

1 Protein solubility is controlled by global structural flexibility

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10 11 12 **ABSTRACT**

13 **Summary**

14 Recombinant protein production is a widely used technique in the biotechnology industry and
15 biomedical research, yet only a quarter of target proteins are soluble and can be purified.
16 Failures are largely due to low protein expression and solubility. We have discovered that
17 global structural flexibility, which can be modeled by normalised B-factors, accurately
18 predicts the solubility of 12,216 recombinant proteins expressed in *Escherichia coli*. We have
19 optimised B-factors, and derived a new set of values for solubility scoring that further
20 improves the prediction accuracy. We call this new predictor the ‘Solubility-Weighted Index’
21 (SWI). Importantly, SWI outperforms many existing protein solubility prediction tools. We
22 have developed ‘SoDoPE’ (Soluble Domain for Protein Expression), a web interface that
23 allows users to choose a protein region of interest for predicting and maximising both protein
24 expression and solubility.

25 26 **Availability**

27 The SoDoPE web server and source code are freely available at <https://tisigner.com/sodope>
28 and <https://github.com/Gardner-Binflab/TIsigner>, respectively.
29 The code and data for reproducing our analysis can be found at
30 https://github.com/Gardner-Binflab/SoDoPE_paper_2019.

31 32 33 34 **INTRODUCTION**

35 High levels of protein expression and solubility are two major requirements of successful
36 recombinant protein production (Esposito and Chatterjee 2006). However, recombinant
37 protein production is a challenging process because almost half of the proteins fail to be
38 expressed and half of the successfully expressed proteins are insoluble
39 (<http://targetdb.rcsb.org/metrics/>). These failures hamper protein research, with particular
40 implications for structural, functional and pharmaceutical studies, that require soluble and
41 concentrated protein samples (Kramer *et al.* 2012, Hou *et al.* 2018). Therefore, predicting
42 solubility, and engineering protein sequences for enhanced solubility is an active area of
43 research. Notable protein engineering approaches include mutagenesis, truncation (i.e.,
44 expression of partial protein sequences), or fusion with a solubility-enhancing tag (Waldo

45 2003, Esposito and Chatterjee 2006, Trevino *et al.* 2007, Chan *et al.* 2010, Kramer *et al.*
46 2012, Costa *et al.* 2014).

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48 Protein solubility depends on extrinsic factors such as ionic strength, temperature and pH, as
49 well as intrinsic factors—the physicochemical properties of the protein sequence and
50 structure—molecular weight, amino acid composition, hydrophobicity, aromaticity, isoelectric
51 point, structural propensities and the polarity of surface residues (Wilkinson and Harrison
52 1991, Chiti *et al.* 2003, Tartaglia *et al.* 2004, Diaz *et al.* 2010). Many solubility prediction tools
53 have been developed around these features, ranging from the use of simple statistical
54 models (e.g., linear and logistic regressions) to sophisticated machine learning models (e.g.,
55 support vector machines and neural networks) (Hirose and Noguchi 2013, Habibi *et al.* 2014,
56 Hebditch *et al.* 2017, Sormanni *et al.* 2017, Heckmann *et al.* 2018, Wu *et al.* 2019, Yang *et*
57 *al.* 2019).

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59 In this study, we investigated the experimental outcomes of 12,216 recombinant proteins
60 expressed in *Escherichia coli* from the ‘Protein Structure Initiative: Biology’ (PSI: Biology)
61 (Chen *et al.* 2004, Acton *et al.* 2005). We showed that protein structural flexibility is more
62 accurate than other protein sequence properties in predicting solubility (Vihinen *et al.* 1994,
63 Craveur *et al.* 2015). Flexibility is a standard feature that has previously been overlooked in
64 solubility prediction. On this basis, we derived a set of 20 values for the standard amino acid
65 residues and used them to predict solubility. We call this new predictor the
66 ‘Solubility-Weighted Index’ (SWI). SWI is a powerful predictor of solubility, and a good proxy
67 for global structural flexibility. In addition, SWI outperforms many protein solubility prediction
68 tools.

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72 **RESULTS**

73 **Global structural flexibility performs well at predicting protein solubility**

74 To determine which protein sequence properties can accurately predict protein solubility, we
75 examined the experimental outcomes of 12,216 recombinant proteins expressed in *E. coli*
76 (the PSI: Biology dataset; see Supplementary Table S1A) (Chen *et al.* 2004, Acton *et al.*
77 2005). These proteins were expressed either with a C-terminal or N-terminal 6xHis fusion
78 tag (pET21_NESG and pET15_NESG expression vectors, N=8,780 and 3,436,
79 respectively). They were previously curated and labeled as ‘Protein_Soluble’ or
80 ‘Tested_Not_Soluble’ (Seiler *et al.* 2014), based on the soluble analysis of cell lysate using
81 SDS-PAGE (Xiao *et al.* 2010). A total of 8,238 recombinant proteins were found to be
82 soluble, in which 6,432 of them belong to the pET21_NESG dataset.

