Decoding sequence-level information to predict membrane protein expression

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1 Summary

The expression of integral membrane proteins (IMPs) remains a major bottleneck in the 2 characterization of this important protein class. IMP expression levels are currently unpredictable, which 3 4 renders the pursuit of IMPs for structural and biophysical characterization challenging and inefficient. Experimental evidence demonstrates that changes within the nucleotide or amino-acid sequence for a 5 given IMP can dramatically affect expression; yet these observations have not resulted in generalizable 6 7 approaches to improved expression. Here, we develop a data-driven statistical predictor named IMProve, that, using only sequence information, increases the likelihood of selecting an IMP that 8 expresses in E. coli. The IMProve model, trained on experimental data, combines a set of sequence-9 derived features resulting in an IMProve score, where higher values have a higher probability of success. 10 The model is rigorously validated against a variety of independent datasets that contain a wide range of 11 experimental outcomes from various IMP expression trials. The results demonstrate that use of the 12 13 model can more than double the number of successfully expressed targets at any experimental scale. IMProve can immediately be used to identify favorable targets for characterization. 14

15 Introduction

The biological importance of integral membrane proteins (IMPs) motivates structural and 16 biophysical studies that require large amounts of purified protein at considerable cost. Only a small 17 percentage can be produced at high-levels resulting in IMP structural characterization lagging far behind 18 that of soluble proteins; IMPs currently constitute less than 2% of deposited atomic-level structures ¹. To 19 increase the pace of structure determination, the scientific community created large government-funded 20 structural genomics consortia facilities, like the NIH-funded New York Consortium on Membrane 21 Protein Structure (NYCOMPS)². For this representative example, more than 8000 genes, chosen based 22 23 on characteristics hypothetically related to success, yielded only 600 (7.1%) highly expressing proteins 3 resulting to date in 34 (5.6% of expressed proteins) unique structures (based on annotation in the RCSB 24 PDB⁴). This example highlights the funnel problem of structural biology, where each stage of the 25 structure pipeline eliminates a large percentage of targets compounding into an overall low rate of 26 success ⁵. With new and rapidly advancing technologies like cryo-electron microscopy, serial 27 femtosecond crystallography, and micro-electron diffraction, we expect that the latter half of the funnel, 28 structure determination, will increase in success rate $^{6-8}$. However, IMP expression will continue to limit 29 targets accessible for study ⁹. 30

Tools for improving the number of expressed IMPs are needed. While significant work has shown promise on a case-by-case basis, *e.g.* growth at lower temperatures, codon optimization ¹⁰, and regulating transcription ¹¹, a generalizable solution remains elusive. Currently, each target must be addressed individually as the conditions that were successful for a previous target seldom carry over to other proteins, even amongst closely related homologs ^{5,12}. For individual cases, simple changes can have dramatic effects on the amount of expressed proteins ^{13,14}. Considering the scientific value of IMP studies, it is surprising that there are no methods that can provide solutions for improved expression outcomes with broad applicability across protein families and genomes.

There are currently no approaches available that can decode sequence-level information for predicting IMP expression; yet it is common knowledge that sequence changes which alter overall biophysical features of the protein and mRNA transcript can measurably influence IMP biogenesis. While physics-based approaches which have proven successful in correlating integration efficiency and

expression ^{12,15}, that and other work revealed that simple application of specific 'sequence features', such as the positive-inside rule, are inadequate to predict IMP expression ^{16,17}. For the positive-inside 43 44 rule, as an example, this contrasts evidence that the number of positive-charges on cytoplasmic loops is 45 known to be an important determinant of IMP biogenesis ^{18,19}. The reasons for this failure to connect 46 sequence to expression likely lie in the complex underpinnings of IMP biogenesis, where the interplay 47 between many sequence features at both the protein and nucleotide levels must be considered. 48 Optimizing for a single sequence feature likely diminishes the beneficial effect of other features (e.g. 49 increasing positive residues on internal loops might diminish favorable mRNA properties). Without 50 accounting for the broad set of sequence features related to IMP expression, it is impossible to predict 51 differences in expression. 52

Development of a low-cost, computational resource that significantly and reliably predicts 53 improved expression outcomes would transform the study of IMPs. Attempts to develop such algorithms 54 have so far failed. Several examples, Daley, von Heijne, and coworkers ^{10,16,17} as well as NYCOMPS. 55 were unable to use experimental expression data sets to train models that returned any predictive 56 performance (personal communication). This is not surprising, given the difficulty of expressing IMPs 57 and the limits in the knowledge of the sequence features that drive expression. In other contexts, 58 statistical tools based on sequence have been shown to work; for example, those developed to predict soluble protein expression and/or crystallization propensities ^{20–22}. Such predictors are primarily based 59 60 on available experimental results from the Protein Structure Initiative ^{23,24}. While collectively these 61 methods have supported significant advances in biochemistry, none of the models are able to predict 62 IMP outcomes due to limitations inherent in the model development process. As IMPs have an 63 extremely low success rate, they are either explicitly excluded from the training process or are implicitly 64 down-weighted by the statistical model (for representative methodology see ²⁵). Consequently, none 65 have successfully been able to map IMP expression to sequence. 66

Here, we demonstrate for the first time that it is possible to predict IMP expression directly from 67 sequence. The resulting predictor allows one to enrich expression trials for proteins with a higher 68 probability of success. To connect sequence to prediction, we develop a statistical model that maps a set 69 of sequences to experimental expression levels via calculated features—thereby simultaneously 70 accounting for the many potential determinants of expression. The resulting IMProve model allows 71 ranking of any arbitrary set of IMP sequences in order of their relative likelihood of successful 72 expression. The IMProve model is extensively validated against a variety of independent datasets 73 demonstrating that it can be used broadly to predict the likelihood of expression in *E. coli* of any IMP. 74 With IMProve, we have built a way for more than two-fold enrichment of positive expression outcomes 75 relative to the rate attained from the current method of randomly selecting targets. We highlight how the 76 model informs on the biological underpinnings that drive likely expression. Finally, we provide direct 77 examples where the model can be used for a typical researcher. Our novel approach and the resulting 78 IMProve model provide an exciting paradigm for connecting sequence space to complex experimental 79 outcomes. 80

81 **Results**

For this study, we focus on heterologous expression in *E. coli*, due to its ubiquitous use as a tool for expression across the spectrum of the membrane proteome. For example, 43 of the 216 unique eukaryotic IMP structures were solved using protein expressed in *E. coli* (based on annotation in the RCSB PDB ⁴). Low cost and low barriers for adoption highlight the utility of *E. coli* as a broad tool if the expression problem can be overcome.

87 Development of a computational model trained on *E. coli* expression data

A key component of any data-driven statistical model is the choice of dataset used for training. 88 Having searched the literature, we identified two publications that contained quantitative datasets on the 89 IPTG-induced overexpression of E. coli polytopic IMPs in E. coli. The first set, Daley, Rapp et al., 90 contained activity measures, proxies for expression level, from C-terminal tags of either GFP or PhoA 91 (alkaline phosphatase)¹⁶. The second set, Fluman *et al.*, used a subset of constructs from the first and 92 contained a more detailed analysis utilizing in-gel fluorescence to measure folded protein ²⁶ (see 93 Methods 4c). The expression results strongly correlated (Spearman's $\rho = 0.73$) between the two datasets 94 demonstrating that normalized GFP activity was a good measure of the amount of folded IMP (Fig. 1A 95 and ^{26,27}). The experimental set-up employed multiple 96-well plates over multiple days resulting in 96 pronounced variability in the absolute expression level of a given protein between trials. Daley, Rapp et 97 al. calculated average expression levels by dividing the raw expression level of each protein by that of a 98 control protein on the corresponding plate. 99

To successfully map sequence to expression, we additionally needed to derive numerical features 100 from a given gene sequence that are empirically related to expression. Approximately 105 sequence 101 features from protein and nucleotide sequence were calculated for each gene using custom code together 102 with published software (codonW²⁸, tAI²⁹, NUPACK³⁰, Vienna RNA³¹, Codon Pair Bias³², Disembl³³, and RONN³⁴). Relative metrics (*e.g.* codon adaptation index) are calculated with respect to the *E*. 103 104 coli K-12 substr. MG1655 ³⁵ quantity. The octanol-water partitioning ³⁶, GES hydrophobicity ³⁷, ΔG of 105 insertion ³⁸ scales were employed as well. Transmembrane segment topology was predicted using 106 Phobius constrained for the training data and Phobius for all other datasets ³⁹. Two RNA secondary 107 structure metrics were prompted in part by Goodman, et al. 40. Supplementary Table 1 includes a 108 detailed description of each feature. All features are calculated solely from the coding region of each 109 gene of interest excluding other portions of the open reading frame and plasmid (e.g. linkers and tags, 5' 110 111 untranslated region, copy number).

Fitting the data to a simple linear regression provides a facile method for deriving a weight for each feature. However, using the set of sequence features, we were unable to successfully fit a linear regression using the normalized GFP and PhoA measurements reported in the Daley, Rapp *et al.* study. Similarly, using the same feature set and data, we were unable to train a standard linear Support Vector Machine (SVM) to predict the expression data either averaged or across all plates (see Supplementary Table 1; Methods 2,3). Due to the attempts by others to fit this data, this outcome may not be surprising and suggested that a more complex analysis was required.

119 We hypothesized that training on relative measurements across the entire dataset introduced errors that were limiting. To address this, we instead only compare measurements within an individual 120 plate, where differences between trials are less likely to introduce errors. To account for this, a 121 preference-ranking linear SVM algorithm (SVM^{rank 41}) was chosen (see Methods 4b). Simply put, the 122 SVM^{rank} algorithm determines the optimal weight for each sequence feature to best rank the order of 123 expression outcomes within each plate over all plates, which results in a model where higher expressing 124 proteins have higher scores. The outcome is identical in structure to a multiple linear regression, but 125 instead of minimizing the sum of squared residuals, the SVM cost function accounts for the plate-wise 126 constraint specified above. In practice, the process optimizes the correlation coefficient Kendall's τ (Eq. 127 1) to converge upon a set of weights. 128

129 130

$$\tau_{\text{kendall}} = \frac{\# \text{ correctly ordered pairs} - \# \text{ swapped pairs}}{\# \text{ total pairs}} \tag{1}$$

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Various metrics summarize the accuracy with which the model fits the input data (Fig. 1B-E). 132 The SVM^{rank} training metric shows varying agreement for all groups (*i.e.*, $\tau_{\text{kendall}} > 0$) (Fig. 1B). For 133 individual genes, activity values normalized and averaged across trials were not directly used for the 134 135 training procedure (see Methods 4a); yet one would anticipate that scores for each gene should broadly correlate with the expression average. Indeed, the observed normalized activities positively correlate 136 with the score (dubbed IMProve score for Integral Membrane Protein expression improvement) output 137 by the model (Fig. 1C, $\rho > 0$). Since SVM^{rank} transforms raw expression levels within each plate to ranks 138 before training, there is no expectation or guarantee that magnitude differences in expression level 139 manifest in magnitude differences in score. As a result, Spearman's ρ , a rank correlation coefficient 140 describing the agreement between two ranked quantities, is better suited for quantifying correlation over 141 more common metrics like the R^2 of a regression and Pearson's r. 142

