very differently to the same input stimuli, depending on their recent patterns of activity or the current brain-state.

Author summary

Ionic concentrations in the brain are not constant. We show that during intense neuronal activity, they can change on the order of seconds and even switch neuronal spiking patterns under identical stimulation from a regular firing mode to an intermittently interrupted one. Triggered by an accumulation of extracellular potassium, such a transition is caused by a specific, qualitative change in of the neuronal voltage dynamics – a so-called bifurcation – which affects crucial features of action-potential generation and bears consequences for how information is encoded and how neurons behave together in the network. Also changes in intracellular sodium can induce measurable effects, like a shrinkage of spike amplitude that occurs independently of the fast amplitude-effects attributed to sodium channel inactivation. Taken together, our results demonstrate that a neuron can respond very differently to the same stimulus, depending on its previous activity or the current brain state. The finding is particularly relevant when other regulatory mechanisms of ionic homeostasis are challenged, for example, during pathological states of glial impairment or oxygen deprivation. Categorization of cortical neurons as intrinsically bursting or regular spiking may be biased by the ionic concentrations at the time of the observation, highlighting the non-static nature of neuronal dynamics.

Introduction

Ever since the introduction of Hodgkin-Huxley's famous neuron model for the squid giant axon, the governing equations have been a useful tool to understand the mechanisms of spike generation. The original model assumed fixed ionic concentrations inside and outside the cell, establishing constant driving forces for ionic flux otherwise modulated only by the channels' gating kinetics [1]. In the brain, however, ionic concentrations are not constant, and the ionic composition of the extracellular space varies with behavioral states [2, 3] and as a function of neuronal activity [4, 5].

The concentrations of sodium $[Na^+]$ and potassium $[K^+]$ ions – the two ionic species essential for sodium action potentials – are known to vary in response to neuronal activity *in vitro* and *in vivo* at relatively slow timescales (on the order of seconds). Intracellular sodium concentration has been found to increase with activity in mammalian pyramidal neurons responding to physiologically relevant stimuli (on the order of 3-10 seconds) [5]. For example, in cat neocortex, the concentration of extracellular potassium can oscillate in correlation with local field potentials (LFPs) during slow wave $(\sim 1 \text{ Hz})$ sleep [3] or when presenting oscillating graded stimuli to the cat's retina on the order of seconds [4]. Nevertheless, how stimulus-induced changes in ionic concentration gradients impact ongoing neuronal activity is currently not well understood.

In this study, we use conductance-based models to predict and experimentally test how changes in transmembrane ionic concentration gradients that arise during periods of increased neuronal activity impact action-potential generation. We find that prolonged stimulation (~10 seconds) can generate ionic concentration changes substantial enough to modify action potential generation in neurons. Intracellular sodium accumulation, in particular, alters action-potential amplitude on slow timescales matching the ionic changes – an effect previously primarily attributed to the inactivation of sodium channels [6–8].

Extracellular potassium accumulation, in turn, can qualitatively switch the spike-generating 24 mechanism, thus changing fundamental properties of firing patterns, encoding, and network behaviour. Mathematically, the transition corresponds to a so-called co-dimension-two bifurcation, at which the spike generating mechanism changes qualitatively from a regular saddle-node on invariant 27 cycle (SNIC), when extracellular potassium concentrations are low, to a homoclinic orbit bifurcation (HOM), when extracellular potassium concentrations become high. The switch in the firing regime 29 most notably results in a transition from regular spiking to a burst-like, intermittently interrupted firing mode in the HOM regime, caused by a so-called bistability of the dynamical system. In the 31 HOM regime, the options of a fixed, resting-like voltage state and regular firing co-exist for the same 32 input levels, resulting in stimulus- and noise-induced switches between both states. 33

Prolonged electrical activity can, therefore, have significant effects on spiking patterns and neuronal dynamics. We uncover these properties by, first, dissecting both potassium ion and sodium ion contributions to spike generation and, second, testing predictions in *in vitro* electrophysiological recordings.

Results

Model response to prolonged stimuli

In order to analyze how neurons respond to prolonged stimulation, we examined the temporal 40 evolution of activity-dependent changes in transmembrane ionic gradients and assessed their impact 41 on ongoing neuronal activity. To this end, we implemented a single-neuron, conductance-based 42 model including dynamic ion concentrations (detailed in Methods). Ionic gradients determine the equilibrium (Nernst) potentials that, in turn, influence the driving forces of spike-generating ionic currents. Accumulation of ions over time, consequently, modifies the Nernst potentials as well as the spike generating currents and, therefore, also spike generation. A regulation of concentration gradients ($[Na^+]$ and $[K^+]$) is mediated by the Na-K-ATPase pump: an electrogenic active-transporter whose activity intensifies when $[Na^+]_i$ accumulates. Due to its electrogenic nature (changing the net charges across the membrane), activity of the Na-K-ATPase pump affects the membrane potential.

Noise-free analysis

First, we investigated the response of the model to a step input current - a typical protocol in patch-clamp experiments. Stimulation of the model for almost 10 seconds (Fig. 1A) led to an accumulation of intracellular sodium, $[Na^+]_i$, as well as an increase in extracellular potassium, $[K^+]_o$ (Fig. 1B). The concentration changes resulted from the prolonged spiking activity and were indeed substantial enough to alter features of the generated action potentials during the duration of the stimulation protocol. Three major changes that have often been reported in experiments were observed in the model: (a) the emergence of a slow after-hyperpolarization (AHP), (b) adaptation (i.e., a reduction) of spike frequency, and (c) reduction of spike amplitudes (Fig. 1A).

a) The slow AHP became visible when the stimulus was set back to baseline and neuronal spiking stopped (Fig. 1A). The slow AHP resulted from the hyperpolarising Na-K-ATPase pump current: Na-K-ATPase pump activity was enhanced with the action-potential-driven rise in intracellular sodium concentration, because $[Na^+]_i$ accumulation, increases the pump activity. When the stimulation ended, the neuron stopped firing and the membrane potential hyperpolarized with respect to the original resting membrane potential (due to the transient change in the Na-K-ATPase pump current). As ongoing Na-K-ATPase activity progressively lowered the intracellular sodium concentration back to baseline levels, the hyperpolarization slowly diminished (Fig. 1A).

b) Spike frequency adaptation, evident in Fig. 1A, also resulted from the activity-dependent increase in Na-K-ATPase current, which effectively reduced the net excitatory drive of the neuron. The model does not contain adaptation currents besides the Na-K-ATPase pump (*e.g.*, M-currents). Note that the pump current used in the model is only sensitive to Na⁺, which idealizes the pump α 3 isoform of the Na-K-ATPase. The pump α 3 isoform is negligibly sensitive to K⁺ and V, but highly sensitive to changes in intracellular sodium concentration over the ranges simulated in this