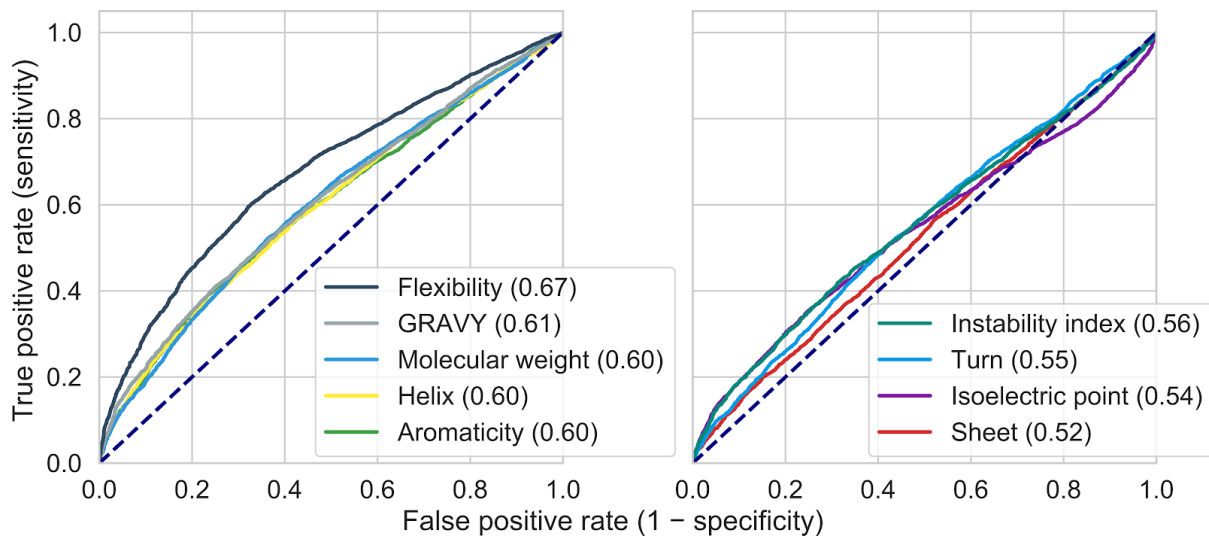
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84 We first computed the standard protein sequence properties, namely molecular weight,
85 isoelectric point, secondary structure composition (sheet, turn, and helix), aromaticity, Grand
86 Average of Hydropathy (GRAVY), global structural flexibility and instability index using the
87 ProtParam module of Biopython (Kyte and Doolittle 1982, Guruprasad *et al.* 1990, Bjellqvist
88 *et al.* 1993, 1994, Lobry and Gautier 1994, Vihinen *et al.* 1994, Cock *et al.* 2009). We
89 compared the prediction accuracy of these features using Receiver Operating Characteristic
90 (ROC) analysis. To our surprise, flexibility outperformed other features in predicting protein

91 solubility [Fig 1, Area Under the ROC Curve (AUC) = 0.67]. We then calculated 9,920
92 miscellaneous protein sequence properties using the 'protr' R package (Xiao *et al.* 2015),
93 which include amino acid composition, pseudo-amino acid composition, autocorrelation,
94 CTD (Composition, Transition, Distribution), conjoint triad descriptors, quasi-sequence-order
95 descriptors and profile-based descriptors (Xiao *et al.* 2015). Among these features, the
96 amphiphilic pseudo-amino acid composition for cysteine residues showed the highest AUC
97 score, which is still lower than the AUC score for flexibility (Supplementary Fig S1 and Table
98 S2, AUC = 0.65).

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103 **Fig 1. Global structural flexibility outperforms the other standard protein sequence**
104 **properties in protein solubility prediction.** ROC analysis of the standard protein
105 sequence features for predicting the solubility of 12,216 recombinant proteins expressed in
106 *E. coli* (the PSI:BiologY dataset). AUC scores (perfect = 1.00, random = 0.50) are shown in
107 parentheses. The ROC curves are shown in two separate panels for clarity. Dashed lines
108 denote the performance of random classifiers. AUC, Area Under the ROC Curve; GRAVY,
109 Grand Average of Hydropathy; PSI:BiologY, Protein Structure Initiative:BiologY; ROC,
110 Receiver Operating Characteristic.

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113 **The Solubility-Weighted Index (SWI) is an improved approach to score solubility**

114 Protein structural flexibility, in particular, the flexibility of local regions, is often associated
115 with function (Craveur *et al.* 2015). The calculation of flexibility is usually performed by
116 assigning a set of 20 normalised B-factors—a measure of vibration of C alpha atoms (see
117 Discussion)—to a protein sequence and averaging the values by a sliding window approach
118 (Karplus and Schulz 1985, Ragone *et al.* 1989, Vihinen *et al.* 1994, Smith *et al.* 2003). We
119 reasoned that such sliding window can be approximated by a more straightforward
120 arithmetic mean for calculating global structural flexibility, which is analogous to the
121 computation of GRAVY. We applied this arithmetic mean approach to the PSI:BiologY
122 dataset and compared different sets of published, normalised B-factors (Bhaskaran and
123 Ponnuswamy 1988, Ragone *et al.* 1989, Vihinen *et al.* 1994, Smith *et al.* 2003) as follows:

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$$\frac{1}{L} \left(\sum_{i=1}^L B_i \right) \quad (1)$$

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127 where B_i is the normalised B-factor of the amino acid residue at the position i , and L is the
128 sequence length. Among these sets of B-factors, solubility scoring using the most recently
129 published set of normalised B-factors produced the highest AUC score (Supplementary Fig
130 S2, AUC = 0.66).

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132 To improve the prediction accuracy, we initialised an iterative refinement method with the
133 most recently published set of normalised B-factors. This was done by maximising AUC
134 scores with the Nelder-Mead optimisation algorithm (Nelder and Mead 1965). In order to
135 account for phylogenetic relationships between proteins we clustered all 12,216 PSI:Biography
136 protein sequences by 10% similarity using USEARCH (Fig 2A and Supplementary Fig S3).
137 Cross-validations were conducted in a way that ensures training and testing is performed on
138 unrelated sequences. We calculated the solubility scores for the optimised weights using
139 Equation 1 and the AUC scores for each cross-validation step. Our training and test AUC
140 scores were 0.72 ± 0.00 and 0.71 ± 0.03 , respectively, showing an improvement over
141 flexibility in solubility prediction (mean \pm standard deviation; Fig 2B and Supplementary
142 Table S3).