For a more quantitative approach to assessing the IMProve model's success within the training 143 data, we turn to the Receiver Operating Characteristic (ROC). ROC curves quantify the tradeoff between 144 true positive and false positive predictions across the numerical scores output from a predictor. This is a 145 more reliable assessment of prediction than simply calculating accuracy and precision from a single, 146 arbitrary score threshold ⁴². The figure of merit that quantifies a ROC curve is the Area Under the Curve 147 (AUC). Given that the AUC for a perfect predictor corresponds to 100% and that of a random predictor 148 is 50% (Fig. 1D, grey dashed line), an AUC greater than 50% indicates predictive performance of the 149 model (percentage signs hereafter omitted) (see Methods 5 and ⁴²). Here, the ROC framework will be 150 used to quantitatively assess the ability of our model to predict the outcomes within the various datasets. 151

The training datasets are quantitative measures of activity requiring that an activity threshold be 152 chosen that defines positive or negative outcomes. For example, ROC curves using two distinct activity 153 thresholds, at the 25th or 75th percentile of highest expression, are plotted with their calculated AUC 154 values (Fig. 1D). While both show that the model has predictive capacity, a more useful visualization 155 would consider all possible activity thresholds. For this, the AUC value for every activity threshold is 156 157 plotted showing that the model has predictive power regardless of an arbitrarily chosen expression threshold (Fig. 1E). In total, the analysis demonstrates that the model can rank expression outcomes 158 across all proteins in the training set. Interestingly, for PhoA-tagged proteins the model is progressively 159 less successful with increasing activity. The implications for this are discussed later (see Fig. 2G below). 160

161 **Demonstration of prediction against an independent large expression dataset**

While the above analyses show that the model successfully fits the training data, we assess the 162 broader applicability of the model outside the training set based on its success at predicting the outcomes 163 of independent expression trials from distinct groups and across varying scales. The first test considers 164 results from NYCOMPS, where 8444 IMP genes entered expression trials, in up to eight conditions, 165 resulting in 17114 expression outcomes (Fig. 2A)². The majority of genes were attempted in only one 166 condition (Fig. 2B), and, importantly, outcomes were non-quantitative (binary: expressed or not 167 expressed) as indicated by the presence of a band by Coomassie staining of an SDS-PAGE gel after 168 small-scale expression, solubilization, and nickel affinity purification³. For this analysis, the 169 experimental results are either summarized as outcomes per gene or broken down as raw outcomes 170 across defined expression conditions. For outcomes per gene, we can consider various thresholds for 171 172 considering a gene as positive based on NYCOMPS expression success (Fig. 2B). The most stringent threshold only regards a gene as positive if it has no negative outcomes ("Only Positive", Fig. 2B, red). 173 Since a well expressing gene would generally advance in the NYCOMPS pipeline without further small-174 scale expression trials, this positive group likely contains the best expressing proteins. A second 175

category comprises genes with at least one positive and at least one negative trial ("Mixed", Fig. 2B,
blue). These genes likely include proteins that are more difficult to express.

ROCs assess predictive power across these groups (Fig. 2C). IMProve scores markedly 178 179 distinguish genes in the most stringent positive group (Only Positive) from all other genes (AUC = 67.1) (Fig. 2C red). A permissive threshold considering genes as positive with at least one positive trial (Only 180 Positive plus Mixed genes) shows moderate predictive power (Fig. 2C pink, AUC = 59.7). If instead the 181 Mixed genes are considered alone (excluding the Only Positive), the model very weakly distinguishes 182 the mixed group from Only Negative genes (Fig. 2C dashed blue, AUC = 53.5). This likely supports the 183 notion that this pool largely consists of more difficult-to-express genes. For further analysis of 184 NYCOMPS, we focus on the Only Positive pool as this likely represents the pool of best expressing 185 proteins. 186

The predictive power of the IMProve model can be assessed by a variety of additional metrics. 187 This can be qualitatively visualized as a histogram of the IMProve scores for genes separated by 188 expression success (Only Positive, red; Mixed, blue; Only Negative, grey) (Fig. 2D). Visually, the 189 distribution of the scores for the Only Positive group is shifted to a higher score relative to the Only 190 Negative and Mixed groups. The dramatic increase in the percentage of Only Positive genes as a 191 function of increasing IMProve score (overlaid as a brown line) further emphasizes this. A major aim of 192 this work is to enrich the likelihood of choosing positively expressing proteins. The positive predictive 193 value (PPV, true positives ÷ predicted positives) becomes a useful metric for positive enrichment as it 194 conveys the degree of improved prediction over the experimental baseline of the dataset. The PPV of the 195 model is plotted as a function of the percentile of the IMProve score for the Only Positive group (Fig. 196 2E). In the figure, the experimental baseline, all are predicted positive (PPV = 11.1%), is represented by 197 a dashed line; therefore, a relative increase reflects the predictive power of the algorithm. For example, 198 considering the top fourth of genes by IMProve score $(75^{\text{th}} \text{ percentile}, \text{IMProve score} = -0.2, \text{PPV} =$ 199 20%) shows that the algorithm increases the positive outcomes by 9% over baseline (1.82 fold change). 200 Higher score cut-offs would have even higher increases in positive outcomes. For further illustration, we 201 plot the fold-change in PPV across all thresholds (Fig. 2F). 202

We next confirm the ability of the IMProve model to predict within plasmids or sequence space 203 distinct from those within the limited training set. For an overfit model, one might expect that only the 204 subset of targets which most closely mirror the training data would show strong prediction. On the 205 contrary, the model shows consistent performance throughout each of the eight distinct experimental 206 conditions tested (Fig. 2G and Supplementary Table 2). One may also consider that the small size of the 207 training set limited the number of protein folds sampled and, therefore, limited the number of folds that 208 could be predicted by the model. To test this, we consider the performance of the model with regards to 209 protein homology families, as defined by Pfam family classifications ⁴³. The 8444 genes in the 210 NYCOMPS dataset fall into 555 Pfam families (~15% not classified). To understand whether the 211 IMProve score is biased towards families present in the training set, we separate genes in the 212 NYCOMPS dataset into either within the 153 Pfam families found in the training set or outside this pool 213 (*i.e.* not in the training set). Satisfyingly, there is no significant difference in AUC at 95% confidence 214 between these groups (68.2 versus 67.2) (Fig. 2H). Combined, this highlights that the model is not 215 sensitive to the experimental design of the training set and predicts broadly across different vector 216 backbones and protein folds. 217

The ability to predict the experimental data from NYCOMPS allows returning to the question of alkaline phosphatase as a metric for expression. For the training set, proteins with C-termini in the periplasm show less consistent fitting by the model (Fig. 1, orange). To assess the generality of this result, the NYCOMPS outcomes are split into pools for either cytoplasmic or periplasmic C-terminal localization and AUCs are calculated for each. There are no significant differences in predictive capacity
 across all conditions (Fig. 2G, green vs. orange) irrespective of whether the tag is at the N- or C terminus. This demonstrates that the IMProve model is applicable for all topologies.

At this point, it is useful to consider the potential improvement in the number of positive outcomes by using the IMProve model. NYCOMPS tested about a tenth of the 74 thousand possible IMPs from the 98 genomes of interest for expression ². Had NYCOMPS tested the same number of genes from this pool, but selected to have an IMProve score greater than 0.5 (at the 91st percentile (Fig. 2D, yellow line)), they would have increased their positive pool of 934 by an additional 1207 proteins. This represents a more than two-fold improvement in the return on investment and is a clear benchmark of success for the IMProve model.

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233 Further demonstration of prediction against small-scale independent datasets

The NYCOMPS example demonstrates the predictive power of the model across the broad range of sequence space encompassed by that dataset. Next, the performance of the model is tested against relevant subsets of sequence space (*e.g.* a family of proteins or the proteome from a single organism), which are reminiscent of laboratory-scale experiments that precede structural or biochemical analyses. While a number of datasets exist ^{5,44–55}, we identified seven for which complete sequence information could be obtained to calculate all the necessary sequence features ^{44–50}.

To understand the predictive performance within each of the small-scale datasets, we analyze the 240 predictive performance of the model and highlight how the model could have been used to streamline 241 those experiments. The clear predictive performance within the large-scale NYCOMPS dataset (Fig. 2) 242 243 serves as a benchmark of expected performance at the scale of the experimental efforts for an individual lab (Fig. 3A). As targets within the various datasets were tested only one or a few times, experimental 244 variability within each set could play a large-role on the outcomes noted. Therefore, we summarize 245 positives within each dataset as those genes with the highest level of outcome as reported by the original 246 authors as this outcome is likely most robust to such variability (e.g. seen via Coomassie Blue staining 247 of an SDS-PAGE gel). To be complete, we have plotted and considered predictive performance across 248 249 all possible outcomes as well (Fig. 3B-D, Supplementary Fig. 1).

The performance of the IMProve model for each of the small-scale datasets is consistent with 250 that seen for the NYCOMPS dataset (Fig. 3A). This is most directly indicated by a mean AUC across all 251 datasets of 65.6, highlighting the success across the varying scales. While the overall positive rate is 252 different for each dataset, considering a cut-off in IMProve score, e.g. the top 50% or 10% of targets 253 ranked by score, would have resulted in a greater percentage of positive outcomes. On average, ~70% of 254 positives are captured within the top half of scores. Similarly, for the top 10% of scores, on average over 255 20% of the positives are captured. Simply put, for one tenth of the work one would capture a significant 256 number of the positive outcomes within the pool of targets in each dataset. 257

For broader consideration, one can consider the fold change in positive rate by selecting targets 258 informed by IMProve scores. Using the data available, only testing proteins within the top 10% of scores 259 would result in an average fold change of 2.0 in the positive rate (*i.e.* twice as many positively expressed 260 proteins). As positive rate is a bounded quantity (maximum is 100%), the possible fold change is 261 bounded as well and becomes relative to the overall positive rate when considering various cut-offs (e.g. 262 for *T. maritima* the maximum fold-change is 15.4 while for archaeal transporters it is 3.3). Taking the 263 average maximum possible fold change (7.5), the IMProve model achieves nearly a third of the possible 264 improvement in positive rate compared to a perfect predictor. 265

Since IMProve model was trained on quantitative expression outcomes, we also expect that it 266 captures quantitative trends in expression, *i.e.* a higher score translates to greater amount of expressed 267 protein. While the NYCOMPS results are consistent with this (Fig. 2b), of the various data sets, only the 268 expression of archaeal transporters presents quantitative expression outcomes for consideration. For this 269 dataset, 14 archaeal transporters were chosen based on their homology to human proteins ⁴⁴ and tested 270 for expression in E. coli; total protein was quantified in the membrane fraction by Coomassie Blue 271 staining of an SDS-PAGE gel. Here, the majority of the expressing proteins fall into the higher half of 272 the IMProve scores, 7 out of 9 of those with multiple positive outcomes (Fig. 3B). Strikingly, 273 quantification of the Coomassie Blue staining highlights a clear correlation with the IMProve score 274 where the higher expressing proteins have higher scores (Fig. 3C). 275

