## 1 MreB filaments create rod shape by aligning along

## 2 principal membrane curvature.

#### 3

Saman Hussain<sup>\*,1,2</sup>, Carl N. Wivagg<sup>\*,1,2</sup>, Piotr Szwedziak<sup>3#</sup>, Felix Wong<sup>4</sup>, Kaitlin 4 Schaefer<sup>5,6</sup>, Thierry Izoré<sup>3</sup>, Lars D. Renner<sup>7,8</sup>, Yingjie Sun<sup>1,2</sup>, Alexandre W. Bisson-5 Filho<sup>1,2</sup>, Suzanne Walker<sup>6</sup>, Ariel Amir<sup>4</sup>, Jan Löwe<sup>3</sup>, and Ethan C. Garner<sup>1,2</sup> 6 7 8 1 Department of Molecular and Cellular Biology, Harvard University, Cambridge, United States. 9 2 Center for Systems Biology, Harvard University, Cambridge, United States. 10 3 MRC Laboratory of Molecular Biology, Cambridge, United Kingdom 11 4 Harvard John A. Paulson School of Engineering and Applied Sciences, Cambridge, MA, United States. 12 5 Department of Microbiology and Immunology, Harvard Medical School, Boston, MA, United States 13 6 Department of Chemistry and Chemical Biology, Harvard University, Cambridge, MA, United States 14 7 Leibniz Institute of Polymer Research, Dresden, Germany 15 8 Max-Bergmann Center of Biomaterials, Dresden, Germany 16 #Current affiliation: Institute of Molecular Biology and Biophysics, ETH Zürich, Switzerland 17 \* These authors contributed equally to this work. 18 19 Corresponding Author: Ethan C. Garner 20 NW 445.20, Northwest Building, 52 Oxford Street, Cambridge, MA 02138 21 E-mail: egarner@g.harvard.edu 22 23 All supplemental movies are available at http://garnerlab.fas.harvard.edu/mreb2017/

#### 24 Abstract

25 MreB is essential for rod shape in many bacteria. Membrane-associated MreB filaments 26 move around the rod circumference, helping to insert cell wall in the radial direction to 27 reinforce rod shape. To understand how oriented MreB motion arises, we altered the 28 shape of *Bacillus subtilis*. MreB motion is isotropic in round cells, and orientation is 29 restored when rod shape is externally imposed. Stationary filaments orient within 30 protoplasts, and purified MreB tubulates liposomes in vitro, orienting within tubes. 31 Together, this demonstrates MreB orients along the greatest principal membrane 32 curvature, a conclusion supported with biophysical modeling. We observed that 33 spherical cells regenerate into rods in a local, self-reinforcing manner: rapidly 34 propagating rods emerge from small bulges, exhibiting oriented MreB motion and 35 increased glycan crosslinking. We propose that the coupling of MreB filament alignment 36 to shape-reinforcing peptidoglycan synthesis creates a locally-acting, self-organizing 37 mechanism allowing the rapid establishment and stable maintenance of emergent rod 38 shape.

39

#### 40 Introduction

41 Although many bacteria are rod shaped, the cellular mechanisms that construct and 42 replicate this geometry have remained largely unknown. Bacterial shape is determined 43 by the cell wall sacculus, a giant, encapsulating macromolecule that serves to resist 44 internal turgor pressure. One of the primary components of the cell wall is peptidoglycan 45 (PG), which is created by the polymerization of single glycan strands linked by peptide 46 crossbridges. Studies of isolated cell walls from rod-shaped bacteria suggest that 47 glycan strands are generally oriented circumferentially around the rod, perpendicular to 48 the long axis of the cell (Gan et al., 2008; Hayhurst et al., 2008; Verwer et al., 1980). 49 This circumferential, hoop-like organization of cell wall material allows the cell wall to 50 better resist the internal turgor pressure, as this pressure causes a stress twice as large 51 in the circumferential direction (on the rod sidewalls) as in the axial direction (on the 52 poles) (Amir and Nelson, 2012; Chang and Huang, 2014). This organization confers a 53 mechanical anisotropy to the wall: the mechanically weaker crosslinks in the axial 54 direction allows the cell wall to stretch more along its length than across its width for a 55 given stress, and this anisotropy may assist rod-shaped cells in preferentially elongating 56 along their length (Baskin, 2005; Chang and Huang, 2014). Concordantly, atomic force 57 microscopy (AFM) has shown that *Escherichia coli* sacculi are 2-3 times more elastic 58 along their length than across their width (Yao et al., 1999). This rod-reinforcing 59 circumferential organization is also observed in the cell walls of plants: hypocotyl and 60 root axis cells rapidly elongate as rods by depositing cellulose fibrils in circumferential 61 bands around their width, resulting not only in a similar dispersive rod-like growth, but

also a similar anisotropic response to stress (Baskin, 2005). The organized deposition
of cellulose arises from cortical microtubules self-organizing into a radial array oriented
around the rod width, and this orients the directional motions of the cellulose synthases
to insert material in circumferential bands (Bringmann et al., 2012; Paredez et al.,

66 **2006**).

67

In contrast to our understanding of the self-organization underlying rod-shaped growth 68 69 in plants, how bacteria construct a circumferential organization of glycan strands is not 70 known. This organization may arise via the actions of a small number of genes known to be essential for the formation and maintenance of rod shape. Collectively termed the 71 72 Rod complex, these include the conserved *mreBCD* operon (Wachi and Matsuhashi, 73 1989) and the glycosyltransferase/transpeptidase enzyme pair RodA/Pbp2 (Cho et al., 74 2016). The spatial coordination of RodA/Pbp2-mediated PG synthesis is conferred by 75 *mreB*, an actin homolog (Jones et al., 2001; van den Ent et al., 2001). MreB 76 polymerizes onto membranes as antiparallel double filaments, which have been observed to bend liposome membranes inward (Fig. 1A) (Salje et al., 2011; van den Ent 77 78 et al., 2014). Loss or depolymerization of MreB causes rod-shaped cells to grow as 79 spheres (Jones et al., 2001). In vivo, MreB filaments move circumferentially around the 80 width of the rod (Domínguez-Escobar et al., 2011; Garner et al., 2011; van Teeffelen et 81 al., 2011). Super-resolution imaging has demonstrated that MreB filaments always 82 translocate along their length, moving in the direction of their orientation (Olshausen et 83 al., 2013). MreB filaments move in concert with MreC, MreD, and RodA/Pbp2

84	(Domínguez-Escobar et al., 2011; Garner et al., 2011), and loss of any one component
85	stops the motion of the others. The directional motion of MreB filaments and associated
86	Rod complexes depends on, and thus likely reflects, the insertion of new cell wall, as
87	this motion halts upon the addition of cell wall synthesis-inhibiting antibiotics
88	(Domínguez-Escobar et al., 2011; Garner et al., 2011; van Teeffelen et al., 2011), or
89	specific inactivation or depletion of Pbp2 (Garner et al., 2011; van Teeffelen et al., 2011)
90	or RodA (Cho et al., 2016).
91	
92	It is not known how MreB and its associated PG-synthetic enzymes construct rod-
93	shaped cells. As the motions of the Rod complexes reflect the insertion of new cell wall,
94	their circumferential motions could deposit glycans in the hoop-like organization
95	required to both build and reinforce rod shape. Therefore, we worked to understand the
96	origin of this circumferential organization, seeking to determine what orients $\mu$ the
97	motions of MreB and associated enzymes around the rod width in Bacillus subtilis. B.
98	subtilis contains 3 MreB paralogs (MreB, Mbl, and MreBH) that co-polymerize into
99	mixed filaments and always colocalize in vivo (Defeu Soufo and Graumann, 2006)
100	(Soufo and Graumann, 2010) (Dempwolff et al., 2011). Thus, we assume throughout
101	that MreB and MbI are interchangeable for fluorescent imaging.
102	
103	Results

104 Oriented MreB Motion Cannot Arise from an Ordered Cell Wall Template

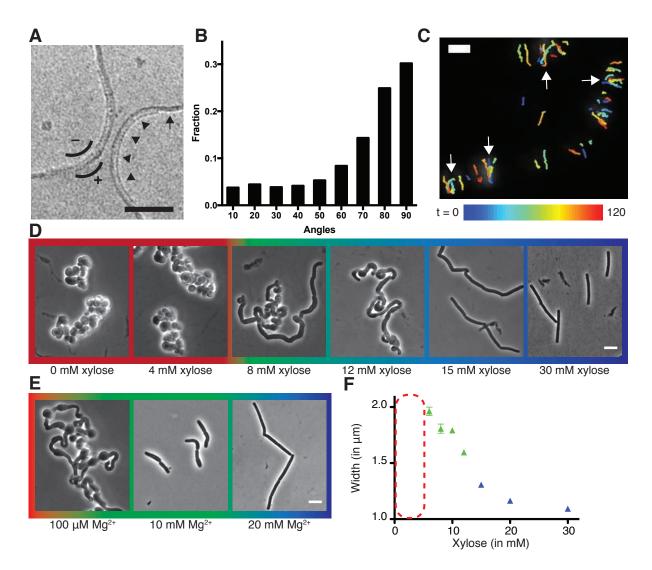
105	The mechanism by which MreB filaments and associated PG synthases orient their
106	motion around the rod circumference is not known. Each filament-synthase complex is
107	disconnected from the others, moving independently of proximal neighbors (Garner et
108	al., 2011). The organized, circumferential motion of these independent filament-
109	synthase complexes could arise in 2 ways: 1) A templated organization, where cell wall
110	synthetic complexes move along an existing pattern of ordered glycan strands in the cell
111	wall as they insert new material into it (Holtje, 1998), or 2) A template-independent
112	organization, where each synthetic complex has an intrinsic mechanism that orients its
113	motion and resultant PG synthesis around the rod circumference.
114	
115	To explore the extent of order within the motions of the Rod complex, we analyzed the
116	trajectories of GFP-MbI filaments during the period of one axial revolution using total
117	internal reflection fluorescence microscopy (TIRFM). We observed that filament
118	trajectories close in time (within the period of one revolution) frequently cross (Fig. 1C,
119	Movie S1), making it unlikely that MreB filaments move along a perfectly ordered
120	template. Rather, the motions of filaments are overall oriented, but not perfectly aligned,
121	a characteristic reflected by the broad distribution of angles that MreB (Fig. 1B) and the
122	other components of the Rod complex move relative to the long axis of the cell
123	(Domínguez-Escobar et al., 2011; Garner et al., 2011). As MreB movement reflects the
124	insertion of new glycan strands, these motions indicate that the sacculus is built from
125	somewhat disorganized, yet predominantly circumferential strands, a conclusion in
126	agreement with previous studies that assayed cell wall organization with cryo-electron

microscopy (Gan et al., 2008), atomic force microscopy (Hayhurst et al., 2008), and Xray diffraction (Balyuzi et al., 1972). Furthermore, preexisting cell wall is not necessary
for the regeneration of rod shape from wall-less *B. subtilis* L-forms (Kawai et al., 2014),
indicating that both oriented MreB motion and rod shape can arise without an ordered
template.
MreB Motions Become Isotropic in the Absence of Rod Shape

134 As it appeared that organized MreB motion does not arise from patterns in the cell wall. 135 we hypothesized there was an intrinsic mechanism orienting the motion of each MreB 136 filament-cell wall synthetic complex. To test this hypothesis, we examined MreB motions 137 as we changed the shape of cells from rods to spheres. As the internal turgor pressure 138 and stiffness of *B. subtilis* resists external mechanical perturbations to its shape 139 (Renner et al., 2013), we first altered the shape of cells by controlling the level of wall 140 teichoic acids (WTAs). WTAs are negatively charged cell wall polymers believed to increase the rigidity of the sacculus via their coordination of extracellular Mg<sup>2+</sup> (Matias 141 142 and Beveridge, 2005) or modulation of hydrolase activity (Atilano et al., 2010). 143 Knockouts in *tagO*, the first gene in the WTA synthesis pathway, create large, slow-144 growing, round cells that still synthesize PG, building extremely thick and irregular cell 145 walls (D'Elia et al., 2006). We placed tagO under xylose-inducible control and grew cells 146 at different induction levels. At high TagO inductions, cells displayed normal widths, as 147 expected. As we reduced TagO levels, rods became gradually wider (Fig. 1D,1F) until, 148 beneath a given induction, cells were no longer able to maintain rod shape, growing as

- spheres (or clumps of spheres) with no identifiable long axis. At intermediate induction
  levels, we observed a transition region between the two states, with cells growing as
  steady state populations of interconnected rods and spheres (Fig 1D). In agreement
  with models that cell wall rigidity is conferred via WTA-mediated coordination of Mg<sup>2+</sup>
  (Thomas and Rice, 2014), both cell width and the amount of TagO induction
  determining the rod/sphere transition could be modulated by Mg<sup>2+</sup> levels (Fig. 1E, S1).
- 155





158 (A) The negative curvature of MreB filaments (arrowheads) aligns with the negative principal curvature of 159 the liposome surface (arrow). Scale bar is 50 nm. (B) Angular distribution of GFP-Mbl trajectories relative 160 to the long axis of the cell indicates that while the distribution has a mode of  $90^{\circ}$ , it is broad (SD =  $34^{\circ}$ ). 161 (C) Particle tracking of MbI-GFP during 100 seconds (1 rotation) indicates trajectories close in time 162 frequently cross paths (white arrows). Scale bar is 1 µm. Modulating teichoic acid levels titrates cell 163 width and shape (D-F). (D) Strains with tagO under inducible control display a teichoic acid-dependent 164 decrease in width. (E) BEG300 at an intermediate level of tagO induction (15mM xylose) shows a Mg<sup>2+</sup> 165 dependent decrease in width. All scale bars are 5 µm. See also Figure S1. (F) Plot of cell width as a 166 function of tagO induction in LB supplemented with 20 mM Mg<sup>2+</sup>, calculated from rod-shaped cells (error 167 bars are Standard Error of the Mean (SEM)). Areas not plotted at lower xylose levels (red dashed 168 rectangle) are regions where cells are round (no width axis). Color scheme for D-F: red indicates round 169 cells (no width axis), blue indicates rods (measurable width axis), and green indicates intermediate 170 regimes where both rods and round cells are observed.

171 By tracking the motion of GFP-MreB filaments in these differing cell shapes, we found 172 that motion is always oriented in rods, moving predominantly circumferentially at all 173 induction levels above the rod/sphere transition. However, in round cells (those induced 174 beneath the rod/sphere transition point or in tagO knockouts) MreB filaments continued 175 to move directionally, but their motions were isotropic, moving in all directions (Fig. 2A, 176 Movie S2A). To quantify the relative alignment of MreB under each condition, we 177 calculated the angle between trajectory pairs less than 1µm apart (Fig. 2B, S2A). This 178 analysis revealed that MreB motions are more aligned when cells are rods: above the 179 rod/sphere transition, trajectories have a median angle difference of 26°; while at low 180 TagO inductions, where cells are round, the angle difference increases to  $42^{\circ}$ , close to 181 that of randomly oriented trajectories (45°).

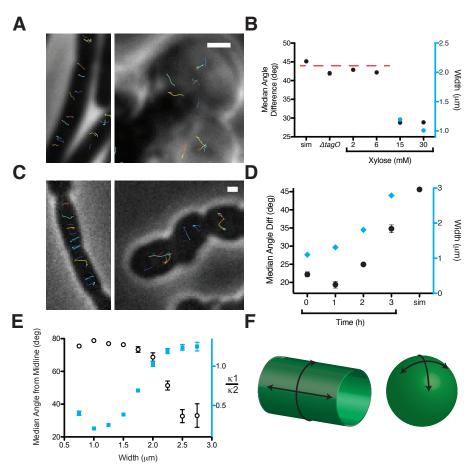
183	To verify that the loss of oriented MreB motion was due to the changes in cell shape,
184	and not from some other effect of reduced WTA levels, we created round cells by
185	alternate means. Depletion of both elongation PG transpeptidases (Pbp2a and PbpH)
186	causes rod-shaped cells to become wider over time as they convert to spheres (Garner
187	et al., 2011). We used this gradual transition of rods into spheres to examine both the
188	width and overall shape dependence of MreB motion. At initial points of depletion (1 - 2
189	hours) the rods widened but maintained circumferential MreB motion. At 2.5 hours of
190	PbpA depletion, cells were a mix of spheres and rods of differing widths. These cells
191	displayed the same pattern of MreB orientation observed above: round cells contained
192	unoriented MreB, while nearby rod shaped cells showed circumferential motion (Fig.
193	2C, Movie S2B). Quantitation of trajectories from all cells (both rods and spheres) at
194	each time point of depletion indicated an increase in the median angle between
195	trajectories as the population grew wider and rounder over time (Fig. 2D, S2D).
196	
197	In E. coli, the angle of mutant MreB filaments relative to the long axis has been reported
198	to increase with cell width (Ouzounov et al., 2016). To test if the angle of MreB
199	movement changes with respect to cell width in <i>B. subtilis</i> , we calculated the angle of
200	each trajectory to the long axis for all cells in our data with an identifiable width axis. At
201	the same time, we also measured the curvature of each cell to determine how the
202	overall shape of the cell affected the orientation of motion (Fig. S2E). This revealed that
203	MreB motion in rods remained equivalently oriented over a wide range of rod widths, up

204 to ~2  $\mu$ m (Fig. 2E, S2B, S2C). Beyond a 2  $\mu$ m width, cells began to lose their rod shape 205 as they became more spherical, and the predominantly circumferential orientation of 206 MreB motion was lost (Fig. 2E, S2E). This suggested that oriented MreB motion does not sense or rely on a specific cell radius; rather the orientation relies on differences 207 208 between the two principal curvatures of the membrane. It appears that the motion of 209 MreB filaments is oriented along the direction of greatest principal curvature: In rods, there is zero curvature along the rod length, and high curvature around the rod 210 211 circumference, along which filaments orient. In contrast, in round cells where MreB 212 motion is isotropic, the two principal curvatures are equal (Fig. 2F).

213

#### Figure 2. Oriented MreB motion correlates with rod shape.

215 (A) BEG300 at maximum tagO 216 induction (30 mM) is rod-shaped. 217 and MreB tracks are largely 218 oriented perpendicular to the 219 midline of the cell (*left*).  $\Delta tagO$ 220 cells show round morphologies 221 with unaligned MreB motion 222 (right). (B) Median inter-track 223 angle difference for track pairs ≤ 224 1 µm apart, plotted for BEG300 225 at several tagO induction levels, 226  $\Delta tagO$  cells, and a simulation of 227 randomly oriented angles (sim).



228 For spherical cells width is not measurable, indicated with a dashed red line. (C) ApppH cells with pbpA 229 under IPTG control display aligned MreB motion when *pbpA* is fully induced and cells are rods (*left*), but 230 display unaligned MreB motion as Pbp2a levels reduce and cells become round (right). (D) Median inter-231 track angle difference for track pairs 1 µm apart during Pbp2a depletion with cell widths at each time 232 point. (E) Median angle from the midline (white circles) calculated for all rod-shaped cells from 233 experiments in 2A-D plotted as a function of cell width. MreB filament alignment falls off rapidly beyond 2 234 μm, a point corresponding to where cells become round, as shown by the ratio of principal curvatures 235 (blue squares) approaching 1. See Fig S2E for further explanation. (F) Schematic showing the difference 236 between the 2D surface curvature profile of rods and spheres. On the inside surface of spheres, all points 237 have negative, yet equal values for both principal curvatures. In rods, however, one principal curvature is 238 negative (the radius), while the other is 0 (the flat axis along the rod). All scale bars are 1  $\mu$  m. All error 239 bars are SEM. See also Figure S2.

240

#### 241 MreB Aligns Within Round Cells and Protoplasts Forced into Rod Shape

242 To further verify that MreB filaments orient in response to overall cell shape, we 243 externally imposed rod shape on cells with unoriented MreB motion. We loaded TagO-244 induced cells into long  $1.5 \times 1.5 \,\mu m$  microfluidic chambers, then reduced TagO 245 expression to levels insufficient to produce rods in liquid culture (Fig. 3A, S3A). After 246 TagO depletion, cells expanded to fill the chamber indicating that WTA-depletion 247 caused shape changes just as in bulk culture (Fig. 3A, S3A). Within these chambers, 248 cells grew as rods, but at a wider width (1.5 µm) than wild-type cells, set by the 249 chamber. When cells grew out of the chamber they swelled just as in bulk culture, 250 showing confinement was required for rod shape at this induction level (Fig. 3B, S3A). 251 In the TagO-depleted cells confined into rod shapes, MreB moved circumferentially (Fig.

