## A novel single-cell based method for breast cancer prognosis

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## Abstract

Breast cancer prognosis is challenging due to the heterogeneity of the disease. Various computational methods using bulk RNA-seq data have been proposed for breast cancer prognosis. However, these methods suffer from limited performances or ambiguous biological relevance, as a result of the neglect of intra-tumor heterogeneity. Recently, single cell RNA-sequencing (scRNA-seq) has emerged for studying tumor heterogeneity at cellular levels. In this paper, we propose a novel method, *scPrognosis*, to improve breast cancer prognosis with scRNA-seq data. *scPrognosis* uses the scRNA-seq data of the biological process Epithelial-to-Mesenchymal Transition (EMT). It firstly infers the EMT pseudotime and a dynamic gene co-expression network, then uses an integrative model to select genes important in EMT based on their expression variation and differentiation in different stages of EMT, and their roles in the dynamic gene co-expression network. To validate and apply the selected signatures to breast cancer prognosis, we use them as the features to build a prediction model with bulk RNA-seq

data. The experimental results show that *scPrognosis* outperforms other benchmark breast cancer prognosis methods that use bulk RNA-seq data. Moreover, the dynamic changes in the expression of the selected signature genes in EMT may provide clues to the link between EMT and clinical outcomes of breast cancer. *scPrognosis* will also be useful when applied to scRNA-seq datasets of different biological processes other than EMT.

## Author summary

Various computational methods have been developed for breast cancer prognosis. However, those methods mainly use the gene expression data generated by the bulk RNA sequencing techniques, which average the expression level of a gene across different cell types. As breast cancer is a heterogenous disease, the bulk gene expression may not be the ideal resource for cancer prognosis. In this study, we propose a novel method to improve breast cancer prognosis using scRNA-seq data. The proposed method has been applied to the EMT scRNA-seq dataset for identifying breast cancer signatures for prognosis. In comparison with existing bulk expression data based methods in breast cancer prognosis, our method shows a better performance. Our single-cell-based signatures provide clues to the relation between EMT and clinical outcomes of breast cancer. In addition, the proposed method can also be useful when applied to scRNA-seq datasets of different biological processes other than EMT.

## Introduction

Cancer prognosis plays an important role in clinical decision making. Traditionally, cancer prognosis is based on several clinical and pathological variables such as tumor size, lymph node status, histological grades, and so on [1]. However, these clinicopathological factors are insufficient for cancer prognosis because cancer is heterogeneous at the molecular (e.g., genes) level. Hence, recent clinical guidelines have highlighted the importance of using multi-gene tests to select patients who should receive adjuvant therapies [2]. The multiple genes in the tests are known as cancer signatures, which are crucial to cancer prognosis. Cancer signatures can be identified by in vivo biological experiments. For example, the LM method [3] analyzed 10 transcriptomics in the cell lines and chose 54 genes associated with lung metastagenicity 11 and virulence. However, these experiments cannot be done on human beings. 12 Meanwhile, experiments on animals would not guarantee that the same conclusion can 13 be drawn for humans. Therefore, computational methods are needed to identify cancer 14 signatures from existing data, including gene expression data and clinical data.

Computational methods for breast cancer prognosis have shown some successes. Generally, these methods select the prognostic genes from a large number of human 17 genes and then train survival models based on the selected genes. For instance, PAM5018 starts with an extended intrinsic gene set from previous studies, then selects genes 19 based on their contributions in terms of distinguishing the five intrinsic breast cancer subtypes [4]. The RS method selects 16 cancer signatures from 250 published candidate 21 genes [5]. Mamma [6] and GGI97 [7] use a statistical test to choose the genes which 22 differentially express between two distinct groups of tumors. Most of these methods use 23 supervised algorithms to select the candidate genes and only GGI97 ranks genes based on the similarities between gene expression profiles and tumor histologic grades. Based 25 on the selected genes, most methods train linear regression models to predict the outcomes of the new coming patients. The clinical benefits of these prognostic genes for 27 breast cancer are well studied on the traditional transcriptomics data, and some of the methods have approved by the Food and Drug Administration for commercial use [2].

The common feature of existing computational methods for breast cancer prognosis is that they are based on bulk RNA-seq data, which can lead to the following problems. 31 Firstly, different tumor samples in bulk RNA-seq data have different proportions of 32 cancer cells (named tumor purities) that can bias the results of these methods [8]. The traditional RNA sequencing technology measures the average expression levels of genes for an ensemble of cells from a tumor sample to obtain the so called bulk RNA-seq data. As a solid tumor tissue is a mixture of normal and cancer cells, the bulk RNA-seq data hence contain mixed signals and the non-cancerous components may have influences on 37 genomic analysis of the bulk RNA-seq data or even bias the results [8]. There are works to uncover tumor purity and correct the bias in the detecting of differential genes [9] and identification of cancer subtypes [10]. It has been shown that differentially 40 expressed genes and cancer subtypes are crucial to the selection of cancer signatures. 41

Secondly, with bulk RNA-seq data, we may not able to determine how gene signatures are related to cell level perturbation during cancer progression. Increasing evidence shows that the expression patterns of genes are heterogeneous from cell to cell [11]. These stochastic expression patterns trigger cell fate decisions and can affect cancer initiation and progress. However, based on the bulk RNA-seq data, the existing cancer prognosis methods cannot determine the correlation between clinical outcomes and dynamic gene behaviors along cellular trajectory.

