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WHEN DOES HIGH-DOSE ANTIMICROBIAL CHEMOTHERAPY PREVENT THE EVOLUTION OF RESISTANCE?

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¹ **Abstract:** High-dose chemotherapy has long been advocated as a means of controlling

drug resistance in infectious diseases but recent empirical and theoretical studies have

begun to challenge this view. We show how high-dose chemotherapy engenders opposing

evolutionary processes involving the mutational input of resistant strains and their release

from ecological competition. Whether such therapy provides the best approach for

6 controlling resistance therefore depends on the relative strengths of these processes. These

7 opposing processes lead to a unimodal relationship between drug pressure and resistance

8 emergence. As a result, the optimal drug dose always lies at either end of the therapeutic

window of clinically acceptable concentrations. We illustrate our findings with a simple

model that shows how a seemingly minor change in parameter values can alter the outcome

11 from one where high-dose chemotherapy is optimal to one where using the smallest

clinically effective dose is best. A review of the available empirical evidence provides broad

support for these general conclusions. Our analysis opens up treatment options not

currently considered as resistance management strategies, and greatly simplifies the

experiments required to determine the drug doses which best retard resistance emergence

in patients.

¹⁷ Significance Statement: The evolution of antimicrobial resistant pathogens threatens

much of modern medicine. For over one hundred years, the advice has been to 'hit hard', in

the belief that high doses of antimicrobials best contain resistance evolution. We argue

that nothing in evolutionary theory supports this as a good rule of thumb in the situations

that challenge medicine. We show instead that the only generality is to either use the

22 highest tolerable drug dose or the lowest clinically effective dose; that is, one of the two

edges of the therapeutic window. This approach suggests treatment options not currently

considered, and greatly simplifies the experiments required to identify the dose that best

²⁵ retards resistance evolution.

- Antimicrobial resistance is one of greatest challenges faced by modern medicine. There is a
- ²⁷ widely held view that the evolutionary emergence of drug resistance is best slowed by using
- 28 high doses of drugs to eliminate pathogens as early and quickly as possible. This view, first
- expounded by Ehrlich (1) ('hit hard') and later Fleming (2) ('if you use penicillin, use
- enough'), is today encapsulated in the advice to administer 'the highest tolerated antibiotic
- dose' (3, 4). The rationale is two-fold. First, a high concentration of drug will eliminate
- drug-sensitive microbes quickly and thereby limit the appearance of resistant strains.
- Second, a high concentration of drug will also eliminate strains that have some partial
- resistance, provided the concentration is above the so-called mutant prevention
- concentration (MPC) (5–12).
- This is an intuitively appealing idea, but several authors have recently questioned whether
- 37 high-dose chemotherapy is, as a generality, defensible in terms of evolutionary theory
- 38 (13–16). This is because the use of extreme chemical force comes at the cost of maximizing
- the selective advantage of the very pathogens that we fear most; namely, those which
- 40 cannot be eradicated by safely administered doses of drug. Some experimental studies have
- 41 also shown that lighter-touch chemotherapy not only better prevents the emergence of
- resistance but it restores host health just as well as high-dose chemotherapy (15–17).
- Here we examine when high-dose chemotherapy is the best strategy and when it is not, by
- developing a general mathematical model for resistance emergence within a treated patient
- using principles from evolutionary biology. The analysis shows that high-dose
- chemotherapy gives rise to opposing evolutionary processes. As a result, the optimal
- 47 therapy for controlling resistance depends on the relative strengths of these processes.
- 48 High-dose therapy can, in some circumstances, retard resistance emergence but
- 49 evolutionary theory provides no support for using this strategy as a general rule of thumb,
- 50 nor does it provide support for focussing on the MPC as a general approach for resistance
- prevention. More broadly we find that the opposing evolutionary processes lead to a

- 52 unimodal relationship between drug concentration and resistance emergence. Therefore the
- optimal strategy is to use either the largest tolerable dose or the smallest clinically effective
- dose. We illustrate these general points with a simple model that shows how a seemingly
- minor change in parameter values can alter the outcome from one where high-dose
- 56 chemotherapy is optimal to one where using the smallest clinically effective dose is best. A
- 57 review of the empirical evidence provides broad support for these conclusions.

A Theoretical Framework for Resistance Evolution

- Determining a patient treatment regimen involves choosing an antimicrobial drug (or
- odrugs) and determining the frequency, timing, and duration of administration. The impact
- of each of these on resistance emergence has been discussed elsewhere (e.g., 9, 18). Here we
- focus solely on drug concentration because it has historically been the factor most often
- discussed, and because it is the source of recent controversy (e.g., 10, 12–14, 16). We seek
- to understand how the probability of resistance emergence changes as a function of drug
- 65 concentration.
- 66 For simplicity we assume that drug concentration is maintained at a constant level during
- 67 treatment and refer to this concentration as 'dose'. This assumption is not meant to be
- 68 realistic but it serves as a useful tool for gaining a better understanding of how drug
- 69 resistance evolves. After laying the groundwork for this simple case we show in the
- 70 Appendix that allowing for more realistic pharmacokinetics does not alter our qualitative
- 71 conclusions.
- 72 Drug resistance is a matter of degree, with different genotypes having different levels of
- resistance (measured, for example, as the minimum inhibitory concentration, MIC). Our
- main focus is on what we call high-level resistance (HLR). This will be defined precisely
- below but for the moment it can be thought of as resistance that is high enough to render

- the drug ineffective (so that its use is abandoned). We begin by supposing that the HLR strain is one mutational step away from the wild type but we relax this assumption in the Appendix.
- Why is it that resistant strains reach appreciable densities in infected patients only once
 drug treatment is employed? The prevailing view is that there is a cost of resistance in the
 absence of the drug, but that this cost is compensated for by resistance in the presence of
 the drug. It is not the presence of the drug per se that provides this compensation; rather,
 it is the removal of the wild type by the drug that does so (13, 19). This implies that the
 presence of the wild type competitively suppresses the resistant strain, and that drugs
 result in the spread of such strains because they remove this competitive suppression (a
 process called 'competitive release'; 19).
- To formalize these ideas, consider an infection in the absence of treatment. The wild type pathogen enters the host and begins to replicate. As it does so, it consumes resources and stimulates an immune response. We use P(t) to denote the density of the wild type and X(t) to denote a vector of within-host state variables (e.g., density of immune system components, resources, etc). Without loss of generality we suppose that the vector X is defined in such a way that pathogen replication causes its components to decrease. This decrease in X, in turn, makes the within-host environment less favorable for pathogen replication. If X is suppressed enough, the net replication rate of the wild type will reach zero. Thus X can be viewed as the quality of the within-host environment from the standpoint of pathogen replication.
- As the wild type replicates it gives rise to the HLR strain through mutation and the initial infection might include some HLR pathogens as well. But the HLR strain is assumed to bear some metabolic or replicative cost, meaning that it is unable to increase in density once the wild type has become established. Mechanistically this is because the wild type suppresses the host state, X, below the minimum value required for a net positive

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replication by the HLR strain (19). Thus, we ignore the effect of the HLR strain when
   modeling the joint dynamics of P(t) and X(t) in the absence of treatment (see Appendix A
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   for details).
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    At some point (e.g., the onset of symptoms) drug treatment is introduced. Provided the
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    dosage is high enough the wild type will be driven to extinction. We use c to denote the
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    (constant) concentration of the drug in the patient. We distinguish between theoretically
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    possible versus feasible doses. Theoretically possible doses are those that can be applied in
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    vitro. Feasible doses are those that can, in practice, be used in vivo. There will be a
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   smallest clinically effective dose that places a lower bound on the feasible values of c
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    (denoted c_L) and a maximum tolerable dose because of toxicity (denoted c_U). The dose
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   range between these bounds is called the therapeutic window (20).
    Once treatment has begun, we use p(t;c) and x(t;c) to denote the density of the wild type
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   strain and the within-host state. This notation reflects the fact that different dosages (i.e.,
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   concentrations) will give rise to different trajectories of p and x during the remainder of the
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   infection. We model the dynamics of p and x deterministically during this phase.
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    As the wild type is driven to extinction it will continue to give rise to HLR microbes
   through mutation. The mutation rate is given by a function \lambda[p(t;c),c] that is increasing in
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   p and decreasing in c. We suppose that \lim_{c\to\infty} \lambda[p,c] = 0 because a high enough drug
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    concentration will completely suppress wild type replication and thus mutation. Any HLR
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   microbes that are present during treatment will no longer be destined to rarity because
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   they will be released from competitive suppression (19). We use \pi[x(t;c),c] to denote the
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   probability of escaping initial extinction when rare. The function \pi is increasing in x
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    because it is through this state that the HLR strain has been competitively suppressed
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   (19). And \pi is decreasing in c with \lim_{c\to\infty}\pi[x,c]=0 because a high enough dose will also
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   suppress even then HLR strain.
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We can now provide a precise definition of high-level resistance (HLR). Although $\lim_{c\to\infty}\pi[x,c]=0$, the concentration at which this limit is reached can lie outside the therapeutic window $[c_L,c_U]$. We define HLR to mean that $\pi[x,c]$ is very nearly equal to $\pi[x,0]$ over the therapeutic window. Biologically this means that, in terms of clinically acceptable doses, significant suppression of HLR is not possible. We focus on HLR because, for genotypes that do not satisfy this property, there is then no resistance problem to begin (since one can always use a high enough dose to remove all pathogens).

With the above formalism, we focus on resistance emergence, defined as the replication of resistant microbes to a high enough density within a patient to cause symptoms and/or to be transmitted (19). In the analytical part of our results this is equivalent to the resistant strain not being lost by chance while rare.