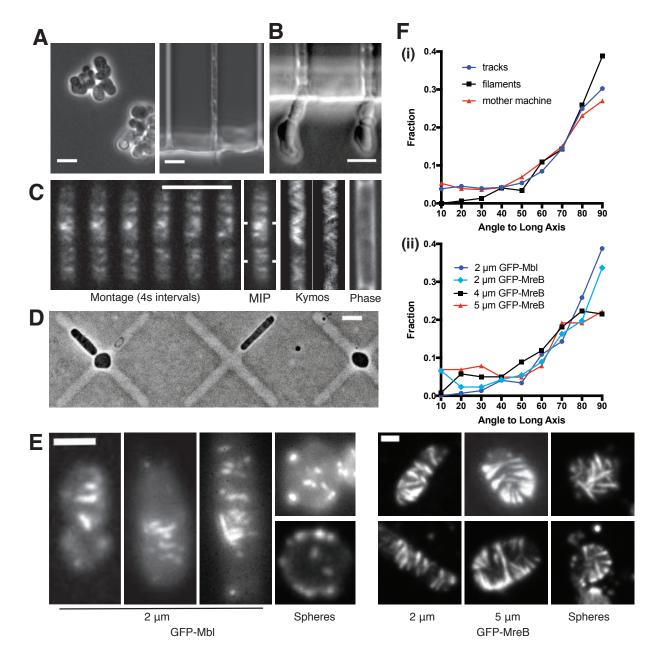
252 3C, Movie S3) with an angular distribution similar to that of wild-type cells ( $90^\circ$ , SD = 36 253 <sup>o</sup>) (Fig. 3F(i)), confirming that MreB orients in response to the cells having rod shape. 254 This experiment demonstrates that the isotropic MreB motion observed in round cells 255 arises from the lack of rod shape, and not from some other effect of our genetic 256 perturbations. This experiment also showed another unexpected result: the doubling time of free (unconstrained) cells induced at similar TagO levels is slow (53  $\pm$  10 min), 257 258 but confining them into rod shape restored their doubling time (44  $\pm$  4 min) toward wild-259 type rates  $(39 \pm 9 \text{ min})$  (Figure S3C). 260

261 Next, we attempted to decouple MreB filament orientation from both A) the directional 262 motion of filaments, and B) any structure within the cell wall. To accomplish this, we 263 examined filament orientation in protoplasts (cells without cell wall) that we confined into 264 different shapes, using highly expressed GFP-MreB to assay long filaments, and GFP-265 Mbl to assay short filaments. We protoplasted cells in osmotically stabilized media 266 (Wyrick and Rogers, 1973), then grew them under agar pads containing micro-267 patterned cross shapes. Cells in the center of these crosses (~5 µm diameter) were 268 forced to grow as spheres, whereas cells in the arms were constrained to grow into rods 269 of various widths ranging from 2-5 µm. (Fig. 3D). Cells growing in these molds did not 270 produce cell wall, as determined by WGA staining (Fig. S3B). As reported previously (Domínguez-Escobar et al., 2011), MreB filaments within protoplasts did not move 271 272 directionally (Movie S4), likely because the cell wall provides the fixed surface across 273 which the PG synthesis enzymes move. Within the protoplasts confined into the

274 smallest rod shapes (2 µm), filaments oriented at a distribution of angles predominantly 275 perpendicular to the cell length (Fig. 3E-F). The angular distributions of short GFP-Mbl 276 filaments and longer GFP-MreB filaments were similar to each other (94°  $\pm$  25 and 93°  $\pm$ 277 34 respectively), and also similar to the distribution of filament trajectories observed in 278 intact, wild-type cells (88°,  $SD = 34^\circ$ ). As we increased the width of the imposed rod 279 shape from 2 to 5 µm, filaments remained predominantly oriented in all cases, but the 280 distribution of alignment became increasingly broad (86°, SD = 41° at 5  $\mu$ m). In contrast 281 to confinement in rods, both short and long filaments in spherically confined protoplasts 282 remained unoriented (Fig. 3E). Together, these data demonstrate that MreB filaments 283 orient to point around the rod width even in the absence of cell wall or directional 284 motion, as long as the cell has a rod shape. These experiments also demonstrate that 285 MreB filaments will align even in wider rods, where the difference in principal curvatures 286 is smaller than in wild-type cells, but that, as the difference in principal curvatures 287 decreases, filament alignment becomes more disordered.

#### **Figure 3. MreB filaments orient when rod shape is induced by external**

#### confinement.





(A) Phase contrast images of BEG300 grown in LB supplemented with 2 mM xylose and 20 mM Mg<sup>2+</sup> in bulk culture (*left*) or confined into microfluidic channels of  $1.5 \times 1.5 \mu m$  (*right*). (B) Confined cells induced at 3 mM xylose in 20 mM Mg<sup>2+</sup> progressively swell upon escaping confinement into free culture. See also Figure S3A. (C) (*Left*) Montage of MreB filaments moving across a confined cell. (*Right*) Maximal intensity projection of montage, kymographs of marked points and a phase contrast image of the cell. Scale bars 297 for a-c = 5  $\mu$ m. (D) Phase contrast images of protoplasts contained in agar crosses. Cells in the center 298 grow to be round while cells in arms grow as elongated rods. (E) (left) Short GFP-Mbl filaments orient 299 circumferentially in rod-shaped protoplasts (2 µm) but lack orientation in round protoplasts (spheres). 300 (right) Long GFP-MreB filaments orient in rod-shaped protoplasts (2 µm); GFP-MreB filaments are still 301 oriented in wider rod-shaped protoplasts (5 µm), but not to the same extent. In round protoplasts, GFP-302 MreB filaments are unoriented (spheres). See also Fig. S3B. Scale bar is 2 μm. (F) (i)The angular 303 distribution of filaments within protoplasts is centered at 90° (SD 25°, n=147), similar to that of MreB 304 motion in TagO-depleted, confined cells (90°, SD 36°, n=359) and MreB motion in wild-type cells (88°, SD 305 34°, n=1041). (ii) In channels of varving widths (2, 4 and 5 μm), the orientation of GFP-MreB filaments 306 remains circumferential but the angular distribution becomes wider at increasing channel width (93°, SD 307 34°, n=258 at 2 μm), (81°, SD 35°, n=260 at 4 μm) and (86°, SD 41°, n=203 at 5 μm).

308

#### 309 MreB Filaments Orient Around Liposome Tubes in vitro

310 To test if MreB filaments are themselves sufficient to align along the predominant 311 direction of membrane curvature, we assembled purified T. maritima MreB within 312 liposomes and visualized it using electron cryo-electron microscopy and tomography. 313 While controlling the final concentration of protein encapsulated within liposomes  $\leq 1 \mu m$ 314 is difficult, we were able to assemble MreB inside liposomes at high concentrations. At 315 these concentrations. MreB filaments tubulated liposomes, creating rod-like shapes 316 (Fig. 4A, S4, Movie S5). In tubulated regions, MreB filaments could be traced around 317 the circumference of the liposome tube, while filaments in spherical regions were found 318 in all possible orientations (Fig. 4A). At the highest concentrations, tubulated liposomes 319 contained closely packed filament bundles, allowing us to observe a regular patterning 320 of the canonical double filaments of MreB (Fig. 4B). Purified wild-type MreB did not bind 321 to the outside surface of small liposomes contained within larger ones (Fig. 4A), 322 indicating that MreB filaments preferentially polymerize on inward (negative) curvatures, 323 akin to the inner leaflet of the bacterial membrane. In the absence of MreB, liposomes are spherical, with no deformations (Fig. S4C). Together, this data suggests that MreB 324 325 filaments themselves are sufficient to align along the predominant direction of 326 membrane curvature, as observed here with laterally associated filaments. We note that 327 the experimental limitations of the liposomal system, combined with the tendency of 328 MreB filaments to self-associate make it difficult for us to acquire and study the 329 alignment of single filaments in vitro. Also, it remains to be determined if membrane-330 associated MreB filaments exist as bundles or isolated filaments in vivo. 331 332 **Biophysical Modeling Suggests Highly Bent MreB Filaments Orient Along the** 333 Greatest Principal Curvature to Maximize Membrane Interactions, a Prediction 334 **Insensitive to Large Variations in Parameters** 335 The above observations demonstrate that MreB filaments sense and align along the 336 direction of greatest principal curvature, i.e., the more curved inner surface of the rod 337 circumference. The ultrastructure of MreB filaments provides a possible mechanism: 338 MreB filaments are bent (Salje et al., 2011), with the membrane-interacting surface on 339 the outer face of the bend (Fig. 4C). This bent conformation could cause filaments to 340 preferentially orient along the curved rod circumference, rather than the flat rod length, 341 to maximize the burial of hydrophobic moleties into the membrane, a mechanism 342 suggested by previous theory (Wang and Wingreen, 2013).

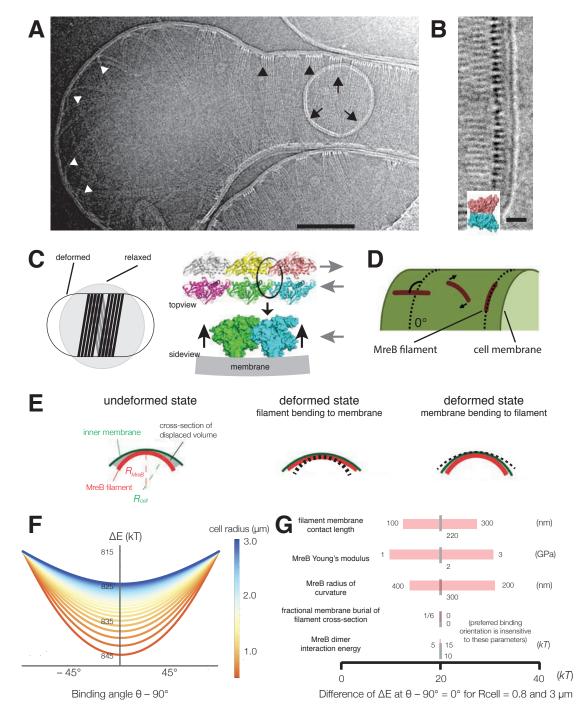
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344 As the curvature of MreB filaments bound to liposomes is much greater (~200 nm 345 diameter) than that of *B. subtilis* cells (~900 nm diameter), we performed analytical 346 calculations to model how highly curved MreB filaments would align within a cell with a 347 less curved surface (Fig. 4D-G, Supplemental Text 1). As many of the biochemical and 348 physical parameters of MreB are still unknown, we first assumed a fixed set of 349 parameters, and later verified that our results were robust over a large parameter range. 350 We initially assumed a membrane interaction energy of 10 kT per monomer (calculated 351 from residues involved in membrane associations (Salje et al., 2011)), and a similar 352 Young's modulus to actin (2 GPa). We modeled filaments as elastic beams made of two 353 protofilaments. In addition, we used the Helfrich free energy to model the energetics of 354 membrane deformation, and accounted for the work done against turgor pressure due 355 to changes in volume (Supplemental Text 1). These calculations indicate that the total 356 energy is minimized when filaments orient along the direction of maximal curvature (Fig. 357 4F) and that, importantly, the energy penalty for incorrectly-oriented filaments is much 358 greater than the energy of thermal fluctuations. Interestingly, this modeling indicates a 359 decrease in energetic preference for the preferred filament orientation as the radius of 360 the cell is increased (Fig. 4F), a prediction in qualitative agreement with our 361 observations of alignment in protoplasts. Furthermore, our calculations indicate that 362 orientation is robust over a large, biologically relevant range of parameters, including 363 the membrane binding energy, filament length, and filament Young's modulus (Fig. 4G). 364

365	These calculations predict that filaments should orient circumferentially both if the
366	membrane deforms to the filament (at low turgor pressures or if filaments are stiff) (Salje
367	et al., 2011), or if filaments deform to the membrane (at high turgor pressures or if
368	filaments are flexible) (Fig. 4E). Our experimental data demonstrates MreB filament
369	alignment across a range of pressures: high within cells, low to none within liposomes,
370	and a pressure between the two within osmotically-stabilized protoplasts. In the
371	absence of turgor pressure, MreB filaments deform liposomes since it is energetically
372	more favorable to bend the membranes than to bend the filaments, as observed in our
373	in vitro data (Fig. 4A, S4). However, in live cells, our modeling predicts that MreB
374	filaments cannot deform the inner membrane due to the large turgor pressure, and
375	instead deform to match the greatest principal membrane curvature. Hence filaments
376	create curvature in liposomes and sense it in cells.

#### 378 Figure 4. *T. maritima* MreB filaments assembled in liposomes align perpendicular

#### 379 to the rod axis.



381 (A) Black arrowheads show aligned bundles of filaments in a tubulated liposome, white arrowheads show382 unaligned bundles in a spherical region of the same liposome. Arrows show a positively curved surface

383 inside the liposome, to which no MreB filaments bind. Scale bar is 100 nm. See also Figure S4. (B) MreB 384 in liposomes adopts a double-stranded antiparallel protofilament arrangement consistent with (van den 385 Ent et al., 2014). Scale bar is 50 nm. (C) (left) Schematic drawing depicting the cause of the shape 386 change from spherical to rod-shaped liposomes: MreB wants to attain greater curvature and since there 387 are many filaments, they are laterally stabilized. As the liposome is much more easily deformable than 388 cells, the resulting energy minimum is a deformed liposome with an MreB helix on the inside. (right) 389 Model showing why the unusual architecture of MreB filaments might have been selected during 390 evolution: its juxtaposed subunits in the two antiparallel protofilaments produce putative hinges that could 391 be the region of bending for these filaments. Canonical F-actin filament architectures, with staggered 392 subunits, would need bending within the subunits, which is less easily achieved. Modeling of MreB -393 membrane interactions and filament orientation. (D, E) Hydrophobic residues are located on the outer 394 edge of the antiparallel MreB double filament, which is here modeled as an elastic cylindrical rod. To 395 achieve maximum hydrophobic burial, membrane deformation, MreB bending, or a combination of the two 396 may occur. (F) A plot of the change in total energy ( $\Delta E$ ) caused by the MreB-membrane interaction 397 against the binding angle  $\theta$  for various cell radii shown in the color scheme on the right. Note that  $\Delta E$  is 398 minimal at  $\theta$ =90°, which agrees with the observed orientation of MreB binding and motion. At larger rod 399 radii, the energetic well becomes flatter and MreB binding becomes more susceptible to thermal 400 fluctuations and other sources of stochasticity, which would result in a broader angular distribution of 401 filaments. (G) A sensitivity analysis of the model over a range of model parameters.

402

#### 403 **Rod-Shape is Lost in a Global Manner, but Reforms Locally**

Together, the above data demonstrate that MreB filaments are sufficient to preferentially orient along the direction of greatest principal membrane curvature. In rod-shaped cells, this direction is along the rod circumference. As filaments move along their length, their orientation constrains the spatial activity of the PG synthetic enzymes such that new cell wall is inserted in a mostly circumferential direction (Hayhurst et al., 2008) to reinforce

409 rod shape (Chang and Huang, 2014; Yao et al., 1999). While the ability of MreB 410 filaments to orient in pre-existing rods can help explain how rod shape is maintained, we 411 also wanted to understand how MreB filaments facilitate the *de novo* formation of rod 412 shape. To explore this, we observed how cells interconvert between spheres and rods. 413 414 We first examined how rod shape fails, by growing our TagO-inducible strain at induction levels that produced rods and then reducing the Mg<sup>2+</sup> concentration to induce 415 416 them to convert to spheres. This transition revealed that rods convert into round cells by 417 continuous swelling: once a rod begins to widen, it continues to do so until reaching a 418 fully spherical state with no reversion during the process (Fig. 5A). Similar rod to sphere 419 transitions could be attained by holding Mg<sup>2+</sup> constant while reducing TagO expression. 420 Likewise, cells grown at intermediate TagO induction levels (8-12mM) grew as steady 421 state populations of interconnected rods and spheres, indicating that cells underwent 422 repeated cycles of rod shape formation followed by reversion to spheres (Fig. 1D, E). 423 These results indicate that rod shape can be maintained only as long as the cell wall is 424 sufficiently rigid to resist the internal turgor pressure. 425 426 We next examined how rod shape forms from round cells. As the recovery of

427 protoplasted *B. subtilis* is so infrequent that it has never been directly visualized

428 (Mercier et al., 2013), we assayed how round cells with preexisting cell walls convert

429 back into rods, using three systems: 1) re-inducing WTA expression within TagO-

430 depleted, spherical cells, 2) holding TagO expression beneath the rod/sphere transition

431	and increasing Mg <sup>2+</sup> levels, and 3) re-inducing Pbp2a expression in spherical, Pbp2a-
432	depleted cells. In all three cases, rods reformed in a discrete, local manner; spheres did
433	not form into rods by progressively shrinking along one axis, but rather, rods abruptly
434	emerged from one point on the cell, growing more rapidly than the parent sphere (Fig.
435	5B, Movie S6, Movie S8). This morphology is similar to the initial outgrowth of
436	germinating <i>B. subtilis</i> spores (Pandey et al., 2013). We occasionally observed another
437	mode of recovery, occurring when round cells were constrained, or divided into, ovoid or
438	near-rod shapes. Once these near-rod shaped cells formed, they immediately began
439	rapid, rod-like elongation along their long axis (Fig. S5D).
440	
441	Rods Form from Local Outward Bulges and Grow Faster than Non-Rod Shaped
442	Cells
443	We focused on two salient features of the rod shape recoveries: 1) rod shape forms
444	locally, most often at one point on the cell surface, and 2) once a rod-like region is
445	formed, it appears self-reinforcing, both propagating rod shape and growing faster than
446	adjacent or attached non-rod shaped cells.
447	
448	We first wanted to understand how rod shape initiates de novo from spherical cell
449	
	surfaces. By examining the initial time points of recoveries, we found that rods begin as
450	surfaces. By examining the initial time points of recoveries, we found that rods begin as small outward bulges: local regions of outward (positive Gaussian) curvature flanked by
450 451	

452 showed a width distribution similar to that of the later emerging rods (Fig. 5D). Once

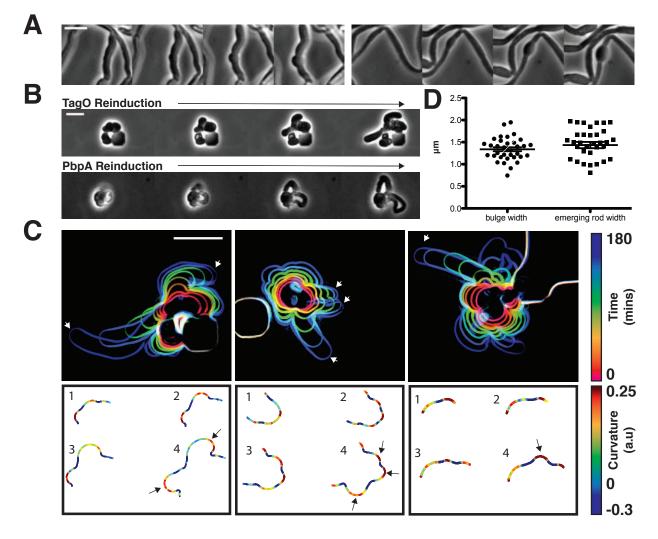
453	these bulges formed, they immediately began rapid elongation into nascent rods, which
454	would then thin down to wild type width over time. Bulge formation and rod recovery
455	were independent of cell division, as cells depleted of FtsZ still recovered rod shape
456	(Fig. S5B). Rather, these bulges appeared to arise randomly, evidenced by the fact that
457	different cells produced rods at different times during WTA or Pbp2a repletion. We
458	conclude that the appearance of a local outward bulge can act as the nucleating event
459	of rod shape formation.
460	

461 As emerging rods appeared to grow faster than adjacent round cells, we tested if the 462 doubling times of rod-shaped cells were faster than those of non-rods by measuring the 463 doubling times in our inducible TagO strain at different induction levels using both OD<sub>600</sub> 464 measurements and single cell microscopy under steady state conditions (Fig. 6B, S3C). 465 This revealed a sharp transition in doubling time that matched the conditions of the 466 rod/sphere transition: growth is slow when cells are spheres, yet greatly increases when 467 cells are rods (Fig. S3C, S5A). Furthermore, the doubling times of recovering rods was 468 similar to that of rods at steady state (Fig. S3C).

469

We believe the lower doubling time of rods is likely due to cell shape and not another
effect, such as the lack of WTAs, as 1) the doubling time of TagO-depleted cells
confined in the microfluidic chambers matched that of wild type cells; and 2) both the
doubling times and the boundary of the rod/sphere transition could be equivalently
shifted by changing the Mg<sup>2+</sup> concentration (Fig. 1E, S1, S5A). Combined, these results

- indicate that rod shape creates local, self-reinforcing regions that are poised for more
- 476 rapid growth; once any small region of the cell approximates a rod shape, growth of the
- rod-like region is amplified, growing faster than other regions, and thereby outcompeting
- 478 non-rod growth at the population level.
- 479
- 480 Figure 5. Sphere to rod transitions occur locally and lead to faster growth.