Single cell RNA sequencing (scRNA-seq) has emerged recently and has many advantages over bulk RNA sequencing. Firstly, scRNA-seq does not have the tumor purity problem because it is possible to discover the existence of the micro-environment 51 cell populations from scRNA-Seq data (See a review on this in [12]). Secondly, 52 scRNA-seq is a powerful method to comprehensively characterize the cellular 53 perturbation or stages within tissues [13] as it measures the expression of genes in individual cells. Additionally, scRNA-seq trajectory methods can provide a precise understanding of dynamic cell fate differentiation (See a systematic comparison in [14]). Through continuous cell stages along the pseudo-trajectory, we can observe the 57 stochastic nature of gene expression [15]. Currently, scRNA-seq data are mostly used to detect cell types or to find novel biomarkers. As far as we know, there has been no work 59 conducted on using scRNA-seq data to improve breast cancer prognosis. 60

In this work, we develop a novel method called *scPrognosis* to use scRNA-seq data 61 to identify breast cancer signatures. Epithelial to Mesenchymal Transition (EMT) is a 62 biological process associated with carcinogenesis, invasion, metastasis, and resistance to 63 therapy in cancer [16]. We hypothesize that genes that play an important role in EMT 64 are associated with breast cancer prognosis. Hence, we use an EMT scRNA-seq dataset for identifying the breast cancer signatures for prognosis. To fully exploit the scRNA-seq data towards optimal identification of breast cancer signatures, we propose to assess the importance of genes in the EMT process by integrating the following three measures: (1) 68 their median absolute deviation in expression level; (2) their differentiation in different 69 stages of EMT; (3) their roles in the dynamic gene co-expression network in EMT. 70 scPrognosis uses a linear model to integrate the three measures for inferring breast 71 cancer signatures. The significant difference between our method and the bulk RNA-seq 72 data based methods is that we reconstruct the pseudotemporal trajectory known as 73 pseudotime of cells [17] in EMT and incorporate this information into differential gene 74 expression analysis and dynamic gene co-expression network construction. To validate the prognostic ability of these discovered gene signatures and apply them to breast cancer prognosis, we use them to build prediction models using bulk RNA-seq data as the data contains matched clinical information (and there are no single cell data with matched clinical information available). We apply *scPrognosis* to four independent bulk breast cancer datasets, ranging from about 200 to 1200 patients. The experimental results show that *scPrognosis* improves cancer prognosis compared with other 81 benchmark breast cancer prognosis methods based on bulk RNA-seq data. A significant 82 portion of the discovered prognostic genes is proved to be associated with breast cancer 83 prognosis. Moreover, the dynamic changes in the expression trends of the genes provide clues to the link between EMT transition and clinical outcomes of breast cancer.

## Materials and methods

## Overview of *scPrognosis*

scPrognosis contains five steps as depicted in Fig 1. In step 1, MAGIC [18] and a gene filter are used to pre-process the noisy and high-dimensional scRNA-seq data. In step 2, 89 EMT pseudotime, pseudotime series gene expression data, and dynamic gene co-expression network are inferred from the scRNA-seq data. In this step, firstly VIM 91 gene expression level and pseudotemporal trajectory estimated by the Wanderlust algorithm [19] are used to identify EMT pseudotime for all cells in the scRNA-seq 93 dataset. The EMT pseudotime describes the gradual transition of the single-cell transcriptome during the EMT transition process and helps to study gene expression dynamics in different EMT transition stages. Secondly, pseudotime series gene expression data is obtained by ordering cells in the scRNA-seq dataset from epithelial stage to mesenchymal stage according to the EMT pseudotime. Thirdly, from the ordered scRNA-seq data, a dynamic gene co-expression network is constructed by using the LEAP R package [20]. In step 3, based on the ordered scRNA-seq data, three 100 methods are adopted to obtain the different gene ranking measures, including Median 101 Absolute deviation (MAD), switchde [15] and Google PageRank. MAD and switchde 102

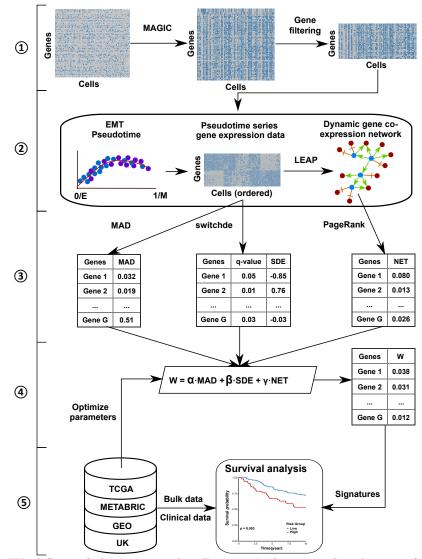


Fig 1. Workflow of the proposed *scPrognosis* framework. There are five main steps in *scPrognosis*, including: ① Pre-processing scRNA-seq data; ② Inferring EMT pseudotime, pseudotime series gene expression data, and dynamic gene co-expression network from the filtered scRNA-seq data; ③ Ranking genes by three measurements; ④ Prioritizing genes via an integrative model; ⑤ Cancer prognosis using the top N ranked genes. The first four steps are based on scRNA-seq data while the last step uses bulk RNA-seq data to select parameters.

are used to compute gene importance based on their expression level. Google *PageRank* <sup>103</sup> ranks genes based on their roles in the dynamic gene co-expression network. In step 4, <sup>104</sup> we integrate the three different rankings obtained in step 3 to prioritize genes. In step 5, <sup>105</sup> the top N ranked genes are selected as signatures to predict the survival outcomes of <sup>106</sup> breast cancer patients in bulk RNA-seq data. Details of each step are described in the <sup>107</sup> following sub-sections. <sup>108</sup>

#### Pre-processing scRNA-seq data

In the first step, *scPrognosis* pre-processes the input scRNA-seq dataset. The 110 scRNA-seq dataset is a data matrix with G rows and C columns, where each column 111 stores the expression levels of G genes in a single cell. Due to the low amounts of 112 transcripts in a cell, an expressed gene may not be detected during sequencing with 113 current scRNA-seq technology. This can lead to missing values of expressed genes, which 114 is called the "dropout" phenomenon. For example, scRNA-seq data by the *inDrops* 115 platform only have about 30% effective reads for each cell. The dropout events can lead 116 to significant bias in gene-gene relationships and other downstream analyses [18]. 117