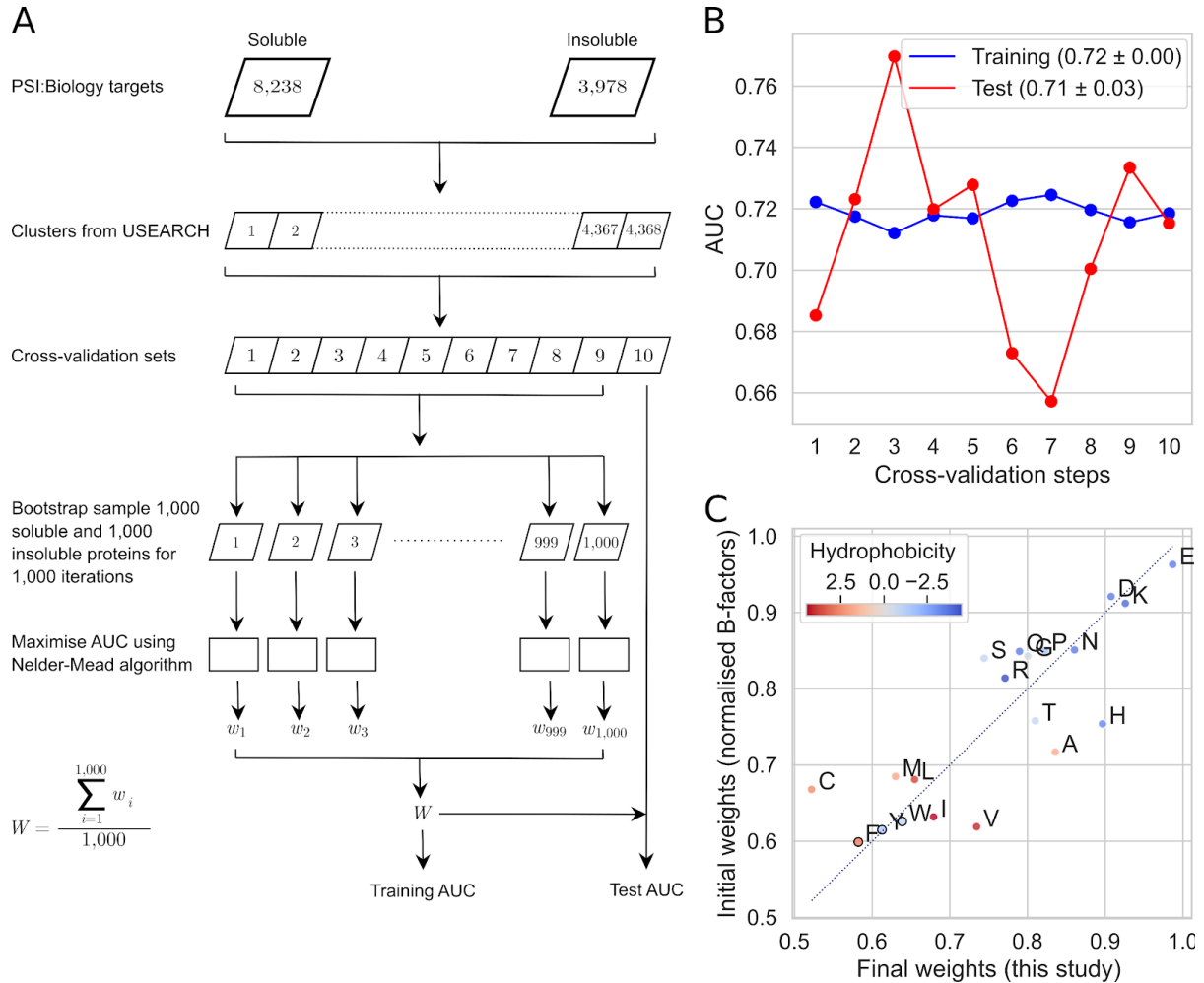
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144 The final weights were derived from the arithmetic means of the weights for individual amino
145 acid residues obtained from the cross-validation step (Supplementary Table S4).
146 Interestingly, we observed over a 20% change on the weights for cysteine (C) and histidine
147 (H) residues (Fig 2C and Supplementary Table S4). These results were in agreement with
148 the contributions of cysteine and histidine residues as shown by the AUC scores of the
149 amphiphilic pseudo-amino acid compositions for cysteine and histidine residues
150 (Supplementary Fig S1B). To ensure that these results are not artifacts, in particular due to
151 the presence of polyhistidine-tags in all the sequences, we repeated the iterative refinement
152 method using the same cross-validation sets without His tag sequences. The final weights
153 with and without His tags are nearly identical, suggesting that the approach is not
154 confounded by tag use (Supplementary Table S4, Spearman's rho = 1).

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159 **Fig 2. Derivation of the Solubility-Weighted Index (SWI).** (A) Flow chart shows an
 160 iterative refinement of the most recently published set of normalised B-factors for solubility
 161 prediction (Smith *et al.* 2003). The solubility score of a protein sequence was calculated
 162 based on an arithmetic mean of the optimised weights as Equation 1 (using W instead of B
 163). These scores were used to compute the AUC scores for training and test datasets. (B)
 164 Training and test performance of solubility prediction using the optimised weights for 20
 165 amino acid residues in a 10-fold cross-validation (mean AUC ± standard deviation). Related
 166 data and figures are available as Supplementary Table S3 and Supplementary Fig S3. (C)
 167 Comparison between the 20 initial and final weights for amino acid residues. The final
 168 weights are derived from the arithmetic mean of the optimised weights from the
 169 cross-validation step. These weights are used to calculate SWI, the solubility score of a
 170 protein sequence, in the subsequent analyses. Filled circles, which represent amino acid
 171 residues, are colored by hydrophobicity (Kyte and Doolittle 1982). Solid black circles denote
 172 aromatic amino acid residues phenylalanine (F), tyrosine (Y), tryptophan (W). Dotted
 173 diagonal line represents no change in weight. Related data is available as Supplementary
 174 Table S4. AUC, Area Under the ROC Curve; ROC, Receiver Operating Characteristic; W ,
 175 arithmetic mean of the weights of an amino acid residue optimised from 1,000 bootstrap
 176 samples in a cross-validation step.

