Page 1 of 29

Computational optical sectioning by phase-space imaging with an incoherent multiscale scattering model

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Optical sectioning is essential for fluorescence imaging in thick tissue to extract in-17 18 focus information from noisy background. Traditional methods achieve optical 19 sectioning by rejecting the out-of-focus photons at a cost of photon efficiency, 20 resulting in a tradeoff between sectioning capability and detection parallelization. 21 Here, we show phase-space imaging with an incoherent multiscale scattering model 22 can achieve computational optical sectioning with ~20 dB improvement for signal-23 to-background ratio in scattering medium, while maximizing the detection 24 parallelization by imaging the entire volume simultaneously. We validated the 25 superior performance by imaging various biological dynamics in Drosophila 26 embryos, zebrafish larvae, and mice.

27 The beauty of life lies in the complexity and variety of cellular behaviors in threedimensional (3D) living organisms, which are difficult to appreciate without optical 28 29 sectioning¹⁻³, as the information can be easily flooded in the severe noisy background. 30 Various methods have been proposed to achieve optical sectioning by rejecting the outof-focus photons either physically or computationally, such as confocal microscopy^{4,5}, 31 two-photon microscopy^{6,7}, light-sheet microscopy^{8,9}, and structured illumination 32 microscopy^{10,11}. However, these methods still require scanning of points, lines, or planes 33 34 for 3D imaging, leading to the tradeoff between the sectioning capability and detection parallelization^{1,3,12}. Such a tradeoff intrinsically restricts the 3D imaging speed in 35 36 fluorescence imaging, especially with a limited photon budget set by the sample health^{1,12,13}. In addition, it's hard to remove the scattered photons due to the lack of depth-37 38 dependent features.

Phase-space imaging, by collecting the high-dimensional local variances of the coherence, provides a new imaging framework with digital synthesis of the partiallycoherent light field, which shows strong robustness to scattering and aberrations^{14–18}. As a typical example, light-field microscopy (LFM)¹⁹ captures the phase-space

Page 3 of 29

measurements within a snapshot by a microlens array²⁰, facilitating various applications 43 in biology, such as imaging hemodynamics²¹ and large-scale neural activities^{14,22}. 44 Different from wide-field imaging with a shallow depth of field $(DOF)^{23-25}$, LFM keeps 45 the photons focused along different angles within the extended depth of field and 46 47 maximize the parallelization by imaging the entire volume simultaneously. However, it suffers from great degradation in thick tissue such as the mammalian brain, due to 48 49 scattering and dense fluorescence labeling. While many efforts in hardware have been made to achieve additional optical sectioning $^{26-28}$ at the cost of temporal resolution, space 50 51 constraints and system compactness, the imaging model of this computational framework 52 has barely been explored, especially for complicated imaging environment in deep tissue^{29,30}. 53

54 Here, we show the necessity of an accurate imaging model in the complete space to unlock the full power of phase-space imaging in thick tissue. With an incoherent 55 56 multiscale multiple-scattering model, phase-space imaging can achieve snapshot 57 quantitative 3D information with optical sectioning computationally in densely labeled 58 or scattering samples. This method is termed as quantitative LFM (QLFM). We find that 59 the severe degradation of traditional LFM in thick tissue mainly results from the incomplete space and ideal imaging model utilized during reconstruction^{14,29,30}. By 60 61 building up the incoherent imaging process in phase-space domain accurately with 62 various factors, including the nonuniform resolution of different axial planes, out-of-63 focus fluorescence across a large range, multiple scattering, and system aberrations, we 64 can not only improve the resolution and contrast with significantly-reduced 65 computational costs, but also achieve two-orders-of-magnitude improvement in signal-66 to-background ratio (SBR) over traditional algorithms and wide-field microscopy (WFM), which is critical for quantitative biological analysis. To demonstrate the versatile 67 68 applications, we imaged various 3D biological dynamics in different specimens, 69 including the zebrafish larvae heart beating, blood flow, and whole-brain neural activity,

- 70 Drosophila embryo development, and mouse brain neural activity with notably better
- 71 performance than that of traditional ideal models without increasing the system
- 72 complexity.

Page 5 of 29

73 **Results**

74 Principle and implementation of QLFM

75 As a general computational model for incoherent conditions, our QLFM method is 76 compatible with different schematics of phase-space imaging. Here, we chose the 77 unfocused LFM for experimental demonstrations by inserting a microlens array at the 78 image plane of a normal wide-field microscope (Fig. 1a). A 4f system was used to relay 79 the back focal plane of the microlens array at the image sensor, with each microlens 80 covering approximately 13×13 sensor pixels (Methods). Once set up, the high-resolution 81 3D range of LFM was fixed with a specific objective. To flexibly adjust the volume size 82 for different specimens, we applied a piezo stage for high-speed axial scanning at large axial steps⁹. With the matched numerical aperture (NA), LFM provides an extended depth 83 of field ~169-times larger than that of WFM, which makes it very different from other 84 wide-field imaging methods. The fluorescence signals far from the focal plane exhibit 85 similar Gaussian backgrounds in WFM²³⁻²⁵, while they show apparent distinguishable 86 87 features between different angular components captured by LFM within a snapshot 88 (Supplementary Fig. 1 and Supplementary Video 1). We find that these depth-dependent 89 features provide LFM with a similar capability of computational optical sectioning as structured illumination microscopy³¹. The 3D out-of-focus fluorescence up to the 90 91 centimeter scale can be reconstructed at low resolution, as long as we take it into 92 consideration in the multislice model as a complete space. These layers far from the native 93 objective plane have usually been neglected in previous methods due to the limited 94 computational resources and contributed considerable background noises and artifacts in 95 the high-resolution range (Fig. 1b). To address this problem, we propose a multiscale 96 model in the phase-space domain by resampling the volume based on the nonuniform 97 resolution of different axial planes, avoiding many unnecessary calculations in a complete 98 space (Fig. 1b, Supplementary Fig. 2 and Methods). We then conducted a numerical

Page 6 of 29

simulation with gradually increasing background levels to show the significantlyimproved quantitative property of the multiscale model, which is barely considered in

101 previous studies but important for biological analysis (Supplementary Fig. 3).