The probability of resistance emergence is approximately equal to $1 - e^{-H(c)}$ where

$$H(c) = D(c) + S(c) \tag{1}$$

139 and

$$D(c) = \int_0^a \lambda[p(s;c),c] \ \pi[x(s;c),c] \mathrm{d}s$$
 (2)

$$S(c) = -n \ln (1 - \pi[x(0;c),c])$$
(3)

(see Appendix A). We refer to H(c) as the resistance 'hazard', and a is the duration of treatment with s=0 corresponding to the start of treatment. The quantity D(c) is the denovo hazard - it is the hazard due to resistant strains that appear de novo during treatment. It is comprised of the integral of the product of $\lambda[p(s;c),c]$, the rate at which resistant mutants appear at time s after the start of treatment, and $\pi[x(s;c),c]$, the probability of escape of any such mutant. The quantity S(c) is the standing hazard - it is the hazard due to a standing population of n resistant microbes that are already present at the beginning of treatment (see Appendix A). To minimize the probability of resistance emergence we therefore want to minimize the hazard H(c), subject to the constraint that the dosage c falls within the therapeutic window $[c_L, c_U]$.

150 Results

To determine how high-dose chemotherapy affects the probability of resistance emergence we determine how H(c) changes as drug dosage c increases. Differentiating expression (1) with respect to c we obtain

$$\frac{dH}{dc} = \underbrace{\int_{0}^{a} \pi \left(\frac{\partial \lambda}{\partial p} \frac{\partial p}{\partial c} + \frac{\partial \lambda}{\partial c}\right) ds}_{\text{de novo hazard}} + \underbrace{\int_{0}^{a} \lambda \left(\nabla_{x} \pi \cdot x_{c} + \frac{\partial \pi}{\partial c}\right) ds}_{\text{replication}} + \underbrace{\frac{n}{1 - \pi} \left(\nabla_{x} \pi^{0} \cdot x_{c}^{0} + \frac{\partial \pi^{0}}{\partial c}\right)}_{\text{standing hazard}} \tag{4}$$

where $\pi^0 = \pi[x(0;c),c]$, $x^0 = x(0;c)$, and subscripts denote differentiation. Equation (4) is partitioned in two different ways to better illustrate the effect of increasing dose. The first is a partitioning of its effect on mutation and replication. The second is a partitioning of its effect on the de novo and standing hazards. We have also indicated the terms that represent competitive release in blue (as explained below).

The first term in equation (4) represents the change in $de\ novo$ mutation towards the HLR strain that results from an increase in dose. The term $(\partial \lambda/\partial p)(\partial p/\partial c)$ is the change in mutation rate, mediated through a change in wild type density; $\partial \lambda/\partial p$ specifies how mutation rate changes with an increase in the wild type density p (positive) while $\partial p/\partial c$ specifies how the wild type density changes with an increase in dose (typically negative for much of the duration of treatment). Thus the product, when integrated over the duration of treatment, is expected to be negative. The term $\partial \lambda/\partial c$ is the change in mutation rate

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that occurs directly as a result of an increased dose (e.g., the direct suppression of wild
    type replication, which suppresses mutation). This, is expected to be non-positive in the
167
    simplest cases and is usually taken as such by proponents of high-dose chemotherapy.
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    Therefore high-dose chemotherapy decreases the rate at which HLR mutations arise during
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    treatment. Note, however, that if the drug itself causes a higher mutation rate (e.g., 21),
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    then it is possible for an increased dose to increase the rate at which resistance appears.
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    The second term in equation (4) represents replication of HLR strains once they have
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   appeared de novo during the course of treatment. The term \nabla_x \pi \cdot x_c is the indirect
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    increase in escape probability, mediated through the effect of within-host state, x.
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    Specifically, x_c is a vector whose elements give the change in each state variable arising
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    from an increased dosage (through the removal of the wild type). These elements are
    typically expected to be positive for much of the duration of treatment because an increase
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    in dose causes an increased rebound of the within-host state through a heightened removal
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    of wild type microbes. The quantity \nabla_x \pi is the gradient of the escape probability with
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    respect to host state x, and its components are expected to be positive (higher state leads
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    to a greater probability of escape). The integral of the dot product \nabla_x \pi \cdot x_c is therefore the
181
    competitive release of the HLR strain in terms of de novo hazard (19). This will typically
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    be positive. The term \partial \pi/\partial c is the direct change in escape probability of de novo mutants
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    as a result of an increase in dosage (i.e., the extent to which the drug suppresses even the
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    HLR strain). This term is negative at all times during treatment but, by the definition of
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    HLR, this is small. Therefore, high-dose chemotherapy increases the replication of any HLR
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    mutants that arise de novo during treatment.
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    Finally, the third term in equation (4) represents the replication of any HLR strains that
    are already present at the start of treatment. The term \frac{n}{1-\pi} (\nabla_x \pi^0 \cdot x_c^0) is the indirect
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    effect of dose on standing hazard, where n is the number of resistant pathogens present at
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    the start of treatment. The quantity x_c^0 is again a vector whose elements give the change in
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state arising from increased dosage (through the removal of the wild type). The components of this are typically expected to be positive because an increase in dose causes 193 a rebound in the within-host state. $\nabla_x \pi^0$ is the gradient of the escape probability with 194 respect to state, and its components are expected to be positive (higher state leads to 195 greater probability of escape). The dot product of the two, $\nabla_x \pi \cdot x_c$, is therefore the 196 competitive release of the HLR strain in terms of standing hazard (19). This will typically 197 be positive. The term $\frac{n}{1-\pi}\frac{\partial \pi^0}{\partial c}$ is the direct change in escape probability of pre-existing 198 mutants as a result of an increase in dosage (i.e., the extent to which the drug suppresses 199 even these HLR mutants) and is negative. Again, however, by the definition of HLR, this 200 will be small and therefore high-dose chemotherapy increases the replication of any HLR 201 mutants that are present at the start of treatment. Appendix B shows that the same set of 202 qualitative factors arise if there are strains with intermediate resistance as well. 203

The above results provide a mathematical formalization of earlier verbal arguments 204 questioning the general wisdom of using high-dose chemotherapy as a means of controlling 205 resistance emergence (13, 16). Advocates of the conventional heavy dose strategy tend to 206 emphasize how high-dose chemotherapy can reduce mutational input and potentially even 207 suppress the replication of resistant strains (the black derivatives in equation 4). However, 208 high-dose chemotherapy leads to competitive release and thus greater replication of any 209 resistant strains that are present (the blue derivatives in equation 4). Equation (4) shows 210 that it is the relative balance among these opposing processes that determines whether 211 high-dose chemotherapy is the optimal approach. We will present a specific numerical 212 example shortly that illustrates these points, but first we draw two more general 213 conclusions from the theory. 214

215 (1) Intermediate doses yield the largest hazard and thus the greatest likelihood of resistance
216 emergence across all theoretically feasible doses

The opposing evolutionary processes explained above are the reason for this result (also see

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16). First note that the functions \lambda and \pi will typically be such that D(0) \approx 0. In other
   words, the HLR strain does not emerge de novo within infected individuals if they are not
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   receiving treatment. Mechanistically, this is because any resistant strains that appear tend
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   to be competitively suppressed by the wild type strain (19). Although, S(0) need not be
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   zero (see Appendix C, Figure C2), the rate of change of S(c) with respect to c (i.e., the
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    third term in equation 4) is positive at c = 0. Therefore the maximum hazard cannot occur
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   at c=0.
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   Second, for large enough doses we have \pi[x(s;c),c]\approx 0 for all s because such extreme
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    concentrations will prevent replication of even the HLR strain. This makes both the de
    novo hazard D(c) and the standing hazard S(c) zero. Furthermore, for large enough c we
227
   also have \lambda[p(s;c),c]\approx 0 for all s as well if HLR can arise only during wild type
   replication, because such extreme concentrations prevent all replication of the wild type.
229
    This is an additional factor making the de novo hazard D(c) decline to zero for large c.
230
   Therefore \lim_{c\to\infty} H(c) = 0 and so the maximum hazard cannot occur for large values of c
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   either (16). Thus, the maximum hazard must occur for an intermediate drug dosage.
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    Although this prediction is superficially similar to that of the mutant selection window
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   hypothesis (5–9), there are important differences between the two as will be elaborated
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    upon in the discussion.
235
    (2) The optimal dose is either the maximum tolerable dose or minimum clinically effective
236
    dose
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    We have seen that the maximum hazard occurs for an intermediate dose. Suppose, further,
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   that the hazard H(c) is a unimodal function of c (i.e., it has a single maximum). Several
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   specific mathematical models (Day unpubl. results) and a body of empirical work (see
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   Discussion) are consistent with that assumption. Then the drug dose which best reduces
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    the probability of resistance emergence is always at one of the two extremes of the
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   therapeutic window. This means that it is best to use either the smallest clinically effective
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dose or the largest tolerable dose depending on the situation, but never anything in between (Figure 1).