482 **(A)** Loss of rod shape proceeds continuously and without reversals, as shown by BEG300 cells grown in 483 12 mM xylose, shifted from 1mM Mg<sup>2+</sup> to 100  $\mu$ M Mg<sup>2+</sup> on a pad. Frames are 5 min apart. **(B)** Increases in 484 expression of *tagO* or *pbpA* from depleted spherical cells causes cells to emit rapidly elongating rods from

discrete points. (Top) BEG300 cells in 20 mM Mg<sup>2+</sup> were grown in 0 mM xylose for 4h, then transferred to 485 486 a microfluidic chamber and grown in 0 mM xylose and 20 mM Mg<sup>2+</sup> for 1h. Following this, tagO 487 expression was induced with 30 mM xylose at the first frame. (Bottom) BRB785 cells in 20 mM Mg<sup>2+</sup> were 488 depleted of Pbp2a by growth in 0 mM IPTG for 4h. At the start of the frames, they were transferred to an 489 agar pad containing 1mM IPTG to induce pbpA expression. Frames are 30 min apart. (C) Plots of cell 490 contours as cells recover from TagO depletion: (top) cell outlines are colored in time red to blue (0-491 180min). White arrows indicate emerging rods; (bottom) heat maps of curvature show that rods emerge 492 from small outward bulges (red) flanked by inward curvatures (blue). Black arrows indicate points where 493 emerging rods form. (D) The width of initial bulges and the rods that emerge from them are highly similar. 494 indicating the initial deformations may set the starting width of the rods. Error bars are SEM. All scale bars 495 are 5 µm. 496 497 Rod-shape Formation Correlates with Aligned MreB Motion and Increased Glycan 498 Crosslinking 499 We next sought to determine what features distinguished rods from round cells. As the 500 elongation of rod-shaped cells requires a sufficiently rigid cell wall (Fig. 1D-E, 5A), the 501 self-reinforcing growth of rods could arise from a few mutually compatible sources 502 relative to round cells in our strain: 1) The arrangement of PG strands could be such to 503 reinforce the rod (Amir and Nelson, 2012; Chang and Huang, 2014), 2) WTAs could be 504 preferentially incorporated into rods, or 3) The extent of crosslinking of newly inserted 505 material in the cell wall could be increased so as to make it more rigid (Loskill et al., 506 2014).

507

508 To assay the orientation of newly inserted cell wall, we imaged the motions of MreB as 509 we induced TagO-depleted cells to recover into rods. This revealed that oriented MreB 510 motion correlates with local shape: emerging rods displayed oriented MreB motion even 511 at the initial points of their formation, while attached round parent cells displayed 512 unaligned motion (Fig. 6A, Movie S7). This demonstrates that oriented MreB motion 513 correlates with local geometry and does not arise from a global, cell spanning change. 514 We next examined the overall cellular distribution of MreB in recovering cells with 515 confocal microscopy. This revealed that, immediately prior to rod emergence, MreB 516 transiently accumulated in a bright ring oriented perpendicular to the direction of rod 517 emergence, most often occurring at the interface of the bulge and the round cells 518 (Figure 6C, S5E).

519

520 The local reinforcement of rod shape in recovering cells could arise from preferential incorporation of the cell wall rigidifying WTAs. As the WTA ligases have been reported 521 522 to interact with MreB (Kawai et al., 2011), we tested if rod shape correlated with 523 increased WTA accumulation in emerging rods. To test this, we labeled recovering cells 524 with fluorescently labeled lectins that specifically bind to WTAs (Fig. S6A). Following 525 TagO reinduction, WTAs in recovering cells had a disperse, diffuse distribution around 526 the cell (Fig. S6B), equally present in the cell walls of both rods and spheres (Fig. 6B). 527 To test if the WTA ligases move with MreB, we created fluorescent fusions to these 528 proteins at their native locus and examined their dynamics with TIRFM. We were unable 529 to observe any of the circumferential motions expected if the WTA ligases moved with

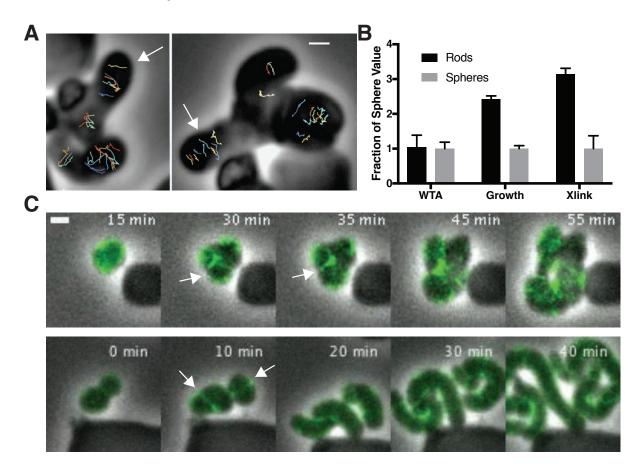
530 MreB; instead they appeared to be rapidly diffusing on the membrane (Fig. S6C, Movie 531 S9, Supplementary Text 2).

532

533 Next, we used muropeptide analysis to examine if there was a difference in the amount 534 of glycan crosslinking between rods and spheres. This revealed that the PG 535 surrounding spheres was significantly less crosslinked than rods (Fig. 6B, S6D). Thus, 536 the cell wall in rods is more crosslinked, and therefore presumably more load bearing 537 (Loskill et al., 2014). This result fits with the finding that WTA-depleted cell walls are 538 thicker and more irregular (D'Elia et al., 2006). Similarly, studies of plant cell walls have 539 shown that decreased crosslinking makes the cell wall more permeable to water, 540 resulting in swollen, less rigid cell walls (Redgwell et al., 1997)(Ishii et al., 2001). 541 542 Previous studies have shown that the rate of PG incorporation is unchanged during the

543 initial phases of depletion of components within the WTA pathway (Pooley et al., 1993). 544 To observe whether both spheres and rods inserted new PG during the process of rod 545 shape recovery in our assay, we used fluorescent D-amino-acids (FDAAs), which 546 crosslink into newly inserted cell wall. We grew TagO-depleted cells in a microfluidic 547 device in the presence of HADA, then switched the media to contain Cy3B-ADA as we 548 re-induced TagO expression. During rod emergence, the old cell wall signal (HADA) 549 remained in the sphere, while the emerging rod was almost entirely composed of new 550 (Cy3B-ADA) material, confirming the discrete nature of rod shape recovery. However,

- the attached spheres also incorporated Cy3B-ADA, indicating PG synthesis occurs in
- 552 both rods and spheres during recovery (Fig. S5C).
- 553
- 554 Figure 6. Cell wall crossslinking and growth are coupled to MreB-guided
- 555 formation of rod shape.



556

**(A)** (*left*) GFP-MreB trajectories during a sphere to rod transition. Emerging rods exhibit oriented MreB motion (white arrows) while attached round cells have unoriented motion. Scale bar is 1  $\mu$ m. **(B)** Fold change in the teichoic acid incorporation, doubling times (assayed by OD<sub>600</sub> measurements), and % crosslinked muropeptides of rods (inducible TagO with 30mM xylose in LB with 20 mM Mg<sup>2+</sup>) compared to spheres (grown in LB with 20 mM Mg<sup>2+</sup>). Error bars are SD. See also Figure S3C and S6. **(C)** During shape recoveries, immediately before rod emergence, MreB transiently accumulates in a bright ring where the bulge connects to the parent sphere. See also Figure S5E. Scale bar is 2  $\mu$ m.

564

565	In summary, this data gives new insights into what properties of the cell wall can be
566	modulated to create and stabilize rod shape: rod shape is not formed by preferential
567	localization of teichoic acids to rods, and both spheres and rods incorporate PG before
568	and during rod shape recovery, in line with reports that PG synthesis is unchanged by
569	the inhibition of WTA synthesis (Pooley et al., 1993). Rather, the only differences
570	between rod shaped and round cells we observed were 1) oriented motion of MreB in
571	rods, coupled with 2) an increased crosslinking of the inserted glycans. Thus, it appears
572	that not only does MreB direct glycan insertion into circumferential hoops, but also these
573	strands are more crosslinked, both properties are expected to increase the strength of
574	the rod sidewalls (Loskill et al., 2014)(Yao et al., 1999). It may be that these two
575	attributes are mechanistically linked, and a more oriented arrangement of glycan
576	strands might provide a more optimal arrangement of peptides for crosslinking
577	reactions. We note that as PG and WTA precursors share a common lipid carrier and
578	WTAs affect hydrolase activity (Kasahara et al., 2016), their depletion may cause other
579	rod-shape inhibiting PG abnormalities that we cannot observe.

580

#### 581 **Discussion**

The above experiments give new insights into the mechanism by which MreB builds rod shape. First, the curved ultrastructure of MreB filaments causes them to orient and move along the direction of greatest membrane curvature, inserting material in that direction. Second, both the formation and propagation of rod shape occurs by a local,

self-reinforcing process: once a local region of rod shape forms, it propagates more rod
shape. Finally, as far as we can determine, the primary differences between the growth
of rods and non-rods is the circumferential orientation of MreB motion and increased
glycan crosslinking.

590

591 Combined, these findings indicate that MreB filaments function as curvature-sensing 592 rudders, a property that allows them to organize cell wall synthesis so that it builds rod 593 shape: MreB filaments orient along the greatest membrane principal curvature, thereby 594 constraining the activity of the associated PG synthases so that, as they move via their 595 synthetic activity, they deposit highly crosslinked glycans oriented in the direction of that 596 curvature, and this arrangement of glycan insertion reinforces rod shape. Even during 597 the initial stages of rod shape formation, oriented MreB motion and rod shape always 598 coincide, and the intrinsic curvature of MreB filaments suggests these properties cannot be uncoupled. This coupling appears to be an essential component of the Rod system: 599 600 by linking filaments that orient along the greatest principal curvature to cell wall 601 synthetic enzymes reinforcing that curvature, the Rod complex creates a local, self-602 organizing system that allows bacteria to both maintain rod shape and also establish 603 rod shape *de novo*.

604

In established rods, we propose that MreB maintains and propagates rod shape via
feedback between existing shape, filament orientation, and subsequent shapereinforcing PG synthesis. As rod-shaped cells grow (Fig. 7A1), MreB filaments orient

608 along the more curved axis around the bacterial width (Fig. 7A2). Because MreB 609 filaments always translocate along their length (Olshausen et al., 2013), filament 610 orientation constrains the activity of the associated PG synthases such that new cell 611 wall is inserted in bands predominantly oriented around the width of the rod (Fig. 7A3). 612 This circumferential insertion of glycan strands, combined with a high level of 613 crosslinking between them, yields a highly connected, anisotropic arrangement of 614 material that reinforces rod shape (Fig. 7A1), which allows continued MreB filament 615 orientation. This feedback loop can continue as long as the material within the rod 616 sidewalls is sufficiently rigid to withstand the stresses arising from the internal turgor 617 pressure, allowing the rod shape to be robust once it is formed.

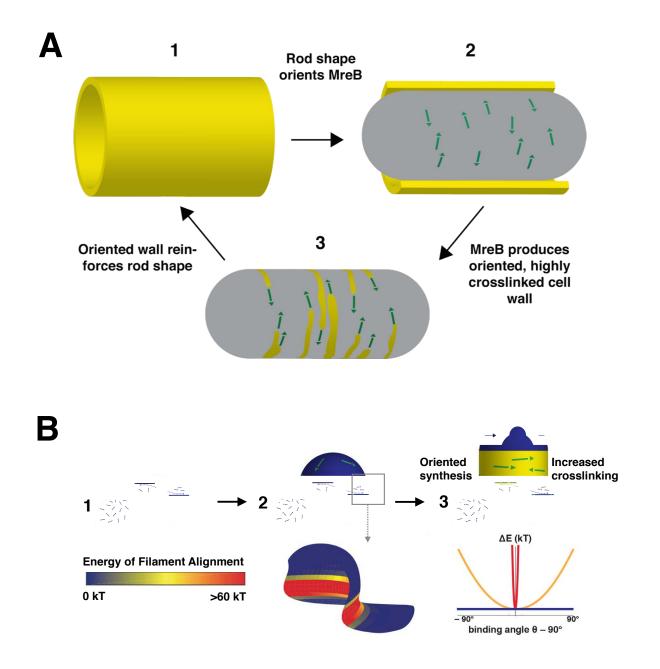
618

619 The coupling between the local sensing and reinforcement of differences in principal 620 curvature could also allow the *de novo* formation of rod shape. In round cells, there is 621 no difference in principal curvatures (Fig. 7B1), so MreB motion is isotropic. Rods do not 622 form by squeezing these round cells across one axis, rather we observe them forming 623 by the amplification of local rod-like regions. Given the rapid timescale of our recoveries, 624 the Rod system appears poised to propagate any shape variations that create curved 625 regions favorable to oriented MreB motion. Once regions of oriented motion are 626 established, they self-propagate and elongate, creating a new rod shape and thus 627 continued oriented MreB motion. The most common shape variation we observe 628 preceding rod emergence is small outward bulges flanked by regions of inward 629 curvature (Fig. 5C). It remains to be determined how these initial bulges form and what

630 cellular factors are involved in this process. They could arise from local changes in cell 631 wall stiffness: a local softening of the cell wall has been observed to induce the rod 632 shaped outgrowth of germinating fission yeast spores (Bonazzi et al., 2014). 633 634 The geometry at the interface of these outward bulges plays a central role in our model 635 of rod shape formation. In three dimensions, the intersection at the bulge and the 636 sphere creates a geometry that can establish a zone of aligned filaments: while both the 637 parent sphere and the outward bulge have principal curvatures in the same direction 638 (positive Gaussian curvature), the intersection of the sphere and bulge creates an 639 interface with strong differences in principal curvatures, one inward, and one outward 640 (negative Gaussian curvature). Upon entering these negatively curved regions it is 641 energetically unfavorable for the inwardly curved MreB filaments to deviate from their 642 preferred binding orientation, as our modeling indicates that this region presents a steep 643 well in the energy profile for alignment (Fig 7B2 and Supplemental Text 1). Thus, 644 filaments moving into this rim from either side would reorient to move along it, creating a 645 concentrated band of filaments moving around the bulge neck. This concentrated ring of 646 oriented MreB filaments may then construct a local region of rod shape that 647 subsequently self-propagates into an emerging rod (Fig. 7B3). In support of this 648 hypothesis, immediately preceding rod shape formation, we observe concentrated 649 bands of MreB transiently appearing at the neck of emerging bulges (Fig. 6C, S5E). 650 Likewise, similar patterns of MreB accumulation at points of negative Gaussian 651 curvatures have been observed in recovering *E. coli* L-forms (Billings et al., 2014).

#### Figure 7. Model for how MreB filament orientation along the greatest curvature

both maintains and establishes rod shape.



652

653 (A) Rod-shaped cells present a single curved axis along which MreB filaments orient (1). This orientation

determines the direction of MreB motion (2), thus orienting the insertion of new cell wall material around

the rod, and allowing an increased crosslinking between strands (3). This highly cross-linked,

656 circumferential arrangement of cell wall material reinforces rod shape (1), leading to more aligned MreB

657 filaments, thus creating a local feedback between the orientation of MreB filaments, oriented cell wall 658 synthesis, structural integrity of the rod, and overall rod shape. (B) MreB motion in spherical cells is 659 isotropic (1), but the introduction of an outward bulge (2, upper) creates a curved geometry (red) at the 660 neck of the bulge that initiates rod shape formation. Due to the high energy of alignment in this region, (2) 661 lower and chart), any filaments that encounter the neck of the bulge would prefer to align to point around 662 the neck rather than cross it, creating a ring-shaped region of aligned MreB motion that nucleates rod 663 formation. Repeated rounds of oriented synthesis around the ring could initiate the elongation of a rod 664 from the initial bulge site (3), beyond which rod shaped elongation would be self-sustaining. Colors 665 correspond to the difference of alignment energies along the two principal curvatures at the negatively-666 curved neck region (red), flat regions with one dimension of curvature (yellow), and the positively-curved 667 sphere/bulge (blue).

668

669 The common observation of MreB accumulation at the necks of rod-producing bulges in 670 both *E. coli* and *B. subtilis* hints at a solution to an outstanding discrepancy: Why do 671 inwardly curved MreB filaments show an enriched localization at negative Gaussian 672 curvatures (inward dimples or the more curved faces of bent cells) (Billings et al., 2014; 673 Renner et al., 2013; Ursell et al., 2014), and how is this enrichment maintained as 674 filaments move around the cell? The finding that MreB filaments align along the greatest 675 curvature poses a solution: If the sharpness of filament alignment changes in response 676 to the difference in principal curvatures in each region they pass through, areas of 677 negative Gaussian curvature may act as points that focus the subsequent motion of 678 filaments so that, on average, more filaments pass through these regions.

679

The tendency of MreB to align and move along the direction of greatest principal curvature may also explain the absence of MreB at cell poles. Consistent with our model for binding, we observed MreB filaments bound to the round poles of liposome tubes *in vitro* (Fig. 4A). In the cell, however, MreB filaments move directionally, and filaments entering the symmetrically curved pole in any orientation would quickly translocate out into the cylindrical cell body where they would reorient along the single direction of curvature.

687

688 While rod-shaped cells show both an increased rate of growth and oriented MreB 689 motion, it is unlikely these phenomena are mechanistically linked. Rather, the 690 decreased rate of growth of non-rods likely arises from a downstream effect of the lack 691 of rod shape on cell physiology. Indeed, many spatial processes in *B. subtilis*, such as 692 chromosome segregation and division site selection, read out and partition along the 693 long axis established by rod shape (Jain et al., 2012). Thus, the slower doubling times 694 observed in non-rod shaped cells may arise from the improper spatial organization of 695 these processes, or stress responses to this spatial disarray.

696

As the curvature of membrane-bound MreB filaments (200nm) observed *in vitro* is much greater than the cell diameter (900nm), these findings suggest that the curvature of MreB filaments does not define a specific cell radius; rather filament curvature acts to orient PG synthesis to maintain (Harris et al., 2014) or reduce cell diameter. If the curvature of MreB filaments reflects the smallest possible cell diameter, bacterial width

702 may be specified by opposing actions from the two spatially distinct classes of PG 703 synthases: a decreasing, "thinning" activity from the action of MreB and its associated 704 SEDS family PG synthases, and an increasing "fattening" activity from the non-MreB 705 associated Class A PG synthases. 706 707 Conclusion 708 To construct regular, micron-spanning shapes made of covalently crosslinked material, 709 nature must devise strategies for coordinating the activities of disperse, nanometer-710 scale protein complexes. This work reveals that the role of MreB in creating rod shape 711 is to locally sense and subsequently reinforce differences in principal curvatures. The 712 local, short-range feedback between differences in curvature, MreB orientation, and 713 shape-reinforcing cell wall synthesis provides a robust, self-organizing mechanism for 714 the stable maintenance and rapid reestablishment of rod shape, allowing the local 715 activity of short MreB filaments to guide the emergence of a shape many times their 716 size. 717 **Author Contributions** 718 719 All authors contributed intellectual and editorial work to the development of the 720 manuscript. S.H., C.N.W., and E.C.G. designed, performed, and interpreted 721 experiments. P.S., T.I., and J.L. contributed the electron microscopy work shown in Fig. 722 4. F.W. and A.A. contributed biophysical modeling work shown in Fig. 4, Fig. 7, and

supplemental text. L.D.R performed microfluidic device fabrication. K.S. and S.W.

- performed peptidoglycan crosslinking analysis. Y.S. wrote software for growth analysis.
- A W. B. performed the FtsZ inhibition experiments.

726

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- 739

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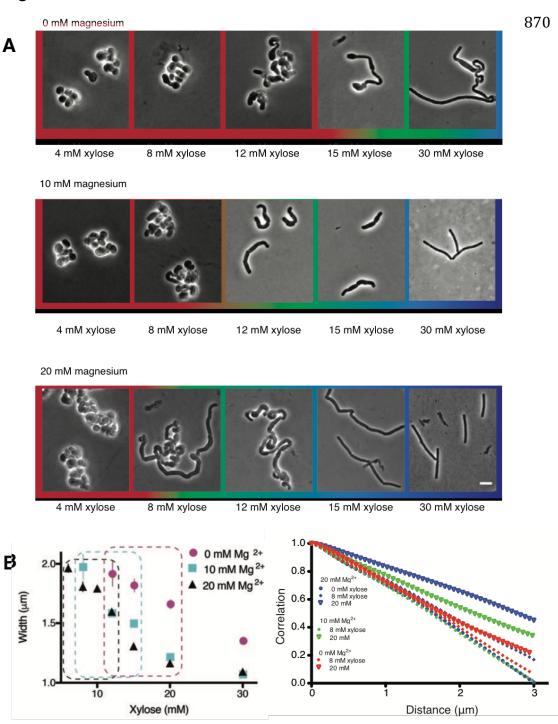
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# 867 Supplemental Figures

# 868 S1– Varying magnesium levels in the growth medium changes cell shape. Related

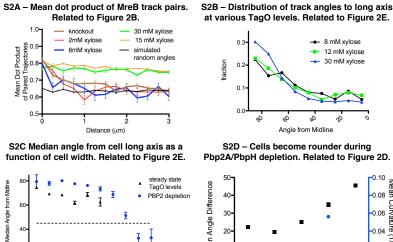
869 to Figure 1.