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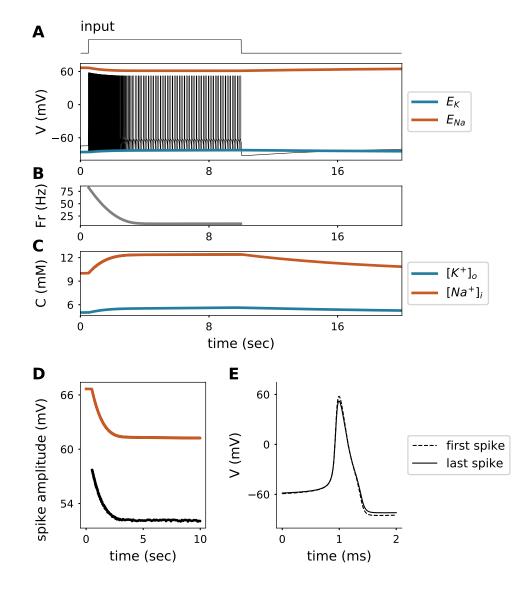


Fig 1. Response of the model to a step current of $2\mu A/cm^2$ input as shown in the top. A. Voltage trace (V) with reversal potentials for sodium (Orange) and potassium (Blue). B. Firing rate (Fr) of neuron model. C. Intracellular sodium (Orange) and extracellular potassium (Blue) concentration (C) dynamics. D. Spike amplitude and reversal potential for sodium (Orange) for the trace shown in A. E. First and last spike (peaks aligned).

study [9,10]. The impact of the pump current on spike-frequency adaptation was, however, preserved in models of other pump isoforms.

c) In our model, reductions in spike amplitude were directly related to intracellular sodium accumulation, see Fig. 1C. Activity-dependent reduction of action potential amplitude has previously been attributed primarily to Na⁺-channel inactivation during prolonged stimulation [6,11]. Our simulations, however, demonstrate that the time course of amplitude reduction mirrors the drop in sodium reversal potential (see Fig. 1A), which is related to the time course of sodium accumulation (see Fig. 1B). The Na⁺-channel inactivation was more than an order of magnitude faster than the timescale of spike-amplitude reduction; the slow spike amplitude decay was modulated by intracellular sodium. A dynamical system's perspective of this finding and an experimental confirmation are presented in the next sections.

Analysis in the presence of noise

The results so far reflect idealized model responses in the absence of noise. To include the stochasticity of synaptic inputs that is typical for many neurons in the central nervous system, we next added coloured noise with stationary statistics to the input current - a useful exercise that reveals an interesting property in the response that was masked in the noise-free case discussed above.

Stimulating the model again with a step current yet in the presence of an additional colored noise 91 component (Fig. 2), the model neuron's response during the first second was comparable to the noise-free case presented before: $[Na^+]_i$ and $[K^+]_o$ accumulated (resulting in changes in the reversal 93 potentials $E_{\rm Na}$ and $E_{\rm K}$); spike frequency adaptation, and spike-amplitude reduction were observed (compare to Fig. 1A). Surprisingly, after the first second of stimulation, the response exhibited a 95 sudden transition from regular spiking to an intermittently-interrupted, burst-like firing mode. Note that the stimulus statistics are in a wide-sense stationary such that there was no qualitative change 97 in the stimulus during the simulation duration. This means that the qualitative switch in the firing pattern must arise from a bifurcation in the neuron's dynamics. The switch in firing pattern 99 occurred 1.2 seconds after stimulus onset, a time scale that largely exceeds the time scale associated 100 with the dynamics of spike-generating conductances (which are about two orders of magnitude 101 faster). Yet this time scale matches the time scale of changes in ionic concentrations, suggesting that 102 the switch is causally related to the ion accumulation. Ion accumulation influences spike generation 103 by changing ionic reversal potentials and engaging the electrogenic Na-K-ATPase. 104

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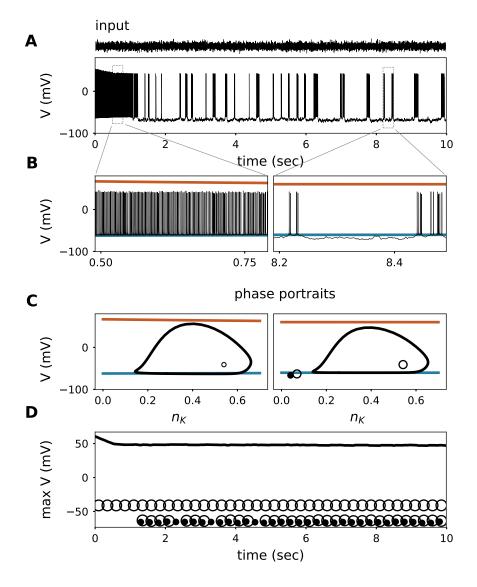


Fig 2. Response of the model to a step current with colored noise filtered at 500Hz (mean input is $1\mu A/cm^2$ and standard deviation $1.05\mu A/cm^2$, shown above). A.: Voltage trace (membrane potential) of the model responding to a noisy step current (Top of panel). B. Zoom of the voltage trace from panel A. at the beginning and towards the end of stimulation showing the evolution of the reversal potentials for sodium (orange) and potassium (blue), as in Fig. 1. C.: Phase portraits of the steady state of the fast spike generating sub-system, when imposing the average reversal potentials of panel B. as parameters. Vertical axes show the voltage and the horizontal axes show the potassium current gating-variable (n_K) . Empty dots are the unstable nodes, filled dots the stable nodes, and the orbits are stable limit cycles. D. Evolution of the stable nodes, and the black line denotes the maximum voltage of the stable limit cycles (action potential peak).

Separating the fast and the slow dynamics

To disentangle the origin of the transition, in a next step, the fast spike-generating dynamics was 106 separated from the slow ionic concentration dynamics using a slow-fast analysis. To this end, we 107 systematically analyzed the fast system with fixed ionic concentrations (i.e., constant values of the 108 slow concentration variables). The latter, however, were chosen from "snapshots" of the values that 109 the concentrations had exhibited in the full system (where concentrations were varying). This 110 approach allowed us to systematically determine how ionic changes shaped the ongoing properties of 111 the fast sub-system. Time scale separation is valid because ionic concentration changes were much 112 slower (\sim seconds) than the spike generating currents (\sim milliseconds) (see the methods section). 113