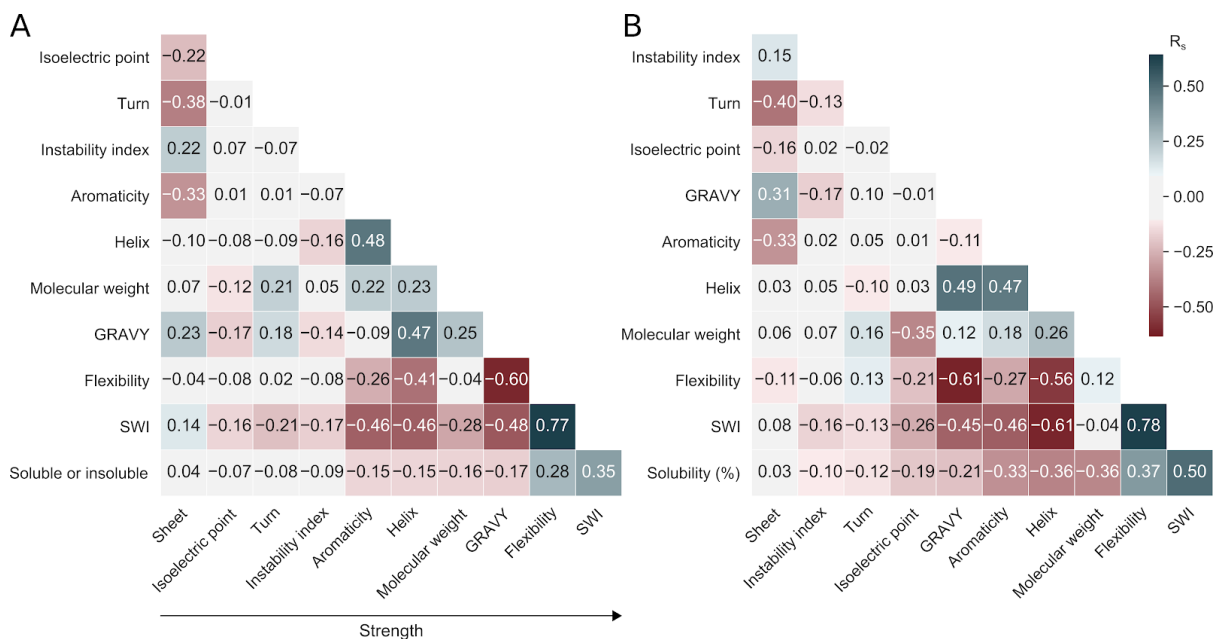
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179 To validate the cross-validation results, we used an independent dataset known as eSOL
 180 (Niwa *et al.* 2009). This dataset consists of the solubility percentages of *E. coli* proteins
 181 determined using an *E. coli* cell-free system (N = 3,198). Solubility scoring using the final
 182 weights showed a significant improvement in correlation with *E. coli* protein solubility over
 183 the initial weights (normalised B-factors) [Spearman's rho of 0.50 ($P = 9.46 \times 10^{-206}$) vs 0.40
 184 ($P = 4.57 \times 10^{-120}$)]. We call the solubility score of a protein sequence calculated using the
 185 final weights as the Solubility-Weighted Index (SWI).

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 187 We performed Spearman's correlation analysis for both the PSI:BiologY and eSOL datasets.
 188 SWI shows the strongest correlation with solubility compared to the standard and 9,920
 189 protein sequence properties (Fig 3 and Supplementary Fig S1). SWI also strongly correlates
 190 with flexibility, suggesting that SWI is still a good proxy for global structural flexibility.

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 195 **Fig 3. SWI strongly correlates with solubility.** (A) Correlation matrix plot of the solubility of
 196 recombinant proteins expressed in *E. coli* and their standard protein sequence properties
 197 and SWI. These recombinant proteins are the PSI:BiologY targets (N = 12,216) with a
 198 solubility status of 'Protein_Soluble' or 'Tested_Not_Soluble'. Related data is available as
 199 Supplementary Table S5. (B) Correlation matrix plot of the solubility percentages of *E. coli*
 200 proteins and their standard protein sequence properties and SWI. The solubility percentages
 201 were previously determined using an *E. coli* cell-free system (eSOL, N=3,198). Related data
 202 is available as Supplementary Table S6. GRAVY, Grand Average of Hydropathy;
 203 PSI:BiologY, Protein Structure Initiative:BiologY; R_s , Spearman's rho; SWI,
 204 Solubility-Weighted Index.