A final test considers the ability of the model to predict expression in hosts other than E. coli. 276 The expression trials of 101 mammalian GPCRs in bacterial and eukaryotic systems ⁴⁷ provides a data 277 set for considering this question. For this experiment, trials in E. coli clearly follow the trend that 278 IMProve can predict within this group of mammalian proteins (AUC = 77.7) (Fig. 3A & Supplementary 279 Fig. 1A,B). However, the expression of the same set of proteins in *P. pastoris* fails to show any 280 predictive performance (AUC = 54.8) (Supplementary Fig. 1A,B). This lack of predictive performance 281 in P. pastoris suggests that the parameterization of the model, calibrated for E. coli expression, requires 282 retraining to generate a different model that captures the distinct interplay of sequence parameters in 283 other hosts. 284

285 **Biological importance of various sequence features**

Considering the success of IMProve, one might anticipate that biological properties driving 286 287 prediction may provide insight into IMP biogenesis and expression. Using a proof-of-concept linear model allowed for a straightforward and useful predictor. With a linear model, as employed here, 288 289 extracting the importance of each feature is ordinarily straightforward; assuming features are distributed 290 identically and independently ("i.i.d."), the weight assigned to each feature should correspond to its relative importance. However, in our case, the input features do not satisfy these conditions and 291 significant correlation exists between individual features (Supplementary Fig. 2). As a result, during the 292 293 training procedure, unequal weight is placed across correlating features that represent the same underlying biological property, thereby, complicating the process of determining the biological 294 295 underpinnings of the IMProve score. For example, the importance of transmembrane segment hydrophobicity for membrane partitioning is distributed between several features: among these the 296 average $\Delta G_{\text{insertion}}$ ³⁸ of TM segments has a positive weight whereas average hydrophobicity, a 297 correlating feature, has a negative weight (Supplementary Table 1, Supplementary Fig. 2). As many 298 299 features are correlated; conclusive information cannot be obtained simply using weights of individual features to interpret the relative importance of their underlying biological phenomena. We address this 300 complication by coarsening our view of the features to two levels: First, we analyze features derived 301 from protein versus those derived from nucleotide sequence, and then we look more closely at features 302 groups after categorizing by biological phenomena. 303

The coarsest view of the features is a comparison of those derived from protein sequence versus those derived from nucleotide sequence. The summed weight for protein features is around zero, whereas for nucleotide features the summed weight is slightly positive suggesting that in comparison these features may be more important to the predictive performance of the model (Fig. 4A). Within the training set, protein features more completely explain the score both via correlation coefficients (Fig. 4B) as well as through ROC analysis (Fig. 4C). However, comparison of the predictive performance of the two subsets of weights shows that the nucleotide features alone can give similar performance to the full model for the NYCOMPS dataset (Fig. 4D). Within the small-scale datasets investigated, using only protein or nucleotide features shows no significant difference in predictive power at 95% confidence (Fig. 4E). In general, this suggests that neither protein nor nucleotide features are uniquely important for IMP expression. However, within the context of the trained model, nucleotide features are critical for predictive performance for a large and diverse dataset such as NYCOMPS. This finding corroborates growing literature that the nucleotide sequence holds significant determinants of biological processes 40,26,56–58.

We next collapse conceptually similar features into biological categories that allow us to infer 318 the phenomena that drive prediction. Categories are chosen empirically (e.g. the hydrophobicity group 319 incorporates sequence features such as average hydrophobicity, maximum hydrophobicity, $\Delta G_{insertion}$, 320 etc.), which results in a reduction in overall correlation (Supplementary Fig. 3A). The full category list is 321 provided in Supplementary Table 1. To visualize the importance of each category, the collapsed weights 322 are summarized in Supplementary Fig. 3B, where each bar contains individual feature weights within a 323 category. Features with a negative weight are stacked to the left of zero and those with a positive weight 324 are stacked to the right. A red dot represents the sum of all weights, and the length of the bar gives the 325 total absolute value of the combined weights within a category. Ranking the categories based on the sum 326 327 of their weight suggests that some categories play a more prominent role than others. These include properties related to transmembrane segments (hydrophobicity and TM size/count), codon pair score, 328 loop length, and overall length/pI. 329

To explore the role of each biological category in prediction, the performance of the model is 330 assessed using only features within a given category. First, the strength of the correlation coefficients for 331 given categories within the training set suggests the relative utility of each category for prediction. 332 (Supplementary Fig. 3C, as in Fig. 4B). Examples of categories with high correlation coefficients are 5' 333 Codon Usage, Length/pI, Loop Length, and SD-like Sites. To verify their importance for prediction, we 334 consider the AUC for prediction using each feature category for the NYCOMPS dataset (Supplementary 335 336 Fig. 3D). In this analysis, only Length/pI shows some predictive power. Overall, the analysis of the training and large-scale testing dataset shows that no feature category independently drives the predictor. 337 Excluding each individually does not significantly affect the overall predictive performance, except for 338 Length/pI (data not shown). Sequence length composes the majority of the weight within this category 339 and is one of the highest weighted features in the model (Supplementary Fig. 3A). This is consistent 340 with the anecdotal observation that larger IMPs are typically harder to express. However, this parameter 341 alone would not be useful for predicting within a smaller subset, like a single protein family, where there 342 is little variance in length (e.g. Fig. 3,5). One might develop a predictor that was better for a given 343 protein family under certain conditions with a subset of the entire features considered here; yet this 344 would require *a priori* knowledge of the system, *i.e.* which sequence features were truly most important. 345 and would preclude broad generalizability as shown for the IMProve model. 346

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348 Usage of the IMProve model for IMP expression

We illustrate the IMProve model's ability to identify promising homologs within a protein family by considering subsets of the broad range of targets tested by NYCOMPS. First, we consider two examples for protein families that do not have associated atomic resolution structures: copper resistance proteins (CopD, PF05425) and short-chain fatty-acid transporters (AtoE, PF02667). In the first two rows of Fig. 5A, genes from the two families are plotted by IMProve score and colored by experimental outcome. In both cases, as indicated by the AUCs of 88.2 and 80.7 (Fig. 5A), the model excels at predicting these families and provides a clear score cut-off to guide target selection for future expression experiments. For example, we expect that CopD homologs with IMProve scores above -1 will have a higher likelihood of expressing over other homologs.

We have calculated predictive performance for each Pfam found in the NYCOMPS data which 358 359 allows us to provide considerations for future experiments (Supplementary Table 3). In particular, we highlight three families with many genes tested, multiple experimental trials and a spread of outcomes: 360 voltage-dependent anion channels (PF03595), Na/H exchangers (PF00999), and glycosyltransferases 361 (PF00535). For these, a very clear IMProve score cut-off emerges from the experimental outcomes 362 (dashed line in Fig. 5A). Strikingly, for these families the IMProve model clearly ranks the targets with 363 Only Positive outcomes (red) at higher scores, again suggesting a preference for the best expressing 364 proteins (see Fig. 2 and 3). Similarly, many more families within NYCOMPS are predicted with high 365 statistical confidence (Supplementary Table 3); we provide a subset as Fig. 5B. For these, if only genes 366 in the top 50% of IMProve score were tested, 81% of the total positives would be captured. As noted 367 before, this is a dramatic increase in efficiency. Excitingly, many of these families remain to be resolved 368 structurally. Considering these results with the broader experimental data sets (Fig. 3), no matter the 369 number of proteins one is willing to test, the IMProve model enables selecting targets with a high 370 probability of expression success in E. coli. 371

372 Sequence optimization for expression

The predictive performance of the model implies that the features defined here provide a coarse 373 approximation of the fitness landscape for IMP expression. Attempting to optimize a single feature by 374 modifying the sequence will likely affect the resulting score and expression due to changes in other 375 features. Fluman, et al. provides an illustrative experiment ²⁶. For that work, it was hypothesized that 376 altering the number of Shine-Dalgarno (SD)-like sites in the coding sequence of a IMP would affect 377 expression. To test this, silent mutations were engineered within the first 200 bases of three proteins 378 379 (genes ygdD, brnQ, and ybjJ from E. coli) to increase the number of SD-like sites with the goal of 380 improving expression. Expression trials demonstrated that only one of the proteins (BrnO) had improved expression of folded protein. While the number of SD-like sites alone does not correlate, only 1 out of 3, 381 the resulting changes in the IMProve score correlate with the changes in measured expression, 3 out of 3 382 383 (Fig. 5C). The IMProve model's ability to capture the outcomes in this small test case illustrates the utility of integrating the contribution of the numerous parameters involved in IMP biogenesis. 384

385 **Discussion**

Here, we have demonstrated a statistically driven predictor, IMProve, that decodes from 386 sequence the sum of biological features that drive expression, a feat not previously possible ^{10,17}. The 387 current best practice for characterization of an IMP target begins with the identification and testing of 388 multiple homologs or variants for expression. The predictive power of IMProve enables this by 389 providing a low barrier-to-entry method to enrich more than two-fold the positive outcomes from such 390 expression. IMProve allows for the prioritization of targets to test for expression making more optimal 391 use of limited human and material resources. For groups with small scale projects such as individual 392 labs, this means that for the same cost one would double the success rate. For large scale groups, such as 393 companies or consortia, IMProve can reduce by half the cost required to obtain the same number of 394 395 positive results. We provide the current predictor as a web service where scores can be calculated, and the method, associated data, and suggested analyses are publically available to catalyze progress across 396 the community (clemonslab.caltech.edu). 397

Having shown that IMP expression can be predicted, the generalizability of the model is 398 399 remarkable despite several known limitations. Using data from a single study for training precludes including certain variables that empirically influence expression such as the features corresponding to 400 401 fusion tags and the context of the protein in an expression plasmid, e.g. the 5' untranslated region, for which there was no variation in the Daley, Rapp, et al. dataset. Moreover, using a simple proof-of-402 concept linear model allowed for a straightforward and robust predictor; however, intrinsically it cannot 403 be directly related to the biological underpinnings. While we can extract some biological inference, a 404 linear combination of sequence features does not explicitly reflect the reality of physical limits for host 405 cells. To some extent, constraint information is likely encoded in the complex architecture of the 406 underlying sequence space (e.g. through the genetic code, TM prediction, RNA secondary structure 407 analyses). Future statistical models that improve on these limitations will likely hone predictive power 408 and more intricately characterize the interplay of variables that underlie IMP expression in E. coli and 409 other systems. 410

A perhaps surprising outcome of our results is the demonstration of the quantitatively important 411 contribution of the nucleotide sequence as a component of the IMProve score. This echoes the growing 412 literature that aspects of the nucleotide sequence are important determinants of protein biogenesis in 413 general ^{40,26,56–58}. While one expects that there may be different weights for various nucleotide derived 414 features between soluble and IMPs, it is likely that these features are important for soluble proteins as 415 well. An example of this is the importance of codon optimization for soluble protein expression, which 416 has failed to show any general benefit for IMPs¹⁰. Current expression predictors that have predictive 417 power for soluble proteins have only used protein sequence for deriving the underlying feature set ^{59,60}. 418 Future prediction methods will likely benefit from including nucleotide sequence features as done here. 419

The ability to predict phenotypic results using sequence based statistical models opens a variety 420 of opportunities. As done here, this requires a careful understanding of the system and its underlying 421 biological processes enumerated in a multitude of individual variables that impact the stated goal of the 422 predictor, in this case enriching protein expression. As new features related to expression are discovered, 423 future work will incorporate these leading to improved models. This can include features derived from 424 other approaches such as the integration efficiency derived from coarse-grained molecular dynamics 425 ^{12,15}. Based on these results, expanding to new expression hosts such as eukaryotes seems entirely 426 feasible, although a number of new features may need to be considered, e.g. glycosylation sites and 427 trafficking signals. Moreover, the ability to score proteins for expressibility creates new avenues to 428 computationally engineer IMPs for expression. The proof-of-concept described here required significant 429 work to compile data from genomics consortia and the literature in a readily useable form. As data 430 becomes more easily accessible, broadly leveraging diverse experimental outcomes to decode sequence-431 level information, an extension of this work, is anticipated. 432

433 Author Contributions

S.M.S., A.M., and W.M.C. conceived the project. S.M.S. developed the approach. S.M.S., A.M.,
and N.J. compiled sequence and experimental data. N.J. created code to demonstrate feasibility. S.M.S.
performed all published calculations. S.M.S. and W.M.C. wrote the manuscript.