MAGIC [18] is a method to denoise scRNA-seq data and impute the missing gene 118 expression profiles. To overcome the sparsity and noise of the raw count matrix, 119 MAGIC uses PCA (principal component analysis) components to calculate cell-cell 120 distance matrix. The distance matrix is converted to a cell-cell affinity (similarity) 121 matrix by an adaptive Gaussian kernel method. The affinity matrix is symmetrized and 122 Markov-normalized to construct a Markov transition matrix. The final denoised and 123 imputed data matrix is obtained by multiplying the exponentiated Markov transition 124 matrix by the raw count matrix. Based on the information sharing across similar cells, 125 MAGIC recovers gene expression from the dropout and other sources of noise. 126

After the imputation, we filter out genes with low coverage rates and low expression <sup>127</sup> levels because these genes are most likely not expressed. It is suggested that these genes <sup>128</sup> should be removed when searching for discriminative genes in microarray data [21] and <sup>129</sup> implementing the *switchde* method. More experimental details of *MAGIC* and the gene <sup>130</sup> filter method are provided in Section 2 in S1 File. <sup>131</sup>

## Inferring EMT pseudotime, pseudotime series gene expression data, and dynamic gene co-expression network

Recently, it has been proposed that EMT transition occurs through continuum stages 134 and there are several intermediate stages known as hybrid (partial) 135 epithelial/mesenchymal (E/M) stages. Interestingly, these hybrid E/M stages are stable 136 and can be the endpoint of a transition [16]. This means that cells may not go through 137 the whole EMT transition and stop at a hybrid E/M stage. Switch-like genes that are 138

up- or down-regulation along the EMT trajectory may induce cells to undergo a <sup>139</sup> transition from one hybrid E/M stage to another hybrid E/M stage. Applying the <sup>140</sup> proposition to the continuum stages of EMT transition, we could characterize the <sup>141</sup> nature of switch-like genes and dynamic gene-gene relationships along the EMT <sup>142</sup> trajectory. The strength of switch-like changes and the importance of genes in the <sup>143</sup> dynamic gene co-expression network will be used to rank genes in our methods. <sup>144</sup>

In this step, we will firstly infer the EMT pseudotime, and then based on the <sup>145</sup> obtained pseudotime, we construct the pseudotime series gene expression dataset from <sup>146</sup> the scRNA-seq dataset, which will be used in Step 3 to capture the switch-like changes <sup>147</sup> along the pseudotime. At the same time, we also construct the dynamic gene <sup>148</sup> co-expression network based on the pseudotime series gene expression dataset. <sup>149</sup>

Even we do not have the true time-series data of individual cells undergoing EMT 150 transition, we still can use scRNA-seq trajectory method to infer pseudotime from static 151 scRNA-seq data. We assume that the EMT trajectory is a linear topology of ordered 152 single cells, and cells represent the entire developmental process from E to M, i.e. each 153 cell in the ordered sequence represents a different stage of the E to M transition. The 154 trajectory then provides an indication of the timeline of the EMT transition, known as 155 the EMT pseudotime. The pseudotime can be obtained using different approaches. One 156 simple way to approximate the EMT pseudotime from a static scRNA-seq dataset is to 157 order cells by their expression values of VIM [18], and we denote this pseudotime as 158 VIM-time. Another way to infer the EMT pseudotime from a scRNA-seq dataset is by 159 using the Wanderlust algorithm [19]. Wanderlust is a graph-based method to infer a 160 linear tread to recapitulate cell trajectory. Wanderlust converts scRNA-seq data into a 161 k-nearest neighbor graph (k-NNG). In k-NNG, each node is a cell, and each cell is 162 connected to k cells that have similar expression profiles. Then Wanderlust generates 163 several l-out-of-k-nearest neighbor graphs (l-k-NNGs) by randomly keeping l of 164 k-nearest neighbors for each node in the k-NNG. For each l-k-NNG, Wanderlust 165 identifies a trajectory score for each cell using a repetitive randomized shortest path 166 algorithm. The final trajectory is computed by the average over all graph trajectories. 167 We use the final trajectory as the EMT pseudotime named W-time. All the parameter 168 assignments of Wanderlust can be found in Section 2 in S1 File. 169

After obtaining the EMT pseudotime, we have a trajectory score ranging from 0 to 1  $_{170}$ 

for each cell which indicates its developmental stage of the E to M transition. Therefore, the scRNA-seq dataset (a data matrix) can be converted to a pseudotime series gene expression dataset by sorting cells (columns) based on the EMT pseudotime.

Then we construct a dynamic gene co-expression network from the above obtained 174 pseudotime series expression dataset. Each node of the network represents a gene in the 175 dataset. To capture the dynamic regulatory relationship between two genes, we use 176 LEAP (lag-based Expression Association Pseudotime-series) [20] package to determine 177 if there is an edge between two nodes. Given C cells ordered by the EMT pseudotime, 178 the  $MAC_counter()$  function in LEAP calculates the maximum absolute correlation 179 (MAC) between the two nodes across all the time lags  $l \in \{0, 1, \dots, C/3\}$  using the 180 pseudotime series expression data. If the MAC between two nodes q and tq is tested to 181 be statistically significant, an edge is added from  $q \to tq$ . 182

#### The three measures for ranking genes

 scPrognosis combines three measures to rank genes, including Median Absolute
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 Deviation (MAD) of gene expression profiles, the Switch-like Differentiation of genes in
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 different stages of EMT (SDE), and the roles played by genes in the gene co-expression
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 NETwork in EMT (NET). In this step, scPrognosis calculates the three measures
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 individually before they are integrated into the next step. In the following, we describe
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 the details of calculating each of the measures.
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Let  $(e_1, e_2, \ldots, e_C)$  represents the expression profile of a gene  $g \in \{1, \ldots, G\}$ , where C is the number of cells. The MAD of the gene can be computed as:

$$m_g = median(e_1, e_2, \dots, e_C)$$

$$MAD(g) = median(|e_1 - m_g|, |e_2 - m_g|, \dots, |e_C - m_g|)$$
(1)

where *median()* is the function returning the median value of a given variable.