102 Except for out-of-focus fluorescence, the scattered photons pose another 103 challenge in thick tissue, which cannot be rejected by optical sectioning due to the depth-104 independent property. Although multislice scattering models have achieved great success in the coherent imaging modalities³², they are barely considered in deconvolution 105 106 algorithms for incoherent fluorescence imaging. As the 4D phase-space measurements 107 can fully describe the partially coherent light-field distributions, they provide an 108 opportunity to infer the native 3D fluorescence as well as the nonuniform 3D scattering 109 coefficients. Here, we derived a multislice multiple-scattering model to differentiate the 110 emission fluorescence and scattered photons based on the first Born approximation in the incoherent condition³³ (Fig. 1c and Supplementary Note 1). Then, we applied the 111 alternating direction method of multipliers (ADMM) algorithm³⁴ with the multiscale 112 113 model to update the volumetric fluorescence and 3D scattering potentials iteratively 114 (Supplementary Fig. 2 and Supplementary Video 1).

115 By modeling both the out-of-focus and scattered photons, we retrieved the 3D 116 fluorescence distribution quantitatively in thick tissue. To show the pipeline, we imaged 117 a GFP-labeled tumor spheroid with a $63 \times /1.4$ NA oil-immersion objective at an axial step 118 of 10 µm for 10 subvolumes. Strong background fluorescence was observed in the raw 119 LF images, which was effectively removed by the capability of computational optical 120 sectioning in QLFM (Fig. 1d). Each LF image has a specific axial range for high-121 resolution 3D components. The large 3D volume with multiple axial steps was 122 reconstructed as a whole during the iterations, making full use of the overlapped axial 123 range and providing a better estimation of the background and uniform resolution at 124 different axial planes (Methods and Supplementary Video 1). In contrast, traditional LFM

125 shows strong artifacts due to crosstalk from the background. The axial side, with larger

126 out-of-focus photons, tends to have higher intensities, demonstrating the loss of the 127 quantitative property in thick tissue.

128 Characterization of QLFM

129 To quantitatively evaluate the improvement of QLFM, we imaged various 2-µm 130 fluorescence beads embedded in a tissue-mimicking phantom made of intralipid and 131 agarose with a 40×1.0 NA objective and calculated the average SBR at different 132 penetration depths (Methods, Fig. 2a, and Supplementary Fig. 4). By comparing with WFM and different LFM models, shown in Fig. 2b, we found that the naive imaging 133 134 model of traditional LFM resulted in a similar performance as WFM in tissue penetration. 135 Our multiscale scattering model fully exploits the capability of LFM in deep-tissue 136 imaging with ~20 dB SBR improvement over WFM. Such a great improvement facilitates 137 QLFM high-speed 3D imaging in thick tissue. We then imaged the same densely labeled 138 Drosophila brain by QLFM, traditional LFM, WFM, and confocal microscopy for 139 comparison (Supplementary Fig. 5). Despite reduced resolution due to the tradeoff 140 between spatial and angular resolutions in LFM, QLFM showed great sectioning 141 capability comparable to that of confocal microscopy without axial-scanning artifacts, 142 which was much better than those of traditional LFM and WFM.

Another problem hindering the quantitative reconstruction in LFM is the inaccurate estimation of the complicated high-dimensional PSF. As shown in Fig. 2c, the system aberration will result in great system errors between the ideal PSF and the experimental PSF measured with a sub-diffraction-limited fluorescence bead. We propose a phase-retrieval-based algorithm to estimate the system aberration by iteratively shrinking the disparity between the simulated PSF and the captured PSF along different angular components with a single image (Supplementary Fig. 6). We find that the

Page 8 of 29

150 calibrated PSF with the aberration wavefront can greatly reduce the reconstruction 151 artifacts close to the native objective plane (Supplementary Fig. 6c). Numerical 152 simulations on different levels of aberrations also shows the effectiveness of the method 153 (Supplementary Fig. 7). We then characterized the system resolution by imaging 500-nm 154 fluorescence beads distributed in 1% agarose with a 40×1.0 NA water-immersion 155 objective. The average full width at half-maximum (FWHM) was used to estimate the 156 lateral and axial resolutions at different axial planes (Fig. 2d). In addition to the improved 157 resolution, QLFM with high-speed axial scanning at a step size of 30 µm for 5 planes has a uniform resolution of approximately $1.8 \times 1.8 \times 2.5$ µm³ across a large depth range 158 covering $\sim 330 \times 330 \times 180 \ \mu\text{m}^3$. Moreover, as the multiscale model in phase-space domain 159 160 avoids the unnecessary up-sampling based on the effective resolution, it can reduce the 161 memory and computing time by orders of magnitude, especially for large depth ranges 162 during reconstruction to get rid of background (Fig. 2e). By modeling the same volume 163 range, our multiscale model with adaptive sampling rate shows the same performance as 164 traditional methods, but reduces the computing time from several hours to several 165 seconds, on a desktop computer equipped with a normal graphical processing unit (CPU: 166 Intel i9-9980XE, RAM: 128 GB, GPU: NVIDIA GeForce RTX 2080 Ti), facilitating the 167 practical use of QLFM.