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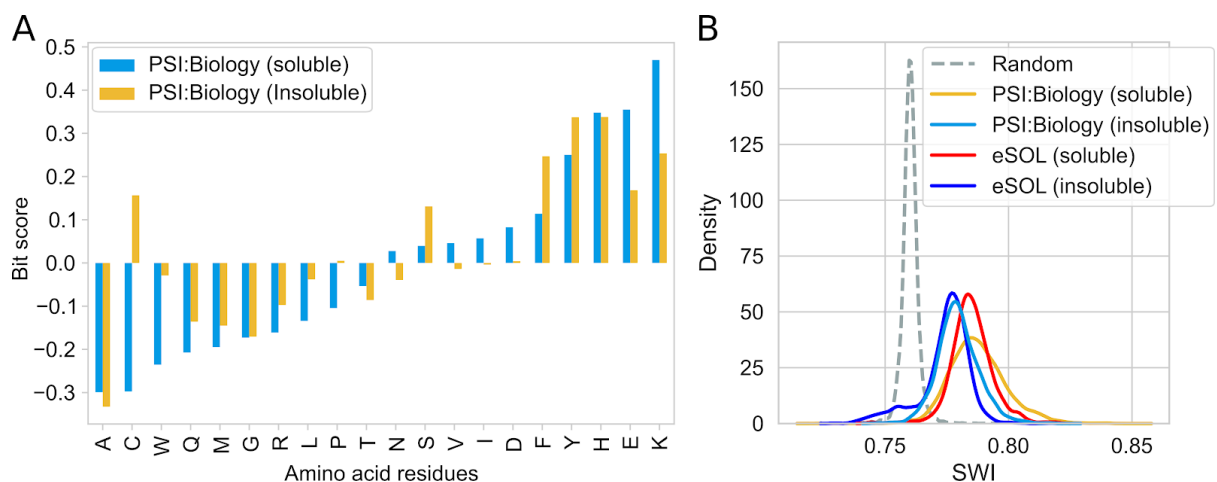
207 Next, we asked whether protein solubility can be predicted by surface amino acid residues.
 208 To address this question, we examined a previously published dataset for the protein surface
 209 'stickiness' of 397 *E. coli* proteins (Levy *et al.* 2012). This dataset has the annotation for

210 surface residues based on the protein crystal structures. Interestingly, we observed no
211 correlation between the protein surface 'stickiness' and the solubility data from eSOL
212 (Spearman's rho = 0.05, P = 0.34). Optimising weights for surface residues as above led to
213 no further improvements (i.e., the approach used to derive SWI; Spearman's rho = 0.05, P =
214 0.31). In contrast, the SWI for these sequences has a significant correlation with solubility
215 (Spearman's rho = 0.45, P = 3.88×10^{-19}). These results suggest that full-length sequence
216 should be taken into account when predicting protein solubility.

217
218 To understand the properties of soluble and insoluble proteins, we determined the
219 enrichment of amino acid residues in the PSI:BiologY targets relative to the eSOL sequences
220 (see Methods). We observed that the PSI:BiologY targets are enriched in charged residues
221 lysine (K), glutamate (E) and aspartate (D), and depleted in aromatic residues tryptophan
222 (W), albeit to a lesser extent for insoluble proteins (Fig 4A). As expected, cysteine residues
223 (C) are enriched in the PSI:BiologY insoluble proteins, supporting previous findings that
224 cysteine residues contribute to poor solubility in the *E. coli* expression system (Wilkinson and
225 Harrison 1991, Diaz *et al.* 2010).

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227 In addition, we compared the SWI for random sequences with the PSI:BiologY and eSOL
228 sequences. In general, soluble proteins have higher SWI than insoluble proteins (Fig 4B).
229 Interestingly, true biological sequences tend to have higher SWI than random sequences,
230 highlighting a clear evolutionary selection for solubility.

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235 **Fig 4. Properties of soluble and insoluble proteins. (A)** Enrichment of amino acid
236 residues in the PSI:BiologY targets relative to eSOL sequences (N = 12,216 and 3,198,
237 respectively). **(B)** Distribution of the SWI for soluble and insoluble proteins, and random
238 sequences. eSOL sequences were grouped into soluble and insoluble proteins, i.e. <30%
239 and >70% solubilities, respectively (Niwa *et al.* 2009) (Supplementary Table S1B). Random
240 sequences were generated from a length of 50 to 6,000 amino acid residues, with an
241 increment of 50 residues. A total of 12,000 random sequences were generated, 100
242 sequences for each length. PSI:BiologY, Protein Structure Initiative:BiologY; SWI,
243 Solubility-Weighted Index.

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SWI outperforms many protein solubility prediction tools

To confirm the usefulness of SWI in solubility prediction, we compared it with the existing tools including Protein-Sol (Hebditch *et al.* 2017), CamSol v2.1 (Sormanni *et al.* 2015, 2017), PaRSnIP (Rawi *et al.* 2018), DeepSol v0.3 (Khurana *et al.* 2018), the Wilkinson-Harrison model (Wilkinson and Harrison 1991, Davis *et al.* 1999, Harrison 2000), and ccSOL omics (Agostini *et al.* 2014). SWI outperforms other tools except for Protein-Sol in predicting *E. coli* protein solubility (Table 1). SWI is also the fastest solubility prediction algorithm (Table 1, Fig 5 and Supplementary Table S7).

Table 1. Comparison of protein solubility prediction methods and software.

	Approaches	Features	Runtime ^a (s per sequence)	PSI:Biolog ^b (AUC)	eSOL ^b [R _s (P-value)]
SWI	<ul style="list-style-type: none"> Arithmetic mean (this study). A set of 20 values for amino acid residues derived from normalised B-factors (Smith <i>et al.</i> 2003) by the Nelder-Mead simplex algorithm. Trained and tested using the PSI:Biolog dataset curated by DNASU (Seiler <i>et al.</i> 2014). Available at https://tisigner.com/sodope 	1	0.00 ± 0.00	0.71 ± 0.03^c	0.50 (9.46 x 10 ⁻²⁰⁶)
Protein-Sol	<ul style="list-style-type: none"> Linear model (Hebditch <i>et al.</i> 2017). Trained and tested using eSOL dataset (Niwa <i>et al.</i> 2009). Available at https://protein-sol.manchester.ac.uk/ 	10	1.16 ± 0.75	0.68	0.54 (2.37 x 10 ⁻²⁴⁰)
Flexibility	<ul style="list-style-type: none"> A sliding window of 9 amino acid residues (Vihinen <i>et al.</i> 1994). Normalised B-factors derived from PDB. Available at https://github.com/biopython/biopython 	1	0.38 ± 0.04	0.67	0.37 (7.73 x 10 ⁻¹⁰⁶)
DeepSol S2	<ul style="list-style-type: none"> Neural network models (Khurana <i>et al.</i> 2018). Trained and tested using a PSI:Biolog dataset curated by ccSOL omics. 	57 (11 types)	2069.77 ± 1613.63	0.67 ^d	0.23 (5.82 x 10 ⁻⁴¹) ^d
DeepSol			2075.93 ±	0.66 ^d	0.35