To calculate SDE, we use the software tool *switchde* [15] which can estimate the <sup>193</sup> differentiation of switch-like genes in different stages of EMT. *switchde* defines a sigmoid <sup>194</sup> function as shown in Eq 2 to fit the profile of a gene g with regard to a pseudotime  $t_c$  (c <sup>195</sup> is the index of a cell and  $c \in \{1, ..., C\}$ ). In Eq 2,  $\mu_g^0$ ,  $k_g$  and  $t_g^0$  are the average peak <sup>196</sup>

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expression value, the active strength and the active time of g.  $k_g$  presents how quickly the gene g is up or down regulated along the pseudotime. We define SDE(g) as the switch-like differential expression level of the gene g, and  $SDE(g) = k_g$ .

$$f(t_c; \mu_g^0; k_g; t_g^0) = \frac{2\mu_g^0}{1 + exp(-k_g(t_c - t_g^0))}$$
(2)

switchde adopts the gradient-based L-BFGS-B optimization algorithm [22] to obtain the maximum likelihood estimates of the parameters  $\mu_g^0$ ,  $k_g$ , and  $t_g^0$ . switchde also do the hypothesis testing associated with gene differential expression and adjust p-value by the Benjamini-Hochberg method. 201

To calculate NET, we follow the modified Google PageRank algorithm presented in [23]. The modified Google PageRank algorithm is used to calculate the regulatory importance of a gene in the dynamic gene co-expression network. Suppose there are G 206 genes, the ranking of a gene g is defined as the following: 207

$$NET(g) = \frac{1-d}{G} + d \sum_{tg \in T(g)} \frac{NET(tg)}{L(tg)}$$
(3)

where d is the damping factor in PageRank and is set to 0.85 by default. tg is a target 200 of g and we use T(g) to denote the set of all targets of g. L(tg) is the number of genes 200 which regulate tg. From Eq 3, we can see that the rank of a gene depends on the rank of 210 all its target genes. NET(g) is initialized to the same value for all g, and can be 211 calculated using a iterative algorithm until it converges. 212

#### Prioritizing genes via an integrative model

Although all the three measures are all associated with the clinical outcomes of cancer, 214 none of the individual measure suffices to cancer prognosis. The expression variation 215 (MAD) helps with distinguishing different cell populations. Genes with high expression 216 variations are also of great clinical interest. The differentiation in different stages of 217 EMT is corresponding to the gene behavior along the trajectory of EMT. SDE helps 218 identify the genes that switch on and off alternatively during the trajectory to trigger 219 EMT. The gene co-expression network is important for us to better understand the 220 mechanisms of cell differentiation and carcinogenesis at a systems level. NET helps us 221

discover hub regulatory genes that target the highest degree of a series of genes (called targets) in the network. It is believed that the hub regulatory genes are more closely related to cancer and have more biological significance compared with their targets [24]. Because each of them only reflects one aspect of the importance of a gene, and a combination of the three would be a more comprehensive measure. Therefore, we propose a linear model to integrate the three measures to obtain the final score for each gene.

Before integrating the three measures, we normalize them as follows:

$$MAD'(g) = \frac{MAD(g)}{\sum_{g=1}^{G} MAD(g)}$$
$$SDE'(g) = \frac{SDE(g)}{\sum_{g=1}^{G} SDE(g)}$$
$$NET'(g) = \frac{NET(g)}{\sum_{g=1}^{G} NET(g)}$$
(4)

Then we integrate the normalised individual measures as follows.

$$W(g) = \alpha \cdot MAD(g) + \beta \cdot SDE(g) + \gamma \cdot NET(g)$$
(5)

#### Cancer prognosis using the top N ranked genes

From the list of ranked genes obtained in Step 4, we select the top N ranked genes as cancer signatures. Then the Cox proportional hazards (PH) model [25] is trained based on these cancer signatures and bulk RNA-seq data. The PH model assumes that the effect of covariances on the survival outcomes is time-independent. Given survival time

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t, the general function of the PH model is defined as the following:

$$h(t|X) = h_0(t)exp(\beta'X) \tag{6}$$

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where  $\beta'$  is a  $N \times 1$  vector that holds estimated regression coefficients, X is the expression data of the top N genes, and  $h_0(t)$  is the baseline hazard function. The risk score of a new patient is calculated by 244

$$r_i = \beta' (X_i - mean(X)) \tag{7}$$

where  $X_i$  is the expression data of the top N genes of the new patient *i*, and *mean()* is the function returning the average values of given data.

#### Performance evaluation

**Concordance index** (C-index) [26] is commonly used to validate the predictive 248 ability of cancer prognostic models. Let  $z_i$  and  $r_i$  be the potential survival time and the 249 risk score predicted using Eq 7 for patient i, respectively. C-index is equal to the 250 concordance probability  $P(r_i > r_j | z_i < z_j)$  for a randomly selected pair of patients i 251 and j. However, we cannot observe potential survival time for some patients who are 252 lost to follow-up or event free at the end of a study (right censored). Hence the actually 253 observed survival time  $t_i = min(z_i, c_i)$ , where  $c_i$  is the potential right censoring time. 254 Let  $\delta_i$  be the censoring status. An event (e.g. death or relapse) is developed within the 255 study period when  $\delta_i = 1$ . For the right censoring data, C-index can be defined as the 256 following: 257

C-index = 
$$\frac{\sum \sum_{i < j} [I(t_i < t_j)I(r_i > r_j)I(\delta_i \equiv 1) + I(t_i > t_j)I(r_i < r_j)I(\delta_j \equiv 1)]}{\sum \sum_{i < j} [I(t_i < t_j)I(\delta_i \equiv 1) + I(t_i > t_j)I(\delta_j \equiv 1)]}$$
(8)

where I() is an indication function. C-index ranges from 0 to 1. The bigger the C-index is, the more accurate of a model will be. 259

Hazard ratio. To assist clinicians in tailoring treatment strategy, we often need to stratify patients into the high-risk group and the low-risk group via dichotomizing the predicted risk scores around their median value. Therefore, we need an accuracy 260

measure to compare different methods. We use the hazard ratio (HR) as a accuracy measure, similar to other work [27]. We binarize the predicted risk scores to obtain the predicted groups R for patients. Then we estimate the risk difference between the two survival groups by Cox's proportional hazards model as: 266

$$h(t|R) = h_0(t)exp(\beta R) \tag{9}$$

where  $h_0(t)$  is the same as that in Eq 9. The quantity  $exp(\beta)$  is defined as HR, which indicates the risk difference between the two groups of patients. The larger the HR is, the larger discrimination between the low- and high-risk group becomes, and therefore the better the prediction method will be.