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455 **Online Methods**

Sequence mapping & retrieval and feature calculation was performed in Python 2.7 ⁶² using
BioPython ⁶³ and NumPy ⁶⁴; executed and consolidated using Bash (shell) scripts; and parallelized
where possible using GNU Parallel ⁶⁵. Data analysis and presentation was done in R ⁶⁶ within RStudio ⁶⁷
using magrittr ⁶⁸, plyr ⁶⁹, dplyr ⁷⁰, asbio ⁷¹, and datamart ⁷² for data handling; ggplot2 ⁷³, ggbeeswarm ⁷⁴,
GGally ⁷⁵, gridExtra ⁷⁶, cowplot ⁷⁷, scales ⁷⁸, viridis ⁷⁹, and RColorBrewer ^{80,81} for plotting; multidplyr ⁸²
with parallel ⁶⁶ and foreach ⁸³ with iterators ⁸⁴ and doMC ⁸⁵/doParallel ⁸⁶ for parallel processing; and
roxygen2 ⁸⁷ for code organization and documentation as well as other packages as referenced.

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1. Collection of data necessary for learning and evaluation

E. coli Sequence Data – The nucleotide sequences from 16 were deduced by reconstructing forward and 465 reverse primers (i.e. ~20 nucleotide stretches) from each gene in Colibri (based on EcoGene 11), the 466 original source cited and later verified these primers against an archival spreadsheet provided directly by 467 Daniel Daley (personal communication). To account for sequence and annotation corrections made to 468 the genome after Daley, Rapp, et al.'s work, these primers were directly used to reconstruct the 469 amplified product from the most recent release of the *E. coli* K-12 substr. MG1655 genome ³⁵ (EcoGene 470 3.0; U00096.3). Although Daniel Daley mentioned that raw reads from the Sanger sequencing runs may 471 be available within his own archives, it was decided that the additional labor to retrieve this data and 472 parse these reads would not significantly impact the model. The deduced nucleotide sequences were 473 verified against the protein lengths given in Supplementary Table 1 from ¹⁶. The plasmid library tested 474 in ²⁶ was provided by Daniel Daley, and those sequences are taken to be the same. 475

476

E. coli Training Data – The preliminary results using the mean-normalized activities echoed the 477 findings of ¹⁶ that these do not correlate with sequence features either in the univariate sense (many 478 simple linear regressions, Supplementary Table 1¹⁶) or a multivariate sense (multiple linear regression, 479 data not shown). This is presumably due to the loss of information regarding variability in expression 480 481 level for given genes or due to the increase in variance of the normalized quantity (See Methods 4a) due to the normalization and averaging procedure. Daniel Daley and Mikaela Rapp provided spreadsheets of 482 the outcomes from the 96-well plates used for their expression trials and sent scanned copies of the 483 readouts from archival laboratory notebooks where the digital data was no longer accessible (personal 484 communication). Those proteins without a reliable C-terminal localization (as given in the original 485 work) or without raw expression outcomes were not included in further analyses. 486

487 Similarly, Nir Fluman also provided spreadsheets of the raw data from the set of three expression
 488 trials performed in ²⁶.

489 New York Consortium on Membrane Protein Structure (NYCOMPS) Data - Brian Kloss, Marco 490 Punta, and Edda Kloppman provided a dataset of actions performed by the NYCOMPS center including 491 expression outcomes in various conditions^{2,3}. The protein sequences were mapped to NCBI GenInfo 492 Identifier (GI) numbers either via the Entrez system⁸⁸ or the Uniprot mapping service⁸⁹. Each GI 493 number was mapped to its nucleotide sequence via a combination of the NCBI Elink mapping service 494 and the "coded by" or "locus" tags of Coding Sequence (CDS) features within GenBank entries. 495 Though a custom script was created, a script from Peter Cock on the BioPython listserv to do the same 496 task via a similar mapping mechanism was found ⁹⁰. To confirm all the sequences, the TargetTrack ²³ 497 XML file was parsed for the internal NYCOMPS identifiers and compared for sequence identity to those 498

that had been mapped using the custom script; 20 (less than 1%) of the sequences had minor inconsistencies and were manually replaced.

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502 **Archaeal transporters Data** – The locus tags ("Gene Name" in Table 1) were mapped directly to the 503 sequences and retrieved from NCBI ⁴⁴. Pikyee Ma and Margarida Archer clarified questions regarding 504 their work to inform the analysis.

GPCR Expression Data – Nucleotide sequences were collected by mapping the protein identifiers given in Table 1 from ⁴⁷ to protein GIs via the Uniprot mapping service ⁸⁹ and subsequently to their nucleotide sequences via the custom mapping script described above (see NYCOMPS). The sequence length and pI were validated against those provided. Renaud Wagner assisted in providing the nucleotide sequences for genes whose listed identifiers were unable to be mapped and/or did not pass the validation criteria as the MeProtDB (the sponsor of the GPCR project) does not provide a public archive.

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514 *Helicobacter pylori* Data – Nucleotide sequences were retrieved by mapping the locus tags given in 515 Supplemental Table 1 from ⁴⁸ to locus tags in the Jan 31, 2014 release of the *H. pylori* 26695 genome 516 (AE000511.1). To verify sequence accuracy, sequences whose molecular weight matched that given by 517 the authors were accepted. Those that did not match, in addition to the one locus tag that could not be 518 mapped to the Jan 31, 2014 genome version, were retrieved from the Apr 9, 2015 release of the genome 519 (NC_000915.1). Both releases are derived from the original sequencing project ⁹¹. After this curation, all 520 mapped sequences matched the reported molecular weight.

In this data set, expression tests were performed in three expression vectors and scored as 1, 2, or 3. Two vectors were scored via two methods. For these two vectors, the two scores were averaged to give a single number for the condition making them comparable to the third vector while yielding 2 additional thresholds (1.5 and 2.5) result in the 5 total curves shown (Supplementary Fig. 2B).

Mycobacterium tuberculosis Data – The authors note using TubercuList through GenoList ⁹², therefore, nucleotide sequences were retrieved from the archival website based on the original sequencing project
 ⁹³. The sequences corresponding to the identifiers and outcomes in Table 1 from ⁴⁶ were validated against the provided molecular weight.

531 *Secondary Transporter* Data – GI Numbers given in Table 1 from ⁵⁰ were matched to their CDS entries 532 using the custom mapping script described above (see NYCOMPS). Only expression in *E. coli* with 533 IPTG-inducible vectors was considered.

535 **Thermotoga maratima Data** – Gene names given in Table 1 ⁹⁴ were matched to CDS entries in the Jan 536 31, 2014 release of the *Thermotoga maritima* MSB8 genome (AE000512.1), a revised annotation of the 537 original release ⁹⁵. The sequence length and molecular weight were validated against those provided.

Pseudomonas aeruginosa Data – Outcomes in Additional file 1 ⁴⁵ were matched to coding sequences
 provided by Constance Jeffrey.

541
 542 Shine-Dalgarno-like mutagenesis Data – Folded protein is quantified by densitometry measurement
 543 ^{96,97} of the relevant band in Figure 6 of ²⁶. Relative difference is calculated as is standard:

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 $\frac{\text{metric}_{\text{mutant}} - \text{metric}_{\text{wildtype}}}{\frac{1}{2} \left| \text{metric}_{\text{mutant}} - \text{metric}_{\text{wildtype}} \right|}$

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2. Details related to the calculation of sequence features 548

Transmembrane segment topology was predicted using Phobius Constrained for the training data 549 and Phobius for all other datasets ³⁹. We were able to obtain the Phobius code and integrate it directly 550 into our feature calculation pipeline resulting in significantly faster speeds than any other option. Several 551 features were obtained by averaging per-site metrics (e.g. per-residue RONN3.2 disorder predictions) in 552 windows of a specified length. Windowed tAI metrics are calculated over all 30 base windows (not 553 solely over 10 codon windows). Supplementary Table 1 includes an in-depth description of each feature. 554 Future work will explore contributions of elements outside the gene of interest, e.g. ribosomal binding 555 site, linkers, tags. 556

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558 **3.** Preparation for model learning

Calculated sequence features for the IMPs in the E. coli dataset as well as raw activity 559 measurements, *i.e.* each 96-well plate, were loaded into R. As is best practice in using Support Vector 560 Machines, each feature was "centered" and "scaled" where the mean value of a given feature was 561 subtracted from each data point and then divided by the standard deviation of that feature using 562 preprocess ⁹⁸. As is standard practice, the resulting set was then culled for those features of near 563 zero-variance, over 95% correlation (Pearson's r), and linear dependence (nearZeroVar, 564 findCorrelation, findLinearCombos)⁹⁸. In particular this procedure removed extraneous 565 degrees of freedom during the training process which carry little to no additional information with 566 respect to the feature space and which may over represent certain redundant features. Features and 567 outcomes for each list ("query") were written into the SVM^{light} format using a modified 568 svmlight.write 99. 569

The final features were calculated for each sequence in the test datasets, prepared for scoring by 570 "centering" and "scaling" by the training set parameters via preprocess ⁹⁸, and then written into 571 SVM^{light} format again using a modified svmlight.write. 572

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4. Model selection, training, and evaluation using SVM^{rank} 574

a. At the most basic level, our predictive model is a learned function that maps the parameter space 575 (consisting of nucleotide and protein sequence features) to a response variable (expression level) 576 through a set of governing weights ($w_1, w_2, ..., w_N$). Depending on how the response variable is defined, 577 these weights can be approximated using several different methods. As such, defining a response 578 variable that is reflective of the available training data is key to selecting an appropriate learning 579 algorithm. 580