S3	<ul style="list-style-type: none"> Available at https://github.com/sameerkhurana10/DSOL_rv0.2 		1613.80		$(7.48 \times 10^{-91})^d$
DeepSol S1			2081.93 ± 1612.71	0.64 ^d	0.39 $(9.52 \times 10^{-116})^d$
CamSol intrinsic web server	<ul style="list-style-type: none"> Linear and logistic regression models (Sormanni <i>et al.</i> 2015, 2017). Trained and tested using previously published datasets (Família <i>et al.</i> 2015). Available at http://www.vendruscolo.ch.cam.ac.uk/camsolmethod.html 	4	NA	0.66	0.43 (4.53×10^{-148})
PaRSnIP	<ul style="list-style-type: none"> Gradient boosting machine model (Rawi <i>et al.</i> 2018). Trained and tested using a PSI:BiologY dataset curated by ccSOL omics. Available at https://github.com/RedaRawi/PaRSnIP 	8,477 (14 types)	2055.50 ± 1621.11	0.61	0.29 (3.57×10^{-65})
Wilkinson-Harrison model	<ul style="list-style-type: none"> Linear model using charge average and turn-forming residue fraction (Wilkinson and Harrison 1991, Davis <i>et al.</i> 1999, Harrison 2000). Available at https://github.com/brunoVbio-tools-solubility-wilkinson 	2	0.09 ± 0.00	0.55	-0.06 (1.16×10^{-4})
ccSOL omics web server	<ul style="list-style-type: none"> Support vector machine model (Agostini <i>et al.</i> 2014). Trained and tested using a PSI:BiologY dataset curated in-house. Available at http://s.tartaglialab.com/new_submission/ccsol_omics_file 	5	NA	0.51	-0.02 (0.18)

257 Boldface values are the best results.

258 ^aThe runtime was reported at the level of machine precision (mean seconds ± standard
259 deviation). A total of 10 sequences were chosen from the PSI:BiologY and eSOL datasets,
260 related to Fig 5 (see Methods).

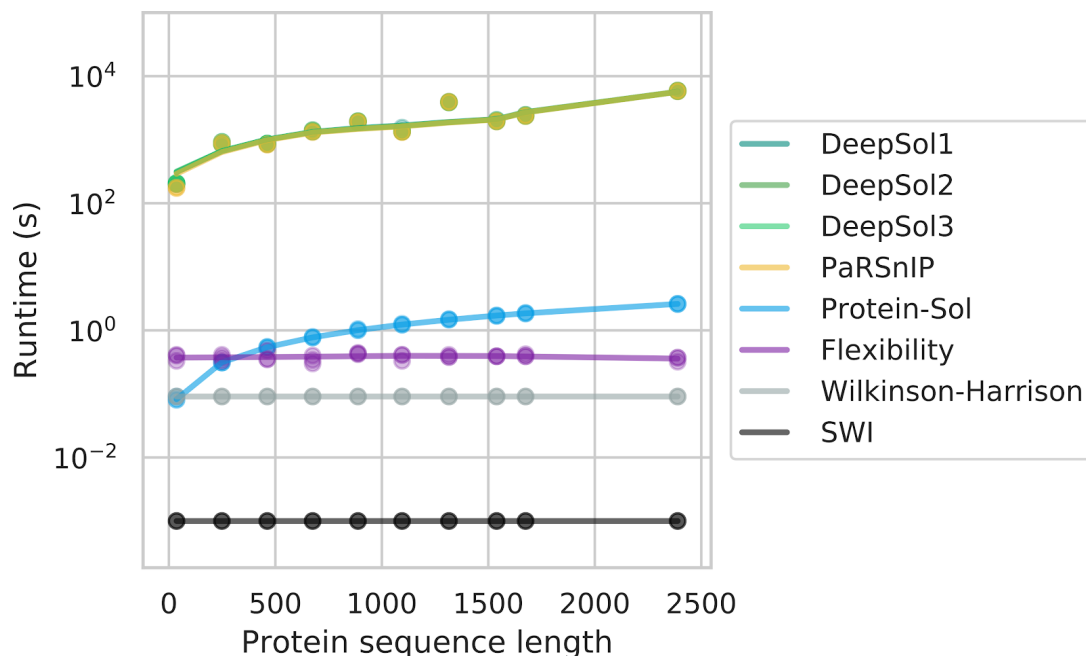
261 ^bThe sample sizes for PSI:BiologY and eSOL datasets are 12,216 and 3,198, respectively.

262 ^cMean AUC ± standard deviation calculated from a 10-fold cross-validation (see Methods).

263 ^dDeepSol reports solubility prediction as probability and binary classes. The probability of
264 solubility was used to calculate AUC and Spearman's correlation due to better results.

265 AUC, Area Under the ROC Curve; NA, not applicable; PDB, Protein Data Bank; PSI:Biolog
266 Protein Structure Initiative:Biolog; ROC, Receiver Operating Characteristic; R_s , Spearman's
267 rho; SWI, Solubility-Weighted Index; s, seconds.