Kaplan-Meier survival curve. The Kaplan-Meier (KM) survival curve [28] 271 combined with the Log-rank [29] test can identify whether the two risk groups show 272 significantly different survival patterns. In the KM curve plot, the Y-axis is the 273 probability of surviving in a given length of time, and the X-axis is survival time. The 274 KM curves should have different characteristics and should not overlap for different 275 groups predicted by a good method. The Log-rank test determines whether the survival 276 curve estimated for each group is identical or not. If the p-value of the Log-rank rest is 277 less than 0.05, the survival curves are statistically significantly different. 278

#### Implementation

scPrognosis has been implemented using MATLAB and R packages. All the datasets 200 and the R scripts to reproduce the results in this paper are available online 201 at https://github.com/XiaomeiLi1/scPrognosis. 202

## Results

#### Data sources and preparation

scRNA-seq data. In this paper, we use the scRNA-seq data of HMLE breast cancer 285 cell lines from [18] to identify the EMT pseudotime for each cell and then select cancer 286 signatures. The cells were stimulated with TGF-beta to induce EMT transition and the 287

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single-cell sequencing was performed using the *inDrops* platform. There are 28910
transcripts effectively measured in 7523 single cells. The scRNA-seq data can be
download from the Gene Expression Omnibus (GEO) database
(https://www.ncbi.nlm.nih.gov/geo/) under accession number GSE114397.

Bulk RNA-seq data. For training and validating the cancer prognosis model based 292 on the selected signatures, we use bulk RNA-seq data of 2979 breast cancer patients 293 from four different repositories, including TCGA (753 samples), METABRIC (1283 294 samples), GEO (736 samples) and UK (207 samples). Most of the breast cancer samples 295 possess detailed clinical data, such as age, nodal, stage, grade, survival time, and event 296 status. The TCGA and METABRIC datasets contain both overall survival time (OS) 297 and relapse-free survival (RF) endpoints. The GEO and UK datasets only have the 298 endpoints of relapse-free survival. The TCGA dataset was downloaded from the TCGA 200 data portal (http://firebrowse.org/) and the dataset consists of level 3 mRNA 300 expression data of primary breast cancer. The METABRIC dataset [30] was downloaded 301 from the European Genome-phenome Archive (https://www.ebi.ac.uk/ega/ 302 accession number EGAS0000000083, approval needed). The GEO dataset consists of 5 303 datasets: GSE12276 (204 samples), GSE19615 (115 samples), GSE20711 (88 samples), 304 GSE21653 (252 samples) and GSE9195 (77 samples). We merge the five GEO datasets 305 into a bigger dataset and adjusted the batch effects by the ComBat algorithm from the 306 sva library [31]. The UK (known as GSE22219) dataset contains 207 early-invasive 307 breast cancer cases with complete follow-up clinical data in 10 years. Both the GEO 308 and UK datasets were downloaded from the Gene Expression Omnibus repository 309 (https://www.ncbi.nlm.nih.gov/geo/). We summarize the details of these bulk 310 RNA-seq datasets in Table 1. 311

Table 1. Th	e description	of bulk RNA-s	eq datasets.
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Dataset	Platform	Sample size	#transcripts
TCGA	Illumina RNA-seq	753	13088
METABRIC	Illumina RNA-seq	1283	25191
GEO	Affymetrix microarray	736	18503
UK	Illumina microarray	207	22172

## scPrognosis is better than benchmark methods for risk score prediction

As discussed in the previous section, the SDE and NET measures have a considerable dependency on the pseudotime. We investigate the performance of two versions of *scPrognosis* based on different pseudotime, including VIM-time and W-time which are based on the expression profile of gene *VIM* and the *Wanderlust* algorithm, respectively. Section 2 in S1 File has more experiment details of calculating VIM-time and W-time. We denote the two versions of the implementations of *scPrognosis* as scP.V and scP.W, corresponding to the use of VIM-time and W-time, respectively.

To illustrate that scRNA-seq data can help to select prognostic signatures of breast 321 cancer, we choose six widely used breast cancer prognosis benchmark methods that are 322 based on the signatures selected from bulk RNA-seq data. More information about the 323 benchmark methods can be found in Section 1 and Table 1 in S1 File. We compare the 324 performance of the two versions of *scPrognosis* (scP.V and scP.W) with the benchmark 325 methods on the datasets listed in Table 1. We report the results on TCGA and 326 METABRIC according to the overall survival (OS) and relapse-free (RF) time. For the 327 GEO and UK datasets, we report the results on the relapse-free time. Table 2 shows the 328 C-indices and the mean ranking scores of all the methods compared. The C-index 329 shown is the average of 100 times 10-fold cross-validation on a dataset. Based on the 330 C-indices, mean ranking scores are calculated by Friedman's test, which is a two-way 331 analysis of variance by ranks for related samples. scP.W is better than other methods 332 since it wins three times. Compared to the benchmark methods, scP.W outperforms all 333 the methods for the prediction of the risk of RF time on the TCGA and UK datasets. 334 Moreover, from the mean ranking results, we can see that *scPrognosis* overall 335 outperforms the benchmark methods. 336

To test whether a method performs significantly better than the other, we conduct the Wilcoxon signed-rank test based on the C-indices of *scPrognosis* and the benchmark methods. The result shows that both scP.V and scP.W perform significantly better than *Mamma* (the p-values are 0.017 and 0.018, respectively) and *GGI97* (the p-values are 0.016 and 0.017, respectively). scP.V significantly outperforms LM (p-value = 0.03) while scP.W is superior to RS significantly (p-value = 0.046). Moreover, as previously