46 A Specific Example

- To illustrate the general theory we now consider an explicit model for the within-host dynamics of infection and resistance. We model an acute infection in which the pathogen elicits an immune response that can clear the infection. Treatment is nevertheless called for because, by reducing the pathogen load, it reduces morbidity and mortality (see Appendix C for details).
- We begin by considering a situation in which the maximum tolerable drug concentration c_U causes significant suppression of the resistant strain (Figure 2a). We stress however that if this were true then, by definition, the resistant strain is not really HLR and thus there really is no resistance problem to begin with. We include this extreme example as a benchmark against which comparisons can be made.
- Not surprisingly, under these conditions a large dose is most effective at preventing resistance (compare Figure 2b with 2c). This is a situation in which the conventional 'hit hard' strategy is best.
- Now suppose that the maximum tolerable drug concentration c_U is not sufficient to directly suppress the resistant strain (Figure 3a). In this case the only difference from Figure 2 is a change in the resistant strain's dose-response curve. Now there really is a potential resistance problem in the sense that, from a clinical standpoint, the drug is largely ineffective against the resistant strain.
- Under these conditions we see that a small dose is more effective at preventing resistance emergence than a large dose (compare Figure 3b with 3c). This is a situation in which the

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conventional or orthodox 'hit hard' strategy is not optimal.
   Equation (4) provides insight into these contrasting results. The only difference between
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    the models underlying Figures 2 and 3 is that \partial \pi/\partial c and \partial \pi^0/\partial c are both negative for
    Figure 2 whereas they are nearly zero for Figure 3 (that is, at tolerable doses, the drug has
    negligible effects on resistant mutants). As a result, the negative terms in equation (4)
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   outweigh the positive terms for Figure 2 whereas the opposite is true for Figure 3.
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    These results appear to contradict those of a recent study by Ankomah and Levin (12).
    Although their model is more complex than that used here, equation (4) and its extensions
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   in the appendices show that such additional complexity does not affect our qualitative
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   conclusions. Ankomah and Levin (12) defined resistance evolution in two different ways: (i)
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    the probability of emergence, and (ii) the time to clearance of infection. For the sake of
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    comparison, here we focus on the probability of emergence. Ankomah and Levin (12)
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    defined emergence as the appearance of a single resistant microbe. As such their emergence
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   is really a measure of the occurrence of resistance mutations rather than emergence per se.
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   In comparison, we consider emergence to have occurred only once the resistant strain
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   reaches clinically significant levels; namely, a density high enough to cause symptoms or to
   be transmitted. There are two process that must occur for de novo resistant strains to
   reach clinically relevant densities. First, the resistant strain must appear by mutation, and
   both our results (Figure 3d) and those of Ankomah and Levin (12) show that a high dose
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   better reduces the probability that resistance mutations occur (this can also be seen in
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   equation 4). Second, the resistant strain must replicate to clinically significant levels.
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    Ankomah and Levin (12) did not account for this effect and our results show that a high
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    concentration is worse for controlling the replication of resistant microbes qiven a resistant
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    strain has appeared (Figure 3d). This is because higher doses maximally reduce
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    competitive suppression. In Figure 3 the latter effect overwhelms the former, making
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   low-dose treatment better. In Figure 2 these opposing processes are also acting but in that
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case the drug's effect on controlling mutation outweighs its effect on increasing the replication of such mutants once they appear.

More generally, Figure 4 illustrates the relationship between drug concentration and the
maximum size of the resistant population during treatment, for the model underlying
Figure 3. In this example a high concentration tends to result in relatively few outbreaks of
the resistant strain but when they occur they are very large. Conversely, a low
concentration tends to result in a greater number of outbreaks of the resistant strain but
when they occur they are usually too small to be clinically significant.

One can also examine other metrics like duration of infection, total resistant strain load 301 during treatment, likelihood of resistant strain transmission, etc. but the above results are 302 sufficient to illustrate that no single, general, result emerges. Whether a high or low dose is 303 best for managing resistance will depend on the specific context (i.e., the parameter values) 304 as well as the metric used for quantifying resistance emergence. In Appendices C and D, 305 we consider cases where there is pre-existing resistance at the start of infection, strains 306 with intermediate resistance, and other measures of drug dosing and resistance emergence. 307 None of these factors alters the general finding that the optimal strategy depends on the 308 balance between competing evolutionary processes.

Discussion

Equation (4) clearly reveals how high-dose chemotherapy gives rise opposing evolutionary processes in the emergence of resistance. It shows how the balance between mutation and competition determines the optimal resistance management strategy (13, 19). Increasing the drug concentration reduces mutational inputs into the system but it also unavoidably reduces the ecological control of any HLR pathogens that are present. These opposing forces generate an evolutionary hazard curve that is unimodal. Consequently, the worst

approach is to treat with intermediate doses (Figure 1) as many authors have recognized (5–7, 9). The best approach is to administer either the largest tolerable dose or the smallest clinically effective dose (that is, the concentration at either end of the therapeutic window). Which of these is optimal depends on the relative positions of the hazard curve and the therapeutic window (Figure 1). Administering the highest tolerable dose can be a good strategy (Figure 1c,d) but it can also be less than optimal (Figure 1b) or even the worst thing to do (Figure 1a). Thus, nothing in evolutionary theory supports the contention that a 'hit-hard' strategy is a good rule of thumb for resistance management.

Empirical evidence

Our framework makes a number of empirical predictions that are consistent with existing data. First, the resistance hazard will be a unimodal function of drug concentration. This 327 is well-verified in numerous studies. In fact a unimodal relationship between resistance 328 emergence and drug concentration (often called an 'inverted-U' in the literature) is arguably the single-most robust finding in all of the empirical literature (e.g., 22-40). 330 Second, the position and shape of the hazard curve will vary widely among drugs and 331 microbes, depending on how drug dose affects mutation rates and the strength of 332 competition. Such wide variation is seen (e.g., 22, 23, 27, 28, 34, 37, 38, 41, 42), presumably 333 reflecting variation in the strength of the opposing processes highlighted by equation (4). 334 Third, the relationship found between drug concentration and resistance evolution in any 335 empirical study will depend on the range of concentrations explored. At the low end, 336 increasing dose should increase resistance evolution; at the high end, increasing dose should 337 decrease resistance evolution. Examples of both cases are readily seen, often even within the same study (e.g., 15, 22–40, 43–49). It is important to note that there are clear 339 examples for which low-dose treatments can better prevent resistance emergence than high

doses (15, 38, 41, 43–46, 48–50), despite an inherent focus in the literature on experimental exploration of high-dose chemotherapy. The theory presented here argues that uniformity is not expected and the bulk of the empirical literature is consistent with this prediction.

An important and influential codification of Ehrlich's 'hit hard' philosophy is the concept

Theory does not support using the MPC as a rule of thumb

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of the mutant selection window, and the idea that there exists a mutant prevention 346 concentration (MPC) that best prevents resistance evolution (7–9). The MPC is defined as 347 'the lowest antibiotic concentration that prevents replication of the least susceptible 348 single-step mutant' (see 8, p. S132). When drug concentrations are maintained above the 349 MPC, 'pathogens populations are forced to acquire two concurrent resistance mutations for 350 replication under antimicrobial therapy' (see 51, p. 731). Below the MPC lies the 'mutant 351 selection window', where single-step resistant mutants can replicate, thus increasing the 352 probability that microbes with two or more resistance mutations will appear. Considerable 353 effort has been put into estimating the MPC for a variety of drugs and microbes (4). 354 The relationship between these ideas and the theory presented here is best seen using the 355 extension of equation (4) that allows for strains with intermediate resistance. Appendix B 356 shows that, in this case, equation (4) remains unchanged except that its first term (the 357 mutational component) is extended to account for all of the ways in which the HLR strain 358 can arise by mutation through strains with intermediate resistance (see expression B-3 in 359 Appendix B). A focus on the MPC can therefore be viewed as a focus on trying to control 360 only the mutational component of resistance emergence. And as the theory embodied by 361 equation (4) shows, doing so ignores the other evolutionary process of competitive release 362 that is operating. The use of the MPC therefore cannot be supported by evolutionary 363 theory as a general rule of thumb for resistance management.

If evolutionary theory does not support the use of MPC as a general approach then why does this nevertheless appear to work in some cases (e.g., 33, 52)? The theory presented here provides some possible explanations. First, if HLR strains can appear only through mutation from strains with intermediate resistance, and if feasible dosing regimens can 368 effectively kill all first step mutants, then such an approach must necessarily work since it 369 reduces all mutational input to zero. But for most of the challenging situations in 370 medicine, achieving this is presumably not possible. For example, if the MPC is not 371 delivered to all pathogens in a population because of patient compliance, metabolic 372 variation, spatial heterogeneity in concentration, etc., then the mutational input will not be 373 zero. Also, if HLR strains can arise in ways that do not require mutating through strains 374 with intermediate resistance (e.g., through lateral gene transfer; 53) then again the 375 mutational input will not be zero. In either case, one must then necessarily account for 376 how the choice of dose affects the opposing evolutionary process of competitive release in 377 order to minimize the emergence of resistance. Figure C3 in Appendix C illustrates this 378 idea by presenting a numerical example in which the MPC is the worst choice of drug 379 concentration for controlling HLR. Second, the theory presented here suggests that the MPC can be the best way to contain 381 resistance if this concentration happens to be the upper bound of the therapeutic window 382 (although see Figure C3 of Appendix C for a counterexample). If, however, the MPC is less 383 than the upper bound then even better evolution-proofing should be possible at either end 384 of the therapeutic window. If the MPC is greater than the upper bound, as it is for 385 example with most individual TB drugs (54) and levofloxacin against S. aureus (27), the 386 MPC philosophy is that the drug should then be abandoned as monotherapy. But our 387 framework suggests that before doing so, it might be worthwhile considering the lower bound of the therapeutic window. Researchers have tended not to examine the impact of the smallest clinically effective dose on resistance evolution, perhaps because of an inherent tendency to focus on high-dose chemotherapy. It would be informative to compare the

effects of the MPC with concentrations from both ends of the therapeutic window on resistance emergence experimentally.