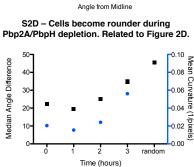


(A) TagO inducible cells grown in LB supplemented with varying Mg<sup>2+</sup> levels (0, 10 and 20 mM), show 872 873 similar trends in cell shape across increasing xylose concentrations, with the appearance of more rodshaped cells that become thinner as xylose levels increase. Exogenous Mg<sup>2+</sup> reduces the amount of 874 875 TagO induction needed for rod shape, evidenced by shift in the amount of xylose required to form rods as  $Mq^{2+}$  is increased. (Color Outlines: Blue = rods, Green = Mixed rods and non-rods, Red = non-rods). (B) 876 877 Left Plot of cell width as a function of TagO induction at different Mg<sup>2+</sup> concentrations (error bars are 878 SEM). Areas not plotted at lower xylose levels are regions where cells are round, with no width axis. 879 Dotted rectangles mark conditions where both round cells and wide rods exist. Error bars are Standard 880 Error of the Mean (SEM). Right At low xylose and magnesium levels, tangential correlation along the cell 881 contours falls off faster, indicating loss of rod shape. Correlation of angles was calculated as described in 882 methods. The curves shown are population averages of tangential correlations at selected xylose and 883 magnesium concentrations. A cutoff of 3 u m is applied as this is the mean cell length of B. subtilis.

884

#### 885 S2 (A-E) – Relationships between cell width, MreB orientation, and cell shape. 886 Related to Figure 2.





S2E Cell roundness as a ratio of principal curvatures. Related to Figure 2E.

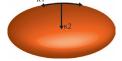
2.0

Width (in µm)

10 1.5 Ŧ

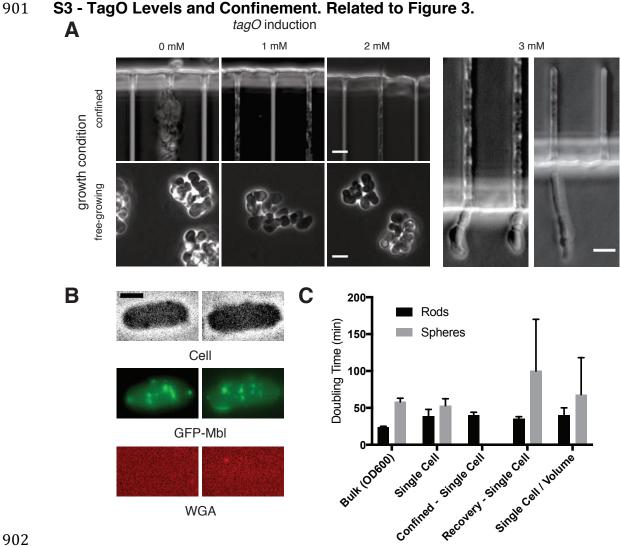
2.5

3.0



887

(A) The mean dot product of MreB track pairs vs. distance between the pairs was calculated and binned 888 889 at 0.25  $\mu$  m intervals. This shows a high alignment between pairs across the cell length for rods at high 890 xylose (15 and 30mM). Round cells (2 and 6mM xylose) show a high alignment at very short distances (< 891 500 nm), beyond which alignment falls off rapidly, approaching the value expected for randomly oriented 892 angles (black line represents a simulation of a uniform angular distribution). (B) MreB filament motion is 893 predominantly circumferentially oriented over a range of xylose levels (8-30mM) even though cells show 894 varying widths. At 8 and 12 mM xylose, cells are a mix of rods and spheres, and therefore angles were 895 only calculated for cells with identifiable long axes. (C) Median angle from the long axis of cells as a 896 function of cell width at steady state TagO levels and PBP2a depletions (shown separately). (D) Mean 897 sidewall curvature of cells increases during a Pbp2a/PbpH depletion (blue circles), along with a decrease 898 in aligned MreB motion (black squares). (E) The principal curvatures along the cell length ( $\kappa$ 1) and cell 899 width ( $\kappa$ 2) are calculated and the ratio  $\kappa$ 1/ $\kappa$ 2 is taken as a measure of cell roundness. Cells become 900 round as this ratio approaches 1. All error bars are SEM.



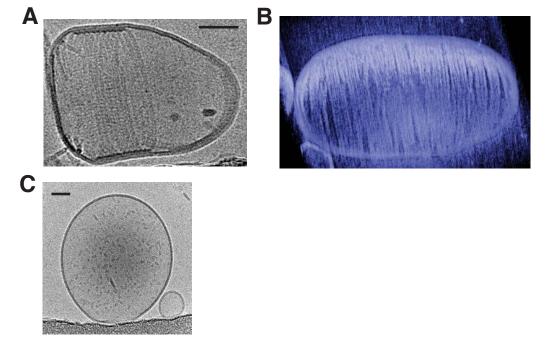
# S3 - TagO Levels and Confinement. Related to Figure 3.

# 902 903

(A) Microfluidic confinement controls cell shape in cells with low TagO levels. (Left) Phase contrast 904 images of BEG300 grown under differing teichoic acid induction levels in bulk culture or confined in 905 chambers. (Right) Cells swell upon escaping from confinement. Swelling is visible both at initial stages of 906 depletion, corresponding to when MreB movies were collected (left panel, cf. Figure 3C and 907 Supplementary Movie 3), or at longer stages when cells were chained (right panel). Scale bars = 5  $\mu$  m. 908 (B) Panels showing images of phase contrast, GFP-Mbl, and Alexa455-conjugated WGA of a 909 representative protoplast confined into rod shape. MreB filaments are aligned along the cell 910 circumference, (middle panel), but do not regrow cell wall as indicated by the lack of signal in the 911 Alexa455 channel. Scale bars are 2  $\mu$  m. (C) Doubling time of BEG300 in different conditions. "Bulk" 912 indicates cultures grown in liquid suspension and measured by OD<sub>600</sub>. "Single Cell" indicates cells were 913 grown under agarose pads, with doubling time measured by assaying the change in cell area over time 914 using phase contrast microscopy. "Confined - Single Cell" indicates the doubling time of cell area of 915 TagO-depleted cells confined into rod shape in microchambers as in Figure 3A and S3A; "Recovery -916 Single Cell' is the single-cell doubling time (in volume) of TagO-depleted cells during rod shape recovery 917 in a cellASIC microfluidic device as in Figure 5B. Note that spherical cells in these recoveries show a 918 slower doubling time with a larger standard deviation due to a subpopulation of cells dying during the 919 experiment; "Single cell / Volume" indicates the doubling time of the volume of single cells grown in a 920 cellASIC microfluidic device. As this chamber has a fixed Z height, cell volume can be approximated from 921 measures of the 2D area. Error bars are standard deviation.

#### 922 S4 – T. maritima MreB filaments assembled in liposomes support alignment to

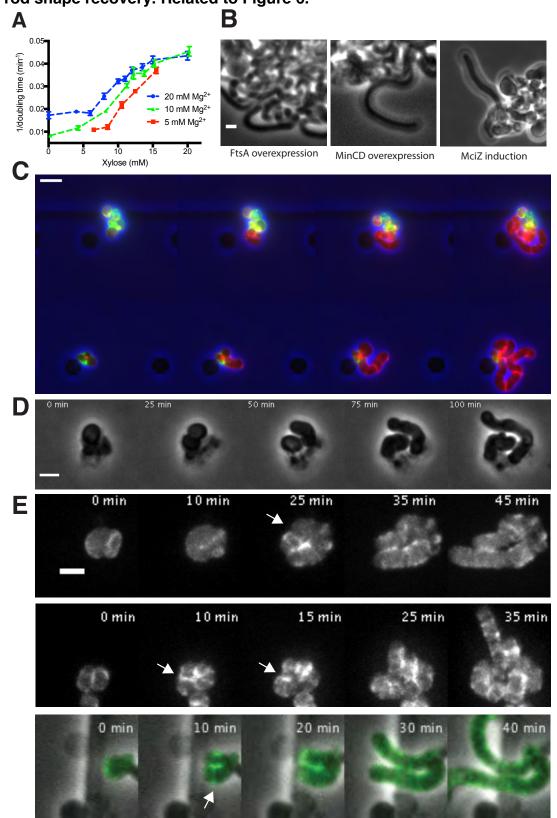
#### rod axis. Related to Figure 4. 923



# 924 925

(A) The arrangement of MreB filaments inside the liposome is helical. Scale bar is 50 nm. (B) Many long 926 T. maritima MreB filaments inside an artificial liposome, assembled in vitro and imaged by electron 927 tomography. Almost the entire inner surface of the liposome is covered with filaments, leading to 928 deformation of the normally spherical liposome. Corresponding movie: SM5, first part. Scale bar is 50 nm. 929 (C) Control showing that liposomes are spherical in the absence of MreB. Scale bar is 50 nm.

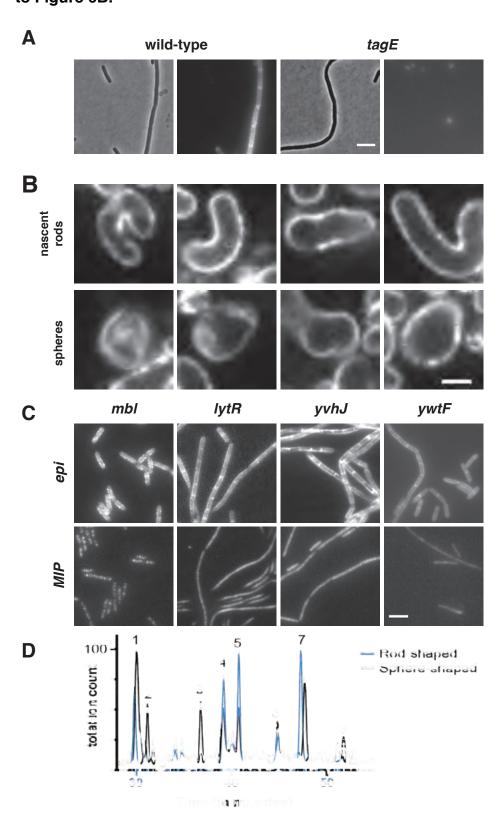
# 931 S5 – Growth of rod-shaped and spherical cells measured by doubling times, and 932 rod shape recovery. Related to Figure 6.



934 A) Rate of doubling (1/doubling time), calculated from  $OD_{600}$ , increases with increasing levels of TagO as 935 round cells become more rod-like. Increasing Mg<sup>2+</sup> causes these curves to shift leftward, as Mg<sup>2+</sup> 936 stabilizes rod shape in combination with WTAs (see Fig S1A). Error bars are SEM. (B) Rod shape 937 recovery occurs in the absence of cell division and FtsZ filaments. Inhibition of FtsZ filaments was 938 conducted by three means: FtsA overexpression (bAB388, grown with 1 mM IPTG and 60 mM xylose). 939 MinCD overexpression (bAB327 grown with 1 mM IPTG and 60 mM xylose), and MciZ induction (bAB343 940 grown in 1 mM IPTG and 30 mM xylose). In all cases, cells recovered rod shape. (C) Pulse chase 941 labeling with FDAAs during TagO recoveries indicates that while emerging rods are composed of new cell 942 wall, both spheres and rods incorporate new cell wall material. BCW82 was grown in a microfluidic chamber with 0 mM xylose, 20 mM Mg<sup>2+,</sup> and 3  $\mu$  M HADA (green). Prior to imaging the medium was 943 944 switched to 30 mM xylose (to induce TagO expression), 20 mM Mg<sup>2+</sup> and 3  $\mu$  M cy3B-ADA (red, to 945 visualize new cell wall incorporation). Cell outline (from phase) is shown in blue. Scale bar is 5  $\mu$  m; 946 frames 30 min apart. (D) A montage of a rod shape recovery occuring after a division that produced an 947 ovoid, near rod-shaped cell that subsequently elongated as a rod. This example taken from an 948 experiment with BRB785, where Pbp2a was first depleted (in a *pbpH* null) to make round cells, then 949 Pbp2a was reinduced with 1 mM IPTG. See also bottom panel of S5E. (E) MreB localizes in a ring-like 950 structure (white arrows) at the neck of emerging bulges, immediately prior to rod shape formation. 951 BEG300, containing GFP-MreB was depleted of TagO by growing in bulk culture in media lacking xylose. 952 Cells were then loaded into a cellASIC device, and grown for 2 hours in the same media with 1 mM IPTG 953 added to induce GFP-MreB expression. At the start of imaging, the media was switched to 30 mM xylose 954 to induce TagO expression, and Z-stacks of GFP MreB were taken using a spinning disk confocal every 5 955 minutes. Shown is the maximal intensity projection of entire cell.

#### 957 S6 - ConA staining of PY79 tagE and muropeptide analysis of BEG300. Related to Figure 6B.

958



960 (A) Concanavalin A conjugated to Alexa Fluor 647 specifically stains wall teichoic acids and localizes 961 uniformly around the entire cell during sphere to rod transitions. A comparison of PY79 and  $\Delta$  tagE cells 962 stained with ConA-A647 reveals specificity of ConA for WTAs. The tagE gene is responsible for the 963 glycosylation of wall-teichoic acids, rendering them susceptible to ConA binding. Scale bar is 5  $\mu$  m. (B) 964 Fluorescence intensity of Alexa647-ConA, is comparable in rod shaped and round cells during sphere to 965 rod recoveries. Furthermore, the WTA incorporation is diffuse, and not banded or localized. BEG300 966 was grown in bulk culture and rod shape was induced by increasing TagO levels (0 to 30 mM xylose). 967 Scale bar is 2.5  $\mu$  m. (C) Wall teichoic acid ligases diffuse homogenously across the cell surface. Ligases 968 were tagged at the native locus and promoter with msfGFP and imaged continuously with 100 ms 969 exposures. Epifluorescent images were collected under obligue laser illumination and maximal intensity 970 projections (MIPs) were created over 100 frames of TIRF illumination (see Movie S8). For comparison, 971 msfGFP-tagged Mbl, which localizes in discrete patches, is shown. Scale bar is 5  $\mu$  m. (D) Overlaid 972 LC/MS traces corresponding to reduced muropeptides isolated from the sacculi of rod-shaped and 973 sphere-shaped B. subtilis. The total ion count was scaled to the highest peak for each trace, and 974 muropeptides were identified under the total ion count. Peaks 1-3 correspond to uncrosslinked 975 muropeptides; peaks 4-8 correspond to crosslinked muropeptides. Muropeptides identified included the 976 following: a tripeptide (GlcNAc-MurNAc-L-Ala-D-Glu-m-DAP by its [M+1]=871.3 (Exact mass=870.3) were 977 identified under peak 1; a dipeptide (GlcNAc-MurNAc-L-Ala-D-Glu) was identified under peak 2 978 [M+1]=699.7 (Exact mass=698.7): a tetrapeptide (GlcNAc-MurNAc-L-Ala-D-Glu-m-DAP-D-ala by its 979 [M+1]=941.2 (Exact mass=940.2) was identified under peak 3; crosslinked, dimeric muropeptides were 980 identified in peaks 4-7 containing the tetrasaccharide (GlcNAc-MurNA- L-Ala-D-Glu-m-DAP-D-ala-m-981 DAP-D-Glu-L-Ala MurNAc-GlcNAc) by [M+1]=1795.8 and [M+2]/2=898.4; (Exact masses=1794.8); and 982 peak 8 corresponded to a crosslinked, trimeric muropeptide containing two tetrapeptides (GlcNAc-MurNA-983 L-Ala-D-Glu-m-DAP-D-ala) and a tripeptide (GlcNAc-MurNAc-L-Ala-D-Glu-m-DAP); [M+3]/3= 906.9 984 (Exact mass=2717.7). To calculate the amount of each species, peaks were integrated by their extracted 985 ion chromatograms. Crosslinked species were calculated using previous literature quantification methods 986 (Glauner et al., 1988). In the rod-shaped B. subtilis, 41% crosslinking was observed; in sphere-shaped 987 Bacillus subtilis, only 11% crosslinking was observed.

# 989 Materials and Methods

990

991 **Overnight culture growth.** All *B. subtilis* strains were prepared for experimentation as 992 follows: strains were streaked from -80°C freezer stocks onto lysogeny broth (LB) agar 993 plates. Following >12 hours of growth at 37°C, single colonies were transferred to 994 serially diluted overnight bulk liquid cultures in LB supplemented with 20 mM 995 magnesium chloride, placed on a roller drum agitating at 60 rpm, and grown at 25°C. 996 After >12 hours growth to  $OD_{600} < 0.6$ , these starter cultures were transferred to or 997 inoculated into subsequent growth conditions. All strains with tagO under inducible 998 control were grown overnight in the presence of 30 mM xylose unless otherwise noted.

999

Single cell and bulk doubling time measurements. For the experiments in Fig. 6B and Fig. S3C, BEG300 cells were inoculated in the indicated medium (LB with 20 mM MgCl<sub>2</sub> unless otherwise stated) from logarithmic phase overnights; "rods" were grown from a low dilution with 30 mM xylose, and "spheres" were grown with 0 mM xylose.

For bulk culture doubling time measurements, doubling times were calculated from the slope of a graph of time vs. dilution for a succession of serial dilutions of a given strain. Time, the dependent variable, was taken as the time for a given dilution to pass the OD cutoff of  $OD_{600} = 0.20$ .

1008 Single cell measurements were made in three ways.

i) Spherical and rod-shaped cells were allowed to grow on agarose pads made
 with LB supplemented with 20 mM MgCl<sub>2</sub>. 30 mM xylose was added to

1011agarose pads for rod-shaped cells. Cells were imaged every 2 minutes for 41012hours with phase contrast microscopy as described in the section below.

- ii) Spherical and rod-shaped cells were grown in the CellASIC B04A plate in LB
  supplemented with 20 mM MgCl<sub>2</sub> for spherical cells and LB supplemented
  with 20 mM MgCl<sub>2</sub> and 30 mM xylose for rod-shaped cells. The CellASIC unit
  confined the cells in the Z dimension due to the fixed height of the ceiling.
  Cells were imaged every 10 minutes for 2 hours using phase contrast
  microscopy as described in the section below.
- 1019iii)For cells growing in the mother machine microfluidic device (see below), the1020expansion of the cell length along the channel was quantified using FIJI1021(Schindelin et al., 2012; Schneider et al., 2012); only the cells closest to the1022mouth of the channel were counted. Since cells were always oriented along1023the length of the channel (see Fig. 3A, S3A), changes in expansion in this1024dimension accounted for all growth.

1025

**Imaging – phase contrast microscopy.** Phase contrast images were collected on a Nikon (Tokyo, Japan) Ti microscope equipped with a 6.5  $\mu$ m-pixel Hamamatsu (Hamamatsu City, Japan) CMOS camera and a Nikon 100X NA 1.45 objective. Cells were collected by centrifugation at 6,000 x *g* for 2 min and re-suspended in the original growth medium. Unless otherwise specified, cells were then placed on No. 1.5 cover qlass, 24 x 60 mm, under a 1 mm thick agar pad (2-3% agar) containing LB

supplemented with 20 mM magnesium chloride. Unless otherwise noted, all cells were
imaged at 37°C on a heated stage.

1034

1035 **Imaging – MreB particle tracking.** Images were collected on a Nikon TI microscope 1036 with a 6.5 µm-pixel CMOS camera and a Nikon 100X NA 1.45 objective. Cells of strain 1037 BEG300 were grown overnight in LB supplemented with 30 mM xylose, 20 mM 1038 magnesium chloride, 1  $\mu$  g/mL erythromycin, and 25  $\mu$  g/mL lincomycin at 25°C at the 1039 specified xylose concentrations. 11  $\mu$  M isopropyl  $\beta$ -D-1-thiogalactopyranoside (IPTG) 1040 was added to induce GFP-MreB and the cells were shifted to 37°C and allowed to grow 1041 for 2 hours before imaging. Cells of strain BEG202 ( $\Delta$  tagO) with GFP-Mbl under a 1042 xylose-inducible promoter were grown overnight at 25°C in LB supplemented with 20 1043 mM magnesium chloride and 0.125 mM xylose, and shifted to 37°C for 2 hours before 1044 imaging. Cells were placed on cleaned glass coverslips thickness No. 1.5, as described 1045 in the next section. 3-6% agar pads were prepared in LB supplemented with 20 mM 1046 magnesium chloride, 11  $\mu$  M IPTG and the desired concentration of xylose. Images 1047 were collected for 3 min at 1 or 2 s intervals, as specified.