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	PAM50	Mamma	RS	GGI97	Endo	LM	scP.V	scP.W
TCGA(OS)	0.63	0.55	0.58	0.51	0.54	0.63	0.63	0.61
TCGA(RF)	0.61	0.58	0.63	0.57	0.59	0.56	0.61	0.68
METABRIC(OS)	0.59	0.57	0.58	0.55	0.60	0.58	0.59	0.60
METABRIC(RF)	0.63	0.61	0.63	0.58	0.65	0.61	0.63	0.64
GEO	0.53	0.54	0.58	0.48	0.55	0.51	0.56	0.56
UK	0.60	0.62	0.63	0.61	0.63	0.64	0.67	0.70
Mean rank	4.50	2.92	5.33	1.33	5.17	3.67	6.08	7.00

Table 2. Performance Comparison of cancer prognosis using benchmark methods and the proposed methods (scP.V and scP.W).

The top-performing result is highlighted for each dataset. The result of C-index is the average of 100 times 10-fold cross-validation on each dataset.

shown (Table 2), according to the mean ranking scores, our methods still marginally <sup>343</sup> improve the other two methods, *PAM50* and *Endo*. <sup>344</sup>

In summary, we only use scRNA-seq data to measure the importance of genes, whereas the benchmark methods use signatures directly obtained from breast cancer clinical data and prior knowledge. Even so, the results have shown that both scP.V and scP.W achieve better or competitive performance compared with the benchmark methods. This indicates scRNA-seq data can improve the performance of breast cancer prognosis, and the signatures of EMT potentially are high quality predictors for breast cancer prognosis.

# scPrognosis is better than benchmark methods for risk group prediction

In this section, we evaluate *scPrognosis* using the Hazard Ratio (HR) criterion, in 354 comparison with the six benchmark methods. For each method, we stratify patients into 355 two groups using the risk scores calculated by the method. If a patient's risk score 356 bigger than the median value the patient is put into the high-risk group, otherwise the 357 patient is put into the low-risk group. The HRs for all the methods are reported in 358 Table 3. We observe that the two versions of scPrognosis (scP.V and scP.W) win once 359 and twice, respectively, but PAM50, RS, and Endo each wines once this time. Based on 360 the mean ranking results, we can conclude that overall *scPrognosis* outperforms the 361 benchmark methods in stratifying patients into two risk groups. 362

Then we use the Wilcoxon signed-rank test to test the significance of the results on the HR criterion. Again, both scP.V and scP.W have perform significantly better than 364

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METABRIC(OS)         4.90         4.67         5.99         2.51         4.80         3.60         4.71           METABRIC(RF)         5.17         3.87         5.29         2.47 <b>7.16</b> 3.95         5.93	
$\begin{array}{cccccccc} {\rm TCGA(RF)} & {\bf 1.61} & 1.01 & 1.26 & 0.97 & 1.17 & 1.09 & 1.30 \\ {\rm METABRIC(OS)} & 4.90 & 4.67 & 5.99 & 2.51 & 4.80 & 3.60 & 4.71 \\ {\rm METABRIC(RF)} & 5.17 & 3.87 & 5.29 & 2.47 & {\bf 7.16} & 3.95 & 5.93 \\ \end{array}$	
METABRIC(OS)         4.90         4.67         5.99         2.51         4.80         3.60         4.71           METABRIC(RF)         5.17         3.87         5.29         2.47 <b>7.16</b> 3.95         5.93	1.32
METABRIC(RF) 5.17 3.87 5.29 2.47 <b>7.16</b> 3.95 5.93	1.45
	6.07
CEO 1.20 1.52 <b>2.50</b> 0.01 1.95 0.96 1.27	5.45
GEO 1.20 1.52 <b>2.50</b> 0.91 1.85 0.86 1.37	1.51
UK 1.54 1.72 1.62 1.68 2.17 1.74 2.90	3.27
Mean rank 4.83 3.33 5.33 1.58 5.25 3.33 6.00	6.33

Table 3. Comparison of the performances of risk group predictions using	
benchmark methods and the proposed methods (scP.V and scP.W).	

The top-performing result is highlighted for each dataset. The result of hazard ratio is the average of 100 times 10-fold cross-validation on each dataset.

Mamma (the p-values are 0.047 and 0.031, respectively), GGI97 (the p-values are 0.016 and 0.016, respectively) and LM (the p-values are 0.016 and 0.030, respectively).

#### Evaluation using independent test

According to the results in Tables 2 and 3, among the two different implementations of 368 scPrognosis, scP.W outperforms scP.V. So we choose scP.W as our final method to identify breast cancer signatures. For further evaluating the robust of scP.W in breast 370 cancer prognosis, we conduct independent tests on three bulk RNA-seq datasets. Due to 371 the small sizes of the GEO, and UK datasets, we don't train scP.W based on these 372 datasets. Fig 2 shows the independent test results on TCGA when training on 373 METABRIC. Figs 2(A) and 2(C) show the comparison of scP.W and the benchmark 374 methods. In these two figures, the Y-axis is the C-index, and the X-axis is the category 375 of methods. Based on C-index, scP.W achieves the best results in predicting overall 376 survival and relapse-free survival time. Figs 2(B) and 2(D) are the KM curves and the 377 Log-rank test of risk group prediction using scP.W on the TCGA dataset. The results 378 show that scP.W successfully stratifies patients into two risk groups of relapse and 379 overall survival. The p-values by the Log-rank test are less than 0.05, which indicates 380 that two risk groups have significantly different survival patterns, and the high-risk 381 group has lower survival probability than that of the low-risk group. The TCGA 382 dataset is the second-largest dataset in breast cancer and widely used in breast cancer 383 research. We report the comparison results of our method based on the TCGA dataset 384 and the current breast cancer prognostic methods in Table 3 in S1 File. The results also 385 show that scP.W achieves the best results in cancer prognosis. 386