Theory does not support using the highest tolerable dose as a rule of thumb

The MPC has yet to be estimated for many drug-microbe combinations (4) and it can be difficult to do so, especially in a clinically-relevant setting (51, 53). Given the uncertainties 396 involved, and the need to make clinical decisions ahead of the relevant research, some 397 authors have suggested the working rule of thumb of administering the highest tolerable 398 dose (3, 4). Our analysis shows that evolutionary theory provides no reason to expect that 390 this approach is best. By reducing or eliminating the only force which retards the 400 emergence of any HLR strains that are present (i.e., competition), equation (4) makes clear 401 that a hit hard strategy can backfire, promoting the very resistance it is intended to 402 contain. 403

How to choose dose

If the relative positions of the HLR hazard curve and the therapeutic window are known,
rational (evidence-based) choice of dose is possible. If the therapeutic window includes
doses where the resistance hazard is zero, then those doses should be used. However, by
definition, such situations are incapable of generating the HLR which causes a drug to be
abandoned, and so these are not the situations that are most worrisome. If the hazard is
non-zero at both ends of the therapeutic window, the bound associated with the lowest
hazard should be used (Figure 1b, c). If nothing is known of the HLR hazard curve (as will
often be the case), then there is no need to estimate the whole function. Our analysis
suggests that the hazards need be estimated only at the bounds of the therapeutic window.
These bounds are typically well known because they are needed to guide clinical practice.

Estimating the resistance hazard experimentally can be done in vitro and in animal models
but we note that since the solution falls at one end of the therapeutic window, they can
also be done practically and ethically in patients. That will be an important arena for
testing, not least because an important possibility is that, as conditions change, the
optimal dose might change discontinuously from the lowest effective dose to the highest
tolerable dose or vice versa. There is considerable scope to use mathematical and animal
models to determine when that might be the case and to determine clinical predictors of
when switches should be made.

Managing resistance in non-targets

Our focus has been on the evolution of resistance in the pathogen population responsible
for disease. Looking forward, an important empirical challenge is to consider the impact of
drug dose on the broader microbiome. Resistance can also emerge in non-target
micro-organisms in response to the clinical use of antimicrobials (44). Resistance in those
populations can increase the likelihood of resistance in future pathogen populations, either
because of lateral gene transfer from commensals to pathogens, or when commensals
become opportunistic pathogens (9, 55). For instance, aggressive drug treatment targeted
at bacterial pneumonia in a rat model selected for resistance in gut fauna. Lower dose
treatment of the targeted lung bacteria was just as clinically effective and better managed
resistance emergence in the microbiota (50).

It is unclear just how important these off-target evolutionary pressures are for patient
health, but if they are quantitatively important, this raises the interesting and challenging
possibility that the real hazard curve should be that of the collective microbiome as a
whole, weighted by the relative risk of resistance evolution in the components of the
microbiome and the target pathogen. It will be challenging to determine that, but our
focus on either end of the therapeutic window at least reduces the parameter space in need

of exploration.

441 Coda

Our analysis suggests that resistance management is best achieved by using a drug concentration from one edge of the therapeutic window. In practice, patients are likely treated somewhat more aggressively than the minimum therapeutic dose (to ensure no patients fail treatment) and somewhat less aggressively than the maximum tolerable dose 445 (to ensure no patients suffer toxicity). This means that medical caution is always driving 446 resistance evolution faster than it need go, particularly when the maximum hazard lies within the therapeutic window (Figure 1b,c). From the resistance management perspective, 448 it is important to determine the level of caution that is clinically warranted rather than 449 simply perceived. 450 For many years, physicians have been reluctant to shorten antimicrobial courses, using long 451 courses on the grounds that it is better to be safe than sorry. It is now increasingly clear 452 from randomized trials that short courses do just as well in many cases (e.g., 56–58) and they can reduce the risk of resistance emergence (56, 59, 60). We suggest that analogous 454 experiments looking at the evolutionary outcomes of lowest clinically useful doses should be the next step. Such experiments in plants have already shown unambiguously that low 456 dose fungicide treatment best prevents the spread of resistant fungal pathogens (61). How 457 generally true this is for other pathogens, or pathogens of other hosts, remains to be seen. 458 We also note that our arguments about the evolutionary merits of considering the lowest 450 clinically useful doses have potential relevance in the evolution of resistance to cancer 460 chemotherapy as well (62). 461

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Figure Captions

Figure 1. Hypothetical plots of resistance hazard H(c) as a function of drug concentration c, with the lowest effect dose and the highest tolerable dose denoted by c_L and c_U respectively. The therapeutic window is shown in green. (a) and (b) drug concentration with the smallest hazard is the minimum effective dose. (c) and (d) drug concentration with the smallest hazard is the maximum tolerable dose.

Figure 2. An example in which the conventional strategy of high-dose chemotherapy best prevents the emergence of resistance. (a) The dose-response curves for the wild type in blue $(r(c) = 0.6(1 - \tanh(15(c - 0.3))))$ and the resistant strain in red $(r_m(c) = 0.59(1 - \tanh(15(c - 0.45))))$ as well as the therapeutic window in green. Red dots indicate the probability of resistance emergence. Probability of resistance emergence is defined as the fraction of 5000 simulations for which resistance reached a density of at least 100 (and thus caused disease).(b) and (c) wild type density (blue), resistant density (red), and immune molecule density (black) during infection for 1000 representative realizations of a stochastic implementation of the model. (b) treatment at the smallest effective dose c_L , (c) treatment at the maximum tolerable dose c_U . Parameter values are P(0) = 10, $P_m(0) = 0$, I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 10^{-2}$, and $\gamma = 0.01$.

Figure 3. An example in which the low-dose strategy best prevents the emergence of resistance. (a) The dose-response curves for the wild type in blue $(r(c) = 0.6(1 - \tanh(15(c - 0.3))))$ and the resistant strain in red $(r_m(c) = 0.59(1 - \tanh(15(c - 0.6))))$ as well as the therapeutic window in green. Red dots indicate the probability of resistance emergence. Probability of resistance emergence is defined as the fraction of 5000 simulations for which resistance reached a density of at least 100 (and thus caused disease).(b) and (c) wild type density (blue), resistant density (red), and immune molecule density (black) during infection for 1000 representative realizations of a stochastic implementation of the model. (b) treatment at the smallest effective dose c_L , (c) treatment at the maximum tolerable dose c_U . (d) The probability that a resistant strain appears by mutation is indicated by grey bars for low and high dose. The probability of resistance emergence is indicated by the height of the red bars for these cases. The probability of resistance emergence, given a resistant strain appeared by mutation, can be interpreted as the ratio of the red to grey bars. Parameter values are P(0) = 10, $P_m(0) = 0$, I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 10^{-2}$, and $\gamma = 0.01$.

Figure 4. Frequency distribution of resistant strain outbreak sizes for the simulation underlying Figure 3. Each distribution is based on 5000 realizations of a stochastic implementation of the model. (a) Low drug dose. (b) High drug dose. Insets show the same distribution on a different vertical scale.