The quantitative 96-well plate results ¹⁶ that comprise our training data do not offer an absolute 581 expression metric valid over all plates-the top expressing proteins in one plate would not necessarily 582 be the best expressing within another. As such, this problem is suited for preference-ranking methods. 583 As a ranking problem, the response variable is the ordinal rank for each protein derived from its 584 overexpression relative to the other members of the same plate of expression trials. In other words, the 585 aim is to rank highly expressed proteins (based on numerous trials) at higher scores than lower 586 expressed proteins by fitting against the order of expression outcomes from each constituent 96-well 587 plate. 588

b. As the first work of this kind, the aim was to employ the simplest framework necessary taking in 589 account the considerations above. The method chosen computes all valid pairwise classifications (*i.e.* 590 within a single plate) transforming the original ranking problem into a binary classification problem. 591 592 The algorithm outputs a score for each input by minimizing the number of swapped pairs thereby maximizing Kendall's τ^{100} . For example, consider the following data generated via context A 593 $(X_{A,1}, Y_{A,1}), (X_{A,2}, Y_{A,2})$ and B $(X_{B,1}, Y_{B,1}), (X_{B,2}, Y_{B,2})$ where observed response follows as index *i*, *i.e.* 594 $Y_n < Y_{n+1}$. Binary classifier $f(X_i, X_i)$ gives a score of 1 if an input pair matches its ordering criteria and 595 -1 if not, *i.e.* $Y_i < Y_j$: 596

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 $f(X_{A,1}, X_{A,2}) = 1; f(X_{A,2}, X_{A,1}) = -1$ $f(X_{B,1}, X_{B,2}) = 1; f(X_{B,2}, X_{B,1}) = -1$ $f(X_{A,1}, X_{B,2}), f(X_{A,2}, X_{B,1}) \text{ are invalid}$

Free parameters describing f are calculated such that those calculated orderings $f(X_{A,1}), f(X_{A,2}) \dots; f(X_{B,1}), f(X_{B,2}) \dots$ most closely agree (overall Kendall's τ) with the observed ordering Y_n, Y_{n+1}, \dots In this sense, f is a pairwise Learning to Rank method.

Within this class of models, a linear preference-ranking Support Vector Machine was employed 604 ¹⁰¹. To be clear, as an algorithm a preference-ranking SVM operates similarly to the canonical SVM 605 binary classifier. In the traditional binary classification problem, a linear SVM seeks the maximally 606 separating hyper-plane in the feature space between two classes, where class membership is determined 607 608 by which side of the hyper-plane points reside. For some n linear separable training examples D = $\{(x_i) | x_i \in \mathbb{R}^d\}^n$ and two classes $y_i \in \{-1, 1\}$, a linear SVM seeks a mapping from the *d*-dimensional 609 feature space $\mathbb{R}^d \to \{-1, 1\}$ by finding two maximally separated hyperplanes $w \cdot x - b = 1$ and $w \cdot x$ 610 x - b = -1 with constraints that $w \cdot x_i - b \ge 1$ for all x_i with $y_i \in \{1\}$ and $w \cdot x_i - b \le -1$ for all 611 x_i with $y_i \in \{-1\}$. The feature weights correspond to the vector w, which is the vector perpendicular to 612 the separating hyperplanes, and are computable in $O(n \log n)$ implemented as part of the SVM^{rank} software package, though in $O(n^2)^{41}$. See ¹⁰¹ for an in-depth, technical discussion. 613 614

c. In a soft-margin SVM where training data is not linearly separable, a tradeoff between misclassified inputs and separation from the hyperplane must be specified. This parameter *C* was found by training models against raw data from Daley, Rapp, *et al.* with a grid of candidate *C* values $(2^n \forall n \in [-5, 5])$ and then evaluated against the raw "folded protein" measurements from Fluman, *et al.* The final model was chosen by selecting that with the lowest error from the process above $(C = 2^5)$. To be clear, the final model is composed solely of a single weight for each feature; the tradeoff parameter *C* is only part of the training process.

Qualitatively, such a preference-ranking method constructs a model that ranks groups of proteins with higher expression level higher than other groups with lower expression value. In comparison to methods such as linear regression and binary classification, this approach is more robust and less affected by the inherent stochasticity of the training data.

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627 5. Quantitative Assessment of Predictive Performance

In generating a predictive model, one aims to enrich for positive outcomes while ensuring they do not come at the cost of increased false positive diagnoses. This is formalized in Receiver Operating Characteristic (ROC) theory (for a primer see 42), where the true positive rate is plotted against the false positive rate for all classification thresholds (score cutoffs in the ranked list). In this framework, the overall ability of the model to resolve positive from negative outcomes is evaluated by analyzing the Area Under a ROC curve (AUC) where AUC_{perfect}=100% and AUC_{random}=50% (percentage signs are 634 omitted throughout the text and figures). All ROCs are calculated through pROC ¹⁰² using the analytic 635 Delong method for AUC confidence intervals ¹⁰³. Bootstrapped AUC CIs ($N = 10^6$) were precise to 4 636 decimal places suggesting that analytic CIs are valid for the NYCOMPS dataset.

637 With several of our datasets, no definitive standard or clear-cut classification for positive 638 expression exists. However, the aim is to show and test all reasonable classification thresholds of 639 positive expression for each dataset in order to evaluate predictive performance as follows:

Training data – The outcomes are quantitative (activity level), so each ROC is calculated by normalizing within each dataset to the standard well subject to the discussion in 4a above (LepB for PhoA, and InvLepB for GFP) (examples in Fig. 1D) for each possible threshold, *i.e.* each normalized expression value with each AUC plotted in Fig. 1E. 95% confidence intervals of Spearman's ρ are given by 10⁶ iterations of a bias-corrected and accelerated (BCa) bootstrap of the data (Fig. 1A,C)¹⁰⁴.

Large-scale – ROCs were calculated for each of the expression classes (Fig. 2E). Regardless of the split, predictive performance is noted. The binwidth for the histogram was determined using the Freedman-Diaconis rule¹⁰⁵, and scores outside the plotted range comprising <0.6% of the density were implicitly hidden.

Small-scale – Classes can be defined in many different ways. To be principled about the matter, ROCs
 for each possible cutoff are presented based on definitions from each publication (Fig. 3C,E,G,
 Supplementary Fig. 2B,D,F). See Methods 1 for any necessary details about outcome classifications for
 each dataset.

654 **6. Feature Weights**

Weights for the learned SVM are pulled directly from the model file produced by SVM^{light} and are given in Supplementary Table 1.

658 8. Availability

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All analysis is documented in a series of R notebooks ¹⁰⁶ available openly at <u>github.com/clemlab/IMProve</u>. These notebooks provide fully executable instructions for the reproduction of the analyses and the generation of figures and statistics in this study. The IMProve model is available as a web service at <u>clemonslab.caltech.edu</u>. Additional code is available upon request.

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Figures and Tables



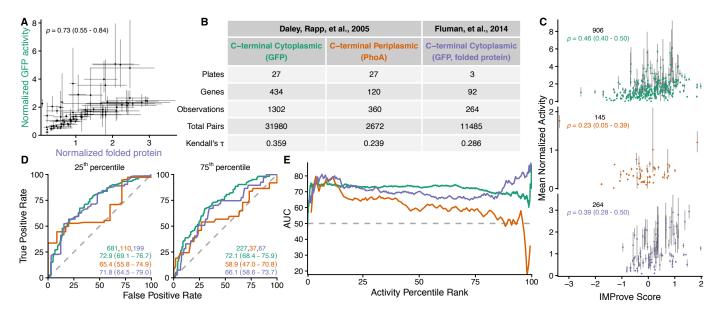
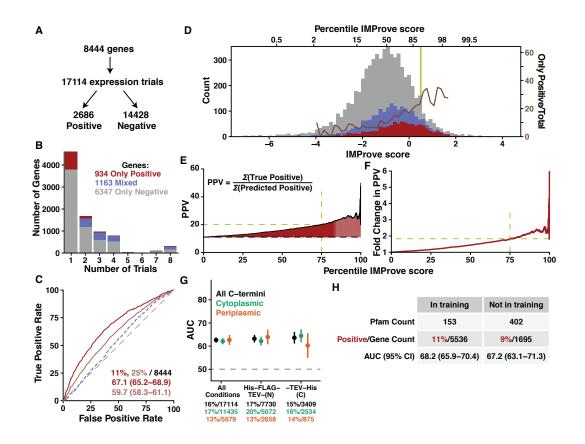


Fig. 1. Training performance. (A) A comparison of GFP activity ¹⁶ with measured folded protein ²⁶ 859 where each point represents the mean for a given gene tested in both works, and error bars plot the 860 extrema. Spearman's rank correlation coefficient and 95% confidence interval (CI)¹⁰⁴ are shown. (B) 861 862 Plates are the number of independent sets of measurements within which expression levels can be reliably compared. Genes are the number of proteins for which the C-terminus was reliably ascertained 863 ¹⁶. Observations are the total number of expression data points accessible. Total pairs are the number of 864 comparable expression measurements (*i.e.* those within a single plate). Kendall's τ is the metric 865 maximized by the training process (See Methods 4b). The color of the column heading identifying each 866 experimental set is retained throughout the figure. (C) Agreement against the normalized outcomes 867 plotted as the mean activity (see Methods 5 for definition) versus the score with error bars providing the 868 extent of observed activities (Spearman's p and 95% CI noted). (D) Illustrative Receiver Operating 869 Characteristics (ROC) for thresholds at 25th and 75th percentile in activity with the number of positive 870 outcomes at that threshold, the Area Under the Curve (AUC), and 95% CI indicated. (E) The AUC of 871 the ROC at every possible activity threshold. 872