Analysis of the slow-fast system revealed that the qualitatively different spiking response was 114 triggered by a switch in the dynamics of action-potential generation. Mathematically, the model 115 started out in a setting where spiking is initiated via a saddle-node on invariant circle bifurcation 116 (SNIC) [12]. This type of dynamics is characterized by the existence of a unique stable attractor for 117 each input level, *i.e.* only one, well-defined state that the system converges to. For low inputs this is 118 a fixpoint, *i.e.* the resting state, while for high inputs it is a limit cyle attractor, *i.e.* the regular 119 spiking state. In models with fixed intra- and extracellular ionic concentrations, this type of 120 dynamics would persist as long as cellular properties remain constant, *i.e.* across the whole 121 stimulation period. Alterations in the level of ionic concentrations (and hence their transmembrane 122 gradients in terms of reversal potentials), however, can qualitatively switch the dynamics to a 123 different spike-generating bifurcation. A switch in the spike generating bifurcation, can be perceived 124 in some qualitative characteristic features of spike trains. Such a transition can, for example, be 125 reflected in an increased or decreased number of attractors. Indeed, when monitoring the number of 126 stable attractors of the corresponding fast system at each point in time, their number changes 127 exactly at the ionic concentrations reached at 1.2 seconds. Here, an additional stable fixed point (i.e. 128 a stable voltage) appears in parallel to the spiking mode for the same size of input current; the 129 system becomes bistable. Which of the two attractors (regular spiking or a fixed voltage) the system 130 converges to, depends on the initial conditions and/or noise in the system. In Fig. 1, initial 131 conditions are such that the neuron keeps up regular spiking because concentration changes are not 132 substantial enough to reach the switch in spiking dynamics (the emergence of an additional fixpoint 133 attractor). When ionic concentration changes are substantial enough the reach the switching point, in 134 the presence of noise (like in Fig. 2), however, the system permanently receives perturbations and, 135

therefore, when entering the bistable dynamics (at $\sim 1.2 \text{ sec}$) only temporarily settles onto one of the two attractors before being kicked into the other one. This dynamical state results in a long-lasting, stochastic back-and-forth between periods of spiking and silence (Fig. 2). The transition from single attractor to bistability ~ 1.2 seconds after stimulation onset is confirmed in the corresponding phase portraits of the fast system (Fig. 2C.).

Bistable vs. uni-stable states lead to qualitatively very different responses. The natural question 141 that follows is: what generates the bistability? Mathematically, the bistability is caused by the 142 emergence of a separatrix attached to a saddle point, i.e. a trajectory in phase space that separates 143 the so-called basins of attraction of the two attractors. Depending on which side of the separatrix 144 the system is located at a given point in time, it will converge towards the respective attractor 145 (unless noise or an input fluctuation kick the system across the separatrix to the other side). 146 Dynamics in this region are strongly affected by the reversal potential for potassium (see Fig. 2 C.). 147 Therefore, we next systematically explored the effects of extracellular potassium on the fast system. 148

Consequences of Extracellular potassium accumulation

Dynamical systems analysis

We analyzed the dynamics of the fast system (i.e., the neuron model with fixed ionic concentrations) ¹⁵¹ for different values of extracellular potassium. Fig. 3 shows the resulting two-parameter bifurcation ¹⁵² diagram, which depicts the dynamical state as a function of extracellular potassium concentration ¹⁵³ and size of the applied input current (for details see the methods section). Four different dynamical ¹⁵⁴ regimes can be found: a silent subthreshold state, a regularly spiking state, a bistable state, and a ¹⁵⁵ silent state of depolarization block (when the model is depolarized so strongly that spiking cannot ¹⁵⁶ occur any more). ¹⁵⁷

Let's look at the diagram in more detail, starting at lower extracellular potassium values (*i.e.*, (i.e., i.e.)) 158 the bottom of the diagram). Depending on the input strength, the system here either remains 159 subthreshold or exhibits regular firing. The transition to spiking corresponds to a SNIC bifurcation 160 (See Fig.S). When elevating the levels of extracellular potassium (to ~ 12 mM), the situation 161 changes. Here, an additional (bistable) region appears between the subthreshold and the regular 162 spiking areas. The transition is marked by a codimension-two bifurcation called a saddle-node loop 163 (SNL) [13]. The width of the bistable region increases for higher values of extracellular potassium 164 concentration (dashed lines in Fig. 3). The firing threshold corresponds to the left border of the 165

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bistable region. The transition to spiking now corresponds to a HOM bifurcation. In the bistable ¹⁶⁶ zone, in the presence of noise intermittently-interrupted firing can be observed. Moreover, at ¹⁶⁷ elevated extracellular potassium values, the depolarization block (as the name suggests, usually ¹⁶⁸ occurring at very large depolarization levels) can be observed at progressively lower input currents. ¹⁶⁹ At very high extracellular potassium values, it directly borders the bistable zone. ¹⁷⁰

The full system (with variable concentrations and pump activity), as analyzed in Fig. 2, "lives" in the bottom part of the bifurcation diagram (Fig. 3) at the onset of the stimulation, as here the values of extracellular potassium are moderate. Over time, extracellular potassium accumulates and the switching point to HOM dynamics is passed. Here, the bistable range is entered and the burst-like, intermittently interrupted firing mode can be observed in Fig. 2 due to the presence of noise. The diagram shows that extracellular potassium is the bifurcating parameter that leads to the qualitative switches in spiking.

Experimental manipulation of extracellular potassium

To experimentally test whether elevated levels of extracellular potassium can induce HOM dynamics 179 of action potential generation, a verification of the model-predicted intermittently-interrupted 180 burst-like firing mode suggests itself. In vitro, activity-driven accumulation of extracellular 181 potassium is difficult to reproduce due to the continuously perfused bathing solution that constrains 182 extracellular ion concentrations. We, therefore, recorded current-induced activity in mouse cortical 183 pyramidal neurons exposed to different fixed concentrations of extracellular potassium. Action 184 potentials were induced by constant-current stimulation in baseline conditions (3 mM extracellular 185 potassium), and after increasing the concentration of extracellular potassium to 10 or 12 mM (see 186 methods section). Neurons were stimulated with somatic current injection sufficient to maintain the 187 membrane potential close to spiking threshold (see first panel of Fig. 4), which, in terms of 188 dynamical system analysis, is close to limit cycle onset and, for HOM dynamics, also to the bistable 189 region, see Fig. 3. 190

Our experimental results support the model prediction portrayed in Fig. 3, in which an increase ¹⁹¹ in extracellular potassium concentration switches the spike generating mechanism. When ¹⁹² extracelluar potassium is low (3 mM), the neuron shows very rhythmic (regular) action potential ¹⁹³ generation over time (see Fig. 4 left panel). In contrast, when extracellular potassium is increased to ¹⁹⁴ 10 or 12 mM, action potential generation in the same neuron becomes irregular (see Fig. 4 right ¹⁹⁵ panel). In 7 out of 8 neurons tested, we observed an increase in spiking irregularity when potassium ¹⁹⁶

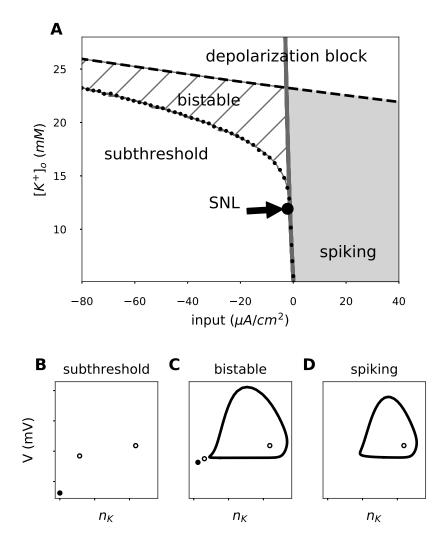


Fig 3. Characteristic phase portraits in the extracellular potassium / applied current space. Different combinations of extracellular potassium and input current yield different phase portraits of the fast spike generating sub-system. A.The background color represents the characteristic response of that area; Subthreshold or depolarization block : White; Bistable: Dashed; Spiking: Gray. The different regions are separated by the disappearance of the stable node (gray line) and the limit cycle onset (black dots). Examples of phase portraits in each region of the extracellular potassium - input current plane are portrayed; B. subthreshold, C. bistable, and D. spiking state.