168 High-speed 3D imaging of *Drosophila* embryo and Zebrafish larvae

169 To demonstrate the superior performance of QLFM over previous methods using compact 170 systems, we performed *in vivo* imaging of various fast biological dynamics in different 171 specimens. First, we imaged the whole-embryo development of histone-labeled 172 *Drosophila* at the millisecond scale with both $40 \times /1.0$ NA (Figs. 3a and b) and $20 \times /0.5$ 173 NA (Figs. 3c and d) objectives for comparison. Different from previous methods 174 capturing only part of the volume at a time³⁵, LFM achieves better photon efficiency with 175 low phototoxicity by illuminating and detecting the entire volume simultaneously. While

Page 9 of 29

there was almost no contrast in traditional LFM due to the dense labeling and strong scattering, QLFM could still distinguish single cells deep in the embryo at the millisecond scale, extending the applications of LFM to developmental biology.

179 Second, we performed *in vivo* imaging of heart-beating dynamics in zebrafish 180 larvae, which are difficult to fully capture without simultaneous exposure of the whole 181 volume at high speed. Traditional LFM shows low resolution and contrast with severe 182 artifacts (Fig. 4a), but QLFM, with a more accurate computational model, could obtain artifact-free high-resolution 3D volumes without the requirement of additional light-sheet 183 184 illumination and multiview objectives (Figs. 4b and c, and Supplementary Figs. 8 and 9). 185 We found successive improvement with increasing model complexity, indicating the 186 necessity of various factors in the model, including out-of-focus fluorescence, sample 187 scattering, and system aberrations (Supplementary Video 2).

188 Whole-brain neural recording in zebrafish larvae is another typical application of 189 LFM, but the imaging performance is far from satisfactory due to the densely packed neurons without complicated systems¹⁴ (Fig. 4d). Although the spatiotemporal sparsity 190 191 facilitates the accurate localization and extraction of neural signals^{36,37}, it is still 192 susceptible to nonuniform background fluorescence and inevitable structural changes in 193 living animals. By imaging the whole-brain neural activities in zebrafish larvae at 24 Hz with a 20×/0.5 NA objective, we demonstrate that QLFM can achieve effective single-194 195 neuron resolution with proper models to remove both out-of-focus and scattered photons 196 for each single frame without the requirement to calculate the standard deviation of many 197 frames for better contrast (Figs. 4e and f, and Supplementary Video 3). The temporal 198 traces of several neurons with simple region-of-interest (ROI) averaging demonstrate the 199 increased contrast and reduced crosstalk between adjacent neurons in QLFM (Fig. 4g).

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Page 10 of 29

201 Large-scale 3D calcium imaging in mice brain

202 The mammalian brain is a more challenging case due to its strong scattering and 203 dense neural structures. We tested the performance of QLFM by imaging the 3D calcium 204 activities in an awake head-fixed mouse, which was labeled with GCaMP6s by virus 205 injection, under a $20 \times / 0.5$ NA objective. To visualize the 3D distribution of neurons, 206 traditional LFM usually requires the standard deviation of thousands of frames to reduce 207 the background (Supplementary Fig. 10a). However, the 3D signals of a single frame are 208 usually flooded in the background fluctuations due to the low SBR (Fig. 5a). In contrast, 209 with the capability of computational optical sectioning, QLFM shows significantly 210 improved contrast (Fig. 5b and Supplementary Video 4). In addition to the detection of 211 more neurons (Supplementary Fig. 10a), QLFM allows the measurement of calcium 212 dynamics in a quantitative manner without the need for additional background 213 subtractions or filtering to improve the contrast, making it more reliable for large-scale 214 neural recording (Fig. 5c). Background fluorescence usually increases with the increasing 215 of NA due to the smaller depth of field, especially for the wide-field imaging. We 216 therefore imaged the same mouse with a 40×1.0 NA water-immersion objective at 217 different depths (Supplementary Figs. 10b-e and Supplementary Video 5). QLFM not 218 only resolved more neurons with better resolution and contrast than traditional LFM but 219 also showed stable performance at different depths up to 300 µm (Figs. 5d and e).

By high-speed axial scanning, we could further increase the axial coverage with redundant 3D imaging speed for calcium dynamics. We then conducted millisecond-scale calcium imaging in awake double-transgenic Rasgrf2-2A-dCre/Ai148D mice across a large volume covering ~ $700 \times 700 \times 180 \ \mu\text{m}^3$ by high-speed scanning of 3 planes. While there was barely contrast in traditional LFM due to the severe artifacts especially in the axial domain, which was similar to previous work³⁶, QLFM showed a much larger

Page 11 of 29

226 penetration depth with uniform resolution (Figs. 5f and g and Supplementary Video 6).

Even the neurons located $\sim 400 \ \mu m$ deep exhibited remarkable calcium responses.

228 Discussion

In summary, we developed an incoherent multiscale scattering model to fully exploit the intrinsic high-dimensional property of phase-space measurements and achieved computational optical sectioning, facilitating high-speed, large-scale, quantitative 3D imaging in deep tissue with a compact system.

233 Different from wide-field imaging with a tight focal plane, phase-space imaging 234 provides a tomographic framework by keeping the photons focused along different angles 235 with an extended depth of field. Such a process makes the signals originated from 236 different axial planes show much more distinguishable features than WFM, which can be 237 utilized to remove background fluorescence far from the native objective plane 238 computationally, as long as we model the imaging process in a complete space. 239 Additional confocal rejection or light-sheet illuminations will definitely further reduce 240 the shot-noise fluctuations by getting rid of the background photons physically but at the 241 cost of system compactness, space constraints, or detection parallelization.

In addition, as a novel computational model, our method is compatible with different phase-space imaging schemes without the requirement of any hardware modifications. In combination with the low phototoxicity and high photon efficiency, the orders-of-magnitude reductions in background fluorescence, artifacts, and computational costs enable the practical and versatile applications of QLFM as a compact and robust add-on to normal wide-field microscopy, making the advanced imaging capability generally accessible to the broad biology community.