1048

1049 **Imaging – slide preparation.** Coverslips were sonicated in 1 M KOH for 15 min, 1050 followed by 5 washes with water. Coverslips were washed twice with 100% ethanol, and 1051 then sonicated in 100% ethanol, followed by one more wash in 100% ethanol. They 1052 were stored in ethanol and dried for 10 min before use.

1053

Imaging – spinning disk confocal. Images were collected on a Nikon TI microscope with a Hamamatsu ImagEM (EM-CCD) camera (effective pixel size 160 nm) and Nikon 1056 100X NA 1.45 TIRF objective. Z stacks were obtained at 0.2  $\mu$  m slices. Total image depth was 3  $\mu$  m. Only the top 3 slices of the cell were used in maximum intensity projections in Figure 3D.

1059

1060 Image processing. All image processing unless otherwise specified was performed in 1061 FIJI (Schindelin et al., 2012; Schneider et al., 2012). Images used for particle tracking 1062 were unaltered, except for trimming five pixels from the edges of some videos to 1063 remove edge artifacts detected by the tracking software. Phase contrast images and 1064 fluorescent images of protoplasts were adjusted for contrast. Phase contrast images 1065 presented in the manuscript collected from cells in the custom microfluidic device, which 1066 did not undergo quantitative processing, were gamma-adjusted ( $\gamma$ =1.5) to compensate 1067 for changes in brightness occurring at the device's feature borders; such processing 1068 was not used for growth quantification. The images for Supplementary Movie 2 were 1069 background-subtracted for viewing purposes; unaltered images were used for 1070 quantitative processing in all cases.

1071

Microfluidics. The custom microfluidic setup used to confine cells in Figure 3A-C, Supplementary Figure 3A, and Supplementary Movie 3 was previously described in (Norman et al., 2013). Briefly, a polydimethylsiloxane slab with surface features was bonded to a 22 x 60 mm glass coverslip by oxygen plasma treatment followed by

1076 heating to 65°C for >1 hr. The features in our setup differed from those described in 1077 (Norman et al., 2013), particularly in the omission of a second, wider layer in the cell 1078 chambers, which enhanced growth at timescales beyond that of our experiments. 1079 Syringes containing growth medium were connected to the microfluidic features using 1080 Tygon tubing stainless steel dispensing needles (McMaster Carr Supply Company, 1081 Elmhurst, Illinois). Medium was supplied to cells at a constant rate of 2-5  $\mu$  L/min using 1082 automatic syringe pumps. Imaging was carried out using phase contrast microscopy as 1083 described above. For the microfluidics experiments in Figures 5 and 6 and 1084 Supplementary Movie 6 (top), 7, and 8, the CellASIC platform from Merck Millipore 1085 (Billerica, Massachusetts) was used with B04A plates.

1086

1087 **Cell confinement experiments.** The cell confinement experiment in Figure 3A-C was 1088 conducted by first loading cells into the chamber: BEG300 cells were grown to 1089 stationary phase ( $OD_{600}$  3.0 – 5.0) in LB supplemented with 20 mM magnesium 1090 chloride, passed through a 5  $\mu$  m filter, and concentrated 100-fold before loading in the 1091 custom-made microfluidic device. Both phase contrast and fluorescent imaging were 1092 performed as described in the "Imaging" section above. For observing MreB movement, 1093 MreB-GFP expression was induced with 50  $\mu$  M IPTG upon loading into the microfluidic 1094 chamber, and cells were imaged every 2 s with a camera exposure time of 300 ms.

1095

1096 **MreB alignment within protoplasts.** Cells of strains bJS18 (GFP-Mbl) and bEG300 1097 (GFP-MreB) were grown overnight at 25°C in the osmoprotective SMM media (LB

1098 supplemented with 20 mM magnesium chloride, 17 mM maleic acid, 500 mM sucrose, brought to a pH of 7.0) with maximum xylose induction (30 mM); cells were shifted to 1099 1100 37°C in the morning. For strain bEG300, the SMM media was supplemented with 8mM 1101 xylose (for intermediate TagO induction). Following 2 hours of growth, 10 mg/mL of 1102 freshly suspended lysozyme was added to the cultures with  $OD_{600} > 0.2$ . After growing 1103 for 1-2 hours in lysozyme, the cells were spun and concentrated. 6% agar pads made in 1104 LB-SMM were made using a polydimethylsiloxane (PDMS) mold with crosses (2, 4 and 1105 5  $\mu$  m arms and 5  $\mu$  m center). The cells were placed on the agar pad for 2 min, 1106 allowing the cells to settle in the crosses. The pad was then placed in a MatTek 1107 (Ashland, Massachusetts) dish for imaging. To check for the presence of cell walls in 1108 protoplasts, wheat germ agglutinin conjugated to Alexa-555 was used. 20  $\mu$  L of 1 1109 mg/mL stock was added to 1 mL of cells 20 min before the start of imaging. Some 1110 cultures, after inoculation in the MatTek dish, were incubated at 37°C for 30 min to allow 1111 cell growth.

1112

**Depletions in liquid culture.** TagO depletions in Figure 2A were conducted using strain BEG300 in liquid culture. Cells were prepared as overnights, as described above, then grown at the specified xylose concentration at 37°C in LB with 20 mM magnesium chloride for 4 hrs. The cells were then imaged as described above in the "Imaging – MreB particle tracking" section.

1118

1119 Pbp2A depletions shown in Figure 2C were conducted in liquid culture using strain

1120 BRB785 with an IPTG - inducible Pbp2A fusion at the native locus with the redundant 1121 transpeptidase PbpH deleted. This strain was grown overnight in the presence of 2 mM 1122 IPTG, and then inoculated into CH media containing 2 mM IPTG, 0.015% xylose, and 1123 20 mM magnesium chloride to stabilize the cells against lysis. At an OD<sub>600</sub> of 0.6, cells 1124 were spun down in a tabletop centrifuge and washed 3 times in CH media lacking IPTG. 1125 Cells were placed under agar pads containing 20 mM magnesium chloride, and 1126 spinning disk confocal images were taken every 5 s on a Nikon Ti microscope with a 1127 100X 1.49 TIRF objective and a Hamamatsu ImagEM C9100-13 EM-CCD camera 1128 (effective pixel size of 160 nm).

1129

**Depletions under solid state medium.** Depletions shown in Figure 5A were conducted using strain BEG300. Cells were prepared as overnights in LB with 1 mM magnesium chloride and 12 mM xylose. In the morning, they were washed in LB with 12 mM xylose and no magnesium and placed under a 3% agar pad with the same medium. Phase contrast images were collected every 5 min using a Photometrics (Tucson, Arizona)

1135 CoolSNAP HQ2 CCD camera.

1136

**Repletions.** Repletions of TagO or Pbp2a on pads, as shown in Figure 5B and Supplementary Movie 6 (bottom), were performed with strains BEG300 and BRB785 respectively. Cells were grown as overnights, as described above, then depleted at  $37^{\circ}$ C for >4 hours in LB with 20 mM magnesium chloride and collected by centrifugation at 6,000 x *g* for 2 min. The cells were re-suspended in LB supplemented with 20 mM magnesium chloride and 1 mM IPTG (BRB785) and 30 mM xylose (BEG300), placed

under 5% agarose pads on coverslips with thickness No. 1.5 for imaging. Phase
contrast images were collected every 5 min using a Photometrics CoolSNAP HQ2 CCD
camera.

1146 For the repletions shown in Figures 5B-C, 6A, Supplementary Figure 5C, and 1147 Supplementary Movie 6 (top) and 7, performed in the CellASIC microfluidic device in a 1148 B04A plate, BCW82 and BEG300 cells were grown to  $OD_{600}$  1.2 – 1.5 in LB 1149 supplemented with 20 mM magnesium chloride, centrifuged to pellet large clumps for 3 1150 min at < 500 x g, and the supernatant loaded into the plate. Growth medium was 1151 supplied at 5-6 PSI. Cells were grown for at least an additional 30 min before the 1152 addition of inducer to the growth medium. Phase contrast images were collected every 1153 10 min. Fluorescent images were collected on the imaging setup described in the 1154 "Imaging – MreB Particle Tracking" section above: GFP-MreB was induced upon 1155 loading into the microfluidic chamber with 1 mM IPTG, and MreB dynamics were 1156 observed for 3 min after every 10 min, using 300 ms camera exposures taken every 2 s. 1157 For the repletions shown in Figure 6C and S5E, the same procedure was used, 1158 but with imaging performed on the spinning disk confocal microscope described in 1159 "Imaging – Spinning Disk Confocal". Z-stacks were collected with a range of 3 µm 1160 around the focal plane and 0.2 µm steps. The MreB localization experiments were done using strain bEG300 with full induction of GFP-MreB (1mM IPTG) and recovering cells 1161

1163 before.

1162

58

were imaged using the spinning disk microscope, collecting Z-stacks as described

1164 Where indicated, instead of visualizing MreB dynamics, fluorescent D-amino 1165 acids (Kuru et al., 2012) (7 µM) were added to the growth medium in the CellASIC 1166 device: HADA during depletions of TagO (0 mM xylose) and Cy3B-ADA during repletion 1167 of TagO (30 mM xylose). Cells were washed with LB supplemented with 20 mM 1168 magnesium chloride containing no D-amino acids for 1-2 min before imaging. 1169 To test if rod shape recovery occurs in the absence of cell division, 3 strains were tested 1170 (BAB327, BAB343 and BAB388). Cells of BAB327 and BAB388 were grown in CH 1171 media with 25 mM magnesium chloride in the absence of xylose at 37°C until OD<sub>600</sub> ~0.5 and diluted 10-fold in fresh media. After 2 hours of growth, IPTG was added to a 1172 1173 final concentration of 1 mM (MinCD and FtsA, respectively) and cells were incubated for 1174 an extra 1 hour. Cells were imaged on a spinning disk confocal under pads with 1 mM 1175 IPTG and 60 mM xylose (for TagO repletion). Phase-contrast and fluorescent images 1176 were acquired at 10 minute intervals for a total of 8 hours. Cells of BAB343 were grown 1177 in LB supplemented with 20 mM, magnesium chloride in the absence of xylose at 25°C 1178 overnight. The next day, after 2 hours of growth in the same media at 37°C, IPTG was 1179 added to a final concentration of 1 mM (MciZ) and cells were incubated for an extra 1 1180 hour. Cells were imaged on a spinning disk confocal under pads with 1 mM IPTG and 1181 30 mM xylose (for TagO repletion). Phase-contrast and fluorescent images were 1182 acquired at 10 minute intervals for a total of 4 hours.

1183

Depletion and repletion of Magnesium in the CellASIC. For Supplementary Movie 8,
cells of BCW51 were grown overnight at 25° C in LB supplemented with 8mM xylose,

1186 20 mM magnesium chloride, 1  $\mu$  g/ml erythromycin and 25  $\mu$  g/ml lincomycin (MLS). 1187 Cells were shifted to 37°C for 2 hours and loaded into the CellASIC B04A plate at OD<sub>600</sub> 1188 ~0.6. At the start of imaging, magnesium was depleted by flowing in LB supplemented 1189 only with 8 mM xylose and MLS at 3 psi. Images were collected every 20 min over a 4 1190 hr period. Magnesium was resupplied to the cells by changing to LB supplemented with 1191 8 mM xylose, 20 mM magnesium chloride, and MLS. Imaging was continued every 20 1192 min for an additional 4 hrs.

1193

1194 Measurements of cell shape at steady state growth. Cells were grown overnight at 1195 25°C in LB supplemented with 30 mM xylose, 20 mM magnesium chloride, 1  $\mu$  g/mL 1196 erythromycin and 25  $\mu$  g/mL lincomycin. In the morning they were collected at OD<sub>600</sub> 1197 ~0.2, spun in a tabletop centrifuge at 9000 rpm for 3 min and washed in LB 1198 supplemented with various xylose (0-30 mM) and magnesium chloride (0-20 mM) 1199 levels. 25-fold serial dilutions into LB supplemented with the same xylose and 1200 magnesium chloride concentrations were made and allowed to grow at 37°C for 4 hrs. 1201 Cells at OD<sub>600</sub> ~0.2 were concentrated by spinning in a tabletop centrifuge at 9000 rpm 1202 for 3 min. They were placed on a coverslip thickness No. 1.5 under 3% agarose pads 1203 made in LB supplemented with the same concentrations of xylose and magnesium 1204 chloride. Images were collected using the imaging setup described in the "Imaging -1205 phase contrast microscopy" section above, as well as with a Photometrics CoolSNAP 1206 HQ2 CCD camera. The magnification and pixel size were the same in both setups.

1207

### 1208 Muropeptide analysis

1209 To prepare muropeptides from strain BEG300, a similar protocol was performed as 1210 reported previously (Atrih et al., 1999; Kühner et al., 2014). An overnight culture of 1211 BEG300 (2 mL) was centrifuged at 10,000 rpm for 5 min. The cell pellet was 1212 subsequently resuspended in 1 ml 0.25% SDS in 0.1 M Tris/HCI (pH 6.8). The mixture 1213 was boiled at 100 at for 20 minutes. After cooling, the suspension was centrifuged at 1214 16,000 rpm for 10 minutes, and the pellet was washed with 1.5 ml H<sub>2</sub>0 and centrifuged 1215 again at 16,000 rpm for 10 minutes. The pellet was then washed two more times with 1216 water. The pellet was then resuspended in 1 ml  $H_20$  and sonicated for 30 minutes. 500 1217  $\mu$  I of a solution containing DNase (15  $\mu$  g/mI) and RNase (60  $\mu$  g/mI) in 0.1 M Tris/HCI 1218 (pH 6.8) was added. After shaking at 37 ₩C for 2 hours, the enzymes were inactivated 1219 at 100 🛍 for 5 minutes. The mixture was pelleted at 16,000 rpm and washed with 1 ml 1220 H<sub>2</sub>0 twice. Wall teichoic acid was removed from the pellet by resuspending the pellet in 1221 500  $\mu$  l of 1 M HCl and incubating the mixture at 37 **i**C for 4 hours. The pellet was then 1222 centrifuged and washed with water at least four times to neutralize the pH to 1223 approximately pH 6. Subsequently, the pellet was resuspended in 100  $\mu$  l of digestion buffer (12.5 mM NaH<sub>2</sub>PO<sub>4</sub>) with 10  $\mu$  I of mutanolysin (5 U/mL in H<sub>2</sub>O, from 1224 1225 Streptomyces globisporus, purchased from Sigma Aldrich, St. Louis, Missouri). 1226 Peptidoglycan was digested overnight, shaking at 37 °C. Subsequently, the sample was 1227 centrifuged at 16,000 rpm for 10 minutes and muropeptides were reduced by adding 50 1228  $\mu$  I of sodium borohydride (10 mg/ml, H<sub>2</sub>0) was added. The mixture was incubated for 1229 30 minutes. To quench the muropeptide reduction, 1.4  $\mu$ l of 20% phosphoric acid was

1230 added to adjust the pH to 4. The mixture was then used for LC/MS analysis. High-1231 performance liquid chromatography (HPLC) was carried out on an Agilent Technologies 1232 (Santa Clara, California) 1260 Quanternary LC system using a SymmetryShield RP18 5 1233  $\mu$ M, 4.6 x 250 mm column (Waters, Part No. 186000112). Solvent A was 0.1% formic 1234 acid in water; Solvent B was 0.1% formic acid in acetonitrile. At a flow rate of 0.5 1235 mL/min, Solvent B was increased from 0-20% in 100 minutes, held at 20% for 20 1236 minutes, increased to 80% by 130 minutes, held at 80% for 10 minutes, and 1237 subsequently reduced to 0% and held at 0% for 10 minutes. To analyze the 1238 muropeptide composition, muropeptides were identified by the masses observed under 1239 specific peaks in the total ion chromatograms. Similar muropeptides were observed as 1240 previously reported for other *Bacillus subtilis* strains (Kühner et al., 2014). To quantify 1241 the amount of muropeptides observed, exact masses were integrated using extracted 1242 ion chromatograms (EICs). Subsequently, we calculated the percentage crosslinking as 1243 previously reported (Glauner et al., 1988). Technical and biological replicates were 1244 performed for each strain background.

1245

Particle tracking. The MATLAB based software uTrack was used for particle tracking (Jaqaman et al., 2008). We used the comet detection algorithm to detect filaments (difference of Gaussian: 1 pixel low-pass to 4-6 pixels high pass, watershed segmentation parameters: minimum threshold 3-5 standard deviations with a step size of 1 pixel) which, at our MreB induction levels gave better localization of the resultant asymmetric particles over algorithms that search for symmetric Gaussians. Visual

1252 inspection of detected particles confirmed that most of the particles and none of the 1253 noise were being detected. A minimum Brownian search radius of 0.1-0.2 pixels and a 1254 maximum of 1-2 pixels was applied to link particles with at least 5 successive frames. 1255 Directed motion propagation was applied, with no joins between gaps allowed. Tracks 1256 were visualized using the FIJI plug-in TrackMate (Tinevez et al., 2017). For sphere to 1257 rod transitions and cells confined in microfluidic channels, movies were processed by subtracting every 8<sup>th</sup> frame from each frame to remove stationary spots using the FIJI 1258 1259 plugin StackDifference before tracking. The tracking was done as described earlier in 1260 this section.

1261

1262 Fluorescent analysis of TagTUV. Strains containing fluorescent fusions to TagT, 1263 TagU, and TagV were grown as described in the "Overnight culture growth" section but 1264 in CH medium instead of LB. Cells were grown for 3 hours at 37°C before imaging, then 1265 collected by centrifugation at 6,000 x g for 2 min and re-suspended in CH. Cells were 1266 then placed on a glass coverslip thickness No. 1.5 under an agar pad thickness 1 mm 1267 made from CH and 1.5% agarose. Timelapse images were collected with TIRF 1268 illumination, using continuous 100 ms 488 nm exposures. Epifluorescent illuminated 1269 images were collected from a single exposure, while maximal intensity projections were 1270 formed from a series of continuous 100 ms TIRF exposures.

1271

1272 **Teichoic acid labeling with Concanavalin A.** BEG300 cells were grown from 1273 overnights as described in the "Fluorescent analysis of TagTUV" section at 37°C for 4

1274 hours without xylose to deplete WTAs, then induced with 30 mM xylose for 1.5 hours to 1275 re-induce WTA expression. Cells were then moved to 25°C for at least 30 min and 1276 incubated with 25 µg/mL Concanavalin A conjugated to Alexa Fluor 647. Cells were 1277 collected by centrifugation at 6,000 x g for 2 min, washed with CH medium, then re-1278 suspended in fresh CH medium. Cells were then placed on a glass coverslip thickness 1279 No. 1.5 under an agar pad thickness 1 mm made from CH medium and 1.5% agarose. 1280 For PY79 and BCW61 controls, lectin-Alexa Fluor conjugate concentration was 200 1281 µg/mL. For non-quantitative analysis, imaging was performed with the microscope described in "Imaging – MreB Particle Tracking"; for quantitative analysis, imaging was 1282 performed with the microscope described in "Imaging - Spinning Disk Confocal". 1283 1284 Quantification was performed in FIJI; pixel values were corrected for mean fluorescent 1285 background.

1286

1287 **Data analysis – selecting directional tracks.** The output of uTrack is the position 1288 coordinates of tracks over frames. We fit a line through these coordinates using orthogonal least squares regression to minimize the perpendicular distance of the points 1289 1290 from the line of best fit. We used principal component analysis for orthogonal regression using custom written MATLAB code. The R<sup>2</sup> values we obtain range from 0.5 to 1. We 1291 1292 calculated mean track positions, angles and displacement using the line of best fit for all 1293 tracks. We also calculated the mean square displacement versus time of individual 1294 tracks and fit these curves to the quadratic equation  $MSD(t) = 4Dt + (Vt)^2$ , using 1295 nonlinear least squares fitting. As later times have fewer points and are noisier, we fit

the first 80% of the data for each track. We determined  $\alpha$  by fitting a straight line to the log(MSD(t)) vs.log(t) curve. The goodness of fit was evaluated by determining the R<sup>2</sup> value. We selected tracks for linearity and directional motion, based on the following cutoffs: R<sup>2</sup> > 0.9, displacement > 0.2  $\mu$  m, velocity > 1e<sup>-9</sup>  $\mu$  m/s, and R<sup>2</sup> of the linear fit of log(MSD(t)) vs.log(t) > 0.6.

1301

**Data analysis – cell segmentation.** The MATLAB-based software Morphometrics (Ursell et al., 2017) was used to segment phase contrast images of cells. We used the phase contrast setting for rod-shaped and intermediate states and the peripheral fluorescence setting for spherical states, because in this latter condition, peripheral fluorescence empirically did a better job of fitting cell outlines. The cell contours obtained were visually inspected and any erroneous contours were removed by custom written MATLAB code.