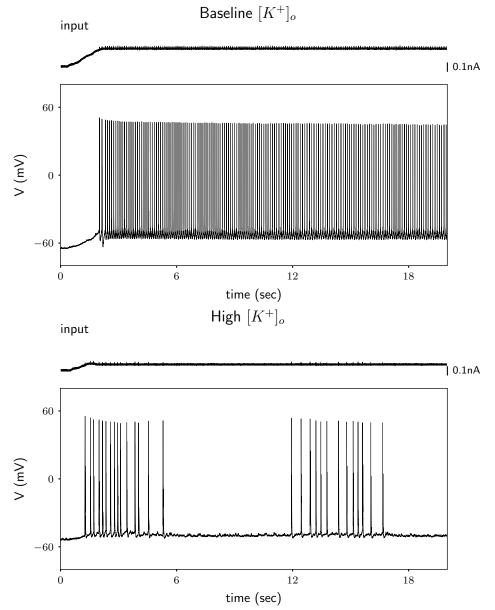


Fig 4. Rodent cortical neurons exposed to high extracellular potassium show intermittently interrupted firing. Example cell; Response of a neuron to a just suprathreshold stimulus in low (3 mM; Top) and high (10 mM; Bottom) extracellular potassium conditions. The suprathreshold current is taken as the current needed to elicit the first spike when injecting a ramp with a shallow slope. The small spikelets visible in the current trace are artifacts resulting from limited capacitive coupling of two channels at the digitizer (i.e., of the action potentials present in the voltage trace), and are not reflective of current injected into the neuron.

> levels were increased from 3 mM to 12 mM (see supplementary material Fig. S. and S.). In 3 out of 197 10 neurons tested, we observed an increase in spiking irregularity when potassium levels were 198 increased from 3 mM to 10 mM (see supplementary material Fig. S), confirming a crucial prediction 199 of the model. We hypothesize that not all neurons exhibited the same qualitative behavior because 200 the distance to the switching point depends on other parameters as well [13] and hence is likely to be 201 variable across cells [14]. It remains to be determined whether the activity of a single neuron 202 generates the $[K^+]_{\rho}$ accumulation that induces the SNL bifurcation. Presumably such transitions 203 would be more likely when there are multiple neurons activated simultaneously, which would 204 generate a larger $[K^+]$ flux to the extracellular space. 205

Consequences of intracellular sodium accumulation

The dynamical system analysis described above provides a mechanistic explanation for the emergence ²⁰⁷ of intermittently-interrupted firing. However, the only concentration we varied for the analysis was ²⁰⁸ that of potassium ions. Yet long periods of spiking accumulate both extracellular potassium and ²⁰⁹ intracellular sodium ions. In the following section, we therefore describe physiological features that ²¹⁰ are altered by sodium accumulation. The space of sodium concentrations is explored to determine ²¹¹ whether the results from the dynamical system analysis performed to understand the consequences ²¹² of extracellular potassium accumulation, hold up under conditions of parallel sodium accumulation. ²¹³

Sodium accumulation shapes two main properties of spike generation: spike amplitude and spiking threshold, which are determinant features for information transmission and encoding, respectively.

Intracellular-sodium-dependent spike amplitude reduction

As outlined above, action potential amplitude is reduced as intracellular sodium accumulates during ²¹⁸ spiking (Fig. 1 and Fig. 2), reducing E_{Na} and hence the driving force. This effect is also reflected in ²¹⁹ the phase portraits (Fig. 2**C**.). The height of the stable limit cycle is squeezed during stimulation, ²²⁰ correlating with the E_{Na} reduction (Fig. 1**A**.). We tested this model prediction in mouse cortical ²²¹ neurons *in vitro* during extended periods of current-induced spiking. ²²²

Extended activation of rodent cortical neurons led to a slow spike amplitude reduction (Fig. 5 223 and Fig. S). Rodent cortical neurons were activated for 40 seconds using short (2 ms) depolarizing 224 current pulses (3 nA) generated at 40 Hz. These neurons exhibited a slow and progressive reduction 225

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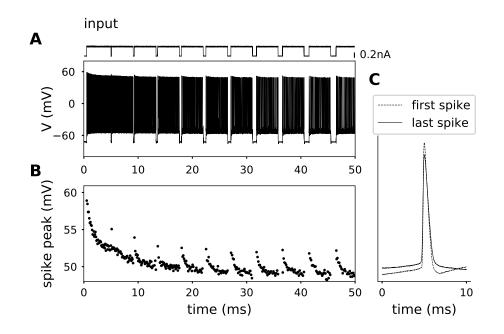


Fig 5. Example trace: Evolution of spike peak in time. A Membrane potential of a rodent cortical neuron, subjected to prolonged stimulation, and brief hyperpolarizing pulses with different duration. B Zoom into the membrane potential peak is shown. C First and last spike aligned at 5ms for comparison.

in spike amplitude that was best fit by a double exponential decay with an average fast time 226 constant (τ_{fast}) of 480 ms and an average slow time constant (τ_{slow}) of 17.7 s (n=50) (see 227 Supplementary material Fig. S. and Table S. for details). The observed slow spike amplitude decay 228 fits the prediction of the model, given that sodium accumulation occurs on the order of seconds, and 229 the faster time scale coincides with the previously reported effects of sodium inactivation [15]. 230

More than one process contributes to spike amplitude decay: a fast process (sodium channel 231 inactivation) and a slow process (sodium accumulation). In order to disentangle the contribution of 232 the two, we used somatic current injection to drive rodent cortical neurons with periodic brief (100 233 to 1000 ms) hyperpolarizing currents (Fig. 5) that were long enough to reset (deinactivate) sodium 234 channels, but too short for the Na-K-ATPase to clear activity-dependent increases in intracellular 235 sodium. We observed a progressive reduction in action potential amplitudes that was not rescued by 236 hyperpolarizations as long as one second. Further, the slow time constant of spike amplitude decay 237 was found to coincide with that measured in the previous protocol, $\tau_{slow} = 15.7s$ (Fig. and Tab. S,). 238 These observations suggest that the slow component of amplitude decay cannot result from sodium 239 channel inactivation, and instead is likely driven by intracellular sodium accumulation and the 240

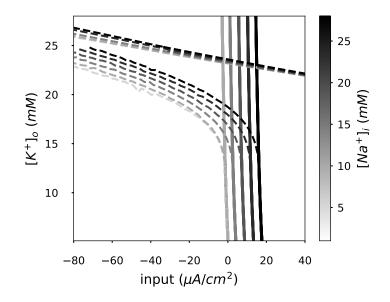


Fig 6. Extracellular potassium and intracellular sodium dependent bistable area. Same bifurcation diagram portrayed in Fig. 3 for different intracellular sodium concentrations $[Na^+]_i$. $[Na^+]_i$ controls the input current required to transition from resting to spiking regimes. $[Na^+]_i$ accumulation shifts the bistable region to higher current values.

resulting decrease in E_{Na} .