Fig. 2



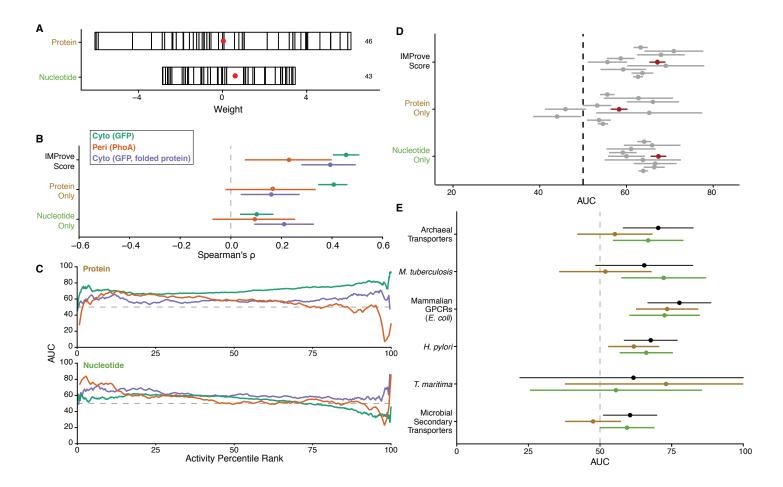
874 Fig. 2. Success of the model against outcomes from NYCOMPS. (A) An overview of the NYCOMPS 875 outcomes and **(B)** a histogram of the number of conditions tested per gene colored based on outcome. (C) Receiver Operating Characteristics for positive groupings given by Only Positive outcomes genes 876 877 (red) and genes with at least one positive outcome (pink). The percent positive for each group (corresponding color), total counts (black), and Area Under the Curve (AUC) values with 95% 878 Confidence Interval (CI) are shown. The ROC considering genes with Mixed outcomes only as positive 879 is shown as a blue dashed line with an AUC of 53.5 (51.8-55.2). The grey dashed line shows the 880 performance of a completely random predictor (AUC = 50). (D) Histograms of genes with Only Positive 881 (red) and Only Negative outcomes (grey) across IMProve scores (binned as described in Methods 5). 882 The percentage of Only Positive outcomes in each bin is overlaid as a brown line (right axis). (E) The 883 Positive Predictive Value (PPV) plotted for each percentile IMProve score, e.g. 75 on the x-axis 884 indicates the PPV for the top 25% of genes based on score for genes, where positive indicates genes 885 with Only Positive outcomes. The dashed line shows the overall success rate of the NYCOMPS 886 experimental outcomes (~11% Only Positive). (F) The fold change in the PPV as a function of IMProve 887 score relative to the success rate of NYCOMPS. (G) The AUCs for outcomes across all trials and within 888 the most-tested plasmids along with 95% CI. Performances are also split by predicted C-terminal 889 localization ³⁹. The numbers below indicate the total number of trials for each group and the percent 890 within that group that were positive. (H) The NYCOMPS dataset split by the presence or absence of a 891 Pfam family in the training set with AUCs calculated by considering Only Positive genes as positive 892 893 outcomes.

Fig. 3

Α Overall Top 50% Top 10% Proportion of Proportion of Fold Change AUC (95% CI) Positive Rate Positive Rate Fold Change Positive Rate Count all positives all positives NYCOMPS 8444 67.1 (65.2-68.9) 11.1 16.0 1.45 72.3 24.5 2.2 22.2 Mammalian GPCRs 92 77.7 (66.7–88.7) 19.6 34.8 1.78 88.9 40.0 2.0 22.2 238 (115)† 67.7 (58.4-77.0) 26.4 1.8 17.4 H. pylori 19.3 1.37 69.6 34.8 Archaeal Transporters 79 (14)† 67.7 (53.9-81.4) 30.4 45.7 1.50 66.7 33.3 1.1 16.7 109 13.0 1.57 77.8 9.1 1.1 11.1 M. tuberculosis 65.4 (48.5-82.4) 8.3 40.0 77 7.9 1.22 60.0 25.0 3.9 T. maritima 61.7 (22.0-100.0) 6.5 514 (87)[†] 61.2 (53.3-69.1) 12.1 14.4 1.19 61.3 24.1 2.0 21.0 P. aeruginosa Secondary Transporters 144 52.0 (39.9–64.2) 18.1 16.0 0.89 46.2 31.2 1.7 19.2 Mean: 65.1 1.37 67.8 2.0 21.2 в 6-Number of Trials 3-D Coomassie Blue Archaeal Transporters Western Blot 0-100. No Expression True Positive Rate 3-50 -1.0 С -3.0 -2.5 -2.0 -1.5 Percentage of Membrane Protein -0. 0. 0. 0.00 -0. 0.00 -0.00 40-. 39/79 Ŧ 67 C 50 100 Ó False Positive Rate Ŧ Ξ Ŧ -0 -3.0 -2.5 -2.0 -1.0 -1.5 IMProve score

895 Fig. 3. Success of the model against small scale outcomes. (A) Summary of the model's performance 896 against NYCOMPS and a variety of small scale expression experiments. Positive outcomes refer to those in the highest group as assigned by the authors of the respective studies. Where targets were tested 897 898 in more than one condition (e.g. different plasmids or strains), the number of distinct proteins are indicated in parenthesis with a dagger. (B) The expression of archaeal transporters in up to 6 trials ⁴⁴. 899 Positive expression count is plotted above the dashed line and negative outcomes below the line. (C) 900 Quantitative expression outcomes of those transporters as detected by Coomassie Blue. (D) Receiver 901 Operating Characteristics (ROC) along with Areas Under the Curves (AUC) and 95% confidence 902 interval as well as the total number of positives for the given threshold (red hues) along with the total 903 904 outcomes (black) are presented. In each curve, increasing expression thresholds are displayed as deeper 905 red.

Fig. 4



907 Fig. 4. Feature contributions to the model. (A) Classifying features by the type of sequence they are calculated from. (B) Considering the training set (as in Fig. 1), Spearman correlation coefficients with 908 95% confidence intervals using individual feature categories for each grouping of data within the 909 910 training set of E. coli IMPs. Colors indicate the subset being assessed (green, whole cell GFP fluorescence; orange, alkaline phosphatase activity; purple, folded protein by in-gel fluorescence). (C) 911 Protein/nucleotide feature dependence within the training set substantiated by the AUC of the ROC at 912 every possible activity threshold for feature subsets independently (as in Fig. 1E). (D) The AUC and 913 914 95% confidence intervals using only protein or nucleotide features. (E) Protein/nucleotide feature dependence across small scale datasets shown as AUCs of the ROC along with 95% CI for the condition 915 916 with the best overall predictive power (black).

Fig. 5

A 20 Genes, 20 Trials, 15% Positive Copper resistance AUC: 88.2 (73.0-100.0), protein D 8 TMs (PF05425) Short-chain 19 Genes, 19 Trials, 37% Positive AUC: 80.7 (67.2-94.3) fatty-acid transporter 10 TMs (PF02667) 35 genes, 76 Trials, 25% Positive AUC: 85.7 (67.9–100.0) Voltage dependent anion channel 10 TMs (PF03595) Na/H 190 genes, 398 Trials, 5% Positive Exchanger 10-12 TMs (PF00999) AUC: 76.1 (65.9-86.2) •• 10 348 BREASO Glycosyl-transferase 2 2 TMs (PF00535) 125 genes, 282 Trials, 22% Positive \$ • AUC: 75.8 (69.7– 81.9) 90 - 90 - 90 2005 - 90 - 93 :. \$ \$ 5 \mathbb{F}_{d} - 6 5 • ...• ana (ż -5 -4 -2 -1 ò -6 -3 ÷ IMProve score

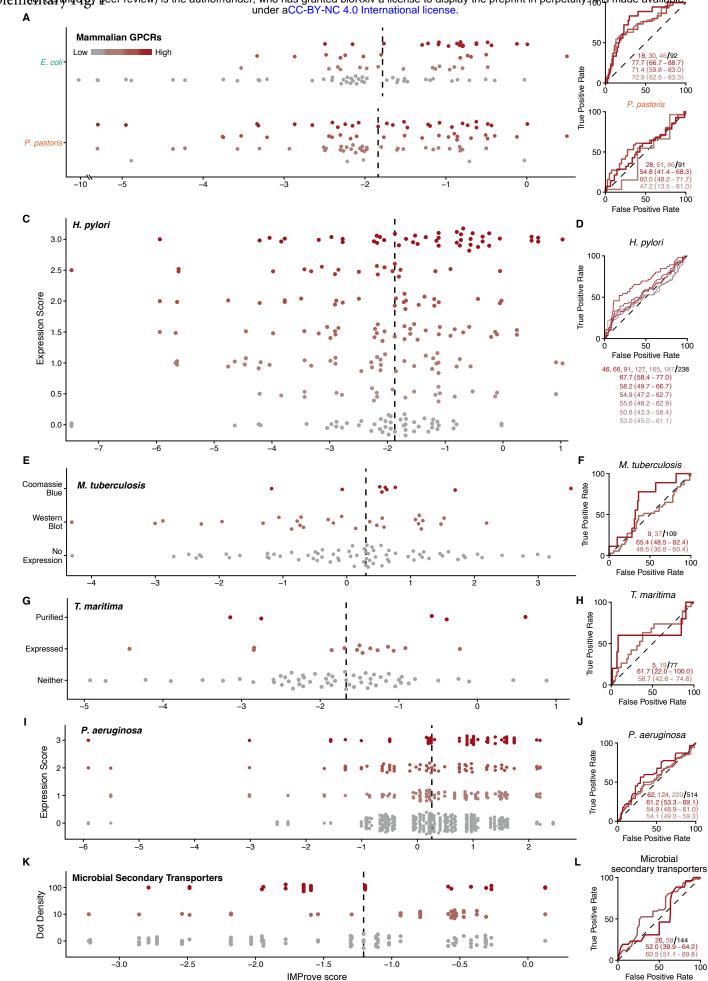
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							L L				
	Pfam	TMs	Number Genes/ Trials	Positive	AUC (95% CI)	Proportion of positives at 50%					
DUF962	PF06127	2	11	54.5	93.3 (77.9–100)	83.3					
DUF412	PF04217	2	12	41.7	88.6 (65.5–100)	100.0		Relative	Prediction		
DUF1282	PF06930	5	12	41.7	82.9 (57.2–100)	80.0		Expression Level	IMProve	SD Sites	
Sulfate exporter	PF03601	10	52	17.3	78.3 (64.3–92.3)	88.9					
Fluoride Channel	PF02537	4	81	24.7	77.0 (66.2–87.8)	80.0	BrnQ	0.30	0.35	0.18	
Acetyltrans- ferase 3	PF01757	10	19/23	26.1	76.5 (52.9–100)	83.3	YbjJ	-0.07	0.05	0.18	
PTS- EIIC	PF02378	8	82	18.3	76.2 (62.1–90.4)	80.0	YgdD	-0.26	-1	0.35	
Na ⁺ /P ⁻ cotransporter	PF02690	8	29/64	14.1	74.6 (54.4–94.9)	77.8					
ABC transp. Family 3	PF00950	7	31/33	21.2	72.5 (51.0–94.1)	71.4					
Biotin transporter	PF02632	5	47	31.9	70.8 (53.8-87.9)	66.7					

c

918 Fig. 5. Usage of the model within IMP families and for optimization of expression. (A) Outcomes 919 for specific protein families with an optimal IMProve score threshold indicated. Genes are shown in the chart as dots colored based on outcomes from trials: Only Positive (red), Only Negative (grey), and 920 921 Mixed (blue). Overall statistics, as in Supplementary Table 3, are noted. Dashed lines represent the optimal threshold from the ROC curves. For the top two rows, each was only tested in a single condition 922 (N: His-FLAG-TEV-gene). The bottom three rows are larger pools from NYCOMPS where there are 923 multiple trials for many of the genes. (B) A table curated from Supplementary Table 3 where Pfams 924 925 were selected based on specific criteria (minimum 10 trials, 4 positive and 4 negative outcomes) and ordered by AUC. Proteins, as in A, that have known crystal structures within the family are highlighted 926 in purple. DUFs are domains of unknown function. For context, the following Pfam families correspond 927 to TCDB classes: PF05425, <u>9.B.62</u>; PF02667, <u>2.A.73</u>; PF03595, 2.A.16; PF00999, 2.A.36, 2.A.37; 928 PF00535, 9.B.32; PF03601, 2.A.98; PF02537, 1.A.43; PF01757, 9.B.97; PF02378, 4.A.1, 4.A.2, 4.A.3; 929 PF02690, <u>2.A.58</u>; PF02632, <u>2.A.88</u>¹⁰⁷. (C) A comparison of the predictive capacity of IMProve 930 compared to using silent mutations engineered to increase anti-SD sequence binding propensity²⁶. The 931 table presents experimental relative expression level (mutant over wild-type sequence) versus 932 predictions from relative changes in either IMProve score or SD-like sites. The cells are colored as a 933 heat map from red (lower expression) to blue (higher expression). 934