Figure I

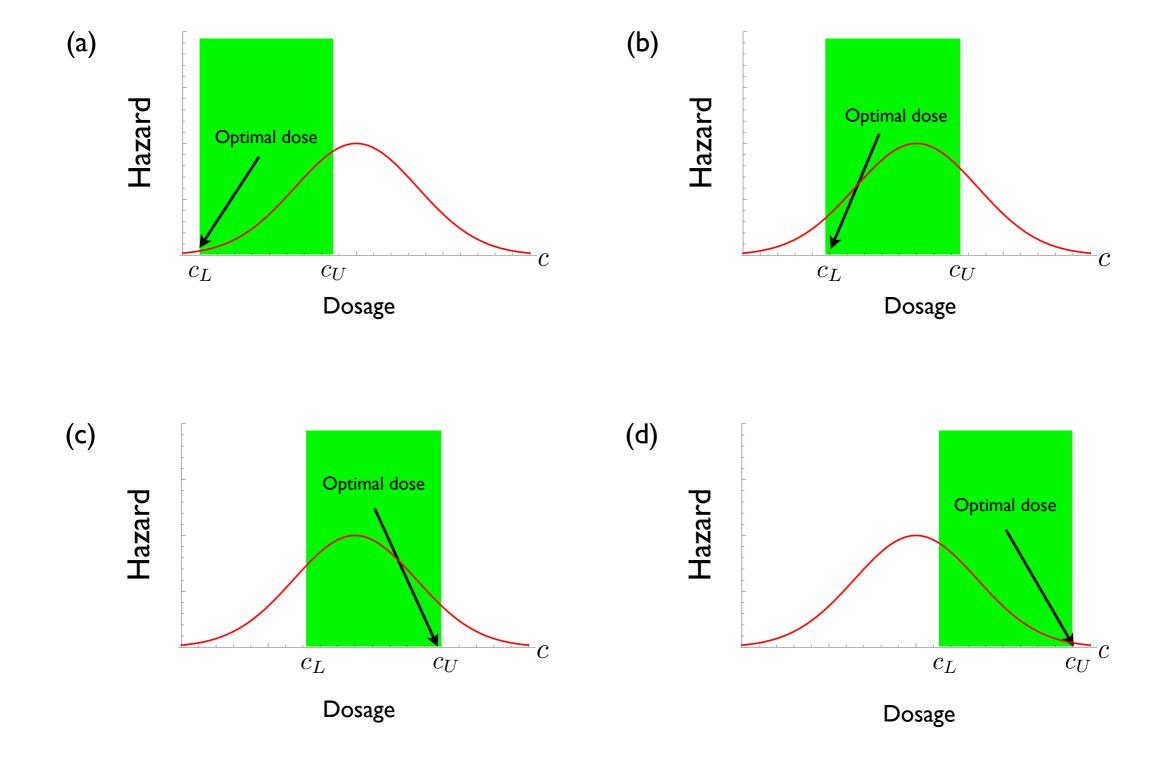


Figure 2

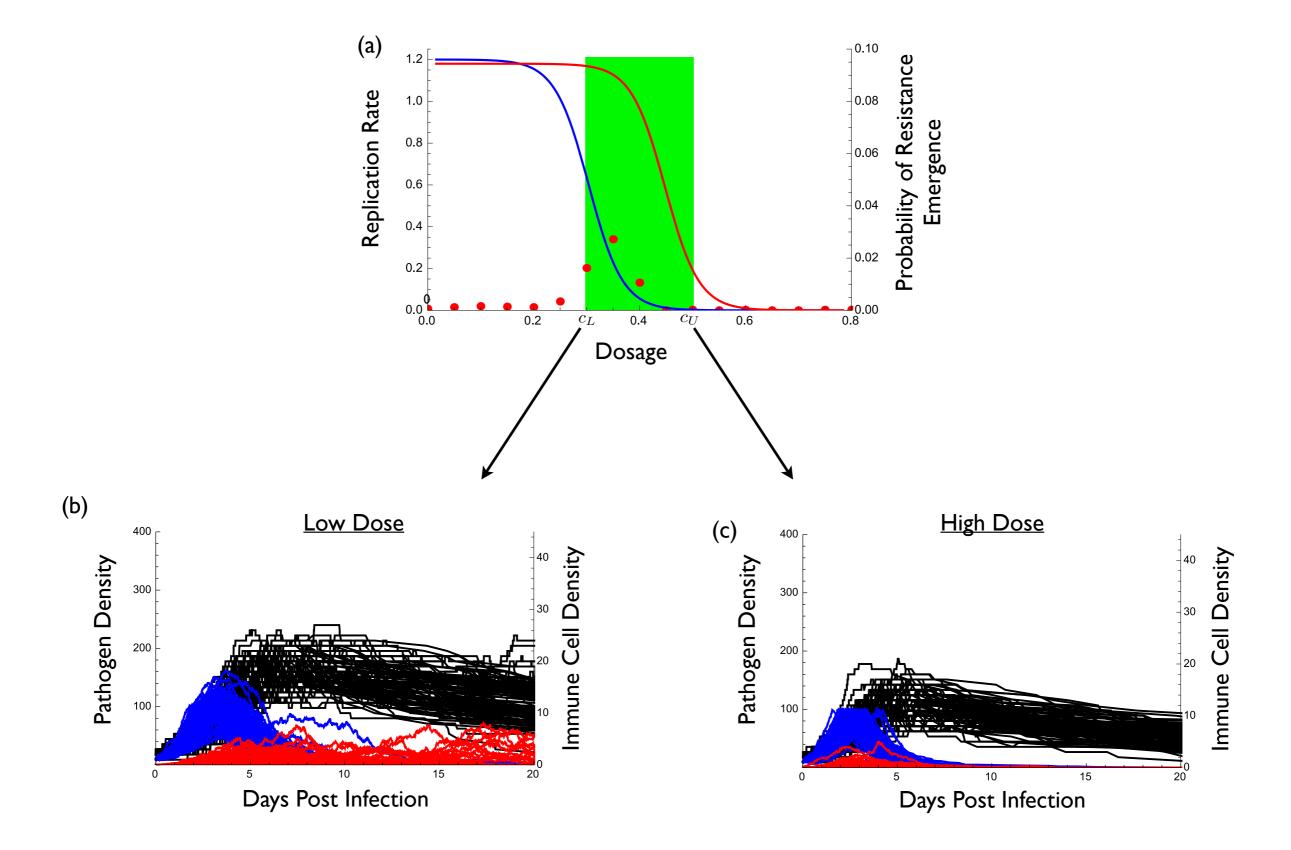


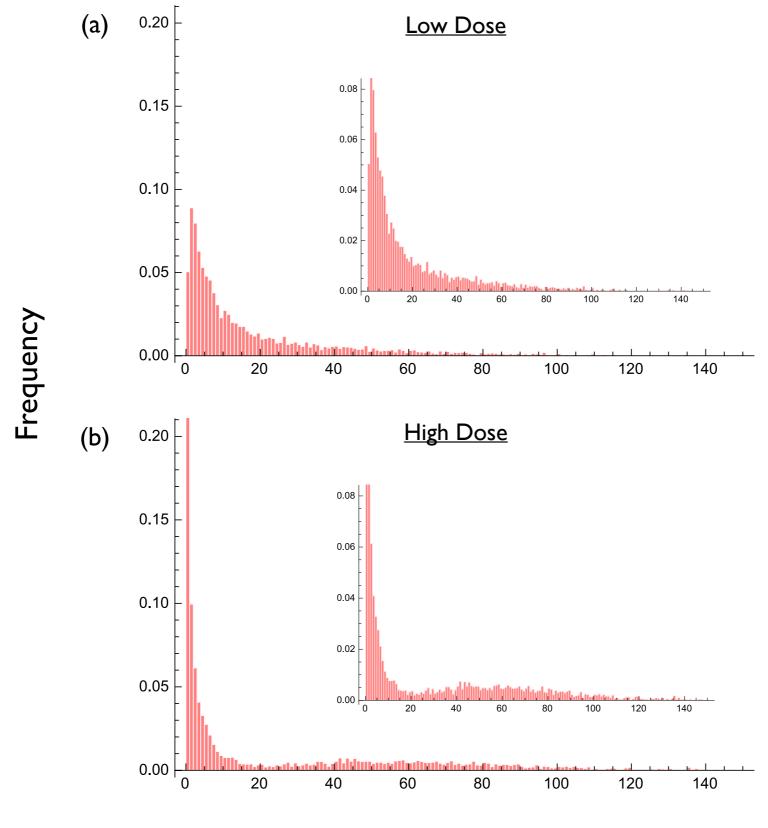
Figure 3 $_{\scriptsize \neg}$ 0.10 (a) 1.2 Probability of Resistance 0.08 1.0 Replication Rate Emergence 8.0 0.06 0.6 0.04 0.4 0.02 0.2 0.00 0.0 0.4 c_U 0.6 0.2 c_L Dosage (b) (c) 400 High Dose Low Dose Immune Cell Density Pathogen Density 300 300 200 200 100 20 Days Post Infection Days Post Infection 1.0 (d) **Probability**

0.2

Low

High

Figure 4



Resistant Strain Outbreak Size

APPENDICES A-E

When does high-dose antimicrobial chemotherapy prevent the evolution of resistance?

Day, T. and A.F. Read

June 1, 2015

Appendix A - Derivation of Equation 4

- In the absence of treatment we model the within-host dynamics using a system of
- 3 differential equations

$$\frac{dP}{dt} = F(P, X) \tag{A-1a}$$

$$\frac{dX}{dt} = G(P, X) \tag{A-1b}$$

- where P is the density of the wild type and X is a vector of variables describing the
- within-host state (e.g., RBC count, densities of different immune molecules, etc). The
- initial conditions are $P(0) = P_0 X(0) = X_0$. At some point, t^* , drug treatment is
- ⁷ introduced. Using lower case letters to denote the dynamics in the presence of treatment,
- 8 we then have

$$\frac{dp}{dt} = f(p, x; c) \tag{A-2a}$$

$$\frac{dx}{dt} = g(p, x; c) \tag{A-2b}$$

- with initial conditions $p(0;c) = P(t^*)$ and $x(0;c) = X(t^*)$, and where c is the dosage. For
- simplicity, here we assume that a constant drug concentration is maintained over the
- 11 course of the infection. Appendix E considers the pharmacokinetics of discrete drug dosing.
- The notation p(t;c) and x(t;c) reflects the fact that the dynamics of the wild type and the
- host state will depend on dosage. For example, if the dosage is very high p will be driven to
- 14 zero very quickly.

- As the drug removes the wild type pathogen, resistant mutations will continue to arise from the wild type population stochastically. For example, if mutations are produced only during replication of the wild type, then the rate of mutation will have the form $\mu r(c)p(t;c)$ 17 where μ is the mutation rate and r(c) is the replication rate of the wild type pathogen 18 (which depends on drug dosage c). With this form of mutation, if we could administer the 19 drug at concentrations above the MIC at the very onset of infection, then resistance evolution through de novo mutation would not occur. In reality symptoms and therefore 21 drug treatment typically do not occur until later in the infection, meaning that some 22 resistant strains might already be present at low frequency at the onset of treatment. 23 There are also other plausible forms for the mutation rate as well, and therefore we simply specify this rate by some general function $\lambda[p(t;c),c]$. Whenever a resistant strain appears it is subject to stochastic loss. We define π as the
- Whenever a resistant strain appears it is subject to stochastic loss. We define π as the probability of avoiding loss (which we refer to as 'escape'). To simplify the present analysis, we use a separation of timescales argument and assume that the fate of each mutant is determined quickly (essentially instantaneously) relative to the dynamics of the wild type and host state (we relax this assumption in all numerical examples). Thus, π for any mutant will depend on the host state at the time of its appearance, x(t;c), and it will therefore depend indirectly on c. Note that π will also depend directly on c, however, because drug dosage might directly suppress resistant strains as well if the dose is high enough. Therefore we use the notation $\pi[x(t;c),c]$, and assume that π is an increasing function of x and a decreasing function of c.
- With the above assumptions the host can be viewed as being in one of two possible states at any point in time during the infection: (i) resistance has emerged (i.e., a resistant strain has appeared and escaped), or (ii) resistance has not emerged. We model emergence as an inhomogeneous birth process, and define q(t) as the probability that resistance has emerged by time t. A conditioning argument gives

$$q(t + \Delta t) = q(t) + (1 - q(t))\lambda \Delta t \pi + o(\Delta t)$$
(A-3)