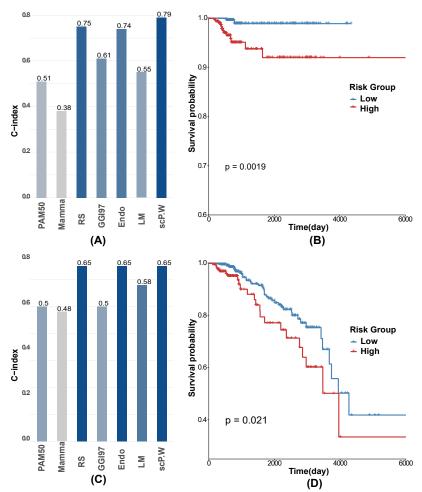


Fig 2. scP.W outperforms benchmark methods. (A) The bar chart of C-indices of scP.W and the benchmark methods on TCGA(OS); (B)The KM curve and Log-rank test of scP.W on TCGA(OS); (C)The bar chart of C-indices of scP.W and the benchmark methods on TCGA(RF); (D)The KM curve and Log-rank test of scP.W on TCGA(RF).

#### Breast cancer signatures identified by scPrognosis

From the previous sections, we see the EMT signatures discovered by our methods are good breast cancer signatures too. To further validate these signatures, we compare the signatures discovered by our method with those discovered by benchmark methods. The EMT signatures are the top N ranked genes based on the scores calculated by Eq 5. Parameters N,  $\alpha$ ,  $\beta$ , and  $\gamma$  are determined by the 10-fold cross-validation results on bulk RNA-seq data.

scP.W selects 10 genes as breast cancer signatures, *KRT15*, *UBE2C*, *TOP2A*, *KRT6B*, *MKI67*, *HMGB2*, *ASPM*, *CDC20*, *KIF20A* and *CDK*, when trained on

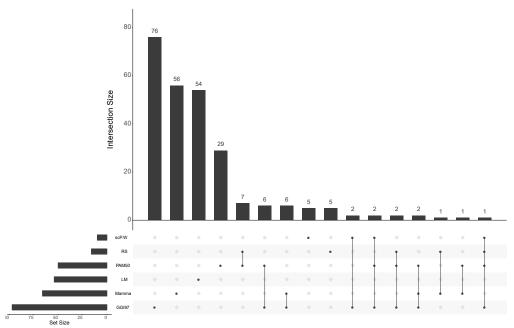


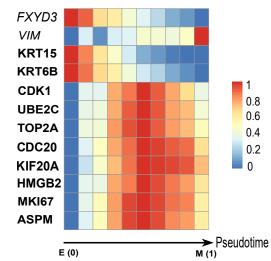
Fig 3. Overlap of signatures among different methods. The bottom left bar shows the number of signatures in each method. The dotted lines and the diagram on top show that the interaction overlaps among different methods. There are three genes (UBE2C, MKI67, and CDC20) in common with the scP.W, PAM50, and GGI97. Besides, scP.W has another two genes that only overlap with GGI97 (ASPM and KIF20A). 5 out of 10 genes using scP.W have proved to associate with breast cancer prognosis.

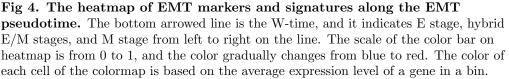
METABRIC. Comparing the 10 genes with the signatures used by the benchmark methods, we find 5 genes (UBE2C, MKI67, ASPM, CDC20, and KIF20A) showed up in 397 one or more benchmark methods. ASPM is the common signature when scP.W is 398 trained on TCGA and METABRIC. In our model, high ASPM levels are associated 300 with adverse prognostic factors and shorter survival and relapse-free time. Recent 400 evidence suggests that ASPM promotes prostate cancer stemness and progression and 401 has important clinical and therapeutic significance [32]. Besides ASPM, other common 402 signatures also have been proved to relate to breast cancer prognosis. For instance, high 403 UBE2C expression is associated with poor prognosis in breast cancer, especially 404 basal-like breast cancer [33]. CDC20 over-expression means short-term breast cancer 405 survival [34]. Fig 3 shows the diagram of overlapping genes among different methods. 406 The diagram shows that a significant portion of the prognostic genes discovered by our 407 method is overlapped with the current signatures of breast cancer prognosis. Though 408 the clinical significance of the other five signature genes discovered by our method 409

(*KRT15*, *TOP2A*, *KRT6B*, *HMGB2*, and *CDK1*) is not clear at present, they can be novel signatures for human breast cancer. There have been researches investigating the relationship between these genes and breast cancer. For example, *KRT6B* and *KRT15* were found to be the makers of basal-like breast cancers [35], and *TOP2A* expression levels were reported to have a significant association with metastasis-free survival in node-negative breast cancer [36].

#### Correlation between EMT markers, breast cancer signatures

### and the EMT pseudotime





This paper is the first work to identify switch-like differential expression genes along 418 the EMT pseudotime to understand their efficacy in deciphering the survival of breast 419 cancer patients. No matter we use VIM-time or W-time, the models built have a good 420 agreement on the performance. This is because W-time is highly related to the 421 expression profile of VIM (the Pearson correlation is 0.46). For visualizing the dynamic 422 behavior of genes in different stages of EMT, we divide W-time into 10 equal sized bins 423 that present pseudo-stages of EMT. The expression level of a gene in a bin is calculated 424 by the average of the profile during the time interval. Fig 4 shows the tendencies of the 425 10 cancer signatures along the pseudo-stages. We also plot the expression profiles of 426

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genes along W-time in Fig 1 in S1 File. Only *KRT15* and *KRT6B* are down-regulated by the EMT transition while other signatures do not vary at the E and M stages, but peak at the hybrid E/M stages. Recent experimental and theoretical evidence suggests that the hybrid E/M stages are stable phenotypes and is associated with aggressive tumor progression [37]. Our method demonstrates the relevance of the hybrid E/M phenotypes to patient survival in breast cancer.