1309

1310 Data analysis - track angles with respect to the long axis of the cell. Track angles 1311 were calculated with respect to the cell midline as defined by the Morphometrics 1312 "Calculate Pill Mesh" feature, which identifies the midline based on a unique 1313 discretization of the cell shape determined from its Voronoi diagram. The difference 1314 between the track angle and midline angle was then calculated. Since the track angles 1315  $\theta_t$  and midline angles  $\theta_m$  both ranged from -90° to 90°, the range of angle differences  $\Delta \theta = \theta_t - \theta_m$  was -180° to 180°. We changed the range to 0 to 180° by the 1316 transformation:  $\Delta \theta = 180 + \Delta \theta \ if \ \Delta \theta < 0$ , and 0 to 90° by the transformation:  $\Delta \theta =$ 1317

1318  $180 - \Delta\theta \ if \ \Delta\theta > 90$ . The standard deviations (SD) reported are measured from the 1319 distributions with a range of 0-180° as this SD most accurately depicts deviations from 1320 90°.

1321 **Data analysis – mean dot product of tracks.** Custom written MATLAB code was used 1322 to calculate the normalized dot product (*DP*) of track pairs along with the distance (*d*) 1323 between their mean positions  $\bar{x}$  and  $\bar{y}$  as follows:

1324 
$$DP_{ij} = \cos(\theta_i - \theta_j), \qquad d_{ij} = \sqrt{(\bar{x}_i - \bar{x}_j)^2 + (\bar{y}_i - \bar{y}_j)^2}$$

To eliminate out-of-cell tracks we only considered those that had 3 other tracks within a 5  $\mu$  m radius of their mean position. The dot product of track pairs (DP) and distance (d) between them was stored in data files, along with all the previous information for each individual track (R<sup>2</sup>, velocities, angles, mean positions, displacement etc). The files were then parsed using the cutoffs described in the "Data analysis – selecting directional tracks" section. The tracks were binned based on the distance and the mean dot product calculated for each distance range as follows:

1332 
$$\overline{DP} = \frac{1}{N} \sum_{i>j}^{N} \cos(\theta_i - \theta_j)$$

1333 A cutoff of 3  $\mu$  m was chosen as the maximum binning distance, which is the average 1334 length of a cell.

1335

1336 **Data analysis – simulation of random angles.** A data file containing simulated tracks 1337 was created by a custom written MATLAB script, which generates random angles 1338 distributed randomly on a 100 x 100  $\mu$  m area. Each track has R<sup>2</sup> = 0.95, velocity = 25 1339 nm/s and displacement = 1  $\mu$  m. The same analysis code was run on these simulated

tracks to generate track pairs with dot product and distance stored in a new data file.
The data file was parsed using the same cutoffs as the real data and the mean dot
product for each distance range calculated. The total numbers of trajectories within the
simulation were much higher than the actual data (2-10 times higher).

1344

1345 **Data analysis – cell width.** Pill meshes were created using Morphometrics (Ursell et 1346 al., 2017), which calculates the coordinates of line segments perpendicular to the cell long axis. For cell widths at various steady state TagO and Mg<sup>2+</sup> levels, the distance of 1347 1348 these line segments were calculated using a custom written MATLAB script and the 1349 maximum width along the length of the cell was taken as the cell width. When 1350 measuring cell width nearest to a track (for calculating track angle as a function of cell 1351 width), the mean width of the 10 nearest contour points from the track was calculated 1352 using a custom written MATLAB script. Cell widths of emerging bulges and rods from 1353 round cells were measured manually in FIJI. Our ability to segment individual spherical 1354 cells was limited by their nonuniform contrast, perhaps arising from the nonuniform 1355 thickness of these cells in the Z dimension; consequently, Morphometrics-based width 1356 measurements in these cells was limited, especially in cells exceeding 2  $\mu$  m in 1357 diameter.

1358

### 1359 **Data analysis – cell curvature.**

1360 Sidewall curvature of cells was extracted from the pill mesh obtained from1361 Morphometrics. The curvature values are calculated from 3 successive contour points

and smoothed over 2 pixels. The mean curvature of 3 nearest points to each track were calculated from both sides of the cell contour and called the mean curvature. Principal curvature ratio was calculated by dividing the sidewall curvature with the curvature in the radial direction (calculated from cell width assuming the cell is radially symmetric). For radial curvature we used the following expression, where  $r_{cell}$  is half the cell width:

1367 
$$\kappa_2 = \frac{1}{r_{cell}}$$

1368 A value close to 1 indicates the two principal curvatures are similar and the cells are 1369 round.

1370

## 1371 Data analysis – time and curvature plots of rod shape recovery.

1372 Phase contrast images were used to show rod shape emergence from local bulges. 1373 Edges were enhanced in FIJI and contrast adjusted to give bright cell outlines in the 1374 images. The stack was then colored in time using temporal color code function in FIJI. 1375 To create the curvature plot, the phase contrast images were run through 1376 Morphometrics which calculates the curvature at each contour point along the cell 1377 outline. The contour points of interest were selected and plotted using a custom written 1378 MATLAB script, which colored each point according to its local curvature as calculated 1379 by Morphometrics. To provide a good resolution for positive curvatures, we rescaled the 1380 color map such that negative curvatures were colored blue and positive curvatures were 1381 scaled by their curvature value.

1382

## 1383 Data analysis – single cell doubling times

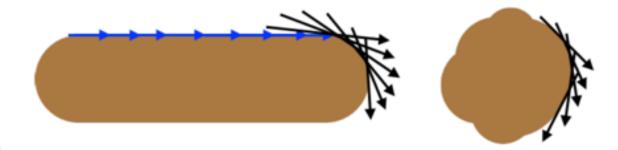
Data from agar pads experiments was analyzed using custom written MATLAB code. Data from cellASIC experiments was analyzed in Morphometrics to get areas for each cell. For doubling times during sphere to rod transitions, the data was collected by manually measuring the areas of the sphere and rod regions of the same cell in FIJI. In all cases, the area of each cell per frame was calculated and the log plot of area vs time was fit to a line. The doubling time was calculated using the slope of this line.

1390

## 1391 Data analysis – Tangential correlation of cell contours.

1392

1393 Cell contours were used to calculate tangent angles using the equation:  $\theta_i = \tan^{-1} \frac{y_{i+1}-y_i}{x_{i+1}-x_i}$ . The correlation between angles was calculated using the cosine of the 1394 angle difference binned as a function of number of points (n) between the 1395 angles:  $G(n) = \frac{1}{N} \sum_{i=1}^{N} \cos(\theta_{i+n} - \theta_i)$ . The number of points was converted to contour 1396 length using the pixel size of the camera to get the final correlation function:  $G(l) = \frac{1}{N} \sum_{i=1}^{N} \cos(\theta_{i+l} - \theta_i)$ .



- As shown above, for straight rods, the contour angles on average remain highly correlated over larger distances, becoming uncorrelated at the cell pole. In spherical cells, the angles become uncorrelated at shorter distances.
- 1403
- 1404 *T. maritima* MreB protein purification
- Full length, un-tagged *Thermotoga maritima* MreB was purified as described previously(Salje et al., 2011).
- 1407

### 1408 *In vitro* reconstitution of *T. maritima* MreB filaments inside liposomes

1409 The protein was encapsulated inside unilamellar liposomes following a previously 1410 published protocol (Szwedziak et al., 2014). For this, 50 µL of E. coli total lipid extract, 1411 dissolved in chloroform at 10 mg/mL, was dried in a glass vial under a stream of 1412 nitrogen gas and left overnight under vacuum to remove traces of the solvent. The 1413 resulting thin lipid film was hydrated with 50  $\mu$  L of TEN100 8.0 (50 mM Tris/HCl, 100 mM NaCl, 1 mM EDTA, 1 mM NaN<sub>3</sub>, pH 8.0), supplemented with 20 mM CHAPS 1414 1415 (Anatrace, Maumee, Ohio), and shaken vigorously at 800 rpm using a benchtop micro 1416 centrifuge tube shaker for 2 hrs. The lipid-detergent solution was then sonicated for 1 1417 min in a water bath sonicator. Subsequently, 50  $\mu$  L of MreB protein solution at 30  $\mu$  M, 1418 supplemented with 0.5 mM magnesium ATP (Jena Bioscience, Germany) was added 1419 and left for 30 min at room temperature. Next, the mixture was gradually diluted within 1420 10-20 min to 600  $\mu$  L with TEN1008.0 plus 0.5 mM magnesium ATP (without detergent) 1421 to trigger spontaneous liposome formation. 2.5  $\mu$  L of the solution was mixed with 0.2  $\mu$ 

- 1422 L 10 nm IgG immunogold conjugate (TAAB, UK) and plunge-frozen onto Quantifoil R2/2
- 1423 carbon grid, using a Vitrobot automated freeze plunger (FEI Company, Hillsboro,
- 1424 Oregon
- 1425 ) into liquid ethane.
- 1426

### 1427 Electron cryomicroscopy and cryotomography

2D electron cryomicroscopy images were taken on an FEI Polara TEM (FEI Company) 1428 1429 operating at 300 kV with a 4k x 4k Falcon II direct electron detector (FEI Company) at a 1430 pixel size of 1.8 Å. For electron cryotomography, samples were imaged using an FEI 1431 Titan Krios TEM (FEI Company) operating at 300 kV, equipped with a Gatan imaging 1432 filter set at zero-loss peak with a slit-width of 20 eV. A 4k x 4k post-GIF K2 Summit direct electron detector (Gatan, a subsidiary of Roper Technologies, Lakewood Ranch, 1433 1434 Florida) was used for data acquisition with SerialEM software (Mastronarde, 2005) at a pixel size of 3.8 Å at the specimen level. Specimens were tilted from -60° to +60° with 1435 1436 uniform 1° increments. The defocus was set to between 8 and 10  $\mu$  m, and the total dose for each tilt series was around 120-150  $e/Å^2$ . 1437

1438

# 1439 Image processing

1440 Tomographic reconstructions from tilt series were calculated using RAPTOR (Amat et 1441 al., 2008) and the IMOD tomography reconstruction package followed by SIRT 1442 reconstruction with the TOMO3D package (Agulleiro and Fernandez, 2011; Kremer et

- 1443 al., 1996). Movies showing liposomes were prepared with Chimera and PyMOL
- 1444 (DeLano, 2002; Pettersen et al., 2004).

- 1446
- 1447

## 1448Strain construction

1449

1450 **BCW51** [*ycgO::Pxyl-tagO, tagO::erm, amyE::sfGFP-mreB, sinR::phleo*] was generated 1451 by transforming BEG300 with a Gibson assembly consisting of three fragments: 1) PCR 1452 with primers Sinr\_up\_F and Sinr\_up\_R and template PY79 genomic DNA; 2) PCR with 1453 primers oJM028 and oJM029 and template plasmid pWX478a (containing *phleo*); 3) 1454 PCR with primers Sinr\_DOWN\_R and Sinr\_DOWN\_F and template genomic DNA.

1455

**BCW61** [*tagE::erm*] was generated by transforming PY79 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW054 and oCW055 and template PY79 genomic DNA; 2) PCR with primers oJM028 and oCW057 and template plasmid pWX467a containing *cat*; 3) PCR with primers oCW058 and oCW059 and template PY79 genomic DNA.

1461

**BCW72** [*yvhJΩPxylA-mazF (cat)*] was generated by transforming PY79 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW139 and oCW141 and template PY79 genomic DNA; 2) PCR with primers oJM029 and oMK047 and template DNA consisting of a fusion of *cat* and the *mazF* counterselectable marker from pGDREF (Yu et al., 2010); 3) PCR with primers oCW142 and oCW143 and template PY79 genomic DNA.

1468

BCW77 [*ywtFΩPxylA-mazF (cat)*] was generated by transforming PY79 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW159 and oCW161 and template PY79 genomic DNA; 2) PCR with primers oJM029 and oMK047 and template DNA consisting of a fusion of *cat* and the *mazF* counterselectable marker from pGDREF (Yu et al., 2010); 3) PCR with primers oCW164 and oCW165 and template PY79 genomic DNA.

1475

BCW78 [*ywtFΩmsfGFP-ywtF*] was generated by transforming BCW77 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW160 and oCW161 and template PY79 genomic DNA; 2) PCR with primers oCW072 and oCW073 and BMD61 genomic DNA; 3) PCR with primers oCW163 and oCW165 and template PY79 genomic DNA.

1481

**BCW79** [*yvhJΩmsfGFP-yvhJ*] was generated by transforming BCW72 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW139 and oCW146 and template PY79 genomic DNA; 2) PCR with primers oCW072 and oCW073 and BMD61 genomic DNA; 3) PCR with primers oCW143 and oCW145 and template PY79 genomic DNA.

1487

1488 **BCW80** [*lytR* $\Omega$ *PxylA-mazF* (*cat*)] was generated by transforming PY79 with a Gibson 1489 assembly consisting of three fragments: 1) PCR with primers oCW101 and oCW109 1490 and template PY79 genomic DNA; 2) PCR with primers oJM029 and oMK047 and 1491 template DNA consisting of a fusion of *cat* and the *mazF* counterselectable marker from 1492 pGDREF (Yu et al., 2010); 3) PCR with primers oCW100 and oCW125 and template 1493 PY79 genomic DNA.

1494

**BCW81** [*lytRΩmsfGFP-lytR*] was generated by transforming BCW72 with a Gibson assembly consisting of three fragments: 1) PCR with primers oCW101 and oCW137 and template PY79 genomic DNA; 2) PCR with primers oCW072 and oCW073 and BMD61 genomic DNA; 3) PCR with primers oCW100 and oCW138 and template PY79 genomic DNA.

- 1500
- 1501 **BCW82** [*tagO::erm*, *ycgO::PxylA-tagO*, *amyE::Pspac-gfp-mreB* (*spec*), *dacA::kan*] was 1502 generated by transforming BEG300 with genomic DNA from BGL19.
- 1503

1504 **BEG202** [*tagO::erm amyE::Pxyl-gfp-mbl (spec)*] was generated by transforming 1505 BEB1451 with genomic DNA from BJS18.

1506

1507 **BEG281** [*ycgO::PxylA-tagO*] was generated by transforming with a plasmid created via 1508 ligating a Gibson assembly into pKM077. pKM77 was digested with EcoRI and Xhol. 1509 The assembly was created with two fragments: 1) PCR with primers oEG85 and oEG86 1510 and template py79 genomic DNA; 2) PCR with primers oEG87 and oEG88.

- 1511
- 1512 **BEG291** [*tagO::erm*, *ycgO::PxylA-tagO*] was generated by transforming BEG281 with genomic DNA from BRB4282.
- 1514
- 1515 **BEG300** [*tagO::erm*, *ycgO::PxylA-tagO*, *amyE::Pspac-gfp-mreB* (*spec*)] was generated 1516 by transforming BEG291 with genomic DNA from BEG275. 1517
- BMD61 [*mblΩmbl-msfGFP* (*spec*)] was generated by transforming py79 with a Gibson assembly consisting of four fragments: 1) PCR with primers oMD44 and oMD90 and template PY79 genomic DNA; 2) PCR with primers oMD47 and oMD56 and template synthetic, codon-optimized *msfGFP*; 3) PCR with primers oJM028 and oJM029 and template plasmid pWX466a (containing *spec*); 4) PCR with primers oMD48 and oMD50 and template genomic DNA.
- 1524

1525 **bSW99** [*amyE::spc-Pspac-mciZ*] was generated by transforming PY79 with a Gibson 1526 assembly consisting of five fragments: 1) PCR with primers oMD191 and oMD108 and 1527 template PY79 genomic DNA (containing upstream region of amyE); 2) PCR with 1528 primers oJM29 and oJM28 and template plasmid pWX466a (containing spec); 3) PCR 1529 with primers oMD234 and oSW76 and template plasmid pBOSE1400 (a gift from Dr. 1530 Briana Burton, containing spec); 4) PCR with primers oAB307 and oAB291 and template PY79 genomic DNA (containing mciZ); 5) PCR with primers oMD196 and 1531 1532 oMD197 and template PY79 genomic DNA (containing downstream region of amyE). 1533

- 1534 **bAB343** [tagO::erm, ycgO::cat-PxylA-tagO, amyE::spc-Pspac-mciZ, ftsAZ::ftsA-
- 1535 *mNeonGreen-ftsZ*] was generated by transforming bAB185 (Bisson-Filho et. al, 2017)

1536 with genomic DNA from bSW99. The resultant strain was then transformed with the 1537 genomic DNA from BEG291 and selected for Cm resistance. Subsequently, the

resultant strain was transformed again with genomic DNA from BEG291, but colonies

1539 were selected for MLS resistance in the presence of 30 mM of xylose and 25 mM

- 1540 MgCl2.
- 1541

1556 1557

1559

1562

bAB327 [tagO::erm, ycgO::cat-PxylA-tagO, amyE::spc-Physpank-minCD, ftsAZ::ftsAmNeonGreen-ftsZ] was generated by transforming bAB185 (Bisson-Filho et al., 2017)
with genomic DNA from JB60 (a gift from Dr. Frederico Gueiros-Filho). The resultant
strain was then transformed with the genomic DNA from BEG291 and selected for Cm
resistance. Subsequently, the resultant strain was transformed again with genomic DNA
from BEG291, but colonies were selected for MLS resistance in the presence of 60 mM
xylose and 25 mM MqCl2.

bAB388 [tagO::erm, ycgO::cat-PxylA-tagO, amyE::spc-Physpank-ftsA, ftsAZ::ftsAmNeonGreen-ftsZ] was generated by transforming bAB199 (Bisson-Filho et al., 2017)
with genomic DNA from BEG291 and selected for Cm resistance. Subsequently, the
resultant strain was transformed again with genomic DNA from BEG291, but colonies
were selected for MLS resistance in the presence of 60 mM xylose and 25 mM MgCl2.

# 1558 Supplemental Text 1 - MreB Modeling

# Modeling predicts preferred MreB orientation and a typical cell width for losing binding orientation

1563 Here we show that energetic modeling of an MreB filament directly binding to the inner 1564 membrane predicts the existence of both a preferred orientation of binding and a typical 1565 cell width for losing binding orientation. MreB monomers assemble into higher-order 1566 oligomers and bind directly to the inner membrane. When an MreB filament binds to the 1567 inner membrane, the combined MreB-membrane system requires an energy of 1568 deformation  $E_{def}(l_b)$  for the membrane to deviate from an equilibrium position and gains an energy of interaction  $E_{int}(l_b)$  from the hydrophobic binding. Both the deformation and 1569 interaction energies are expressed as functions of the bound MreB length,  $l_b$ . Note that 1570 1571 the rigid cell wall imposes a boundary constraint on the cell membrane and that the 1572 equilibrium membrane configuration arises from a balance of membrane bending, turgor 1573 pressure, and cell wall confinement. If the MreB filament were to bind, the change in the 1574 total energy *E* of the membrane-MreB system is:

$$1575$$

$$1576 \qquad \Delta E = E_{def} - E_{int}.$$
(1)

1577

1578 The binding configuration that minimizes  $\Delta E$  corresponds to the one that is observed 1579 physically. We therefore wish to minimize  $\Delta E$ . bioRxiv preprint doi: https://doi.org/10.1101/197475; this version posted October 2, 2017. The copyright holder for this preprint (which was not certified by peer review) is the author/funder, who has granted bioRxiv a license to display the preprint in perpetuity. It is made available under aCC-BY-ND 4.0 International license.

#### 1580

1582

#### 1581 Estimate of the hydrophobic interaction energy $E_{int}$

We assume that the biochemistry of MreB is conserved in prokaryotes so that, like C. 1583 crescentus and E. coli MreB (van den Ent et al., 2014), B. subtilis MreB is assembled 1584 1585 into antiparallel double protofilaments consisting of many monomeric units. Consider an MreB filament containing N<sub>int</sub> interaction sites with a membrane, each with some 1586 independent and additive interaction energy  $E_{int}^0$ . Due to the antiparallel arrangement of 1587 the protofilaments (Salje et al., 2011; van den Ent et al., 2014), there are two binding 1588 sites per monomeric unit of MreB. We therefore estimate the number of binding sites 1589 1590 per MreB binding length  $l_b$  as:

1593

$$N_{int} = \frac{2l_b}{l_{\rm MreB}},\tag{2}$$

1594 where  $l_{\rm MreB} \approx 5.1$  nm is the length of a monomeric unit. The energy of burying the 1595 amino acids relevant to the binding is approximately:

1596 1597

$$E_{int}^0 \approx 6.04 \frac{\mathrm{kcal}}{\mathrm{mol}} = 10 \ kT,\tag{3}$$

1598

1599 where *k* denotes Boltzmann's constant and *T* denotes the ambient temperature; the 1600 energies of burying individual amino acids were derived from water/octanol partitioning. 1601 At a room temperature of  $T = 25^{\circ}$  C, the interaction energy per MreB binding length  $l_b$ 1602 is therefore:

1603  
1604 
$$\varepsilon_{int} = \frac{2 \times 10kT}{l_{harp}} = 1.8 \times 10^{-1}$$

$$= \frac{2 \times 10kT}{l_{\rm MreB}} = 1.8 \times 10^{-11} \, {\rm J/m},$$

(4)

1606 and the hydrophobic interaction energy is:  $E_{int}(l_b) = \varepsilon_{int}l_b$ .