Intracellular sodium accumulation shifts the spiking threshold in the model

Given that an accumulation of intracellular sodium $([Na^+]_i)$ is likely to affect spike generation, we next systematically evaluated the dynamical regimes identified in the bifurcation diagram at different, fixed $[Na^+]_i$ concentrations (Fig. 6).

We find an identical bifurcation structure and splitting into different dynamical regimes for a 246 wide range of $[Na^+]_i$ levels, with the exception of a shift towards higher input currents with larger 247 $[Na^+]_i$ (Fig. 6). In other words, as $[Na^+]_i$ accumulates, the spiking threshold is shifted to higher 248 inputs. This shift can be attributed to the dependence of the Na-K pump on $[Na^+]_i$; accumulation 249 of $[Na^+]_i$ thus strengthens the hyperpolarizing pump current, counteracting the input current and 250 reducing the net excitatory drive. Consequently, also the bistable region is shifted along the current 251 axis. Neither a significant change in the area of the bistable region, nor in the location of the 252 transition point towards bistability (i.e., the SNL bifurcation) on the $[K^+]_o$ axis are observed. 253

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Consequences of simultaneous $[Na^+]_i$ and $[K^+]_o$ changes

The effect of ionic concentrations on neuronal voltage dynamics unfolds via changes in the respective 255 reversal potentials, E_{Na} and E_K . Fixing the input current, we can summarize how the spiking 256 regime depends on the concentrations $([Na^+]_i \text{ and } [K^+]_o)$ in a plot that depicts the spiking regime 257 (reached in the steady-state of the fast subsystem) as a function of the two corresponding reversal 258 potentials (Fig. 7). The regime was determined via the phase plane of each system (Fig. 3B.,C.,D.) 259 and can be classified as bistable, regularly spiking, or stable-resting (i.e., either subthreshold or in 260 depolarization block). To relate the reduced fast subsystem with the complete system including slow 261 concentration dynamics, three example trajectories of the complete system at different initial 262 conditions in the space of reversal potentials are shown on top of the steady states of the fast 263 subsystem. Each trajectory represents the evolution of ionic concentrations during 10 seconds of 264 stimulation with a fixed current in the presence of noise (as in Fig. 2). The corresponding voltage 265 traces are presented for comparison (Fig. 7B., C., D.). Traces that started at a higher firing rate 266 (and, consequently, were accompanied by larger changes of ionic concentrations) moved farther than 267 the ones that started out at a lower rate. 268

Which spiking regime a model neuron enters during stimulation, can be read off the 269 corresponding trajectory in the complete system. The trajectory depends on the initial ionic 270 concentrations at stimulation onset. A neuron starting with a very low E_K yet high E_{Na} tends to 271 move from regular spiking either to a resting state or to a lower firing rate within the regularly 272 spiking regime (yellow trajectory in Fig. 7, similar to the example trace in Fig. 7D.). Biophysically, 273 spike-frequency adaptation results from the activity of the electrogenic pump, which generates a 274 progressively larger hyperpolarizing current as levels of intracellular sodium increase. Trajectories 275 initialized at low E_K do not reach the bistable region. They tend to a quiescent mode, remaining 276 close to the border to regular firing. If the initial E_K is more elevated, however, a neuron that starts 277 in the regularly spiking regime can reach the bistable region (orange trajectory in Fig. 7, similar to 278 the example trace in Fig. 2). Very high initial extracellular potassium concentrations promote 279 depolarization block, but, depending on initial conditions, the bistable regime may also be 280 encountered as an intermediate state (magenta trajectory in Fig. 7). 281

The three example trajectories displayed in Fig. 7, illustrate that a neurons with identical ion channels and stimulation can generate extremely different responses depending on the extracellular environment. Recent spiking activity of neurons alters their response, even when stimulation is 284

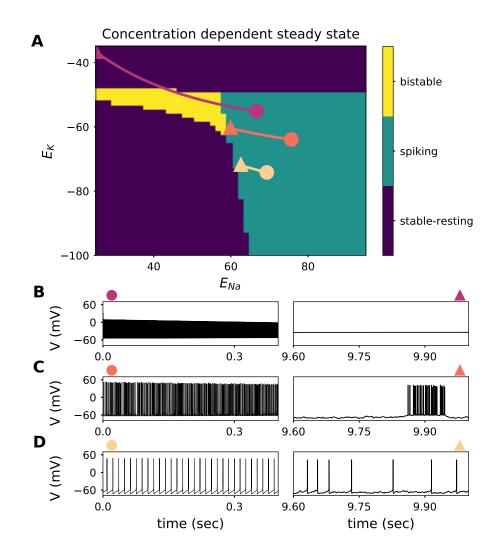


Fig 7. Consequences of simultaneous $[Na^+]_i$ and $[K^+]_o$ changes A.: Characteristic response of the reduced model (receiving a constant input current stimulus of $1\mu A/cm^2$) along the reversal potential plane. The characteristic response can be split in three categories; stable-resting state (lower left corner, subthreshold regime; upper part of the figure: depolarization block. Both represented in purple), spiking state (green), and bistable (yellow). Three example trajectories of the complete system (Including the slow concentration dynamics) simulated during 10 seconds (with an irregular input of mean of $1\mu A/cm^2$ and standard deviation of $1\mu A/cm^2$). The initial conditions represented by a circle, and the state of the system 10000 ms later with a triangle. **B.**: Membrane potential trace of the trajectory with initial conditions $E_K = -55.1mV$ and $E_{Na} = 66.7mV$ displayed in A. Left panel shows the first 400ms of simulation (marked with a circle), and the right panel shows the last 400ms out of the 10 seconds simulation (marked with a triangle). **C.**: Membrane potential trace of the trajectory with initial conditions $E_K = -63.9mV$ and $E_{Na} = 75.7mV$ displayed in A. **B.**: Membrane potential trace of the trajectory with initial conditions $E_K = -74.2mV$ and $E_{Na} = 69.3mV$ displayed in A.

> unchanged; the rate of change of ionic concentrations strongly depends on neuronal firing rate. Consequently, neurons receiving strong and prolonged stimulation are more likely to experience dynamical regime changes due to ionic accumulation than neurons with weaker stimulation.