We also visualize the EMT markers' dynamic behavior to determine whether the 433 W-time could successfully model the cell evolved from the E stage to the M stage. The 434 results from Fig 4 and Fig 1 in S1 File both show that the marker of epithelial 435 (FXYD3) is down-regulated along W-time, while the marker of mesenchymal (VIM) is 436 up-regulated along W-time. The tendencies of EMT markers along the W-time are 437 consistent with prior knowledge that the expression of VIM increases while the 438 expression of FXYD3 decreases during the E to M transition. Therefore, W-time can 439 successfully model the continuum of the E to M transition, and the results about the 440 correlation between breast cancer signatures and EMT are reliable. 441

### Enrichment analysis of the signatures discovered by *scPrognosis* 442

We validate discovered breast cancer signature genes against the literature knowledge of pathways using the WikiPathways (http://www.wikipathways.org) platform [38]. The results in Table 4 show that the 10 signatures are highly relevant to the regulation of cancer. For instance, pathways 1, 2, 3, and 8 are direct pathways of cancer, and others are important pathways involved in the process of tumorigeneses. 447

We also conduct gene ontology enrichment analysis for the 10 breast cancer 448 signatures. From Table 4 in S1 File, we can see that they are regulators of cell cycle 449 progress and ubiquitin-protein ligase activities. Table 1 in S1 File shows that current 450 signatures based on bulk RNA-seq data are also enriched in cell cycle regulation. Recent 451 studies reveal the important roles of ubiquitin-protein ligase activity played in breast 452 cancer [39, 40].

Id	Maps	P-value
1	Gastric Cancer Network 1 WP2361	9.07E-05
2	Gastric Cancer Network 2 WP2363	1.04E-04
3	Retinoblastoma Gene in Cancer WP2446	9.33E-06
4	Regulation of sister chromatid separa- tion at the metaphase-anaphase transi- tion WP4240	7.48E-03
5	PPAR Alpha Pathway WP2878	1.29E-02
6	Cell Cycle WP179	1.56E-03
7	ATM Signaling Pathway WP2516	1.98E-02
8	Integrated Cancer Pathway WP1971	2.18E-02
9	ATM Signaling Network in Develop- ment and Disease WP3878	2.23E-02
10	Regulation of Microtubule Cytoskele- ton WP2038	2.28E-02

Table 4. WikiPathways mapped pathways for the 10 breast cancer signatures.

The pathways are highly relevant to the regulation of cancer.

## Discussion and conclusion

Breast cancer is a complex disease caused by intricate genetic and molecular alterations. 455 Thus traditional clinicopathological factors are not sufficient for the accurate prognosis of breast cancer. Recently, a wide range of computational methods have been proposed 457 to identify multi-genes for breast cancer prognosis, and some of the methods have been 458 approved for commercial use, including PAM50, Mamma, and RS test. These methods 459 lead to a revolution in the breast cancer treatment paradigm. However, all of the 460 progress in cancer prognosis has not been enough to overcome therapy resistance in 461 breast cancer under current cancer therapeutics. Some tumor cells acquire resistance to 462 targeted cancer therapy, which leads to worse survival of cancer patients. scRNA-seq 463 can reveal genes that affect cell fate decision by monitoring the expression of genes in 464 different cell states and sub-populations. In this paper, we use scRNA-seq data to detect 465 signatures related to EMT that affect the clinical outcomes of breast cancer patients. 466

For almost two decades, the prospect that EMT may play an important role in tumor stemness, metastasis, and drug resistance has been vigorously debated. However, evidence demonstrating the prognosis power of EMT markers in breast cancer clinical studies has not been identified. Recently scRNA-seq is used to identify the continuum of EMT transition. We try to use the EMT scRNA-seq data to link the EMT related genes to breast cancer survival. To investigate how genes are related to cell level perturbation during EMT, we use the computational method *Wanderlust* to infer the 477

EMT pseudotime. We integrate multiple measurements, MAD, SDE, and NET to 474 measure the importance of a gene based on its expression variance, its dynamic 475 differentiation, and its role in the dynamic gene co-expression network. We apply our 476 method to four breast cancer cohorts. The experimental results illustrate that 477 scPrognosis is more efficient than the benchmark methods based on bulk RNA-seq data 478 and single-cell based methods only using individual measurements (Table 2 in S1 File). 479 Our work also emphasizes the benefit of EMT mechanisms that incorporate background 480 knowledge for identifying biologically relevant signatures of cancer prognosis. And the 481 results show the good performance of the signatures in breast cancer prognosis. 482

Moreover, the results of *scPrognosis* may give us some clues for interpreting the EMT process. We look at the dynamic change of the gene expression along the EMT pseudotime. Interestingly, only two identified breast cancer signature genes are down-regulated along the EMT pseudotime, while the remaining genes peak at the intermediate of the E to M transition. These genes could be novel biomarkers for the hybrid E/M stages. We assume that the hybrid E/M stage is more relevant to patient survival as supported by the recent study in [41].

To identify the activity of EMT-related breast cancer signatures, we conduct a pathway analysis of the discovered breast cancer signatures. The results show that a significant number of the identified signatures are enriched in the pathways associated with cancer. Through the GO enrichment analysis, the signatures found by our method are closely related to the biological functions of cell cycle activity and ubiquitin-protein ligase activity, and the latter activity is not showing up in most of the current signatures.

However, there is no universal method that outperforms all the other methods. We still need to discover novel mechanisms involved in breast cancer progress, metastasis or resistance. In the future, our method can be extended to improve breast cancer prognosis by immune cell trajectories. Understanding immune cell development and response to disease is a crucial step for conquering cancer metastasis by immunotherapy. Recently there are some single cell experiments for investigating cellular dynamics in the context of immunology [42].

In conclusion, we have proposed a novel method *scPrognosis* for breast cancer prognosis based on scRNA-seq data. *scPrognosis* uses an integrative model to infer 505

breast cancer signatures based on MAD, SDE, and NET measurements. We empirically compared our method with the existing methods on four breast cancer datasets. The results show that the scRNA-seq based method is a good and useful method for breast cancer prognosis. The signatures detected by our method show the link between EMT and the clinical outcomes of breast cancer, which may give some clues for current cancer therapeutics.

## Supporting information

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S1 File. Supplementary information.

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