Page 12 of 29

250 Methods

251 Experimental setup

252 Our QLFM system works as an add-on to a normal epifluorescence microscope, with a 253 microlens array inserted at the image plane. A customized upright microscope was used 254 for mouse experiments, while a commercial inverted microscope (Zeiss Observer Z1) was 255 used for the others. Another 4f system (with a magnification of 0.845) relayed the back 256 focal plane of the microlens array (with a pitch size of 100 µm and focal length of 2.1 257 mm) to the camera (Andor Zyla 4.2 plus, $2,048 \times 2,048$ pixels) so that each microlens 258 covered $\sim 13 \times 13$ sensor pixels, corresponding to a 2.15 µm \times 2.15 µm area at the sample plane for the 40×/1.0 NA water-immersion objective. Multiple lasers (488 nm and 561 259 nm) were used for the fluorescence excitation of multiple channels, which were 260 261 synchronized with the camera for time division multiplexing. A piezo objective scanner 262 (PI P-725.4CD) was used for high-speed axial scanning with a resolution of 1.25 nm at 263 100 Hz. Detailed imaging conditions and reconstruction parameters for all fluorescence 264 experiments in the paper, including the excitation power, exposure time, frame rate, voxel 265 size, fluorophore, protein, filter set, and objective, are illustrated in Supplementary Table 266 1.

267

268 **3D** deconvolution with a multiscale scattering model

To reconstruct the 3D fluorescence information in deep tissue in a quantitative way, we propose a novel 3D deconvolution algorithm with a multiscale scattering model to iteratively update both the emission fluorescence and scattering photons across an extremely large depth range (Fig. 1c). The whole pipeline of the algorithm with the pseudocode is shown in Supplementary Fig. 2.

With simple pixel realignment, the raw LF data can be represented as multiple angular components, or smoothed phase-space measurements²⁰, which can be used for

Page 13 of 29

276 phase-space deconvolution²⁹ to reduce artifacts and increase the convergence speed. However, the reconstructed volume, regardless of the deconvolution $algorithm^{29,30}$, is 277 278 limited to only dozens of axial planes due to the heavy computational cost. Therefore, the 279 out-of-focus fluorescence has usually been modeled as a constant in previous methods, 280 which is fine for thin samples but leads to severe artifacts and background noise in deep 281 tissue with nonuniform out-of-focus distributions. Fortunately, both the lateral and axial 282 resolution of LFM will gradually decrease with increasing distances from the native 283 objective plane. We can establish a multiscale grid to sample a large 3D volume at 284 different intervals based on the characterized resolution with an exponential fit 285 (Supplementary Fig. 2). The out-of-focus fluorescence with a nonuniform 3D distribution 286 can then be estimated with the depth-dependent features within a large depth of field 287 (Supplementary Fig. 1), akin to structured illumination microscopy exhibiting 288 computational optical sectioning. As this method does not require dense axial sampling 289 and a lateral sampling rate as high as the camera pixel number for each plane, which was necessary in previously reported methods due to the spatially variant PSF³⁰, the unknown 290 291 variables can be reduced by orders of magnitude to accelerate the reconstruction speed 292 when modeling the out-of-focus fluorescence of a much larger volume (Fig. 2e). For the 293 same volume size, our multiscale model can achieve almost the same performance as 294 traditional dense-sampling models at a much faster speed. In contrast, the traditional 295 method²⁹, without a sufficient axial range in the model, shows apparent artifacts and an 296 increase in the background.

Scattering is a recurring challenge in thick tissue and is the fundamental limitation of the penetration depth in light microscopy, leading to reduced resolution and contrast³⁸. Although the multilayer scattering model has recently achieved great success in coherent imaging modalities, such as diffraction tomography³⁹, the spatially nonuniform influence of scattering is barely considered in fluorescence imaging. LFM provides a great opportunity to differentiate emission fluorescence and scattered photons with its 4D

Page 14 of 29

303 phase-space measurements. We propose a multilayer scattering model based on the first

Born approximation in incoherent conditions by describing the relation between the emission fluorescence $I^{(i)}(\mathbf{r})$ and scattered photons $I^{(s)}(\mathbf{r})$ as follows:

306
$$I^{(s)}(\mathbf{r}) = \frac{1}{2} \int_{V} F(\mathbf{r}') I^{(i)}(\mathbf{r}') \frac{1}{\|\mathbf{r} - \mathbf{r}'\|_{2}^{2}} d^{3}r',$$

307 where *F* is defined as the scattering potential energy at the 3D position *r*, and *v* is the 308 whole 3D volume range. The detailed derivations and discretized version are illustrated 309 in Supplementary Note 1. Then, an ADMM framework³⁴ is used to iteratively update the 310 sample information and the scattered photons to retrieve the quantitative fluorescence 311 distributions in deep tissue with increased contrast and resolution (Supplementary Fig. 312 2). The reconstruction time of a single volume with a full FOV of the sensor used here is 313 about several seconds for a normal desktop computer with a graphical processing unit.