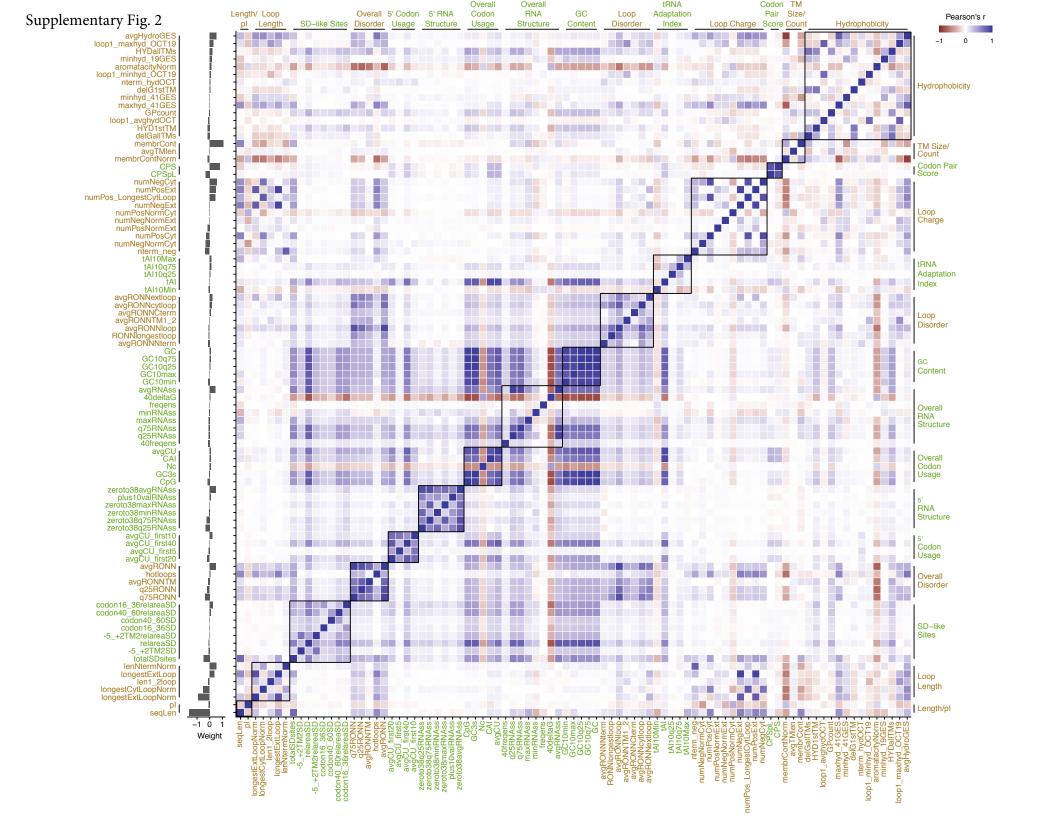
1 Supplementary Material



bioRxiv preprint doi: https://doi.org/10.1101/098673; this version posted November 6, 2017. The copyright holder for the preprint (which was Supplementational license to display the preprint in perpetuity the available under a CC-BY-NC 4.0 International license.

3 Supplementary Fig. 1. Success of the model against a variety of small scale outcomes. For each set, 4 vertical lines indicate the median IMProve score. Receiver Operating Characteristics (ROC) along with Areas Under the Curves (AUC) and 95% confidence interval as well as the total number of positives for 5 the given threshold (red hues) along with the total outcomes (black) are presented. In each curve, 6 increasing expression thresholds as defined by the original publication are displayed as deeper red. The 7 8 Reciever Operating Characteristic (ROC) with each cutoff is plotted, where a higher cutoff is represented 9 by a deeper red, followed by the Area Under the Curves (directly below) in colors that correspond to the respective curve. (A,B) Mammalian GPCR expression in either E. coli (top) or P. pastoris (bottom). (C,D) 10 Experimental expression of 116 H. pylori membrane proteins in E. coli in at most 3 vectors (238 trials) 11 scored as either a 1, 2, or 3 from the outcome of a dot blot as well as Coomassie Staining of an SDS-12 PAGE gel for two of the vectors. To compare the three vectors with a single set of scores, the two scores 13 were averaged to give a single number for a condition making them comparable to the third vector while 14 vielding 2 additional thresholds (1.5 and 2.5) and the 6 total levels shown. (E.F) Experimental expression 15 of *M. tuberculosis* membrane proteins plotted based on outcomes. (G,H) Pooled outcomes from the 16 expression of 87 P. aeruginosa membrane proteins in E. coli across 3 plasmids and 2 strains scored on a 17 relative scale. (I,J) Expression of 77 T. maritima membrane proteins in E. coli noted as purified (5), not 18 purified but expressed (14), or neither. (K,L) Expression of 37 microbial secondary transporters in 4 19 IPTG-inducible vectors (144 trials) in E. coli quantified as 10 ng/mL (pink) or 100 ng/mL (red) via dot 20

21 blot.

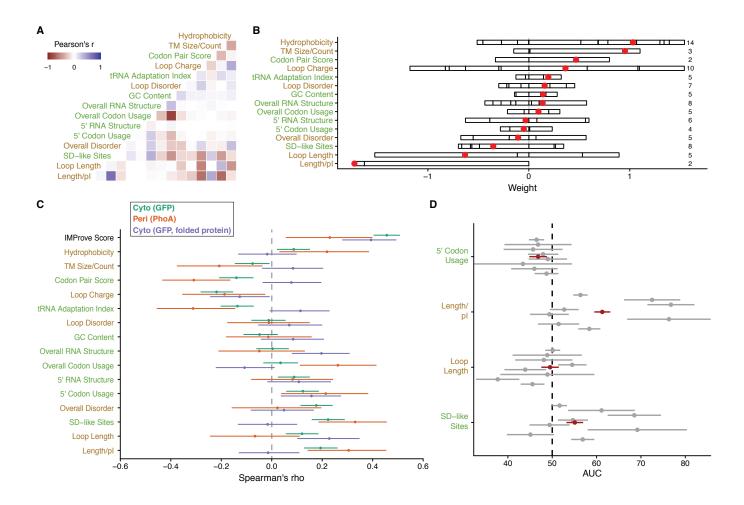


23 Supplementary Fig. 2. Complete set of feature correlations and their individual contributions to the

24 model. Features are ordered first by category and then by weight (grey bars). Labels are green for protein-

- 25 sequence derived and brown for nucleotide-sequence derived features. Pearson correlation coefficient
- 26 between each pair of features across the NYCOMPS dataset is plotted (right). See S1 Table for a detailed
- 27 description of each feature. Feature categories are overlaid as square boxes and indicated by black bars on
- the top, left, and right of the correlation matrix.

Supplementary Fig. 3



30 Supplementary Fig. 3. Feature contributions to the model across datasets used for training and 31 validation. (A) Pearson correlation coefficients between feature categories are shown. Feature labels are green for protein-sequence derived and brown for nucleotide-sequence derived. (B) Total weight for each 32 33 category is represented as a bar. The contribution of each feature to the category is shown by partitioning the bar. The red dot indicates the total sum of weights within the category. (C) Feature category 34 dependence within the training set is shown by Spearman's p and 95% CI between the normalized 35 outcomes versus the feature subset. (D) Considering the NYCOMPS data set (as in Fig 2), the Area Under 36 the Curve (AUC) of a Receiver Operating Characteristic and 95% confidence interval when predicting 37 solely by features from the specified category against the NYCOMPS dataset. Red, using positive only as 38 39 the cut-off for individual genes (Fig 2C); grey, using positive outcomes within each plasmid and solubilization condition (as in Fig 2E). 40