Discussion

In this study, we show that activity-dependent changes in ionic gradients during prolonged neuronal 2299 activation can indeed qualitatively change the underlying neuronal dynamics. This fact is reflected 200 most pronouncedly in a change in spiking pattern from regular to an intermittently interrupted 201 mode, which appears when extracellular potassium accumulates. Intracellular sodium accumulation, 202 in contrast, mediates a long-lasting spike-frequency adaptation via engagement of the sodium 203 potassium pump, and lowers spike amplitude by its effect on the reversal potential E_{Na} . 204

We claim that for highly active neurons, an assumption of stationarity of neuronal dynamics is not precise; neurons are intrinsically affected by their recent electrical activity, beyond any other changes that may arise from network feedback. Extended spiking activity results in modifications of her intracellular and extracellular concentrations of sodium and potassium, respectively, and triggers homeostatic mechanisms that regulate ionic gradients at time scales much slower than action potential genesis and bears consequences for neural computation.

Switching to the HOM firing regime: We demonstrate that neuron models that start out with SNIC dynamics (i.e., the classical type I dynamics that has been thought to underlie the firing of most cells with a smooth onset of firing at threshold) can flip to HOM dynamics only seconds after the onset of the spike-inducing stimulation. This transition most obviously manifests in the spiking pattern, which turns from a regular firing mode to an intermittently interrupted one. Our bifurcation analysis shows that an accumulation of extracellular potassium drives this change, instantiating a bistability of the membrane potential.

This finding is consistent with previous work in neuronal models with static ionic concentrations ³⁰⁸ at different levels of extracellular potassium [16, 17]. In the presence of a fluctuating input (be it noise or signal), the bistability renders neurons susceptible to switches between the two stable states, giving rise to an irregular, intermittently interrupted firing pattern of short firing phases and pauses of different durations. Long periods of silence, which can be prominent in this mode, can resemble the ones observed during deterministic bursting reported by [18–22]. In contrast to these deterministic bursters, however, the burst-like firing we describe here is driven by the input

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fluctuations and the bistable state. Thus, neurons in an environment with high extracellular ³¹⁵ potassium concentration, promoting HOM dynamics, may be more sensitive to input variability. ³¹⁶

The SNIC and the HOM regimes yield very different neuronal encoding properties. For instance, 317 the relationship between the input current and the neuronal firing rate (i.e., the gain) depends on 318 the dynamical regime. The gain function of a neuron in the SNIC regime is continuous, the firing 319 rate of such neuron is a continuous function of the input current. The gain function of a neuron in 320 the HOM regime is discontinuous when irregular input is injected, meaning that the firing rate 321 doesn't smoothly increase as a function of the input current but it transitions from no spikes to high 322 frequency spiking abruptly. The phase response curve (PRC), which captures the temporal 323 sensitivity to inputs, also differs between the two regimes. In the SNIC regime, neurons display 324 symmetric PRCs. As PRC symmetry predicts the synchronization of the neurons in the 325 network [13, 23, 24], the switch in firing regime and the underlying bifurcation must also impact the 326 propensity of the neuron to synchronize with other cells in its local network and beyond. Encoding 327 capabilities (such as the profile of frequencies transmitted) are likely to be affected, as they also 328 depend on the PRC characteristics. 329

Interestingly, intracellular sodium accumulation only quantitatively modulates the qualitative ³³⁰ change in spiking regime, underlining the importance of potassium accumulation in this process. The ³³¹ effect of extracellular potassium on neuronal activity has been widely studied [25–27]. Experimental ³³² observations have found extracellular potassium dependent bursting [27] and its influence on other ³³³ dynamical features [16, 17, 28]. While a bistability has been previously observed "in passing" [16, 17], ³³⁴ we report a systematic effect and provide mechanistic explanations for the activity-driven changes. ³³⁵

Interpreting these results, we speculate that activity-dependent extracellular potassium 336 accumulation can contribute to, or even induce, epileptiform activity [20]. Both the bursting nature 337 of HOM dynamics [29, 30], as well as their comparatively high susceptability to synchronization in 338 inhibitory networks because of the HOM-characteristic PRC [13], favour synchronized, 339 hyperexcitable states. In vivo, Singer and Lux observed that extracellular potassium accumulates in 340 the visual cortex when a rapidly changing visual stimulus is presented to the cat's retina [4]. 341 Remarkably, similar visual stimuli elicit reflex seizures in 4–7% of human epilepsy patients [31]. 342 Reflex seizures could be promoted by extracellular potassium accumulation occurring throughout the 343 visual cortical region that is activated by visual stimulation. 344

Indeed, the observed drastic consequences of potassium accumulation might occur more 345 frequently *in vivo* than *in vitro*. *In vitro*, extracellular potassium concentrations are clamped. The 346

> tissue is perfused with a solution that has a fixed $[K^+]_{a}$ (consequently $[K^+]_{a}$) concentration, 347 analogue to an infinite buffer. In vivo, however, extracellular potassium concentration undergoes 348 stimulus-induced changes. In the cat visual cortex, for instance, extracellular potassium accumulates 349 when a graded stimulus is presented to the cat's retina [4]. Regarding the universality of the 350 dynamical changes described here, we expect these to generalize beyond the specific model choice of 351 this study. Specifically, the bistability of conductance based models arises from a slow-down of 352 hyperpolarization, which pushes the limit cycle trajectory to approach the saddle node through a 353 very attractive path (i.e., a strong manifold). This feature can be expected in any neuron model that 354 starts out with SNIC dynamics and ubiquitously favours a switch to HOM dynamics [13, 32]. The 355 exact reversal potential at which the bistability is induced, could be shifted by other parameters. 356 Thus, the exact switching point between the two dynamical regimes can vary between neurons, as 357 their properties are diverse [14,33]. Therefore, we expect that the exact location of the switching 358 point (i.e., the potassium concentration at which the switch is to be expected) depends on cellular 359 characteristics, both in neuron models as well as in experiments. Along these lines, milder 360 extracellular potassium accumulations could suffice to induce the transition in cells with a lower 361 critical value, singling out cells with a higher likelihood to switch their dynamics. 362

> Attenuation of the spike amplitude: Next to the very promiment change in spiking regime, 363 accumulation of ions are also reflected in the shape of action-potentials, namely their peak 364 amplitude. Such an attenuation is a regular feature observed in electrophysiological recordings. It 365 has, however, been previously attributed to an inactivation of sodium channels [6, 15]. Our data now 366 suggest that the activity-induced changes in reversal potentials contribute substantially to the 367 attenuation, especially during long periods of activity, as they far outlast the effects inactivation. 368 Our deinactivation experiments with hyperpolarizing current steps support this hypothesis and 369 confirm that the larger and slower component of spike amplitude reduction persist even when 370 sodium channel inactivation is largely diminished. Moreover, the timescales of E_{Na} and amplitudes 371 attennuation are matched. 372