314 **3D** deconvolution with axial scanning for LFM

315 The high-resolution 3D range of LFM for a snapshot is fixed for a specific objective. 316 High-speed axial scanning at a large step size is a straightforward method to flexibly 317 adjust the depth range and 3D imaging speed. Such a capability is important for versatile 318 applications with different requirements for the volume size and imaging speed. However, traditional methods show severe artifacts at the stitching edges at low contrast 319 320 (Figs. 1d and 5f), as they usually reconstruct each subvolume based on every single LF image separately and stitch the subvolumes in the axial domain³⁶. Here, with the 321 322 multiscale model in QLFM, we take the entire 3D volume as a whole with the multiscale 323 sampling rate during reconstruction. As shown in Supplementary Video 1, after pixel 324 realignment of all the raw LF images, we can achieve multiple focal stacks for different 325 angular components, making full use of the intrinsic continuous property of different 326 angular components in the axial domain. Due to the large depth of field for each angular 327 component in QLFM, we can use a large step for axial scanning with much less time

Page 15 of 29

328 required to cover the same volume than in WFM. Then we update the entire large volume 329 as a whole along different angles, viewing each angular focal stack as the minimum unit 330 to calculate the error map for each iteration. Such a process is akin to wide-field 331 deconvolution first for each angle followed by tomographic reconstruction later for 332 different angles. Finally, the same ADMM framework is applied to the entire volume to 333 update the emission fluorescence and scattered photons iteratively. In this case, uniform 334 resolution can be achieved at different axial planes across a large depth range without any 335 artifacts (Fig. 1d and 2d). In addition, the computational cost can be further reduced, as 336 we can conduct 3D deconvolution with the phase-space PSF for each angular focal stack.

337 Phase-retrieval-based PSF calibration

338 The PSF of traditional LFM is calculated based on wave optics theory in an ideal imaging condition^{29,30}. However, the experimental imaging system usually has complicated 339 340 system aberrations, which will not only reduce the imaging resolution but also introduce 341 severe reconstruction artifacts close to the native objective plane. Here, we propose a 342 phase-retrieval-based algorithm to calibrate the experimental PSF with a single image of subdiffraction-limited fluorescence beads (Supplementary Fig. 6). The simulated PSF is 343 344 first initialized with experimental parameters without any aberration wavefront. Then, we 345 calculate the correlations between the captured image and the simulated PSF along 346 different angular components to estimate the wavefront error at different sub-apertures. 347 The aberrated wavefront of the whole NA is then integrated from the correlation map for 348 continuous distributions. The estimated wavefront is fitted with Zernike polynomials and 349 fed into the wave optics model to generate the new simulated PSF, which is used again 350 to match with the captured PSF. The calibrated PSF is iteratively updated through the 351 above process until the phase map converges, which usually takes approximately 3~4 iterations. Interestingly, we found that the experimental system with spherical aberrations 352 353 can remove the reconstruction artifacts close to the native objective plane as long as we 354 had an accurate estimation of the aberration wavefront.

Page 16 of 29

355

356 Fluorescence bead preparation for system characterization

For resolution characterization, 500-nm yellow-green fluorescent microspheres (Thermo Scientific, FluoSpheres, carboxylate-modified microspheres) were mixed with 1% agarose at a ratio of 1:1,000,000. We placed the mixture in a 35-mm petri dish and captured ~100 LF images for statistical analysis with a $40 \times /1.0$ NA water-immersion objective. We then calculated the FWHM of the lateral and axial profiles of the reconstructed beads on different axial planes. For each block covering 10 µm, we chose 10 beads with the highest fitting degree to calculate the mean and standard deviation.

364 For SBR characterization, we fabricated a scattering phantom with the mixture of 365 1% agarose, 1% intralipid (Absin 68890-65-3, 20% emulsion), and 0.025% 2-µm 366 fluorescence beads, which was placed in a 35-mm petri dish. The 2-µm fluorescence 367 beads (Thermo Scientific, FluoSpheres, carboxylate-modified microspheres) were 368 randomly distributed in the intralipid and imaged using a 40×1.0 NA water-immersion 369 objective. The reconstructed mean intensity of the beads was viewed as the signal, while 370 the mean intensity of the reconstructed background without samples was viewed as the 371 background. Several reconstructed slices at different imaging depths are shown in 372 Supplementary Fig. 4.

373 Tumor spheroid preparation

B16 cells (ATCC® CRL-6475TM, mouse skin melanoma cells) were purchased from ATCC and cultured in RPMI 1640 medium supplemented with 10% FBS, 1% pen/strep antibiotics and 1% NEAA (all from GIBCO). Cells were then transfected with the EGFP-PH plasmid (Addgene Plasmid #96948), and stable EGFP-expressing B16 cells were selected by neomycin (G418) and maintained. To prepare tumor spheroids, 4×10^3 EGFPexpressing B16 cells per well were seeded in round-bottomed 96-well plates (Corning) and cultured in RPMI 1640 medium supplemented with 10% FBS, 2% B-27 supplement

Page 17 of 29

381 (GIBCO), 2% methyl cellulose (Sigma-Aldrich), 1% pen/strep antibiotics and 1% NEAA.

- 382 After 2 days, each formed spheroid was transferred as 1 spheroid per well and cultured
- 383 for another 2 days. During LFM imaging, the GFP-B16 tumor spheroids were transferred
- 384 to Lab-Tek II cover-glass-bottomed 8-chamber slides and imaged in HBSS supplemented
- 385 with 2% FBS (all from Invitrogen) using a $63 \times /1.4$ NA oil-immersion objective.

386 In vivo imaging of zebrafish larvae

387 All zebrafish experimental procedures were conducted with ethical approval from the 388 Animal Care and Use Committee of Tsinghua University. For imaging of the vasculature 389 and blood flow dynamics, Tg(flk:EGFP; gata1:DsRed) transgenic zebrafish embryos 390 were collected and cultured at 28.5 °C in Holtfreter's solution. At 4-5 days 391 postfertilization (dpf), the zebrafish larvae were anesthetized by ethyl 3-aminobenzoate 392 methanesulfonate salt (100 mg/L) and mounted in 1% low-melting-point agarose for 393 imaging at 26–27 °C. For whole-brain calcium imaging, Tg(huc:GCaMP6) transgenic 394 zebrafish embryos were collected and kept at 28.5 °C in Holtfreter's solution. At 4-5 dpf, 395 the larvae were mounted in 1% low-melting-point agarose for imaging at 26–27 °C.