Supplementary Table 1

Туре	Category	Calculation Method/Tools	Abbreviation	Description	Used for Model	SVM Weight	Index by Weight
			CAI	Codon Adaptation Index	Т	0.10882621	25
		codonW 1.4.2	Nc	Effective number of codons	F	0.088591106	26
	Overall Codon usage	Codon W 1.4.2	GC3s	GC content at the synonymous position	Т	-0.04667477	51
			CpG	Frequency of CG di-nucleotides	Т	-0.16528028	72
		Biopython	avgCU	Average Codon Usage	Т	0.11009531	21
	Codon Pair Score	Code from Coleman, et al., 2008	CPS	Sum of Codon Pair Score values	Т	0.79854816	2
			CPSpL	Codon Pair Bias	Т	-0.33074614	77
			tAI	tRNA Adaptation Index	Т	-0.03330641	47
	tRNA adaptation index		tAI10Min	Minimum tAI score over 10 codon windows	Т	-0.09449133	58
		codonR	tAI10Max	Maximum tAI score over 10 codon windows	Т	0.14543056	19
			tAI10q25	25 th percentile of tAI scores over 10 codon windows	Т	0.057585392	29
			tAI10q75	75 th percentile of tAI scores over 10 codon windows	Т	0.11830714	19
			avgCU_first40	Codon Usage over the first 40 codons	Т	0.008758551	35
	5' Codon Usage	Biopython	avgCU_first20	Codon Usage over the first 20 codons	Т	-0.18854903	65
			avgCU_first5	Codon Usage over the first 5 codons	Т	-0.09333684	52
		_	avgCU_first10	Codon Usage over the first 10 codons	Т	0.22332223	14
			GC	Overall GC content	Т	0.11720225	18
			GC10min	Minimum %GC over 10 codon windows	Т	-0.12703171	56
	GC content	Custom	GC10q25	25 th percentile of %GC over 10 codon windows	Т	0.052650452	25
			GC10q75	75 th percentile of %GC over 10 codon windows	Т	0.11153498	18
			GC10max	Maximum %GC over 10 codon windows	Т	-0.01430641	34
Nucleotide	5' RNA Structure	RNAfold 2.1.9	X40deltaG	ΔG of the lowest free energy structure for the first 40 codons	Т	0.075478621	22
			X40freqens	Frequency of the lowest free energy structure within the ensemble for the first 40 codons	Т	-0.12966549	51
			plus10valRNAss	Average hybridization probability centered around +10 base, <i>i.e.</i> average of +5 to +15 (Goodman, et al., 2013)	Т	0.080081761	21
			zeroto38avgRNAss	Average hybridization probability over 10 base windows from 0 to +38	Т	0.48096541	7
		NUPACK	zeroto38minRNAss	Minimum hybridization probability over 10 base windows from 0 to +38	Т	-0.0451249	34
			zeroto38q25RNAss	25 th percentile of hybridization probability over 10 base windows from 0 to +38	Т	-0.34232038	56
			zeroto38q75RNAss	75 th percentile of hybridization probability over 10 base windows from 0 to +38	Т	-0.24050736	53
			zeroto38maxRNAss	Maximum hybridization probability over 10 base windows from 0 to +38	Т	0.034986421	23
	Overall RNA structure	RNAfold 2.1.9	deltaG	ΔG of the lowest free energy structure	F	#N/A	#N/A
		NUPACK	freqens	Frequency of the lowest free energy structure within the ensemble	Т	0.027135454	27 7
			avgRNAss	Average hybridization probability over 10 base windows	T	0.46994936	
			minRNAss	Minimum hybridization probability over 10 base windows 25 th percentile of hybridization probability over 10 base windows	T	-0.0498676 -0.09537871	32 39
			q25RNAss q75RNAss	75 th percentile of hybridization probability over 10 base windows	т	-0.08084998	39
			q/JRNASS maxRNAss	Maximum hybridization probability over 10 base windows	Т	-0.07990561	36
			totalSDsites	Total number of Shine-Dalgarno (SD)-like sites	т	-0.48917305	51
	Shine-Dalgarno-like sites (Fluman, et al., 2014)		relareaSD	Average anti-SD - SD hybridization energy for the whole protein	Т	-0.07600968	33
			codon16 36SD	Total number of SD-like sites between codons 16 and 36	T	-0.01342936	27
			codon16 36relareaSD	Average anti-SD - SD hybridization energy between codons 16 and 36	T	0.25027758	10
			codon40 60SD	Total number of SD-like sites between codons 40 and 60	т	0.013446409	22
	(codon40_003D	Average anti-SD - SD hybridization energy between codons 40 and 60	T	0.082086273	17
			-5 +2TM2SD	Total number of SD-like sites lying in the region starting 5 residues before and ending 2 residues after the start of the 2^{nd} transmembrane domain	T	-0.08689712	31
			-5 +2TM2relareaSD	Average anti-SD - SD hybridization energy between 5 codons prior to and 2 codons after the start of the 2 nd TM segment	T	-0.03265401	26
		DisEMBL 1.4	hotloops	Number of "hot" loops, which are classified as "highly" dynamic based on C _n temperature, minus 1	T	0.071120471	17
	Overall Disorder	DISLIMBL 1.4	avgRONNTM	Average RONN score for TMs	Т	-0.12197997	27
			avgRONN	Average RONN score for the entire protein	т	0.49654859	6
			q25RONN	25 th percentile of RONN scores	Т	-0.19440715	37
			q25RONN q75RONN	75 th percentile of RONN scores	т	-0.35734981	40
				Average RONN score of loops	т	-0.0781056	26
		RONN 3.1	avgRONNloop avgRONNextloop	Average RONN score of extracellular loops	Т	0.20923467	10
	Loop Disorder	KONN J.I	avgRONNextloop	Average RONN score of extracellular loops Average RONN score of cytoplasmic loops	т	0.16293134	10
			avgRONNcyttoop	Average RONN score of cytoplasmic loops Average RONN score of the N-terminus, <i>i.e.</i> loop that precedes the first TM segment	F	-0.11986996	28
			avgRONNNterm	Average RONN score of the K-terminus, <i>i.e.</i> loop that precedes the first TM segment	F	0.082627214	28
			avgRONNCterm avgRONNTM1 2	Average RONN score for the loop between the first 2 TM segments	т	-0.02097784	13
			uvghONNINII_2	Average room score for the loop between the first 2 Twi segments	T	0.0209//04	19

			RONNlongestloop	Average RONN score for the longest loop	т	-0.07889783	22
			avgTMlen	Average length of TM segments	Т	0.012067568	16
	TM Size/Count	Phobius/Biopython	membrCont	Number of residues predicted to be part of a TM segment	Т	1.0901064	1
			membrContNorm	MembrCont / length of protein	Т	-0.1495994	23
			avgHydro GES	Average hydrophobicity (GES scale as in Daley, et al., 2005)	Т	0.51562566	2
			minhyd_19 GES	Minimum hydrophobicity over 19 residue windows	Т	0.16866946	7
			minhyd_41 GES	Minimum hydrophobicity over 41 residue windows	Т	0.004997028	12
			maxhyd_41 GES	Minimum hydrophobicity over 41 residue windows	Т	-0.00273499	12
		Custom	nterm_hyd OCT	Average hydrophobicity of the N-terminus	Т	0.052106239	9
		Custoin	loop1_avghyd OCT	Average hydrophobicity of the first loop (Octanol-water partitioning scale)	Т	-0.10978091	15
	Hydrophobicity		loop1_minhyd_OCT19	Minimum hydrophobicity of 19 residue windows	Т	0.094023138	8
	riyurophobicity		loop1_maxhyd_OCT19	Maximum hydrophobicity of 19 residue windows	Т	0.2844961	5
Protein			HYD1stTM	Hydrophobicity of the first TM segment	Т	-0.15915927	14
110000			HYDallTMs	Average hydrophobicity of all TM segments	Т	0.23088375	5
		T. Hessa, et al., 2007	delG1stTM	ΔG of insertion of the 1 st TM segment	Т	0.041452195	6
		1. messa, et al., 2007	delGallTMs	Average ΔG of insertion of all TM segments	Т	-0.18423484	13
		Biopython (ProtParam)	aromatacityNorm	Average aromaticity	Т	0.15027378	1
			GPcount	Total number of glycines and prolines in TMs / number of TMs	Т	-0.05606809	1
	Loop charge	Phobius/Custom	numPosCyt	Total (-) charges (R, K, H) on cytoplasmic loops	Т	-0.27489546	13
			numPosNormCyt	numPosCyt / the total cytoplasmic loop length	Т	-0.02318138	7
			numNegCyt	Total (+) charges (E, D) on cytoplasmic loops	Т	0.57904214	1
			numNegNormCyt	numNegCyt / the total cytoplasmic loop length	Т	-0.32880098	11
			numPosExt	Total (+) charges (R, K, H) on extracellular loops	Т	0.50109029	1
	Loop enange		numPosNormExt	numPosExt / divided by the total extracellular loop length	Т	-0.16209885	9
			numNegExt	Total (-) charges (E, D) on extracellular loops	Т	0.015456084	4
			numNegNormExt	numNegExt / the total extracellular loop length	Т	-0.03816556	4
			numPos_LongestCytLoop	Total (+) charges (R, K, H) on the longest cytoplasmic loop	Т	0.44503307	1
			nterm_neg	Total (-) charges (E, D) on the N-terminus	Т	-0.35054731	6
			len1_2loop	Length of the loop between the first two TM segments (Fluman, et al., 2014)	Т	-0.11428721	5
			longestCytLoopNorm	Length of the longest cytoplasmic loop divided by the length of the protein	Т	-0.50917369	5
	Loop length		longestExtLoop	Length of the longest extracellular loop	Т	0.36319321	1
	Loop engin		longestExtLoopNorm	Length of the longest extracellular loop divided by the length of the protein	Т	-0.90276045	4
			lenNterm	Length of N-terminus	F	#N/A	#N/A
			lenNtermNorm	LenNterm / length of protein	Т	0.53105849	2
			seqLen	Protein length, <i>i.e.</i> number of residues	T	-1.62956 #N/A	4
	Length/pI	Biopython (ProtParam)	weight				#N/A
			pI	Isoelectric point	Т	-0.09808014	3

- 43 Supplementary Table 1. Sequence parameter weights and descriptions. Weights are presented after
- normalizing to the mean value for clarity. Features that were calculated but removed in pre-processing are
 noted (Methods 3).

Supplementary Table 2

	Solubilization	NYCOMPS Abbreviation	All					C-terminal Cytoplasmic (Predicted) C-terminal Periplasmic (Predicted)				
Gene Structure	Detergent		Count	Positive Count	AUC	Lower bound 95% CI	Upper bound 95% CI	Count	Positive Count	AUC	Lower bound 95% CI	Upper bound 95% CI
	Gene Outcomes			934	67.1	65.2	68.9	5680	693	66.3	64.2	68.5
	(Only positive)		8444		0,1,1	00.2	00.5	2764	241	67.6	64.0	71.2
	Gene Outcomes		0	2097	59.7	58.3 61.1	61 1	5680	1528	58.9	57.3	60.6
	(At least 1 positive)							2764	569	59.9	57.3	62.6
	All Expression Trials		17114	2686	62.6	61.5	63.8	11435	1966	62.1	60.8	63.5
	The Expression Thus			2000	02.0	02.0		5679	720	62.7	60.5	64.8
His-FLAG-TEV-	DDM	Ν	7730	1344	63.2	61.6	64.8	5072	991	62.2	60.2	64.1
								2658	353	63.9	60.8	67.1
-TEV-His	DDM	С	3409	524	63.6	61.1	66.1	2534	405	64.5	61.6	67.3
		-	0.000					875	119	60.3	54.9	65.6
-TEV-His	LDAO	C LDAO	763	128	59.2	54.0	64.4	532	99	58.7	52.5	64.8
112 (1115	LDIIO	e_bbrio	100	120	33.2	01.0	04.4	231	29	59.3	49.3	69.3
His-GST-TEV-	DDM	MSGC.24	383	31	69.0	60.1	77.8	226	21	67.2	55.3	79.0
1115 651 121	bbm	11566.21		<u></u>	09.0	00.1	,,,,,	157	10	72.2	59.8	84.6
-TEV-His	DDM	MSGC.28	1810	178	55.6	51.1	60.1	1117	129	55.4	50.0	60.8
-12 -1113	DDW	M6GC.20	1010	1/0	55.0	J1.1	00.1	693	49 54.0 4	45.5	62.5	
His-TEV-	DDM	MSGC.7	2125	316	58.6	55.4	61.8	1381	216	58.5	54.6	62.3
1115-112 V -	DDW	mbde./	2123	510	50.0	55.4	01.0	744	100	58.6	52.9	64.2
His-MBP-TEV-	DDM	MSGC.9	511	93	67.9	62.4	73.4	347	61	64.4	57.5	71.3
1113-141DI = I E V =	DDW	MISGC.9	511	55	07.9	02.4	/3.4	164	32	74.9	66.4	83.3
His-MBP-TEV-	LDAO	MSGC.9 LDAO	383	72	70.8	64.0	77.6	226	44	65.2	55.9	74.4
1115-WIDF-1EV-	LDAO	MISOC.7_LDAU	202	12	/0.0	04.0	//.0	157	28	79.1	69.8	88.4

47 Supplementary Table 2. AUC values for the NYCOMPS dataset. AUC values and 95% confidence 48 intervals are presented in summary, by expression condition, and by predicted C-terminal localization as 49 well as for IMProve scores calculated without the most computationally expensive RNA secondary 50 structure calculation.

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- 51 Supplementary Table 3. Predictive performances of the model across protein families. The proteins
- and performances are with respect to those tested by NYCOMPS as summarized in Fig 2. This data is available in an interactive format at clemonslab.caltech.edu.