- where $\lambda \Delta t$ is the probability that a mutant arises in time Δt , and π is the probability that
- such a mutant escapes. Re-arranging and taking the limit $\Delta t \to 0$ we obtain

$$\frac{dq}{dt} = (1 - q(t))\lambda\pi\tag{A-4}$$

- with initial condition $q(0) = q_0$. Note that q_0 is the probability that emergence occurs as a
- result of resistant mutants being present at the start of treatment. Again employing a
- separation of timescales argument, if there are n mutant individuals present at this time,
- then $q_0 = 1 (1 \pi[x(0;c),c])^n$.
- The solution to the above differential equation is

$$q(t) = 1 - (1 - \pi[x(0; c), c])^n \exp\left(-\int_0^t \lambda \pi ds\right).$$
 (A-5)

- 48 If a is the time at which treatment is stopped, and Q is the probability of emergence
- occurring at some point during treatment, then Q = q(a). If we further define
- 50 $S = -n \ln (1 \pi[x(0; c), c])$ then we can write Q as

$$Q = 1 - \exp(-D - S) \tag{A-6}$$

- where $D = \int_0^a \lambda \pi ds$. We refer to D as the de novo hazard and S as the standing hazard. D
- 52 is the contribution to escape that is made up of mutant individuals that arise during the
- course of treatment. S is the contribution to escape that is made up of mutant individuals

- ⁵⁴ already presents at the start of treatment.
- Given the expression for Q, all else equal, resistance management would seek the treatment
- strategy, c that makes Q as small as possible. Since Q is a monotonic function of D+S,
- we can simplify matters by focusing on these hazards instead. Thus we define

$$H = \int_0^a \lambda \pi \mathrm{d}s + S \tag{A-7}$$

- which is the 'total hazard' during treatment. Equation (4) is then obtained by
- differentiating the total hazard H with respect to c.

60 Appendix B - Extensions involving intermediate

strains and horizontal gene transfer

- 62 The results of the main text (which are derived in Appendix A) are based on the
- assumption that a single mutational event can give rise to high-level resistance. In some
- 64 situations several mutational events might be required. These so-called 'stepping stone
- 65 mutations' towards high-level resistance might themselves confer an intermediate level of
- 66 resistance. One of the arguments in favour of aggressive chemotherapy has been to prevent
- 67 the persistence of these stepping stone strains, and thereby better prevent the emergence of
- 68 high-level resistance (1–8). Here we incorporate such stepping stone mutations into the
- 69 theory, again placing primarily attention on the emergence of high-level resistance.
- As in Appendix A, in the absence of treatment we model the within-host dynamics using a
- 71 system of differential equations

$$\frac{dP}{dt} = F(P, X) \tag{B-1a}$$

$$\frac{dX}{dt} = G(P, X) \tag{B-1b}$$

but now P is also a vector containing the density of the wild type and all potential intermediate mutants. All intermediate strains are assumed to bear some metabolic or replicative cost as well, meaning that they are unable to increase in density in the presence of the wild type. Mechanistically again this is because the wild type has suppressed the 75 host state, X, below the minimum value required for a net positive growth by any 76 intermediate strain. Thus, in the absence of treatment we expect most of these mutants to have negligible density. Once treatment is introduced we have

$$\frac{dp}{dt} = f(p, x; c) \tag{B-2a}$$

$$\frac{dp}{dt} = f(p, x; c)$$

$$\frac{dx}{dt} = g(p, x; c)$$
(B-2a)
(B-2b)

where again p is now a vector. As before we have initial conditions $p(0;c) = P(t^*)$ and $x(0;c)=X(t^*)$, and where c is the dosage. Now, however, different choices of c will generate different distributions of strain types p(t;c) during the infection. Furthermore, 81 each type will give rise to the high-level resistance strain with its own rate. Therefore, the function specifying the rate of mutation to the HLR strain $\lambda[p(t;c),c]$ is a function of the vector variable p(t;c).

The calculations in Appendix A can again be followed. We obtain an equation identical to equation (4) except that the first term is replaced by

$$\int_0^a \pi \left(\nabla_p \lambda \cdot p_c + \frac{\partial \lambda}{\partial c} \right) ds \tag{B-3}$$

where subscripts denote differentiation with respect to that variable. The difference is that $(\partial \lambda/\partial p)(\partial p/\partial c)$ in equation (4) is replaced with $\nabla_p \lambda \cdot p_c$. The quantity p_c is a vector whose components are the changes in the density of each intermediate strain arising from an increased dosage. The quantity $\nabla_p \lambda$ is the gradient of the mutation rate with respect to a change in the density of each intermediate strain. The integral of the dot product of the two, $\nabla_p \lambda \cdot p_c$, is therefore the overall change in mutation towards the HLR strain during treatment. Whereas the first term of equation (4) is expected to be negative, expression (B-3) can be negative or positive depending on how different doses affect the distribution of intermediate mutants during the infection (i.e., the elements of p_c) and the rate at which each type of intermediate mutant gives rise to the strain with high level resistance (i.e., the 96 elements of $\nabla_p \lambda$). Either way, however, this does not alter the salient conclusion that the optimal resistance management dose will depend on the details. 98

In an analogous fashion we might also alter the derivation in Appendix A to account for 99 the possibility that some microbes acquire high-level resistance via horizontal gene transfer 100 from other, potentially commensal, microbes. To do so we would simply need to alter the 101 way in which λ is modelled. In particular, it might then be a function of the densities of 102 commensal microbes as well, who themselves could be affected by drug dosage. Thus, once 103 treatment has begun, we might have a system of equations of the form

$$\frac{dp}{dt} = f(p, x, y; c) \tag{B-4a}$$

$$\frac{dp}{dt} = f(p, x, y; c)$$

$$\frac{dx}{dt} = g(p, x, y; c)$$
(B-4a)
(B-4b)

$$\frac{dy}{dt} = h(p, x, y; c) \tag{B-4c}$$

where y is a vector of commensal microbe densities. We might then model λ as $\lambda[p(t;c),y(t;c)]$. Again, calculations analogous to those of Appendix A can be followed to 106 obtain an appropriate expression for the resistance hazard. As with the above examples, 107 there will again be a tradeoff between components of this expression as a function of drug 108 dosage. 109

Appendix C - A Model of acute immune-mediated infections

The dynamics of the mutant and wild type in the absence of treatment are modeled as

$$\frac{dP}{dt} = [r(0)(1-\mu) - \gamma]P - \kappa PI \tag{C-1}$$

$$\frac{dP_m}{dt} = [r_m(0) - \gamma_m]P_m - \kappa P_m I + r(0)\mu P \tag{C-2}$$

$$\frac{dP}{dt} = [r(0)(1-\mu) - \gamma]P - \kappa PI \qquad (C-1)$$

$$\frac{dP_m}{dt} = [r_m(0) - \gamma_m]P_m - \kappa P_m I + r(0)\mu P \qquad (C-2)$$