396

397 Preparation of fixed *Drosophila* brain samples

398 All Drosophila experimental procedures were conducted with ethical approval from the 399 Animal Care and Use Committee of Tsinghua University. Female Drosophila brains were 400 dissected and fixed in 4% paraformaldehyde (PFA, Cat# AR-0211, Dingguo Biotech, 401 China) at room temperature for 30 mins on a shaker. Each brain was rehydrated with 402 0.3% Triton X-100 (Solarbio 524A0513) in phosphate-buffered saline (PBS) for 4×20 403 mins at room temperature and then incubated in block solution (5% goat serum in washing 404 buffer) for 30 mins at room temperature. The brain was then incubated overnight with 405 primary antibody (mouse monoclonal nc82 (Developmental Studies Hybridoma Bank)), 406 which was diluted at 1:500 in block solution at 4 °C. The brain was then washed in 0.5%

Page 18 of 29

407 PBST for 3×1 hour at room temperature. Finally, the brain was mounted directly for 408 imaging by LFM.

409 Imaging of *Drosophila* embryos

410 All Drosophila embryos (Fig. 3) expressed histones tagged with EGFP (His2Av, 411 BL24163). The collection and preparation of Drosophila embryos were performed according to the commonly used protocol⁴⁰. Two-hour *Drosophila* embryos were 412 413 collected within a specific collection chamber. After incubation at 25 °C for 10 hours, 414 each embryo was attached to a glass microscope slide with double-sided sticky tape. We 415 used forceps to carefully roll the embryo on the tape until its chorion popped open. Then, 416 the embryo was transferred to the glue line on a dish (Ibidi µ-Dish, 35 mm, high) and 417 covered with mineral oil (Sigma-Aldrich, Halocarbon 27 oil) for live imaging.

418 Mouse experiments

419 All procedures involving mice were approved by the Institutional Animal Care and Use 420 Committee of Tsinghua University. We used both male and female C57BL/6 mice 10 421 weeks to 6 months old without randomization or blinding. We performed the craniotomy 422 as previously described⁴¹, with a window size of ~8 mm×8 mm. Then, we installed a flat 423 optical window and cemented a custom-made coverslip (D-shape) and aluminum head 424 posts to the skull. For acute imaging, we used adult double-transgenic Rasgrf2-2A-425 dCre/Ai148D mice (JAX No.: 022864 and 030328) to specifically label cortical layer 2/3 neurons⁴². For chronic imaging, adult C57BL/6 mice injected with diluted AAV9-hSyn-426 427 GCaMP6s virus (from BrainVTA Technology Co., Ltd., China) were allowed to recover 428 for at least 2 weeks after craniotomy. During LFM imaging, awake mice were placed in 429 a tube with the head restrained under the objective.

430 Data analysis

Page 19 of 29

All data analyses were performed with customized MATLAB (MathWorks, MATLAB
2018) programs and Amira (Thermo Fisher Scientific, Amira 2019). The hardware was
controlled using LabVIEW 2018 (National Instruments). The 3D rendering of the
volumes in figures and videos was performed by Amira. The 3D tracking of 7
representative blood cells in the heart of the zebrafish larvae was carried out manually in
MATLAB.

437

438 Neural activity extraction

439 The calcium responses in both zebrafish and mice were extracted directly through signal 440 averaging of the manually selected ROIs covering the selected neurons. The ROIs were 441 $\sim 8 \times 8 \times 10 \ \mu\text{m}^3$ in size for zebrafish larvae and $\sim 10 \times 10 \times 10 \ \mu\text{m}^3$ in size for mice to match 442 the size of the neuron. The temporal traces of neural activity were calculated by $\Delta F/F_0$ = $(F - F_0)/F_0$, where F is the raw averaged intensity of the ROI, and F_0 is the baseline 443 444 fluorescence intensity. To estimate F_0 for each ROI, we first calculated the average 445 intensity of the trace and averaged all time points with signals below 120% of the 446 calculated average.

447

448 **Data availability**

449 All relevant data are available from the corresponding authors upon reasonable request.

450

451 Code availability

We will open all of codes with example datasets in Google Drive and Github after thepaper is accepted.

454

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Page 20 of 29

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465 **Author contributions**

466 Q.D., X.J., and J.W. conceived and designed the project. Q.D. and X.J. supervised the 467 research. Z.L. and J.W. designed and built the optical system. Y.Z., X.J. and J.W. 468 conducted the numerical simulation and developed the deconvolution algorithm with the 469 multiscale scattering model. J.W. and D.J. designed the biological experiments. X.L. 470 conducted the hardware synchronization. J.X. derived the scattering model in incoherent 471 conditions. T.Z. designed the graphical user interface for software control. D.J. prepared the zebrafish larvae. Z.L., Y.Z., D.J. and J.W. conducted most biological experiments, 472 data collection and volume reconstructions. X.L. and Y.C. conducted algorithm 473 performance optimization. Y.Z. designed the system calibration method. J.W., Z.L., Y.Z., 474 475 X.J., and Q.D. prepared figures and wrote the manuscript with input from all authors.