> Concentration-change induced spike-frequency adaptation: Spike-frequency adaptation resulted from an activity-dependent increase in the hyperpolarizing sodium pump current (again mediated by sodium accumulation). This observation was previously reported for leech mechanoreceptor neurons [34] as well as for rodent cortical neurons [5]. The later study [5] demonstrated not only that the pump current produces a slow afterhyperpolarization (AHP) as a consequence of neural activity, but that its time-course mirrors the time-course of intracellular

sodium decay. Results from our model are consistent with this finding.	379	
Interestingly, for both spike amplitude attenuation and spike frequency adaptation,	380	
ion-channel-mediated equivalent effects on short timescales are well known. The dynamics of	381	
concentrations seem to smoothly extend these effects in time.	382	
Limitations: We note that our model does not consider extracellular uptake of potassium by	383	
glial cells. The latter maintain the ionic homeostasis of the extracellular environment and serve as	384	
extracellular potassium buffers [35]. Experimental work Dallerac et al. [36] has shown that glial	385	
buffering of extracellular potassium saturates at high values when changes are relatively fast. Yet	386	
the presence of glial cells <i>in vivo</i> is likely to slow the timescale of potassium accumulation. The	387	

effects described here can be expected to arise most prominently in pathological conditions, be it 388 glial dysfunction or energy-deprivation that impairs the pumps and thus facilitates accumulation of 380 both extracellular potassium and intracellular sodium. 390

We also note that the experiments in this study were performed in the absence of synaptic 391 blockers. This keeps the pharmacological cocktail "neater", but it also raises the possibility that 392 changes in synaptic input may contribute to the irregularity displayed in the single-cell 393 measurements. Specifically, two opposing effects may come into play: (i) Extracellular potassium 394 accumulation shifts E_K to more depolarized potentials; this in turn may foster the passive inflow of 395 chloride, moving also E_{Cl} to a more depolarized state. These effects reduce GABA-A and GABA-B 396 efficacy and reduce synaptic inhibition, by depolarizing the IPSP equilibrium potential [37]. (ii) Also 397 extracellular potassium dependent inhibition of glutamate transporters may contribute [38], 398 decreasing excitatory synaptic transmission. Having said so, an increase in extracellular potassium 390 also increases the firing rate of neurons in the whole network and it is not probable that the synaptic 400 efficacy reduction could counterbalance the increase in the network input. Network interactions may 401 have many nonlinear effects, and it is not trivial to draw conclusions on causality. 402

Conclusion

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Our analysis shows that a consideration of the slow ionic concentration dynamics inherent to *in vivo* 404 brain activity unravels the nonstationary nature of neurons as computational units. Cortical neurons 405 are typically grouped as either intrinsically bursting, regular spiking, or fast spiking [39]. Here, we 406 reveal a more dynamic situation: by accumulation of ions during prolonged activity, regularly 407 spiking neurons may transition to an intermittently firing mode, or even resemble intrinsically 408 bursting neurons, via activity-induced switches in the underlying bifurcation structure of its dynamics. Neuronal firing patterns are dynamical even in the absence of network changes and strongly depend on the concentrations in the extracellular and intracellular medium. In particular, HOM-type dynamics are likely to be induced in situations of impaired ionic homeostasis, such as glial pathologies or reduced energetic supplies, affecting neural encoding and potentially the network state.

Materials and methods

With the purpose of understanding the effect of different ionic concentrations on the neuron's response, we used two approaches: simulations of a single-neuron mathematical model with dynamic concentrations, and patch-clamp of rodent cortical neurons while perfusing the medium to control the extracellular ionic concentrations.

Computational model

Our goal is to understand the effects of ionic concentration dynamics on the excitability of neurons. ⁴²¹ Two ingredients are needed: an excitable system (capable of generating spikes) for which we use the ⁴²² Traub-Miles formulation [40] (See equations (1),(2),(3),(4)), and a description for the ionic ⁴²³ concentration changes that occur due to ionic currents. The action potential dynamics at a ⁴²⁴ membrane is governed by a current balance equation involving the following ionic currents, ⁴²⁵

$$C_{\rm m}\frac{dV}{dt} = I_{\rm app} - I_{\rm Na} - I_{\rm K} - I_{\rm L} - I_{\rm pump}.$$
(1)

$$I_{\rm Na} = g_{\rm Na} m_{Na}^3 h_{Na} (V - E_{\rm Na}) \tag{2}$$

$$I_{\rm K} = g_{\rm K} n_K^4 (V - E_{\rm K}) \tag{3}$$

$$I_{\rm L} = g_L (V - E_{\rm L}) \tag{4}$$

$$I_{\text{pump}} = \begin{cases} 0 & [\text{Na}^+]_i \le [\text{Na}]_s \\ \frac{I_{\text{maxp}}}{1 + \exp(k_{\text{Na}}([\text{Na}^+]_i - [\text{Na}]_s))} & [\text{Na}^+]_i > [\text{Na}]_s \end{cases} (5)$$

The pump model in Eq. (5) constitutes a homeostatic mechanism that counteracts the movement 428

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of ions due to chemical gradients during neuronal spiking activity. Specifically, the sodium 429 potassium pump (Na-K-ATPase) pumps 3 sodium ions out of the cell, while 2 potassium ions enter 430 the cell every pump cycle. The pump is represented by sigmoidal function of the intracellular Na⁺ 431 concentration in Eq. (5) [19,41]. I_{maxp} is the maximum pump rate, k_{Na} is the sodium sensitivity of 432 the pump, and $[Na]_s$ is the sodium concentration at which the pump current is most sensitive to 433 concentration changes. We ignore the pump's dependence on potassium and on voltage. This is an 434 analog of Na-K-ATPase (isoform 3), which reacts very strongly to intracellular sodium changes, and 435 is rather insensitive to potassium in the range we study ($[K^+]_o$ 4-20 mM) [9]. 436

The concentration dynamics is influenced by the transmembrane currents due to ion channels 437 and the pump as follows. 438

$$\frac{d[\mathrm{Na}^+]_i}{dt} = \frac{\rho}{F} (-3I_{\mathrm{pump}} - I_{\mathrm{Na}}) \tag{6}$$

$$\frac{d[\mathrm{K}^+]_i}{dt} = \frac{\rho}{F} (2I_{\mathrm{pump}} - I_{\mathrm{K}} - I_{\mathrm{L}}) \tag{7}$$

$$\frac{d[\mathbf{K}^+]_o}{dt} = -\frac{d[\mathbf{K}^+]_i}{dt} \frac{\mathrm{Vol}_i}{\mathrm{Vol}_e} \tag{8}$$

$$E_{\rm K} = \frac{RT}{F} \ln\left(\frac{[{\rm K}^+]_o}{[{\rm K}^+]_i}\right) \tag{9}$$

All expressions and parameters used in the simulations can be found in Tables S., S., and S.. 439 Simulations where performed in python and code is available here. 440

Time scale separation

Simulating the model dynamics with an ODE solver is very time consuming (This was done for voltage traces in Fig. 1, 2, and 7). Therefore, in order to characterize the system's response to a broad set of initial conditions using shorter simulation times, we used time scale separation for the analysis. This technique is particularly useful for our set of equations because the system contains variables changing in very slow and very fast time scales. 442

Ionic concentration dynamics change with a time scale in the order of seconds, while spike generating currents are changing in the order of milliseconds. Thus, we can split the system into two subsystems. The fast subsystem (Equations 2,3,4,5,9,1) receives ionic concentrations 449

 $([Na^+]_i, [K^+]_i, [K^+]_o)$ as fixed parameters. For each parameter combination the steady states are portrayed in phase portraits (See Fig. 2 bottom panel). A parameter combination that yields a phase portrait containing only one stable node is characterized as resting state, one containing only a stable limit cycle is characterized as regular firing, and one with a stable node and a stable limit cycle is characterized as bistable (See Fig. 7 A.).