$$\frac{dI}{dt} = \alpha(P + P_m) - \delta I. \qquad (C-3)$$

where $r(\cdot)$ and $r_m(\cdot)$ are the growth rates of the wild type and mutant as a function of drug 113 concentration, μ is the mutation probability from wild type to resistant, and γ and γ_m are 114 the natural death rates of each. We assume a cost of resistance in the absence of 115 treatment, meaning that $r(1-\mu) - \gamma > r_m - \gamma_m$ The immune response, I, grows in 116 proportion to the density of the pathogen population and decays at a constant per capita 117 rate δ . Immune molecules kill the pathogen according to a law of mass action with 118 parameter κ for both the wild type and the resistant strain (i.e., immunity is completely 119 cross-reactive). This is a simple deterministic model for an immune-controlled infection.

```
When the mutation rate is zero (\mu = 0) and the pathogen can increase when rare, the
   model displays damped oscillations towards an equilibrium with the wild type present
122
   (\hat{P} = (r - \gamma)\delta/\alpha\kappa), the mutant extinct (\hat{P}_m = 0), and the immune system at a nonzero
   level (\hat{I} = (r - \gamma)/\kappa). For many choices of parameter values (including those that we focus
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   on here) the first trough in pathogen density is very low, and therefore once we introduce
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   stochasticity the entire pathogen population typically goes extinct at this stage, at which
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   point the immune molecules then decay to zero. It is in this way that we model an
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   immune-controlled infection.
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   Under treatment the dynamics are the same as above but where r(\cdot) and r_m(\cdot) are then
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   evaluated at some nonzero drug concentration. Throughout we assume that the
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   dose-response functions r(\cdot) and r_m(\cdot) are given by the function b_1(1-\tanh(b_2(c-b_3))) for
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   some constants b_1, b_2, and b_3. The model used to explore the emergence of resistance
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   employs a stochastic implementation of the above equations using the Gillespie algorithm.
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   Figure C1 presents output for several runs of the model using three different drug
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   concentrations. In all cases we have set the mutation rate to zero (no resistant strains
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   arise). In the absence of treatment an infection typically results in a single-peak of wild
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   type pathogen before the infection is cleared. To model realistic disease scenarios we
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    (arbitrarily) suppose that infected individuals become symptomatic only once the pathogen
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   density exceeds a threshold of 100 and treatment is used only once an infection is
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   symptomatic. For the parameter values chosen in this example, 99% of untreated
   infections are symptomatic (Figure C1a,b). We further suppose (again arbitrarily) that a
   pathogen load greater than 200 results in substantial morbidity and/or mortality. With
   this assumptions we can then proceed to define the therapeutic window. The upper limit
   c_U is arbitrary in the model and so we set c_U = 0.5. The lower limit c_L is the smallest dose
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   that prevents significant morbidity and/or mortality. Therefore it is the smallest dose that,
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   in the absence of resistance emergence, keeps pathogen load below 200. Figure C1c shows
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that, for the parameter values used, $c_L \approx 0.3$. Notice from Figure C1a that a dose of $c_L \approx 0.3$ does not fully suppress growth as measured in vitro but it nevertheless controls the infection in vivo because the immune response also contributes to reducing the pathogen load.

For simulations in which the mutation rate to resistance is non-zero we quantify the
emergence of resistance in the following way. For each simulation run we record the
maximum density of the resistant strain before the infection is ultimately cleared. Runs in
which this density reaches a level high enough to cause symptoms (a density of 100 in this
case) are deemed to be infections in which resistance has 'emerged'. The probability of
resistance emergence is quantified as the fraction of runs in which this threshold level is
reached. In Figure 4 of the text we also consider the consequences of using other threshold
densities to define emergence.

The simulation results of the main text assume that all resistant strains arise de novo in a infection but in some cases we might expect resistant strains to already be present at the start of infection. The general theory presented in the main text reveals that again we should not expect any simple generalities. For example, one might expect that when the initial infection already contains many resistant microbes the relevance of de novo mutation might be diminished and so a lower dose might be optimal for managing resistance.

Although this is sometimes the case (Day, unpubl. results) the opposite is possible as well.

As an example, Figure C2 presents results for the probability of emergence as a function of dose, for three different levels of resistance frequency in the initial infection. As the frequency of resistance in the initial infection increases, the optimal concentration changes from a low dose to a high dose. The reason is that, if resistance is already very common early in the infection, then the competitive release that occurs from removing the wild type is greatly diminished since the resistant strain will have already managed to gain a foothold before the wildtype numbers increase significantly. Put another way, the benefits

of low dose therapy have decreased because the magnitude of competitive release (the blue terms in equation (4) of the main text) has decreased. Experimental results have verified 174 this prediction; namely, that drug resistant pathogens can reach appreciable within-host 175 densities in the absence of treatment if the initial infection contains a substantial number 176 of these (9). 177

A common suggestion is that, when strains with intermediate levels of resistance are 178 possible, aggressive chemotherapy is then optimal because anything less will allow these 179 intermediate strains to persist and thereby give rise to HLR through mutation. We 180 therefore conducted simulations to explore this idea. We note, however, that again the 181 general theoretical results of Appendix B reveal that no generalities should be expected and our simulations bear this out. For example, we extended equations for the within-host 183 dynamics to allow for a strain with intermediate resistance by using the following equations:

$$\frac{dP}{dt} = [r(c)(1-\mu) - \gamma]P - \kappa PI \tag{C-4}$$

$$\frac{dP}{dt} = [r(c)(1-\mu) - \gamma]P - \kappa PI \qquad (C-4)$$

$$\frac{dP_{m1}}{dt} = [r_{m1}(c) - \gamma_{m1}]P_{m1} - \kappa P_{m1}I + r(c)\mu P \qquad (C-5)$$

$$\frac{dP_{m2}}{dt} = [r_{m2}(c) - \gamma_{m2}]P_{m2} - \kappa P_{m2}I + r_{m1}(c)\mu_1 P_{m1} \qquad (C-6)$$

$$\frac{dP_{m2}}{dt} = [r_{m2}(c) - \gamma_{m2}]P_{m2} - \kappa P_{m2}I + r_{m1}(c)\mu_1 P_{m1}$$
 (C-6)

$$\frac{dI}{dt} = \alpha(P + P_{m1} + P_{m2}) - \delta I. \tag{C-7}$$

where P_{m1} is the density of the mutant strain with intermediate resistance and P_{m2} is the 185 strain with HLR. Also, $r(\cdot)$, $r_{m1}(\cdot)$, and $r_{m2}(\cdot)$ are the growth rates of the wild type and 186 the two mutant types as a function of drug concentration, μ is the mutation probability 187 from wild type to the intermediate strain, μ_1 is the mutation rate from the intermediate 188 strain to HLR, and the γ 's are the natural death rates of each. Again the immune 189 response, I, grows in proportion to the density of the pathogen population and decays at a 190 constant per capita rate δ . 191

Again the simulation was conducted with a stochastic implementation of the above model using the Gillespie algorithm. While the presence of intermediate strains does alter the relative balance of factors affecting resistance emergence, this balance can still move in either direction.

As an example, Figure C3 presents simulation results in which low-dose treatment yields
the lowest probability of HLR emergence. Note, however, that high-dose treatment controls
the emergence of the intermediate strain the best.

The results of Figure C3 can also be interpreted within the context of the mutant selection window hypothesis and the mutant prevention concentration or MPC. The MPC is the 200 drug concentration that prevents the emergence of all single-step resistant mutants. In 201 Figure C3 we can see that the emergence of the intermediate, single step, mutant strain is 202 prevented by using the maximum tolerable dose. Nevertheless, even though the HLR strain 203 can arise only by mutation from this intermediate strain, it it the lowest effective dose that 204 best controls the emergence of HLR. The reason for this is that it is not possible to achieve 205 the MPC early enough in the infection to prevent all mutational input from occurring 206 because treatment starts only once symptoms appear. For the specific case illustrated in 207 Figure C3 the possibility of HLR arising is then enough to tip the balance so that the lower 208 edge of the therapeutic window is the best strategy for controlling HLR. 209

Appendix D - Other results for the model of acute immune-mediated infections

In the main text we focus on the emergence of the resistant strain but in many clinical studies researchers focus instead on successful treatment. For example, one common approach is to quantify the probability of treatment failure as a function of drug dose (or some proxy thereof). Such studies cannot provide information about resistance evolution

per se but they nevertheless might involve a component of resistance evolution if this is one

of the potential reasons for treatment failure.