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477 Competing financial interests

478 The authors declare no competing financial interests.

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480 Materials & correspondence

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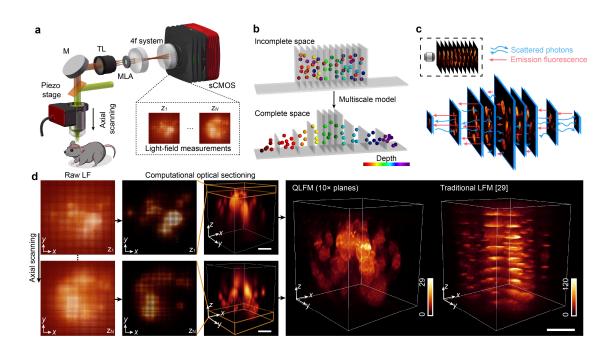
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Page 22 of 29

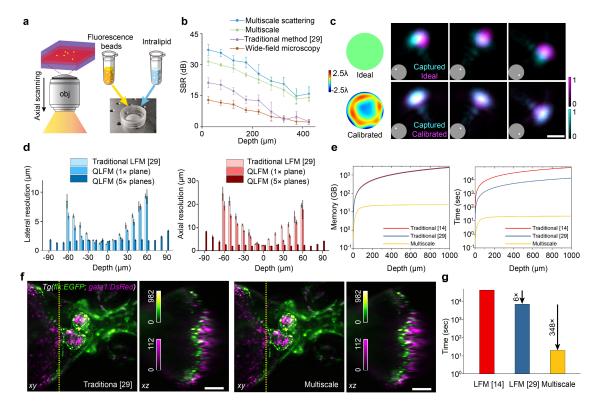
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581 Fig. 1 | Schematic of quantitative light-field microscopy (OLFM). a. Experimental 582 setup of our QLFM system with a simple microlens array (MLA) inserted at the image 583 plane for snapshot phase-space measurements. A piezo stage is used for high-speed axial 584 scanning at a large step size periodically. **b**, Concept of the multiscale model. Incomplete 585 space used in traditional LFM reconstruction results in strong background noise and loss 586 of quantitative properties in complicated environments. We apply different sampling rates 587 in 3D based on the effective resolution of LFM at different axial planes to model a large 588 volume for background rejection with an orders-of-magnitude reduction in computational cost. c, Schematic of the multiscale scattering model. We differentiate the multiple-589 590 scattered photons from native emission fluorescence in the multislice model based on the 591 first Born approximation to retrieve 3D fluorescence quantitatively in deep tissue. d, 592 Illustrations of the algorithm by imaging GFP-labeled B16 tumor spheroids. Due to the 593 extended depth of field, even the out-of-focus fluorescence far from the native objective 594 plane has apparent depth-dependent features in LFM, which can be reconstructed in the 595 multiscale model for computational optical sectioning. The axially scanned LF images of 596 10 planes can be realigned into multiple angular focal stacks to reconstruct the entire 597 volume as a whole without artifacts. QLFM shows greatly improved resolution and 598 contrast over traditional LFM which reconstructs each subvolume separately. Scale bars, 599 30 µm.

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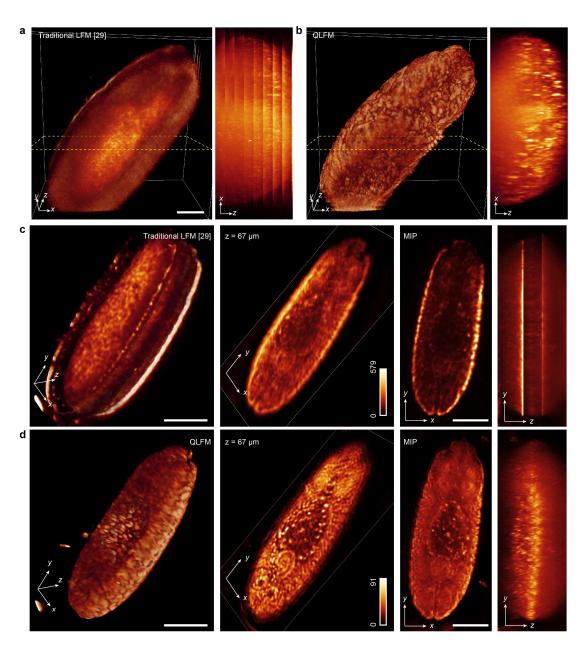


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602 Fig. 2 | Characterization of quantitative light-field microscopy (OLFM). a. 603 Illustrations of the SBR characterization experiment. We fabricated the scattering 604 phantom with the mixture of 0.025% 2-µm fluorescence beads, 1% intralipid, 1% agarose 605 in a petri dish. Then we imaged the sample with a 40×1.0 NA water-immersion objective 606 at different penetration depths with WFM and LFM. b, SBR curves of the fluorescence 607 beads at different penetration depths in the intralipid-based tissue-mimicking phantom 608 obtained by WFM, traditional LFM, QLFM with the multiscale model only, and QLFM 609 with the multiscale scattering model. We chose 10 fluorescence beads with the highest 610 fitting degrees for each block covering approximately 40 µm. QLFM shows ~20 dB 611 improvement in the SBR over WFM, indicating an improved penetration depth in deep 612 tissue. c, Comparisons among the experimental PSF, the ideal PSF without aberrations, 613 and the calibrated PSF of several selected angular components marked in the inset under 614 the 40×1.0 NA water-immersion objective. The calibrated wavefront of the system 615 aberration estimated by our iterative phase-retrieval algorithm is shown on the left. d, 616 Lateral and axial resolution at different axial planes in traditional LFM and QLFM with 617 1 and 5 axially scanned planes, which is estimated by the FWHM of subdiffraction-618 limited fluorescence beads. For each block covering 10 µm, we chose 10 fluorescence