Bifurcation analysis

The numerical bifurcation software AUTO [42] was used to find the limit cycle onset (spike onset), 456 the disappearance of the steady state, and the hopf bifurcation (depolarization block). The analysis 457 was repeated for different ionic concentrations (See in Fig. 3 and 6). 458

Experimental protocol

Physiological experiments were approved by the Institutional Animal Care and Use Committee of Dartmouth College. Female and male adult (3- to 4-month-old) C57BL/6J mice were bred in facilities accredited by the Association for Assessment and Accreditation of Laboratory Animal Care and maintained on a 12h-12h light-dark cycle with continuous free access to food and water.

On the day of experiments, mice were anesthetized with vaporized isoflurane and decapitated, with brains rapidly removed into an artificial cerebral spinal fluid (aCSF) composed of (in mM): 125 NaCl, 25 NaHCO₃, 3 KCl, 1.25 NaH₂PO₄, 0.5 CaCl₂, 6 MgCl₂ and 25 glucose (saturated with 95% O2-5% CO₂). Coronal brain slices (250 *m* thick) of the frontal cortex were cut using a Leica VT 1200 slicer and stored in a holding chamber filled with aCSF containing 2 mM CaCl₂ and 1 mM MgCl₂. Slices were maintained in the holding chamber for 45 minutes at 35° C, and then at room temperature ($\sim 25^{\circ}$ C) until use in experiments.

Slices were transferred to a recording chamber on a fixed-stage microscope (Olympus), and 471 continuously perfused ($\tilde{7}$ ml/min) with oxygenated aCSF heated to 35-36 °C. Layer 5 pyramidal 472 neurons in the prelimbic cortex were visually targeted using a 60X water-immersion objective, and 473 whole-cell recordings made with patch pipettes (5-7 M) filled with a solution containing the following 474 (in mM): 135 potassium gluconate, 2 NaCl, 2 MgCl₂, 10 HEPES, 3 Na₂ATP and 0.3 Na₂GTP, pH 475 7.2 with KOH. Data were acquired using a BVC-700 amplifier (Dagan Corporation) connected to a 476 HEKA 8+8 digitizer driven by AxoGraph software (AxoGraph Scientific; RRID: SCR - 014284). 477 Membrane potentials were sampled at 50 to 100 kHz and filtered at 5 or 10 kHz. Voltage 478

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> measurements were corrected for a +12 mV liquid junction potential. Concentrations of KCl (3, 10, 479 or 12 mM) and NaCl (125, 118, or 116 mM, respectively) were adjusted as indicated to test the 480 impact of extracellular potassium concentration on action potential dynamics. 481

Data analysis

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Data analysis was done in python.

Spiking irregularity Spiking irregularity is measured as

$$CV = \frac{\sigma}{\mu},\tag{10}$$

where σ is the standard deviation of the interspike interval (ISI), and μ is the mean.

Time scale of spike amplitude decay

The fast and the slow components of the spike amplitude decay were calculated by fitting the 487 time dependent spike-voltage-peak to a double exponential function, 488

$$D_{fast} \exp\left[\frac{-t}{\tau_{fast}}\right] + D_{slow} \exp\left[\frac{-t}{\tau_{slow}}\right] + D_{ss}.(11)$$

The distribution of the parameters that yield the best fit across all traces measured are shown in 499 Fig., Table. and Table.. 490

Supporting information

S1 Fig. Transition from rest to spiking (limit cycle onset bifurcations) for different 492 extracellular potassium concentrations. From bottom to top; SNIC (saddle-node on invariant 493 circle): Purple, SNL (Saddle-node-loop): Blue; HOM (saddle homoclinic orbit): Green. In the SNIC 494 regime the stable node collides with an unstable node, giving rise to a saddle node. The limit cycle 495 orbit passes through the saddle node, the trajectory leaves the saddle node along the semi-stable 496 manifold. After one period trajectory approaches the saddle node along the same semi-stable 497 manifold. At the SNL point, trajectories leave the saddle node along the semi-stable manifold as in 498 the SNIC case, but after one period those trajectories approach the saddle node along the strongly 499 stable manifold. Notice that the SNL orbit is smaller than the SNIC orbit, and has a shorter period. 500 In the HOM regime a stable node and a limit cycle coexist. External perturbations shift the state of 501 the system from the stable node to the attraction domain of the limit cycle attractor.

S2 Fig. Spike amplitude slow decay. Depolarizing pulses applied at a 40Hz rate. Spike amplitude decay $\tau_{slow} = 13.6(seg)$, and $\tau_{fast} = 410(ms)$. Notice that the amplitude of the last spike doesn't recover its amplitude after the hyper-polarizing pulse. 503

S3 Fig. Distribution of time scales of the double exponential decay (equation 11) of the spike amplitude. Two protocols were used to measure the time scales of spike amplitude decay, an example of the "40 Hz Depolarizations" is shown in Fig., and an example of the "Hyperpolarization" is shown in Fig. 5. Notice that the distribution of τ_{slow} is independent of the protocol used.

S4 Fig. Spiking variability calculated as the coefficient of variation $(CV = \frac{\sigma}{\mu})$ for all cells sampled, when stimulating with white noise added to the baseline input. An increase from 3mM to 12mM in extracellular potassium increased the spiking variability of 5 out of 6 cells measured.

S5 Fig. Spiking variability calculated as the coefficient of variation $(CV = \frac{\sigma}{\mu})$ for all cells sampled, when stimulating with baseline input. An increase from 3mM to 12mM in extracellular potassium increased the spiking variability of 2 out of 2 cells measured. The main source of stimuli irregularity was the network activity.

S6 Fig. Spiking variability calculated as the coefficient of variation $(CV = \frac{\sigma}{\mu})$ for all cells sampled. An increase from 3mM to 10mM in extracellular potassium increased the spiking variability of 3 out of 10 cells measured. The main source of stimuli irregularity was the network activity.

S1 Table. Summary of the distribution of the best fit of the parameters for each of ⁵²³ the 50 traces. Depolarizing pulses applied at a 40Hz rate ⁵²⁴

S2 Table. Summary of the distribution of the best fit of the parameters for each of the 73 traces. Hyperpolarizing pulses.

S3 Table. Gating dynamics used for the Traub-Miles model.

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S4 Table.	Expressions used for the Traub-Miles model.	528
S5 Table.	Parameters used for the Traub-Miles model.	529

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