#### 1608 Estimate of the membrane deformation energy

1609

1605

1607

1610 The membrane deformation energy  $E_{def}(l_b)$  can be decomposed as:

$$E_{def}(l_b) = E_{bend}^{\text{MreB}}(l_b) + E_{int}^{\text{membrane}}(l_b),$$
(5)

1613

1614 where  $E_{bend}^{\text{MreB}}$  denotes the bending energy of the MreB filament and  $E_{int}^{\text{membrane}}$  denotes 1615 the indentation energy of the membrane. We wish to find the MreB-membrane 1616 configuration that minimizes the sum of these terms. We prescribe the forms of these 1617 terms as follows.

1618

#### 1619 The bending energy of an MreB filament

1620 We model an MreB filament as a cylindrical rod, with circular cross-sections of radius 1621  $r_{\rm MreB}$  and an intrinsic curvature  $1/R_{\rm MreB}$ . The elastic energy density per unit length of bending a cylindrical rod of cross-sectional radius  $r_{\rm MreB}$  from a curvature of  $1/R_{\rm MreB}$  to a curvature of 1/R is given by:

1624

$$\varepsilon_{bend} = \frac{\pi Y_{MreB} r_{MreB}^4}{8} \left( \frac{1}{R} - \frac{1}{R_{MreB}} \right)^2 = \frac{B}{2} \left( \frac{1}{R} - \frac{1}{R_{MreB}} \right)^2,$$
(6)

1626

where Y<sub>MreB</sub> is the Young's modulus of an MreB filament and B is its flexural rigidity 1627 (Landau and Lifshitz, 1970). Assuming the Young's modulus of actin, we note that B =1628 1629  $1.65 \times 10^{-25}$  J m, which is two orders of magnitude smaller than that previously 1630 assumed by Wang and Wingreen for an MreB bundle of cross-sectional radius 10 nm (Wang and Wingreen, 2013). In particular, we assume that MreB binds to the inner 1631 membrane as pairs of protofilaments and does not bundle. For a uniform flattening of 1632 the MreB filament corresponding to  $R = \infty$ ,  $\varepsilon_{bend} \le 8.2 \times 10^{-13}$  J/m, which is less than 1633 the MreB-membrane interaction energy  $\varepsilon_{int}$  computed above. This suggests that an 1634 MreB filament may be susceptible to bending at our energy scale of interest. How much 1635 the MreB bends is determined by a trade-off between the polymer bending energy and 1636 1637 the indentation energy of the membrane, which we discuss next.

1638

#### 1639 **The membrane Hamiltonian**

We model the inner membrane as an isotropic, fluid membrane composed of a phospholipid bilayer, where there is no in-plane shear modulus and the only in-plane deformations are compressions and expansions. The membrane indentation energy can be expressed as the minimum of an energy functional over the indented states of the membrane. This functional is given by the Helfrich Hamiltonian:

1645

$$F[S] = \int_{S} \left[ \frac{k_{b}}{2} (2H - H_{s})^{2} + \frac{k_{t}}{2} K + \gamma \right] dA + p \int_{S} dV,$$
(7)

1647

1648 where  $k_b$  is the bending rigidity of the membrane,  $k_t$  is the saddle-splay modulus of the 1649 membrane,  $H_s$  is the spontaneous curvature of the bilayer,  $\gamma$  is the membrane surface tension, p is the pressure differential at the membrane interface, and H and K are the 1650 1651 mean and Gaussian curvatures of the surface S, respectively (Safran, 2003; Zhong-Can and Helfrich, 1989). The bending rigidity  $k_b$ , which depends on membrane composition, 1652 is typically 10 to 20 kT for lipid bilayers (Phillips et al., 2012). Assuming that 1653 phospholipids are in excess in the bulk and rearrange themselves on the membrane 1654 1655 surface to accommodate areal changes (Safran, 2003), we take the membrane surface tension  $\gamma = 0$ . For large deformations of the inner membrane such as those induced by 1656 1657 cell wall lysis (Deng et al., 2011), the assumption that the phospholipids are in excess in 1658 the bulk may fail to hold and result in a nonzero surface tension. A nonzero surface 1659 tension would only enhance the energetic preference of the correct binding orientation; hence, taking a finite surface tension would not change our conclusions. The 1660 1661 mechanical energy needed to deform the membrane is the difference between the free 1662 energies in the deformed S and undeformed  $S_0$  states:

1663

1664 
$$E_{ind}^{\text{membrane}} = F[S] - F[S_0].$$

(8)

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1665

The surface integrals of the Gaussian curvature are topological invariants by the Gauss-1666 1667 Bonnet theorem and therefore cancel in the difference, hence:

1668  
1669 
$$E_{ind}^{\text{membrane}} = \left[\frac{k_b}{2} \int_{S} (2H - H_s)^2 dA + p(\text{vol}[S])\right] - \left[\frac{k_b}{2} \int_{S} (2H_0 - H_s)^2 dA + p(\text{vol}[S_0])\right].$$
 (9)

1670

Here H denotes the mean curvature of the state S, and  $H_0$  denotes the mean curvature 1671 of the state  $S_0$ . For simplicity, we set the spontaneous curvature  $H_s = 0$ ; the case of 1672 1673 nonvanishing spontaneous curvature can be considered in a similar manner. We 1674 therefore write:

1675

1676 
$$E_{ind}^{\text{membrane}} = \min_{S} \left[ 2k_b \int_{S} (H^2 - H_0^2) \, dA + p \int dV \right],$$
 (10)

1677 1678 where the volume integral is understood to be the difference of the volumes in the deformed and undeformed states and the areal change accompanying the membrane 1679 deformation is small, i.e.  $dA_0 \approx dA$ . We define the membrane bending energy 1680  $E_{bend}^{\text{membrane}}[S; S_0]$  for a conformation S to be the former term and the membrane pV1681 energy  $E_{nv}^{\text{membrane}}[S; S_0]$  to be the latter term in the right hand side of Equation 10. 1682

1683

As  $k_b$  is typically 10 to 20 kT, we take  $k_b = 10$  kT and p as a parameter of the model. 1684 Note that *p* denotes the pressure difference acting on the membrane. The value of *p* is 1685 important for determining the tradeoff between the membrane indentation energy 1686  $E_{ind}^{\text{membrane}}$  and the MreB bending energy  $E_{bend}^{\text{MreB}}$  accurately, but we will show that the 1687 preferred orientation of MreB binding is robust over a broad range of p. 1688

1689

1691

#### 1690 Mechanical equilibrium of the undeformed membrane

1692 Consider the balance of forces on the inner membrane in the undeformed state. 1693 Assuming that the undeformed membrane is a cylinder with radius r and length L and that sufficient phospholipids exist in the bulk so that  $\gamma = 0$ , the membrane free energy is 1694

1695 1696

1696 
$$E(r) = 2k_b \int_S H_0^2 dA + p \int dV = \frac{\pi k_b L}{r} - \pi p L r^2,$$
1697 (11)

1698 which is monotonically decreasing in r. This implies that the membrane radius should be maximal at equilibrium. If p = 0, then the membrane should press against the cell 1699 1700 wall and squeeze out the periplasmic space due to minimization of the bending energy. A model in which the periplasm and cytoplasm are isosmotic (Sochacki et al., 2011) 1701 1702 with no mechanical force exerted by the periplasm is therefore inconsistent with the 1703 existence of a periplasm. For the periplasm to exist at equilibrium, it must contribute an additional energy term  $E_{peri}$  to the total energy, so that the total energy  $F = E + E_{peri}$  as 1704 a function of *r* has a stable fixed point at  $r_0 = r^* + \delta r^*$ . Here we define  $r^* = R_{cell} - h_{peri}$ , 1705 where  $R_{cell}$  is the radius of the cell and  $h_{peri}$  is the thickness of the periplasm, and  $\delta r^*$ 1706 1707 as the initial deformed height where  $F'(r) = 0|_{r=r_0}$ . We consider expansions of  $E_{peri}$ 

1708 and F(r) around  $r_0$ . As a function of the deviation in membrane height  $\delta r = r - r_0$ , we 1709 take  $E_{peri} \approx \kappa L (\delta r)^2$  and

1710

1711  $F(\delta r) \approx \kappa^* L(\delta r)^2$ , (12)

1712

1713 where  $\kappa^* = \kappa - p\pi$  is the effective membrane pinning modulus, which has been examined before in Wang and Wingreen's work (Wang and Wingreen, 2013). For the 1714 stability of the fixed point at  $r_0$ , the condition that the second derivative  $F''(\delta r)$  is 1715 positive at  $\delta r = 0$  implies that  $\kappa^* \ge 0$ , or  $\kappa \ge p\pi$ . However, the validity of the expansion 1716  $E_{peri}(\delta r) = \kappa L(\delta r)^2$  may be questionable when the deformed height due to polymer 1717 binding is larger than or comparable to  $\delta r^* \sim pr/\kappa$ . Hence, the pinning model may be 1718 invalid when p is vanishingly small. For various combinations of  $\kappa$  and the polymer 1719 1720 bending rigidity where this double-bind is avoided, such as that assumed by Wang and Wingreen's model, the periplasm is effectively a rigid body. In this case, although a 1721 pinning potential can self-consistently penalize deviations in membrane height, it is 1722 more intuitive to take the formal limit  $\kappa \to \infty$  and treat the periplasm as undeformable. 1723 We therefore model the periplasm as a rigid, undeformable body that mechanically 1724 supports the cell membrane and imposes a boundary condition on the membrane 1725 1726 shape. Any deviation from the equilibrium membrane shape induced by MreB binding is 1727 then resisted by the full effect of turgor. For this reason, in the following analysis we take  $p = p_{cell}$ , stipulate that the MreB cannot indent the inner membrane outwards, and 1728 1729 do not consider the energetic contribution of  $E_{neri}$ .

1730

#### 1731 Configuration with a uniformly bent MreB filament: first-order approximation

1732 With the membrane Hamiltonian as defined in the section above, we now see that the 1733 total membrane deformation energy is given by the sum of the MreB bending energy 1734 and the membrane indentation energy:

1735 
$$E_{def}(l_b) = E_{bend}^{MreB}(l_b) + E_{ind}^{membrane}(l_b) = \min_{R,S} \left[ \frac{B}{2} \int \left( \frac{1}{R} - \frac{1}{R_{MreB}} \right)^2 ds + 2k_b \int_S (H^2 - H_0^2) dA + p \int dV \right].$$
 (13)

1737

The minimization of equation (13) over all surfaces S and MreB curvatures R = R(s) is 1738 1739 generally difficult since minimization of the MreB bending energy determines the 1740 preferred conformation of MreB, which in turn restricts the set of surfaces S that equation (13) must be minimized over. In their work, Wang and Wingreen undertook an 1741 elegant approach to minimizing a similar combination of energies by writing the 1742 1743 membrane indentation energy in Fourier space. Unlike a membrane pinning term, the 1744 pressure-volume energy in equation (13) does not admit a simple Fourier space representation. Nevertheless, considerable insight can be obtained by assuming that 1745 MreB bends uniformly. In this case, MreB deforms from a bent cylinder with a native curvature  $\frac{1}{R_{MreB}}$ , to a bent cylinder with a constant, membrane-bound curvature  $\frac{1}{R}$ . In the 1746 1747 following, we will take the radius R of the bend to be a parameter in estimating the 1748

corresponding membrane indentation energy  $E_{ind}^{\text{membrane}}(l_b)$ ; R will be determined later. 1749 We will also assume that MreB binds perpendicular to the cell's long axis, so that the 1750 curvature of the membrane in its undeformed state is simply  $\frac{1}{R_{equ}}$ , and determine the 1751 1752 corrections due to a deviatory binding angle later.

1753

To estimate  $E_{ind}^{\text{membrane}}$ , we first examine the energetic contribution of the region C of S 1754 directly involved in the MreB-membrane interaction. Note that the biochemical 1755 1756 conformation of MreB, particularly, the antiparallel orientation of its protofilaments, 1757 constrains the geometry of the MreB-membrane binding interface. Since we describe the interface C as the surface of a bent cylinder with principal radii of curvature  $\frac{1}{r_{curr}}$  and 1758

1759 
$$\frac{1}{R}$$
, we have:

12

1760 
$$H \approx \frac{1}{2} \left( \frac{1}{r_{MreB}} + \frac{1}{R} \right), \quad A = 2\pi b r_{MreB} l_b$$
 (14)

where  $r_{MreB}$  is the cross-sectional radius of MreB and b is the fraction of interaction 1761 along a cross-section of the MreB filament. Thus: 1762

1763 
$$E_{bend}^{\text{membrane}}[C] \approx \pi b k_b r_{MreB} l_b \left(\frac{1}{r_{MreB}} + \frac{1}{R}\right)^2 - \pi b k_b r_{MreB} l_b \left(\frac{1}{R_{cell}}\right)^2,$$
 (15)

where  $H_0 = 1/2R_{cell}$  and  $R_{cell}$  denoting the cell radius, is the mean curvature of the 1764 undeformed surface. The contribution of the pV energy over C can be similarly 1765 approximated by finding the area between two circles, one being the MreB filament and 1766 the other being the cross-section of a cell with radius  $R_{cell}$ , with  $R_{cell} \ge R$  as follows: 1767

1768 
$$E_{pV}^{\text{membrane}}[C] \approx 2pr_{MreB} \int_{-R \sin(\frac{l_b}{2R})}^{R \sin(\frac{l_b}{2R})} \left(\sqrt{R_{cell}^2 - x^2} - \sqrt{R^2 - x^2} + R - R_{cell}\right) dx \approx$$
1769 
$$\frac{pr_{MreB}l_b^3}{12} \left(\frac{1}{R} - \frac{1}{R_{cell}}\right),$$
(16)

where we have assumed that  $l_b \ll R$  and  $\frac{1}{R} \ge \frac{1}{R_{cell}}$ . This means that the approximation 1770 above is only valid for cases where the MreB filament can only bend up to a curvature  $\frac{1}{R_{cell}}$ . Now, since  $\frac{1}{R} \ll \frac{1}{r_{MreB}}$ , we deduce that the principal bending energy contribution 1771 1772 over C arises from having the inner membrane tightly wrapped around an MreB 1773 filament. For  $k_b = 10kT$  and b = 1/6,  $E_{bend}^{\text{membrane}}[C]$  takes on a value of: 1774

1775 
$$E_{bend}^{\text{membrane}}[C] \approx \pi b k_b l_b \left(\frac{1}{r_{MreB}}\right) \equiv \varepsilon l_b, \ \varepsilon = 1.0 \times 10^{-11} \text{J/m},$$
 (17)

1776 which is smaller than, but comparable in scale to, the interaction energy  $E^{\text{int}}$  computed 1777 above. Writing out only the energetics of the binding region C under the uniform bending assumption, we therefore see that: 1778

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1779 
$$E_{def}(l_b) \approx \min_R \left[ \frac{B}{2} \left( \frac{1}{R} - \frac{1}{R_{MreB}} \right)^2 l_b + \frac{\pi b k_b l_b}{r_{MreB}} + \frac{p r_{MreB} l_b^3}{12} \left( \frac{1}{R} - \frac{1}{R_{cell}} \right) + \min_S F[H] \right],$$
 (18)

1780 where the last term is the energetic contribution of the falloff region H = S - C. In the case that  $\frac{1}{n} \rightarrow 0$ , estimates of the values of the first three terms in equation (18), for the 1781 parameter values summarized in Table S1, are  $10^{-19}$ J,  $10^{-18}$ J and  $10^{-17}$ J, respectively. 1782 1783 This means that, as MreB binds to the inner membrane, the resulting deformation will 1784 tend to minimize volumetric changes at the cost of inducing membrane curvature and 1785 filament bending. The energetic contribution of the falloff region H can only be 1786 quantitatively accounted for by explicitly finding the membrane shape, which encompasses a tradeoff between the membrane bending energy and the pV energy: 1787 the former term favors a gradual decay of the indentation, while the latter term prefers a 1788 steep decay as to minimize volume. Below, we find that it suffices to consider the case 1789 where MreB bends to match the cell curvature:  $R = R_{cell}$ . In this case, the energetic 1790 1791 contribution of the falloff region H is vanishingly small compared to that of the binding 1792 region, since the membrane can heal in a manner in which its mean curvature is small 1793 compared to the mean curvature of the binding region. The energetic contribution of H 1794 can therefore be neglected, and we quantify it in future work.

1795

#### 1796 $\Delta E$ for the pure bending of an MreB filament

1797 By examining the form of the energetics just over the region C, we note that the 1798 inclusion of a large pressure p increases the energetic preference of an MreB filament 1799 binding perpendicular to the cellular long axis.

1800

1801 Consider a case where  $p \ge p^*$  for some  $p^*$  to be determined, so that it is energetically 1802 unfavorable to displace the membrane volume as opposed to bending the MreB 1803 filament. In this case, as discussed above, the energetic contribution of the falloff region 1804 *H* can be neglected, and an estimate for the minimal value of such a pressure can be 1805 obtained by requiring that:

1806

1807 
$$E_{def}(l_b) \approx \min_R \left[ \frac{B}{2} \left( \frac{1}{R} - \frac{1}{R_{MreB}} \right)^2 l_b + \frac{\pi b k_b \, l_b}{r_{MreB}} + \frac{p r_{MreB} l_b^3}{12} \left( \frac{1}{R} - \frac{1}{R_{cell}} \right) \right]$$
 (19)

1808

1809 as a function of *R*, be minimal at  $R_{cell}$ . For the numerical values relevant to MreB above 1810 and summarized in Table S1, this indicates that:

1813

$$p^* \approx \frac{12 B}{r_{MreB} l_b^2} \left( \frac{1}{R_{MreB}} - \frac{1}{R_{cell}} \right) \approx 20 \text{ kPa},$$
(20)

1814 which is  $1/100^{\text{th}}$  of the turgor pressure of *B. subtilis*. In this case, assuming  $R = R_{cell}$ , 1815

1816 
$$\Delta E(l_b) \approx \left[\frac{B}{2} \left(\frac{1}{R} - \frac{1}{R_{MreB}}\right)^2 + \frac{\pi b k_b}{r_{MreB}} - \varepsilon_{int}\right] l_b, \qquad (21)$$

1818 The energetic dependence on  $R_{cell}$  is then manifested through the pure bending of 1819 MreB when binding to the inner membrane: in particular, we may assume that the MreB 1820 filament will always bend to attain a curvature matching that of the cell's (although small 1821 deviations in the membrane height may lead to an even lower energy conformation), 1822 and the energetic contribution of the falloff region *H* can be neglected.

1823

1824 If  $p < p^*$ , note that both the membrane and the MreB filament can deform each other in 1825 a manner that minimizes the total energy, with the membrane shape determined by the 1826 geometry of the falloff region H. For vesicles with a pressure gradient  $p \approx 0$ , the fact 1827 that an MreB filament grossly deforms the membrane and generates membrane curvature (Salje et al., 2011) is predicted by the shape of *H*. For  $p \approx 0$ , it can also be 1828 shown that the energetic difference between MreB binding at  $R_{cell} = 500$  nm and  $R_{cell} =$ 1829 3000 nm is on the order of several kT, and so a perpendicular alignment of MreB 1830 1831 filaments may also be energetically favorable. For simplicity, in the following discussion we shall consider the wild-type cell scenario, where  $p = p_{cell} > p^*$ , so that only the pure 1832 1833 bending of MreB and the associated membrane bending energy need to be considered 1834 in  $\Delta E$ . We will therefore assume the form of equation (21) for  $\Delta E$  in the discussion that 1835 follows.