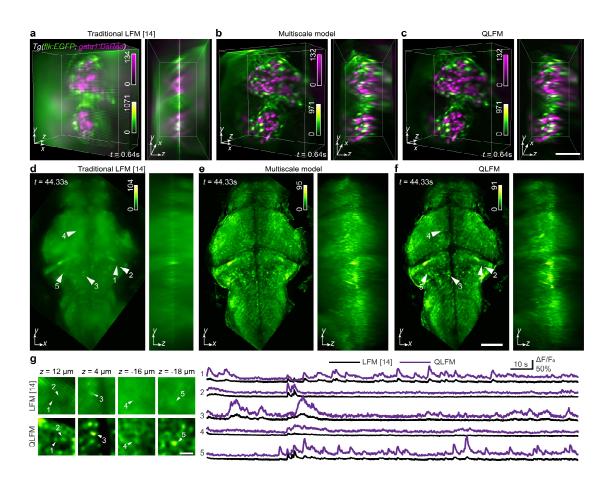
619 beads with the highest fitting degree for statistical analysis. e, The curves of the required 620 memory and computation time versus the reconstructed depth range for each volume by different methods with a $20 \times /0.5$ NA objective, indicating that the multiscale model is 621 622 essential to cover a large depth of range for computational optical sectioning. f, 623 Orthogonal MIPs of the beating heart in zebrafish larvae reconstructed by different 624 methods with a large axial range. The multiscale model shows similar performance as 625 traditional methods with orders-of-magnitude reduction in computational costs. g, The 626 bar graph shows the time required by different methods to reconstruct the volumes shown

627 in f, covering about ~ $700 \times 700 \times 560 \ \mu\text{m}^3$. Scale bars, 5 μm (c) and 100 μm (f).





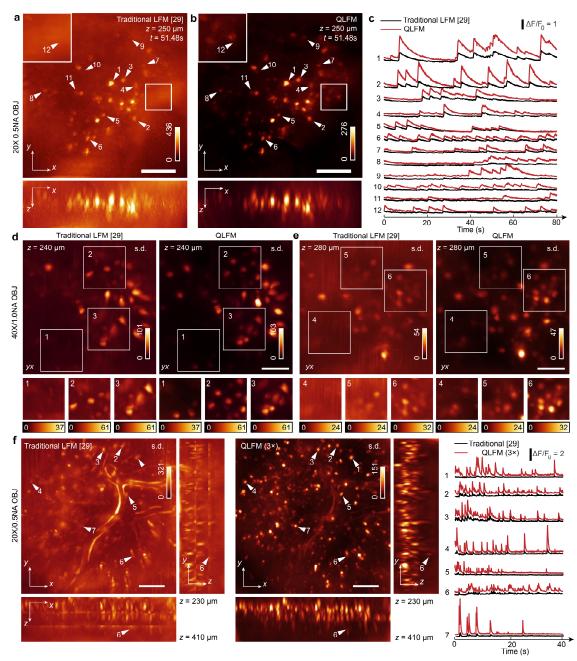
629 Fig. 3 | Experimental comparisons on the *Drosophila* embryo with high-speed axial 630 scanning. a-b, 3D rendered volumes and 180-µm-xz MIPs at the same time point of 631 traditional LFM and QLFM imaged with a $40 \times /1.0$ NA water-immersion objective at a 632 step of 15 µm. QLFM show much better contrast and resolution than traditional LFM 633 without artifacts, illustrating the capability of computational optical sectioning by QLFM 634 with the improved penetration depth. c-d, The comparisons between traditional LFM and QLFM with a 20×/0.5NA objective in the form of 3D rendered volumes, slices, and 635 636 orthogonal MIPs with axial scanning at a step of 50 µm indicating the uniform resolution of QLFM without edge artefacts. Scale bars, 50 µm (**a-b**) and 100 µm (**c-d**). 637





639 Fig. 4 | High-speed volumetric imaging in larval zebrafish. a-c, 3D rendered volumes 640 of the beating heart at the same time point reconstructed by the traditional LFM, QLFM 641 with the multiscale model only, and QLFM with the multiscale scattering model 642 (Supplementary Video 2). Successive improvements can be observed with significantly 643 reduced artifacts and background for quantitative imaging. d-f, Orthogonal maximum-644 intensity projections (MIP) of the whole brain at the same time point reconstructed by the 645 traditional LFM, QLFM with the multiscale model only, and QLFM with the multiscale 646 scattering model, illustrating the effectiveness of computational optical sectioning in 647 densely labeled samples (Supplementary Video 3). g, Zoom-in slices of the same neurons 648 marked in d and f and their temporal traces for comparison, illustrating the improved 649 SBR. Scale bars, 50 μ m (**a-c**), 100 μ m (**d-f**) and 20 μ m (**g**).

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Fig. 5 | **3D functional imaging in awake mouse brains. a-b**, Orthogonal MIPs of GCaMP6s-labeled neurons at t=51.48 s reconstructed by traditional LFM and QLFM with a 20×/0.5NA objective, indicating the reduced background with computational optical sectioning (Supplementary Video 4). More neurons were revealed by QLFM in the mouse cortex with the native objective plane at a depth of ~ 250 µm. c, Temporal traces of the marked neurons in a and b, demonstrating the quantitative calcium responses in QLFM with improved contrast. **d-e**, Orthogonal MIPs of the standard deviation across 2000

659	volumes imaged at a center depth of 240 μm and 280 μm in the cortex, respectively, under
660	a $40 \times /1.0$ NA water-immersion objective (Supplementary Video 5). f , Orthogonal MIPs
661	of the standard deviation across 500 volumes for GCaMP6f-labeled L2/3 neurons in an
662	awake behaving mice. The video was captured with high-speed axial scanning at a step
663	of 50 μm for 3 planes at 24 Hz with a 20×/0.5 NA objective. Temporal traces of several
664	marked neurons at different depths are shown on the right. QLFM shows uniform
665	resolution and consistent calcium responses across a large depth range, while there is
666	barely contrast in traditional LFM due to severe background. Scale bars, 100 μ m (a-b , f)
667	and 50 µm (d-e).