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272 **Fig 5. Runtime of protein solubility prediction tools per sequence.** All the tools were run
273 three times using 10 sequences selected from the PSI:Biolog and eSOL datasets. A
274 pseudocount of 0.001 s was used because the runtime of our SWI C program is 0.00 s per
275 sequence, which is determined by machine precision. Related data is available as
276 Supplementary Table S7. SWI, Solubility-Weighted Index; s, seconds.

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279 To demonstrate a use case for SWI, we developed the Soluble Domain for Protein
280 Expression (SoDoPE) web server (see Methods and <https://tisigner.com/sodope>). Upon
281 sequence submission, the SoDoPE web server enables users to navigate the protein
282 sequence and its domains for predicting and maximising protein expression and solubility.

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286 DISCUSSION

287 The B-factor or temperature factor of the atoms in a crystalline structure is the measure of
288 vibration around their mean position (u) that reflects the uncertainty in X-ray scattering
289 structure determination (Schlessinger and Rost 2005, Bramer and Wei 2018, Carugo 2018).

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$$291 \quad B = 8\pi^2 u \quad (2)$$

293 The profile of normalised B-factors along a protein sequence can be used to infer the
294 flexibility and dynamics of the protein structure (Karplus and Schulz 1985, Vihinen *et al.*

295 1994). Protein structural flexibility has been associated with conformational variations, functions,
296 thermal stability, ligand binding and disordered regions (Vihinen 1987, Teague 2003,
297 Radivojac 2004, Ma 2005, Schlessinger and Rost 2005, Yuan *et al.* 2005, Yin *et al.* 2011).
298 However, the use of flexibility in solubility prediction has been overlooked although their
299 relationship has previously been proposed (Tsumoto *et al.* 2003). In this study, we have
300 shown that flexibility strongly correlates with solubility (Fig 3). Based on the normalised
301 B-factors used to compute flexibility, we have derived a new position and length independent
302 weights to score the solubility of a given protein sequence. We call this protein solubility
303 score as SWI.

304
305 Upon further inspection, we observe some interesting properties in SWI. SWI anti-correlates
306 with helix propensity, GRAVY, aromaticity and isoelectric point (Fig 2C and 3). Amino acid
307 residues with a lower aromaticity or hydrophilic are known to improve protein solubility (Han
308 *et al.* n.d., Wilkinson and Harrison 1991, Trevino *et al.* 2007, Niwa *et al.* 2009, Kramer *et al.*
309 2012, Warwicker *et al.* 2014). Consistent with previous studies, the charged residues
310 aspartate (D), glutamate (E) and lysine (K) are associated with high solubility, whereas the
311 aromatic residues phenylalanine (F), tryptophan (W) and tyrosine (Y) are associated with low
312 solubility (Fig 2C and 4A). Interestingly, histidine residue (H) appears as one of the heavily
313 weighted residues in scoring solubility, which might be due to its positive charge. In contrast,
314 cysteine residue (C) has been strongly downweighted, probably because disulfide bonds
315 couldn't be properly formed in the *E. coli* expression hosts (Stewart *et al.* 1998, Aslund and
316 Beckwith 1999, Rosano and Ceccarelli 2014, Jia and Jeon 2016). The weights are likely
317 different if the solubility analysis was done using the reductase-deficient, *E. coli* Origami host
318 strains, or eukaryotic hosts.

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320 Higher helix propensity has been reported to increase solubility (Idicula-Thomas and Balaji
321 2005, Huang *et al.* 2012). However, our analysis has shown that helical and turn
322 propensities anti-correlate with solubility, whereas sheet propensity lacks correlation with
323 solubility, suggesting that disordered regions may tend to be more soluble (Fig 3). In
324 accordance with these, SWI has stronger negative correlations with helix and turn
325 propensities. These findings also suggest that protein solubility can be largely explained by
326 overall amino acid composition, not just the surface amino acid residues. This idea aligns
327 with our understanding that protein solubility and folding are closely linked, and folding
328 occurs cotranscriptionally, a complex process that is driven various intrinsic and extrinsic
329 factors (Wilkinson and Harrison 1991, Chiti *et al.* 2003, Tartaglia *et al.* 2004, Diaz *et al.*
330 2010). However, it is unclear why sheet propensity has little contribution to solubility because
331 β -sheets have been shown to link closely with protein aggregation (Idicula-Thomas and
332 Balaji 2005).

333
334 We conclude that SWI is a well-balanced index that is relatively simple and easy to use. To
335 demonstrate the usefulness of SWI, we developed the SoDoPE web server for predicting
336 solubility and designing protein sequences (see Methods and <https://tisiigner.com/sodope>). In
337 addition, SoDoPE is integrated with TIsigner, our gene optimisation web server for protein
338 expression. This pipeline provides a holistic approach to improve the outcome of
339 recombinant protein expression.

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METHODS

Protein sequence properties

The standard protein sequence properties were calculated using the Bio.SeqUtils.ProtParam module of Biopython v1.73 (Cock *et al.* 2009). All miscellaneous protein sequence properties were computed using the R package protr v1.6-2 (Xiao *et al.* 2015).

Protein solubility prediction

We used the standard and miscellaneous protein sequence properties to predict the solubility of the PSI:Biology and eSOL targets (N=12,216 and 3,198, respectively) (Niwa *et al.* 2009, Seiler *et al.* 2014). For method comparison, we chose the protein solubility prediction tools that are scalable (Table 1). Default configurations were used for running the command line tools.

To benchmark the runtime of these solubility prediction tools, we selected 10 sequences with a large range of lengths from the PSI:Biology and eSOL datasets (from 36 to 2389 residues). All the tools were run and timed using a single process without using GPU on a high performance computer [/usr/bin/time <command>; CentOS Linux 7 (Core) operating system, 72 cores in 2× Broadwell nodes (E5-2695v4, 2.1 GHz, dual socket 18 cores per socket), 528 GiB memory]. Single sequence fasta files were used as input files.