1836

#### 1837 **Preferred orientation of MreB binding**

1838 Equations (19) and (21) describe the change in free energy due to MreB binding at a perpendicular angle and bending completely to match the curvature  $\frac{1}{R_{cell}}$  of the cell 1839 membrane at this angle. Our modeling then predicts that MreB filaments tend to bind at 1840 an angle of  $\theta = 90^{\circ}$  relative to the long axis of *B. subtilis*: at any deviatory angle  $|\theta - \theta|$ 1841  $90^{\circ}$  | > 0°, the leading-order correction to the cell radius  $R_{cell}$  in the MreB bending 1842 energy is a multiplicative factor of  $1/\cos\theta$ , which monotonically increases the MreB 1843 1844 bending energy. Since the MreB bending energy is minimal when the principal axis of 1845 curvature of the MreB filament matches that of the cell and the curvature of the cell is 1846 maximal at a perpendicular binding angle, the angle distribution is symmetric about a 1847 minimum centered at  $\theta = 90^{\circ}$ . This reasoning suggests the existence of a potential well centered at  $\theta = 90^{\circ}$ , as shown in Figure 4F under the simplifying assumption that 1848 1849 b = 0. The depth of this potential well is on the order of tens of kT, which appears to be a large enough energetic preference as to be robust to sources of stochasticity such as 1850 1851 thermal fluctuations. Furthermore, our discussion shows that membrane binding 1852 energetics, and in particular the pure bending of an MreB filament, may complement the 1853 conjecture in Salje et al.'s work that the membrane insertion loop and amphipathic helix 1854 help ensure orthogonal membrane binding (Salje et al., 2011).

1855

1856 A sensitivity analysis shows that the energetic difference of an MreB filament 1857 perpendicularly binding to a region of ambient curvature  $R_{cell} = 0.5 \,\mu\text{m}$  and  $R_{cell} =$ 1858 1.5  $\mu\text{m}$  is still on the order of tens of *kT* over a wide range of binding energy and flexural 1859 rigidity values, as shown in Figure 4G. Thus, we anticipate the alignment to be robust to 1860 changes in these two parameters.

#### 1862A typical cell radius for losing orientation

1863 Our modeling shows that the depth of the potential well in  $\theta$  is inversely related to  $R_{cell}$ , 1864 so that at larger cell diameters the angle distribution becomes more uniform. Varying 1865 the cell radius  $R_{cell}$  from 0.5 microns to 3.0 microns results in a reduction of the depth of 1866 the potential well, as illustrated in Figure 4F. We therefore anticipate MreB filaments to 1867 bind with more variance in angle for higher values of  $R_{cell}$ , consistent with the existence 1868 of a typical radius at which the binding angle becomes less robust and affected by 1869 factors such as thermal fluctuations or other sources of stochasticity.

1870

#### 1871Binding orientation at regions of different Gaussian curvatures

Our modeling predicts that, in live cells, MreB filaments will bend to conform to the shape of the inner membrane. Since the binding sites are located at the outer edge of a curved MreB filament, our modeling also predicts that the binding angle distribution becomes more narrow at regions of negative Gaussian curvature: to bind in a conformation that deviates significantly from the preferred binding orientation, in which the filament's deformed curvature remains of the same sign as its intrinsic curvature, an

- 1878 MreB filament must bend to the extent that its curvature flips sign. Similarly, at regions
- 1879 of positive Gaussian curvature, the binding angle distribution will be less narrow.
- 1880 Representative binding angle distributions are shown in three cases of positive,
- 1881 vanishing, and negative Gaussian curvatures in Fig. 7B of the main text.
- 1882
- 1883

# 1884 Supplemental Text 2 – Localization of WTA ligases and WTAs

1885

1886 In order to understand how wall teichoic acid (WTA) depletion and recovery affects cell 1887 shape, we observed the spatial localization of WTAs and the extracellular ligases (the genes lytR, yvhJ, and ywtF (Kawai et al., 2011)) that determine their attachment to the 1888 1889 cell wall. Previous work has suggested that YwtF and LytR localize in MreB-like patterns 1890 (Kawai et al., 2011) and associate with MreB (assayed by in vivo crosslinking and 1891 tandem affinity purification). We reasoned that if the synthesis or insertion of WTAs is 1892 MreB associated, then the emergence of discrete rod-shaped cells upon tagO repletion 1893 might correlate with preferential WTA insertion at the emerging rod, where MreB shows 1894 oriented motion. To test this, we examined 1) the localization and dynamics of 1895 fluorescent tagged WTA ligases, and 2) the spatial localization of WTAs in cells 1896 recovering from spheres into rods. We constructed sfGFP fusions to each of the WTA ligases under their native promoters, and examined their localization using TIRF and 1897 1898 epifluorescent illumination. Although we did observe variation in ligase intensity around 1899 the cell periphery under epifluorescent illumination, we did not see any characteristic 1900 banding across the cell surface as is seen with MreB using TIRF microscopy (Fig. S6C). 1901 Furthermore, TIRF imaging of these fusions at different frame rates did not show any 1902 directional motions, indicating they are not moving along with MreB filaments; rather 1903 these motions suggested the WTA ligases were diffusing on the cell membrane (Movie 1904 S9). We cannot rule out the possibility that the WTA ligases interact with MreB through 1905 transient associations.

#### 1906

1907 We next explored the localization of WTAs, using fluorescently labeled Concanavalin A 1908 (ConA). ConA is a sugar-binding protein with specific affinity for a-D-glucose, which 1909 decorates WTA polymers. ConA has previously been used to localize WTAs (Birdsell et 1910 al., 1975; Doyle et al., 1975). The gene tagE encodes the glycosylase that adds  $\alpha$ -D-1911 glucose to WTA molecules (Allison et al., 2011), which is recognized by ConA. ConA 1912 staining of cells deleted for *tagE* shows no staining (Fig. S6A), verifying the specificity of 1913 ConA for WTAs over other surface sugars. We then used this probe to examine WTA 1914 localizations during recoveries. Addition of ConA to WTA-depleted cells in bulk culture 1915 shows very little staining at the cell periphery, consistent with a basal level of WTA 1916 expression; induction of tagO results in a dramatically increased intensity of staining. 1917 Even at early time points, when rod-shaped cells are just starting to appear in the 1918 population, WTA staining is relatively uniform, with no patterns reminiscent of the patchy 1919 distribution of MreB (Fig. S6B). Together, this data indicates that WTA ligases and WTA 1920 incorporation occur uniformly around the cell in both wild type cells as well as in TagO 1921 depleted spheres recovering into rods. These findings suggest that the changes in 1922 activity of TagO that cause the loss of rod shape (or the reformation thereof) occur 1923 uniformly around the cell wall. Furthermore, these findings also suggest that the WTA 1924 ligases do not consistently localize to MreB within *B. subtilis*.

1925 1926

# 1927 Supplemental Movie Legends

1929 All supplemental movies are available at http://garnerlab.fas.harvard.edu/mreb2017/

1930

1928

S1. Related to Figure 1C - Movie showing the trajectories taken by Mbl filaments
frequently cross each other close in time. BDR2061, containing GFP-Mbl expressed at
the native locus under a xylose-inducible promoter, was induced with 10 mM xylose and
imaged with TIRFM. Frames are 1 s apart. Scale bar is 5 μm.
S2A. Related to Figure 2A – (*first sequence*) Timelapse showing circumferential

1937 motions of GFP-MreB in rod shaped cells with high TagO expression (BEG300 with 30

1938 mM xylose, and GFP-MreB induced with 50  $\mu$ M IPTG) (second sequence) Timelapse

1939 of GFP-MreB trajectories in equivalent conditions. (third sequence) Timelapse

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showing isotropic motions of GFP-Mbl in a *tagO* knock out strain (BEG202, GFP-Mbl
was induced with 0.125 mM xylose). *(fourth sequence)* Timelapse of GFP-Mbl
trajectories in equivalent conditions as above. Frames are 1 s apart in the first and
second sequences, 2 s apart in the third and fourth. All Scale bars are 1 μm.

1944

1945 **S2B.** Related to Figure 2C – (top) Timelapse of GFP-Mbl trajectories occurring 2 1946 hours after the initiation of Pbp2a depletion (middle and bottom). Timelapse of GFP-1947 Mbl trajectories occurring 3 hours after initiation of Pbp2a depletion, where cells 1948 become a mixture of rod shaped and round cells. GFP-Mbl shows a mixture of 1949 circumferential (bottom) and isotropic (middle) motion. BRB785 was grown in 1 mM 1950 IPTG, washed, then grown in media lacking IPTG. Cells were placed under a pad at the 1951 indicated times, and imaged with spinning disk confocal. Frames are 5 s apart. Scale 1952 bar is  $2.5 \,\mu m$ .

1953

1954 **S3. Related to Figure 3A-C** - Timelapse showing circumferential motion of GFP-MreB 1955 in BEG300 induced at low TagO levels (2 mM xylose) when confined into long 1.5 x 1.5 1956  $\mu$  m channels. GFP-MreB was induced with 50  $\mu$ M IPTG. Frames are 2 s apart. Scale 1957 bar is 5  $\mu$ m.

1958

S4. Related to Figure 3D-F – Timelapse of GFP-Mbl in protoplasted cells showing Mbl
does not move directionally. BJS18 (containing GFP-Mbl expressed at an ectopic site
under xylose control) was induced with 30 mM xylose. Cells were then protoplasted in

1962 SMM and grown in molds as detailed in methods. Frames are 1 s apart. Scale bar is 5 1963  $\mu$ m. Movie was gamma-adjusted,  $\gamma = 0.8$ .

1964

**S5. Related to Figure 4** – *(first sequence)* PyMOL volume rendering of an electron cryotomography 3D map *of T. maritima* MreB included in a liposome (corresponds to liposome depicted in Fig. 4E. *(second sequence)* Typical field view of an MreB liposome reconstitution experiment. The movie scans through consecutive Z-layers of the tomographic 3D reconstruction. Note that the smaller, round liposomes trapped inside the rod-shaped liposomes are not decorated with MreB filaments.

1971

**S6. Related to Figure 5** – *(top and middle)* Timelapses showing the local recovery of rod shape upon TagO reinduction from depleted cells. Note the relatively fast growth of rods compared to parent spheres. BEG300 was grown in media lacking xylose, then either loaded into a cellASIC device (top row) or placed under an agar pad (middle row). Both rows were shifted to 30 mM xylose to induce rod-shape recovery, prior to image acquisition. Frames are 10 min apart. Scale bar is 5  $\mu$ m.

(*bottom*) Timelapse showing the local recovery of rod shape upon Pbp2a reinduction
from cells depleted of Pbp2a/PbpH. BRB785 was grown media lacking IPTG for 4.5
hours, then placed on a pad with 1 mM IPTG before the start of imaging. Frames are 5
min apart. Scale bar is 5 μm.

1982

1983 S7. Related to Figure 5 and 6 – Timelapse of rod shape recoveries showing that 1984 circumferential MreB-GFP motion A) occurs immediately upon the formation of rod 1985 shape, and B) that circumferential motion only occurs in rod-shaped cells, even while 1986 attached non-rod cells show unaligned motion. BEG300 was grown overnight in 0mM 1987 xylose to deplete TagO. Cells were then loaded into a cellASIC chamber and grown in 1988 the same media with 1 mM IPTG to induce GFP-MreB. Prior to imaging, tagO 1989 expression was reinduced by switching media to contain 30mM xylose. GFP-MreB was 1990 imaged with TIRFM. Frames are 2 s apart in the fluorescent channel (green) and 10 min 1991 apart in the phase contrast channel (grayscale). Scale bar is 5  $\mu$ m.

1992

1993 **S8.** Related to Figure 5 – Timelapse showing the loss and recovery of rod shape in 1994 cells with intermediate TagO levels when magnesium is removed and added back to the 1995 BCW51 was grown in LB supplemented with 8 mM xylose and 20 mM medium. 1996 magnesium, then loaded into a cellASIC chamber, and grown in the same media for 30 1997 minutes. At the start of the video the media is switched to contain 0 mM magnesium, 1998 causing the cells to lose rod shape. At 4:00:00 the media is switched to contain 20 mM 1999 magnesium where the cells revert back into rod-shaped cells. Frames are 20 min apart. 2000 Scale bar is 1 µm.

2001

2002 **S9. Related to Figure 6B** – Timelapse showing that the teichoic acid ligases TagTUV 2003 do not move circumferentially. Strains shown are BMD61, BCW81, BCW79 and 2004 BCW78, where Mbl, TagU (LytR), TagV (YvhJ), and TagT (YwtF) respectively are fused

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- 2005 to msfGFP, and expressed from their native promoters. Cells were grown in CH medium
- and imaged using TIRF illumination every 100 ms. Scale bar is 5  $\mu$ m.

2007

2008

## 2010 Supplemental Tables

### 2012 Table S1: Model Parameters. Related to Figure 4 and Supplemental

#### **Text 1.**

Quantity	Estimate	Source
MreB values		
MreB bound length <i>l</i> <sub>b</sub>	220 nm	This work
MreB monomer length <i>l</i> <sub>MreB</sub>	51 angstroms	(van den Ent et al., 2014)
MreB cross-sectional radius r <sub>MreB</sub>	3.2 nm	(van den Ent et al., 2014)
MreB wild-type principal radius of curvature R <sub>MreB</sub>	300 nm	This work
MreB Young's modulus Y <sub>MreB</sub>	Similar to actin; 2 GPa	(Kojima et al., 1994)
MreB cross-sectional binding fraction b	0	This work
Cell values		
B. subtilis periplasm thickness h <sub>peri</sub>	22 nm	(Matias and Beveridge, 2005)
<i>B. subtilis</i> cross-sectional radius <i>R</i> <sub>cell</sub>	500 nm	This work
<i>B. subtilis</i> internal turgor pressure $p_{cell}$	20 atm	(Whatmore and Reed, 1990)
Binding energy values		
Unit MreB-cell membrane interaction energy $E_{int}^0$	10 kT	This work
Absolute temperature T	300 K	This work
<i>B. subtilis</i> typical cross-sectional radius $R_{cell}^*$ for losing shape	about 1-1.5 microns	This work

#### 

#### **Table S2 – Strains used in this study**

Strain	Genotype (all strains are Py79 unless otherwise noted)	Source
BCW51	ycgO::Pxyl-tagO, tagO::erm, amyE::sfGFP-mreB, sinR::phleo	This work
BCW61	tagE::erm	This work
BCW72	yvhJΩPxylA-mazF (cat)	This work
BCW77	ywtFΩPxylA-mazF (cat)	This work
BCW78	ywtFΩmsfGFP-ywtF	This work
BCW79	yvhJΩmsfGFP-yvhJ	This work
BCW80	lytRΩPxyIA-mazF (cat)	This work
BCW81	lytRΩmsfGFP-lytR	This work
BCW82	tagO::erm, ycgO::PxylA-tagO, amyE::Pspac-gfp-mreB (spec), dacA::kan	This work
BDR2061	amyE::PxylA-gfp-mbl (spec), mblΩpMUTIN4 (erm)	(Carballido-Lopez and Errington, 2003)
BEB1451	hisA1 argC4 metC3 tagO::erm	(D'Elia et al., 2006)
BJS18	amyE::PxylA-gfp-mbl (spec)	(Defeu Soufo and Graumann, 2004)
BMD61	mblΩmbl-msfGFP (spec)	This work
BRB785	yhdG::Pspank-pbpA (phleo), pbpH::spec, pbpA::erm, mblΩPxylA-gfp-mbl (cat)	(Garner et al., 2011)
BEG202	ΔtagO::erm amyE::Pxyl-gfp-mbl (spec)	(Kawai et al., 2011)
BEG281	ycgO::PxylA-tagO	This work
BEG291	tagO::erm, ycgO::PxylA-tagO,	This work

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BEG275	amyE::Pspac-gfp-mreB (spec)	(Billings et al., 2014)
BEG300	tagO::erm, ycgO::PxylA-tagO, amyE::Pspac-gfp-mreB (spec),	This work
BRB4282	168 trpC2 ΔtagO::erm	(D'Elia et al., 2006)
bAB343	ftsZΩmNeonGreen-15aa-ftsZ, amyE::spc-Pspank-mciZ, ycgO::cat-Pxyl-tagO, tagO::erm	This work
bAB327	ftsZΩmNeonGreen-15aa-ftsZ, amyE::Phyperspank-minCD, ycgO::Pxyl-tagO, tagO::erm	This work
bAB388	ftsZΩmNeonGreen-15aa-ftsZ, amyE::Physpank-ftsA ycgO::cat-Pxyl-tagO, tagO::erm	This work

### **Table S3 – Oligonucleotides used in this study**

Primer	Sequence
oCW054	TGCAATTTCAGGGTTGACTG
oCW055	ATACGAACGGTACTGAGCGAGGGAGCAGAACGGCATCTAGAATATATGATCATTG
oCW056	ACTTATTAAATAATTTATAGCTATTGAAAAGAGAT
oCW057	TTTTCAATAGCTATAAATTATTTAATAAGTCTTGGAGGGTCACGGAAATAAA
oCW058	TTTCATCCTTGTTTTCAGGCTA
oCW072	ATGCGAAAAGGGGAAGAATTGTTTA
oCW073	GCCGCTTCCTTGGCCTGA
oCW100	TCCGTATGGAGATGGAGAGG
oCW101	CCGCTTATCCTTTTCACAGC
oCW109	ATACGAACGGTAGTTGACCAGTGCTCCCTGCCTTTGCACCTCGTCTGTTAAAT
oCW125	AAAATTAACGTACTGATTGGGTAGTCTAGAATGAGAAACGAACG
oCW137	GCCTGTAAACAATTCTTCCCCTTTTCGCATCCTTTGCACCTCGTCTGTTAAAT
oCW138	CAGGGACCGGGCTCAGGCCAAGGAAGCGGCATGAGAAACGAACG
	G
oCW139	ATAAACGGTTTCTCGCATGG
oCW141	ATACGAACGGTAGTTGACCAGTGCTCCCTGTTATTCAGTCTCCTTTATGTGATTGA
oCW142	AAAATTAACGTACTGATTGGGTAGTCTAGAATGGCTGAACGCGTTAGAGTG
oCW143	GAGCTGTCAGTCCCGTCTTC
oCW145	CAGGGACCGGGCTCAGGCCAAGGAAGCGGCATGGCTGAACGCGTTAGAGTG
oCW146	GCCTGTAAACAATTCTTCCCCTTTTCGCATTATTCAGTCTCCTTTATGTGATTGAC
oCW159	ATACGAACGGTAGTTGACCAGTGCTCCCTGATATCAATACCTCACGTTTCTTTAAT ATTT
oCW160	GCCTGTAAACAATTCTTCCCCTTTTCGCATATATCAATACCTCACGTTTCTTTAATA TTT
oCW161	CTTTGCTTTCTTCGCCATTC
oCW163	CAGGGACCGGGCTCAGGCCAAGGAAGCGGCATGGAAGAACGATCACAGCGC
oCW164	AAAATTAACGTACTGATTGGGTAGTCTAGAATGGAAGAACGATCACAGCGC
oCW165	CGCCATCCCGTTCATTATAC
oMD44	AATTCTCGAAGGAGAGCCTGTTC
oMD47	TGATTTCACAAACCTCATTCTGAAAAAGAATGAGGTTTTTTTATGAAAAATTCTGCT
	CCCTCGCTCAG
oMD48	CGTCATTTAACATCTTTTCGTGAAGGCCAGGGAGCACTGGTCAAC

CGTGAACTCATCGCTCC
TTCTTTTCAGAATGAGGTTTGTGAAATCATTTGTAAAGTTCATCCATTCCATGCG
TGGCCAGGGACCGGGCTCAGGCCAAGGAAGCGGCATGCGAAAAGGGGAAGAAT
TGTTTAC
ACGAACGGTAGTTGACCAGTGCTCCCTGTCTTGACACTCCTTATTTGATTTTTGA
AGAC
TTTGGATGGATTCAGCCCGATTG
GGGCAAGGCTAGACGGG
TCACATACTCGTTTCCAAACGGATC
ATACGAACGGTACTGAGCGAGGGAGCAGAATAATGGATTTCCTTACGCGAAATAC
G
GAGAGCTTGATGTCACAAGCAGCTGGGAAGGAATTCGTGCCATGTCACTATTGCT
ATAAAGAAGTCTCCTTTGGACTCGAGGCATTCAAATACAGATGCATTTTATTTCATA
TGAAATAAAATGCATCTGTATTTGAATGCCTCGAGTCCAAAGGAGACTTCTTTATG
CTTG
AATAAGGGTAACTATTGCCGTATGGGATCCATGCTAGCTTAATTCCTTTTCACCAG
CCG
TTCTGCTCCCTCGCTCAG
CAGGGAGCACTGGTCAAC
TCTAGACTACCCAATCAGTACGTT
CAGTTGAAATGGACAAACAAATC
ACTGAGCGAGGGAGCAGAAGTGTCATCACCTTCCTTG
GTTGACCAGTGCTCCCTGTGCCTGAGCAGAGGC
GGACAGCACCATGTCTACTTAAC
TAGATCACCTCCTTAAGCTT
CGGTAAGTCCCGTCTAGCCTTGCCCTTATGGCTTTGAGATCCAATCTTT
CAATTAAGCTTAAGGAGGTGATCTAGTGAAAGTGCACCGCATGCC

2021

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