We can explore a similar idea in the context of the model in the main text. Suppose we 218 measure clinical success as the complete eradication of infection by day 20. In the 219 simulations some individuals then display treatment failure because, through the 220 stochasticity of individual infection dynamics, they fail to clear the infection by this time. 221 Figure D1a presents the probability of treatment failure, measured by the fraction of the 222 simulations for which the infection (wild type or resistant) was still present on day 20 for 223 the model underlying Figure 3. Failure occurs under both treatment scenarios but it 224 happens more frequently for the high dose treatment (compare red portion of bar graphs in Figure D1a). There is an important structure to these failures, however, that can be better appreciated by calculating the probability of failure by conditioning on whether or not a 227 resistant mutation ever appeared during treatment; i.e.,

$$P(F) = P(F|M)P(M) + P(F|M^{c})P(M^{c})$$
 (C-8)

where P(F) is the probability of failure, P(M) is the probability of a resistant mutation appearing during treatment $(P(M^c))$ is the probability that this doesn't occur), and 230 P(F|M) is the probability of failure given a resistant mutation appears (with $P(F|M^c)$ the 231 probability of failure given a resistant mutation does not appear). The bar graphs in Figure 232 D1a show again that a high dose better controls the appearance of resistant mutations (i.e., 233 P(M) is lower for the high dose treatment), but if a resistant mutation does occur, then a 234 high dose results in a greater likelihood of treatment failure (i.e., P(F|M) is higher for the 235 high dose treatment - note that this quantity can be interpreted graphically as the ratio of 236 the red to grey bars). And in this case the latter effect overwhelms the former, making the

probability of treatment failure P(F) greater overall for the high dose treatment.

It is not difficult to obtain diametrically opposite results, however, with a small change in 239 parameter values. Figure D1b show analogous results for the very same simulation, but 240 where the probability of mutation is an order of magnitude lower. In this case we see that, 241 even though a high dose results in a greater probability of failure if a resistant mutation 242 appears, the effect is diminished such that, overall, the high dose results in a lower overall 243 probability of failure. Notice also though that, even though a high dose results in a lower 244 likelihood of treatment failure, it nevertheless still results in a higher probability of 245 resistance emergence during treatment. The former is measured only by whether or not the infection still persists on day 20 whereas the latter is measured by whether or not a large outbreak of resistance occurs at some point during treatment. This provides an example illustrating the general idea that treatment failure cannot be taken as a proxy for resistance emergence.

Appendix E - Generalizing the pharmacokinetics

Here we illustrate how the qualitative conclusions of the main text hold more broadly by
deriving the analogue of equation (4) for quite general forms of pharmacokinetics. For
simplicity we will ignore the possibility that resistant strains might be present at the start
of treatment.

For the sake of illustration we suppose that the drug is administered in some arbitrary way for a period of time of length T and then treatment is stopped. The question we ask is, how does increasing the duration of treatment T affect the probability of resistance emergence? More generally we might alter other aspects of treatment like dose size, inter-dose interval, etc but our focus on T will be sufficient to see how one would deal with these other factors as well.

To allow for more general pharmacokinetics we must model the dynamics of drug concentration explicitly. Once treatment has begun the model becomes 263

$$\frac{dp}{dt} = f(p, x, c) \tag{E-1a}$$

$$\frac{dx}{dt} = g(p, x, c)$$
(E-1b)
$$\frac{dc}{dt} = h(p, x, c, t)$$
(E-1c)

$$\frac{dc}{dt} = h(p, x, c, t) \tag{E-1c}$$

The third equation accounts for the pharmacokinetics of the drug and allows for the treatment protocol to vary through time. These equations must also be supplemented with an initial condition specifying the values of the variables at the start of treatment.

After time T has elapsed treatment is stopped and the dynamics then follow a different set 267 of equations given by 268

$$\frac{d\tilde{p}}{dt} = \tilde{f}(\tilde{p}, \tilde{x}, \tilde{c})$$
(E-2a)
$$\frac{d\tilde{x}}{dt} = \tilde{g}(\tilde{p}, \tilde{x}, \tilde{c})$$
(E-2b)

$$\frac{d\tilde{x}}{dt} = \tilde{g}(\tilde{p}, \tilde{x}, \tilde{c}) \tag{E-2b}$$

$$\frac{d\tilde{c}}{dt} = \tilde{h}(\tilde{p}, \tilde{x}, \tilde{c}, t)$$
 (E-2c)

The tildes reflect the fact that the functional form of the dynamical system might change 269 when treatment is stopped (e.g., there is no longer any input of the drug in the function h270 as compared with the function h), and thus the variables follow a different trajectory than 271 they would have under treatment. This system of differential equation must also be 272 supplemented with an initial condition as well, and this requires $\tilde{p}(T) = p(T)$, $\tilde{x}(T) = x(T)$, 273 and $\tilde{c}(T) = c(T)$. Notice that the trajectories of the new variables \tilde{p}, \tilde{x} and \tilde{c} therefore

- depend on the duration of treatment T because this duration will affect their initial values.
- 276 With the above formalism we can write the hazard as

$$H(T) = \int_0^T \lambda \pi ds + \int_T^\infty \tilde{\lambda} \tilde{\pi} ds$$
 (E-3)

where we have simplified the notation by using a tilde above a function to indicate that the function is evaluated along the variables with a tilde. Differentiating with respect to T gives

$$\frac{dH}{dT} = \lambda \pi|_{s=T} - \tilde{\lambda}\tilde{\pi}|_{s=T} + \int_{T}^{\infty} \frac{d}{dT} \tilde{\lambda}\tilde{\pi} ds$$
 (E-4)

By the continuity of the state variables the first two terms cancel and therefore we have

$$\frac{dH}{dT} = \int_{T}^{\infty} \frac{d}{dT} \tilde{\lambda} \tilde{\pi} ds \tag{E-5}$$

Now $\tilde{\lambda}$ and $\tilde{\pi}$ depend on T because they depend on the trajectories of the variables \tilde{p}, \tilde{x} and \tilde{c} , and the trajectories of these variables in turn depend on their initial conditions (which depend on T as described above). We can capture this notationally by treating the variables \tilde{p}, \tilde{x} and \tilde{c} as functions of T. Thus we have

$$\frac{dH}{dT} = \int_{T}^{\infty} \frac{d}{dT} \tilde{\lambda} \tilde{\pi} ds$$

$$= \int_{T}^{\infty} \pi \left(\frac{\partial \lambda}{\partial \tilde{p}} \frac{\partial \tilde{p}}{\partial T} + \frac{\partial \lambda}{\partial \tilde{c}} \frac{\partial \tilde{c}}{\partial T} \right) + \lambda \left(\nabla_{\tilde{x}} \pi \cdot \tilde{x}_{T} + \frac{\partial \pi}{\partial \tilde{c}} \frac{\partial \tilde{c}}{\partial T} \right) ds$$

We can see that this has a form that is identical to de novo part of equation (4) except that

now the drug concentration is no longer directly under our control. Instead, changes in T affect resistance emergence by how they affect changes in drug concentration. More generally, the very same potentially opposing processes as those in equation 4 will arise regardless of how we alter the drug dosing regimen because any such alteration must ultimately be mediated through its affect on the drug concentration at each point in time during an infection.

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Figure Captions

Figure C1. (a) The dose-response curve $r(c) = 0.6(1 - \tanh(15(c - 0.3)))$ as well as the therapeutic window in green. (b), (c) and (d) show wild type pathogen density (blue) and immune molecule density (black) during infection for 1000 representative realizations of a stochastic implementation of the model. (b) no treatment, (c) treatment at the smallest effective dose c_L , (d) treatment at the maximum tolerable dose c_U . Parameter values are P(0) = 10, I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 0$, and $\gamma = 0.01$.

Figure C2. The effect of different levels of standing variation for resistance in the initial infection. Simulation is identical to that for Figure 3a except for the initial conditions. The dose-response curves for the wild type in blue $(r(c) = 0.6(1 - \tanh(15(c - 0.3))))$ and the resistant strain in red $(r_m(c) = 0.59(1 - \tanh(15(c - 0.6))))$ as well as the therapeutic window in green. Red dots indicate the probability of resistance emergence, and for three different initial conditions. Probability of resistance emergence is defined as the fraction of 5000 simulations for which resistance reached a density of at least 100 (and thus caused disease). Top set of dots have P(0) = 5, $P_m(0) = 5$; middle set of dots have P(0) = 7, $P_m(0) = 3$; bottom set of dots have P(0) = 10, $P_m(0) = 0$. Other parameter values are I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 10^{-2}$, and $\gamma = 0.01$.

Figure C3. Simulation results when there is a strain with intermediate resistance. (a) The dose-response curves for the wild type in blue $(r(c) = 0.6(1 - \tanh(15(c - 0.3))))$, the intermediate strain in yellow $(r_{m2}(c) = 0.595(1 - \tanh(15(c - 0.45))))$, and the HLR strain in red $(r_{m2}(c) = 0.59(1 - \tanh(15(c - 0.6))))$ as well as the therapeutic window in green. Dots indicate the probability of emergence for the intermediate strain (yellow) and the HLR strain (red). Probability of emergence is defined as the fraction of 5000 simulations for which the strain reached a density of at least 100. (b) and (c) wild type density (blue), intermediate strain density (yellow), HLR strain density (red), and immune molecule density (black) during infection for 1000 representative realizations of a stochastic implementation of the model. (b) treatment at the smallest effective dose c_L , (c) treatment at the maximum tolerable dose c_U . Parameter values are P(0) = 10, $P_{m1}(0) = 0$, $P_{m2}(0) = 0$, I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 10^{-2}$, $\mu_1 = 10^{-2}$, and $\gamma = \gamma_{m1} = \gamma_{m2} = 0.01$.

Figure D1. The effect of drug concentration on resistance emergence and treatment failure. (a) The dose-response curves for the wild type in blue $(r(c) = 0.6(1 - \tanh(15(c - 0.3))))$ and the resistant strain in red $(r_m(c) = 0.59(1 - \tanh(15(c - 0.6))))$ as well as thetherpeutic window in green. Dots indicate the probability of resistance emergence. Probability of resistance emergence is defined as the fraction of 5000 simulations for which resistance reached a density of at least 100 (and thus caused disease). Parameter values are P(0) = 10, I(0) = 2, $\alpha = 0.05$, $\delta = 0.05$, $\kappa = 0.075$, $\mu = 10^{-2}$, and $\gamma = 0.01$. Bar graphs: the probability that a resistant strain appears by mutation is indicated by the left-hand grey bars for each drug concentration (the right-hand grey bar is the probability that a resistant strain does not appear). The probability of treatment failure for a specific drug dose is the sum of the red bars for that dose. (b) Same as panel (a) but with mutation rate decreased to $\mu = 10^{-3}$.

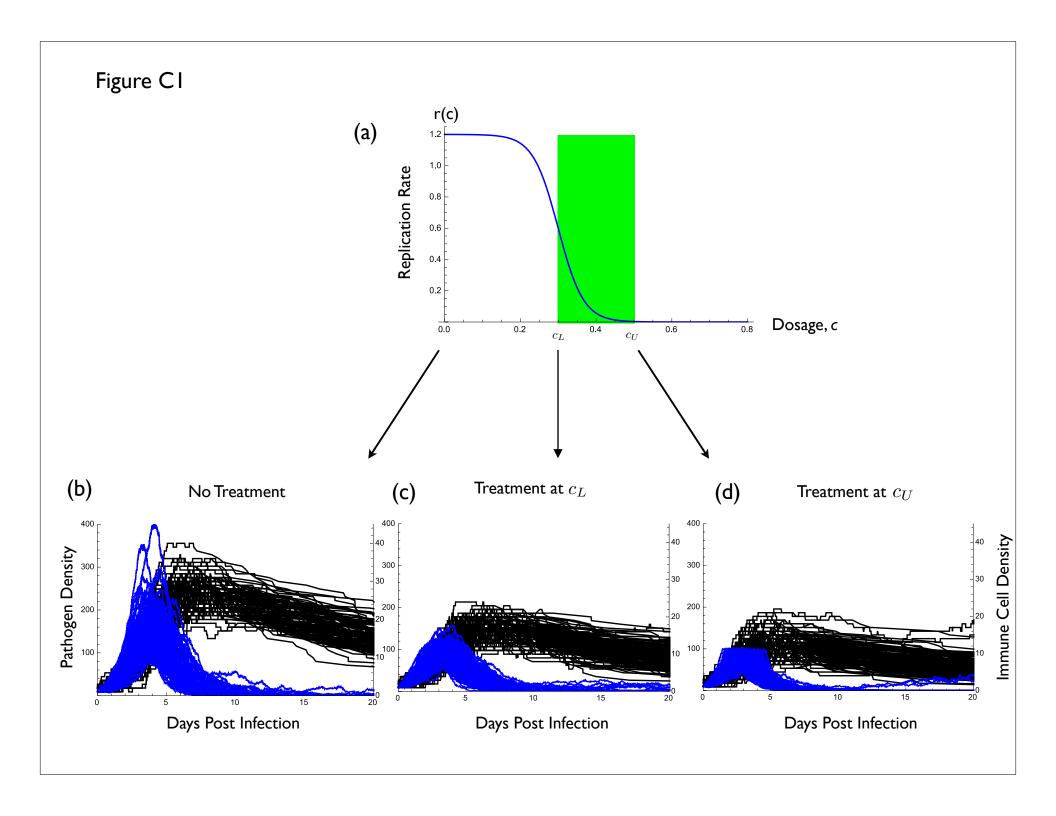


Figure C2

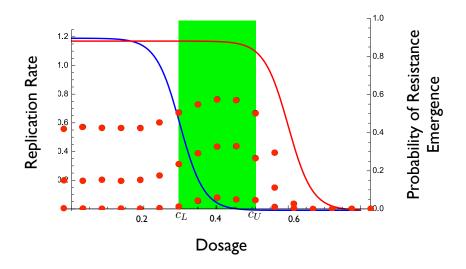


Figure C3