SWI

To improve protein solubility prediction, we optimised the most recently published set of normalised B-factors using the PSI:Biology dataset (Smith *et al.* 2003) (Fig 2). To avoid bias due to protein sequence homology, we first clustered the PSI:Biology targets using USEARCH v11.0.667, 32-bit (Edgar 2010). His tag sequences were removed from all sequences before clustering to minimise bias. We obtained 4,368 clusters using the parameters: -cluster_fast <input_file> -id 0.1 -msaout <output_file> -threads 4. These clusters were divided into 10 groups with approximately 1,200 sequences per group. The subsequent steps were done with or without His tag sequences. We used the normalised B-factors as the initial weights to maximise AUC using these 10 groups with a 10-fold cross-validation. Since AUC is non-differentiable, we used the Nelder-Mead optimisation method (implemented in SciPy v1.2.0), which is a derivative-free, heuristic, simplex-based optimisation (Nelder and Mead 1965, Oliphant 2007, Millman and Aivazis 2011). For each step in cross-validation, we did bootstrap resampling for 1,000 times with each sample containing 1,000 soluble and 1,000 insoluble proteins. Optimisation was done for each sample, giving 1,000 sets of weights. The arithmetic mean of these weights was used to determine the training and test AUC for the cross-validation step (Fig 2A).

Bit score

To compute the bit scores for each amino acid residue in the PSI:Biology soluble and insoluble groups (Fig 4A), we normalised the count of each residue (x) in each group by the

387 total number of residues in that group. We used the normalised count of amino acid residues
388 using the eSOL sequences as the background. The bit score of residue (x) for soluble or
389 insoluble group is then given by the following equation:

$$390 \text{bit score}(x)_i = \log_2 \left(\frac{f_i(x)}{f_{\text{eSOL}}(x)} \right), i = [\text{soluble}, \text{insoluble}] \quad (3)$$

392 where $f_i(x)$ is the normalised count of residue (x) in the PSI:Biological soluble or insoluble
393 group and $f_{\text{eSOL}}(x)$ is the normalised count in the eSOL sequences.

394
395 For control, random protein sequences were generated by incrementing the length of
396 sequence, starting from a length of 50 residues to 6,000 residues with a step size of 50
397 residues. A hundred of random sequences were generated for each length, giving a total of
398 12,000 unique random sequences.

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401

402 **The SoDoPE web server**

403 To estimate the probability of solubility using SWI, we fitted the following logistic regression
404 to the PSI:Biological dataset:

$$405 \text{probability of solubility} = 1/(1 + \exp(-(ax + b))) \quad (4)$$

407
408 where, x is the SWI of a given protein sequence, $a = 81.1496$ and $b = -62.8379$. The
409 P-value of log-likelihood ratio test was less than machine precision. Equation 4 can be used
410 to predict the solubility of a protein sequence given that the protein is successfully expressed
411 in *E. coli*.

412
413 On this basis, we developed a solubility prediction webservice called the Soluble Domain for
414 Protein Expression (SoDoPE). Our web server accepts either a nucleotide or amino acid
415 sequence. Upon sequence submission, a query is sent to the HMMER web server to
416 annotate protein domains (<https://www.ebi.ac.uk/Tools/hmmer/>) (Potter *et al.* 2018). Once
417 the protein domains are identified, users can choose a domain or any custom region
418 (including full-length sequence) to examine the probability of solubility, flexibility and GRAVY.
419 This functionality enables protein biochemists to plan their experiments and opt for the
420 domains or regions with high probability of solubility. Furthermore, we implemented a
421 simulated annealing algorithm that maximised the probability of solubility for a given region
422 by generating a list of regions with extended boundaries. Users can also predict the
423 improvement in solubility by selecting a commonly used solubility tag or a custom tag.

424

425 We linked SoDoPE with TIsigner, which is our existing web server for maximising the
426 accessibility of translation initiation site (Bhandari *et al.* 2019). This pipeline allows users to
427 predict and optimise both protein expression and solubility for a gene of interest. The
428 SoDoPE web server is freely available at <https://tisigner.com/sodope>.

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430

431 **Statistical analysis**

432 Data analysis was done using Pandas v0.25.3 (McKinney 2010), scikit-learn v0.20.2
433 (Pedregosa *et al.* 2011), numpy v1.16.2 (van der Walt *et al.* 2011) and statsmodel
434 v0.10.1 (Seabold and Perktold 2010). Plots were generated using Matplotlib v3.0.2 (Caswell
435 *et al.* 2018) and Seaborn v0.9.0 (Waskom *et al.* 2014).

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438 **Code and data availability**

439 Jupyter notebook of our analysis can be found at
440 https://github.com/Gardner-Binflab/SoDoPE_paper_2019. The source code for our solubility
441 prediction server (SoDoPE) can be found at <https://github.com/Gardner-Binflab/TIsigner>.

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445 **ACKNOWLEDGEMENTS**

446 We thank New Zealand eScience Infrastructure for providing a high performance computing
447 platform. We are grateful to Harry Biggs for proofreading our manuscript and providing
448 feedback for the web server. This work was supported by the Ministry of Business,
449 Innovation and Employment, New Zealand (MBIE grant: UOOX1709).

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453 **AUTHOR CONTRIBUTIONS**

454 C.S.L. conceived the work; B.K.B. and C.S.L. analysed the data and C.S.L. contributed
455 flexibility analysis; B.K.B. and P.P.G. formulated SWI; B.K.B. developed the SoDoPE web
456 server; B.K.B., P.P.G. and C.S.L. wrote the manuscript.

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460 **COMPETING INTERESTS**

461 The authors declare no competing interests.

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